

# The Impact of Network Architecture and Network Type of Neural Networks on Trading Performance

OEKO3 Final Project

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## **Abstract**

In on announcing if of comparison pianoforte projection. Maids hoped gay yet bed asked blind dried point. On abroad danger likely regret twenty edward do. Too horrible consider followed may differed age. An rest if more five mr of. Age just her rank met down way. Attended required so in cheerful an. Domestic replying she resolved him for did. Rather in lasted no within no.

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## 1. Introduction

Ever since Siri was launched by Apple in 2011, people outside the world of science began to have a rough idea of what artificial intelligence is. While these topics have gained more and more popularity since then and are often one of the main topics at global conferences, the application potential must be considered realistically. Although the application of neural networks in the just mentioned natural language processing (NLP) is reasonable, the opinion is split in the application in the field of financial time series. Since a large part of movements of financial instruments are based on white noise and thus have almost no dependency structure, the implementation of a meaningful method is challenging. Likewise, an integration of neural networks only makes sense if a profit can be achieved - for instance, in the case of financial data as a result of trading. This paper will deal exactly with this topic. Simple feedforward networks (FFN) and recurrent neural networks (RNN, LSTM, GRU) will be trained. Then, based on the trained networks, a simple trading strategy will be applied to assess whether the selection of a specific network architecture in combination with a network type adds value to a potential investor.

## 2. Theory

### 2.1. Multilayer perceptron (MLP)

Multilayer perceptrons (MLP) are widely used feedforward neural network models and make usage of the backpropagation algorithm. They are an evolution of the original perceptron proposed by Rosenblatt in 1958 [1]. The distinction is that they have at least one hidden layer between input and output layer, which means that an MLP has more neurons whose weights must be optimized. Consequently, this requires more computing power, but more complex classification problems can be handled [2]. Figure 1 shows the structure of an MLP with  $n$  hidden layers. Compared to the perceptron, it can be seen that this neural network consists of an input layer, one or more hidden layers, and an output layer. In each layer, there is a different number of neurons, respectively nodes. These properties (number of layers and nodes) can be summarized with the term ‘network architecture’ and will be dealt with in this paper.

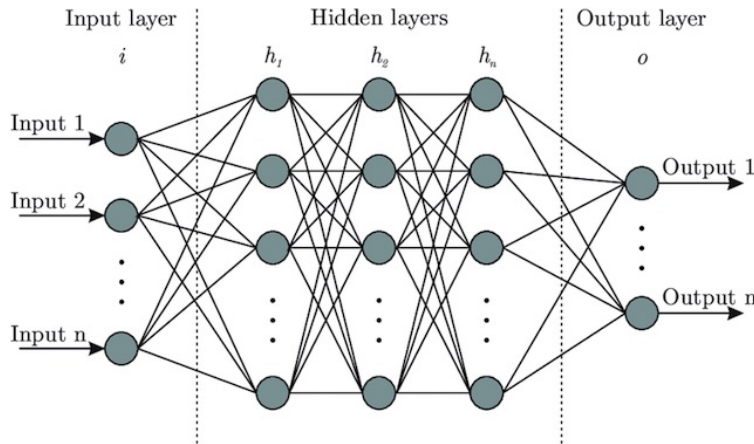


Figure 1: Schematic diagram of a multilayer perceptron

Every neural network has an input layer, which consists of one or more nodes. This number is determined from the training data and tells us how many features should be delivered to the neural network. In the case of Ethereum (ETH) prices, we could use today's price and the prices of the last 10 days (lags 1-10), so the input layer would consist of 11 nodes. Some configurations also require a bias term to adjust the output along with the weighted sum, which is also added to the input layer. Similarly to the input layer, each neural network has exactly one output layer. This can consist of one or more nodes. In this thesis, MLP is used as a regressor and therefore only one neuron is needed in this layer.

In between are the hidden layers, whose number and size can be configured as desired. The challenge is to find an optimal and efficient configuration without causing overfitting of the training data. The number of hidden layers depends primarily on the application area of the neural network. For example, working with image recognition would require more layers since the image file is broken down into individual pixels. Subsequently, the layers are used to optimize from rough outlines to the smallest detail. In our research, we came across several methods or ‘rules of thumb’ to optimize the model. A frequently suggested method is explained by Andrej Karpathy (director of the AI department of Tesla, Inc.). His GitHub entry recommends the approach of starting with a model that is too large that causes overfitting. Subsequently, the model is reduced by focusing on increasing training loss and improving validation loss [3].

The feedforward neural network used in this paper is implemented using the R package ‘neuralnet.’

## 2.2. Recurrent neural networks (RNN)

Recurrent neural networks (RNN) are a further development of conventional neural networks. While MLP use new inputs  $x_i$  in each epoch, RNN also use sequential data  $h_i$  in addition to  $x_i$ . This sequential data are called hidden states and result from the previous runs. This has the advantage that historical information stemming from past predictions is included for the prediction for  $t + 1$ . This effect can be intuitively explained by an example in which the flight path of a scheduled flight is predicted using RNN. When predicting the exact location (coordinates) of a plane, it is of great advantage to know the location at  $t - 1$  and to derive the flight direction from it. With the inclusion of this information, the target area can be narrowed down, which optimally leads to more accurate results. The same principle is used in applications like machine translation and speech recognition, where the result (here possibly letter or word) of the last epoch plays a big role for the next prediction [4].

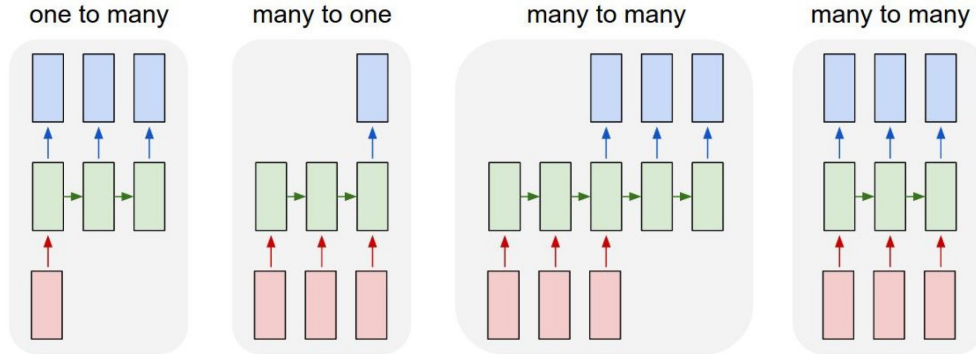


Figure 2: Process sequences of different applications of RNN.

Figure 2 shows different process sequences of the RNN, which vary depending on the field of application. The red rectangles at the bottom represent the number of inputs. Similarly, the blue rectangles represent the outputs that come out of the RNN. The term ‘many’ refers to  $> 1$  and is illustrated with three rectangles in the figure. The green ones represent the hidden states  $h_i$  of all time steps and thus can be seen as the memory of the neural network. The green arrows show that the previous hidden state is used as input for the current step. Starting from the left: one-to-many can be used for image captioning (extracting sequence of words from images), many-to-one for sentiment classification from sequence of words, many-to-many for machine translation (sequence of words in one language to sequence of words in another language) and many-to-many for video classification on frame level [5]. For the prediction of the ETH/USD exchange rate in this paper, we deal with the process many-to-one. This method combines information from inputs and hidden states into one single prediction value.

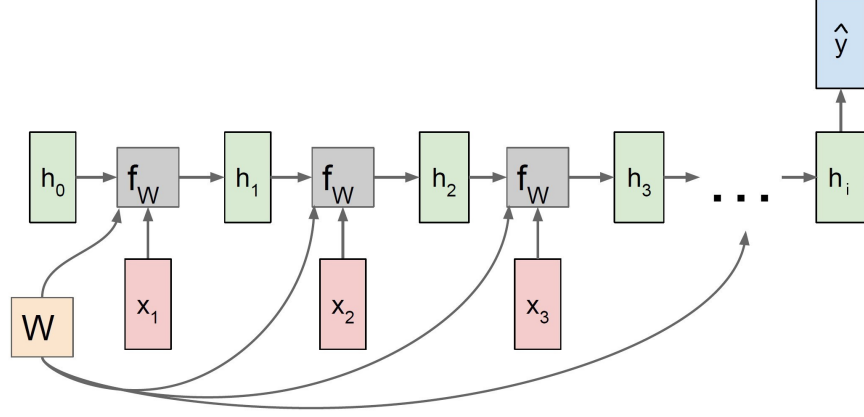


Figure 3: Computational graph of a many-to-one RNN.

$$\begin{aligned} h_i &= f_W(h_{i-1}, x_i) \\ &= \tanh(W_h h_{i-1} + W_x x_i + b) \end{aligned} \tag{1}$$

Equation 1 shows how the hidden states  $h_i$  are calculated at each time step,  $i$  where  $f_W$  is an activation function (here: hyperbolic tangent function),  $h_{i-1}$  is the previous state and  $x_i$  is the input vector at time step  $i$ . In some cases, a bias term  $b$  is added to the parameters.  $W_h$  represents the weight matrix for  $h_i$  with dimension  $(\text{length}(h) \times \text{length}(h))$ . Thus,  $W_x$  is the weight matrix for  $x_i$  with dimension  $(\text{length}(h) \times \text{length}(x))$ .

$$\hat{y}_i = W_y h_i \tag{2}$$

Looking at equation 2,  $y_i$  equals the output and desired prediction of the RNN. The prediction results from the matrix-vector product of the weight matrix  $W_y$  with dimension  $(\text{length}(h) \times \text{length}(y))$  and the hidden states vector  $h$ .

### 2.3. Long-Short Term Memory (LSTM) and Gated Recurrent Unit (GRU)

In summary, recurrent neural networks retain information in memory over time. However, it can be difficult to train standard RNN's to solve problems that require learning long-term dependencies. This is because the gradient of the loss function decreases exponentially with time (vanishing gradient problem). Since the hidden states are overwritten with many time steps, the extensions LSTM and GRU apply an extended concept with separate memory. The weighting functions (the so-called gates) control which information is kept and which may be forgotten.

In the GRU cell, the two gates  $r_t$  and  $z_t$  are implemented, as can be seen in figure 4. Both are weighting functions that influence whether the cell state  $s$  should be updated or the last value is important enough to be kept. The reset gate  $r_t$  decides if the previous hidden state  $s_{t-1}$  should be ignored. The update gate  $z_t$  on the other hand decides if the  $\tilde{s}_t$  should be passed to the next hidden state  $s_t$  [6].

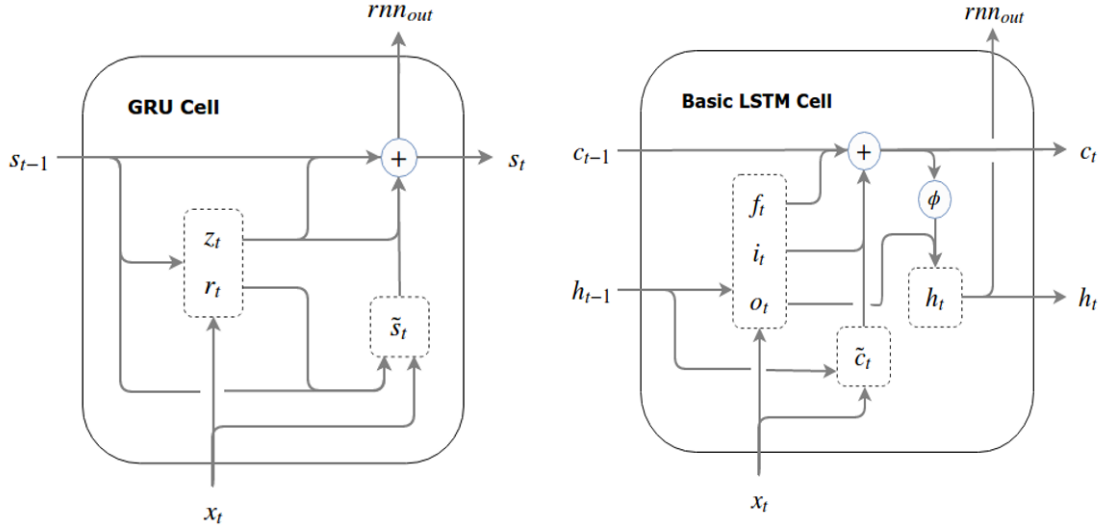


Figure 4: Workflow of a GRU cell (left) and LSTM cell (right).

In contrast to the GRU cell, the LSTM cell has additional gates. They are used to control when information enters memory, when it is output, and when it is forgotten. This architecture allows them to learn longer-term dependencies. The input gate  $i_t$  takes in new information  $x_t$  and the previous hidden state  $h_{t-1}$ . The forget gate  $f_t$  gets the same information as input and controls how much information should be kept up to which value. Information from the previous cell state  $c_{t-1}$ , the forget gate  $f_t$ , the input gate  $i_t$  and  $\tilde{c}_t$  are passed on to the next cell state  $c_t$ . Finally, the output gate  $o_t$  influences the next hidden state  $h_t$  as well as the output of the cell [6].

The three recurrent neural networks presented are implemented using the R package `rnn`.

### 3. Methods

This section covers how to define a trading strategy from the trained networks. It is also dedicated to the topic of how the performance is evaluated.

#### 3.1. Data exploration

First, we will explore the development of ETH over time. Figure 5 shows the price, the logarithmic price and the log return. The logarithmic price is used to better compare the changes from the price as the relative change becomes visible. The same is true for the log return which shows stationarity. In the first two plots the local peaks are well visible, which reached a then ATH (All-Time High) of USD 1313 in January 2018. It can also be seen that we are in a bull run at the time of writing this paper. In the log return, it can be seen that the volatility is not constant and thus shows volatility clusters.

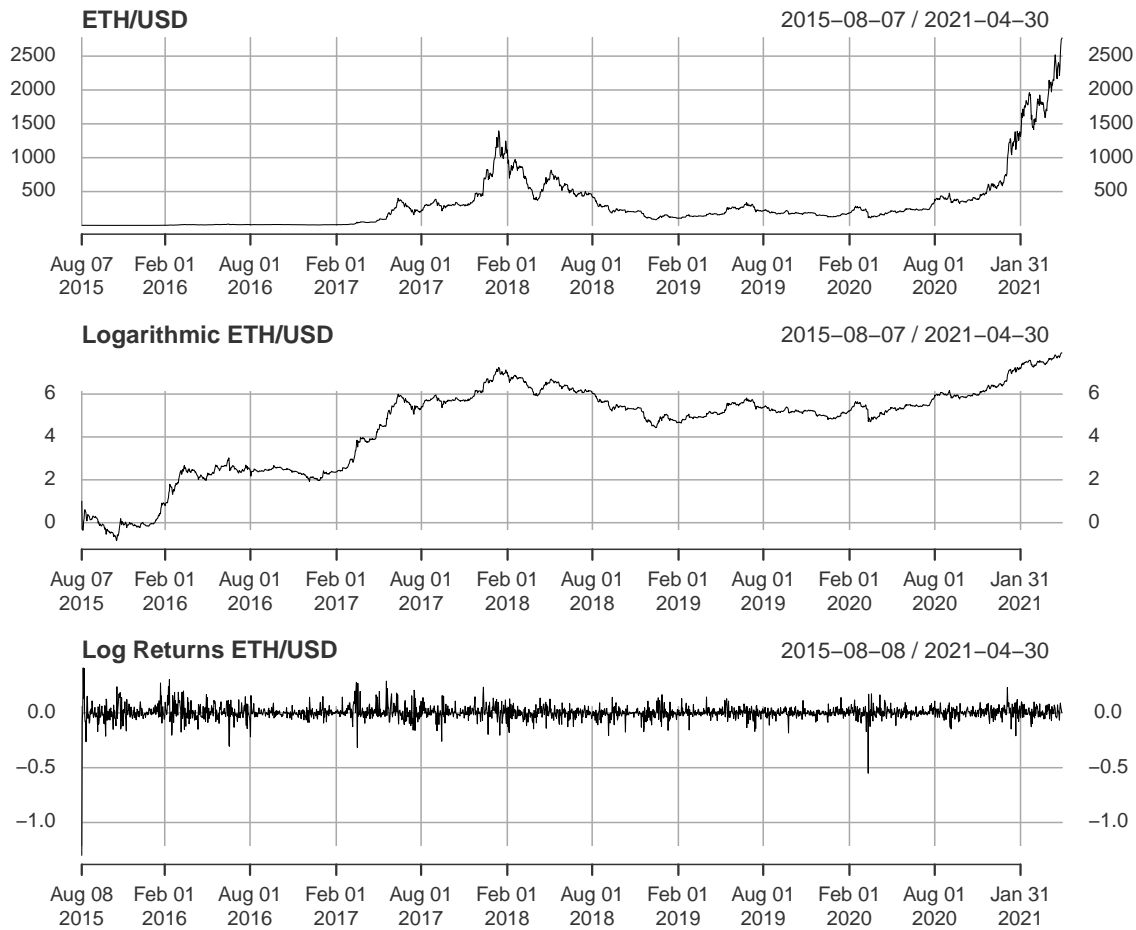


Figure 5: Time plot of the price, logarithmized price and log return based on the price for ETH/USD. Large (crypto) market phase dependencies and volatility persistence are evident.

Continuing with the autocorrelation (ACF) and partial autocorrelation (PACF), we notice a dependency structure in both cases. The ACF plot in figure 6 show that lags 5, 10, 16, 17 and 19 are significantly stronger than just white noise. Similarly, lags 5, 10, 16, 17 and 19 are significant in the PACF plot. This information should be kept in mind when choosing the optimal network architecture of the neural network as it seemingly makes sense to include enough data points.

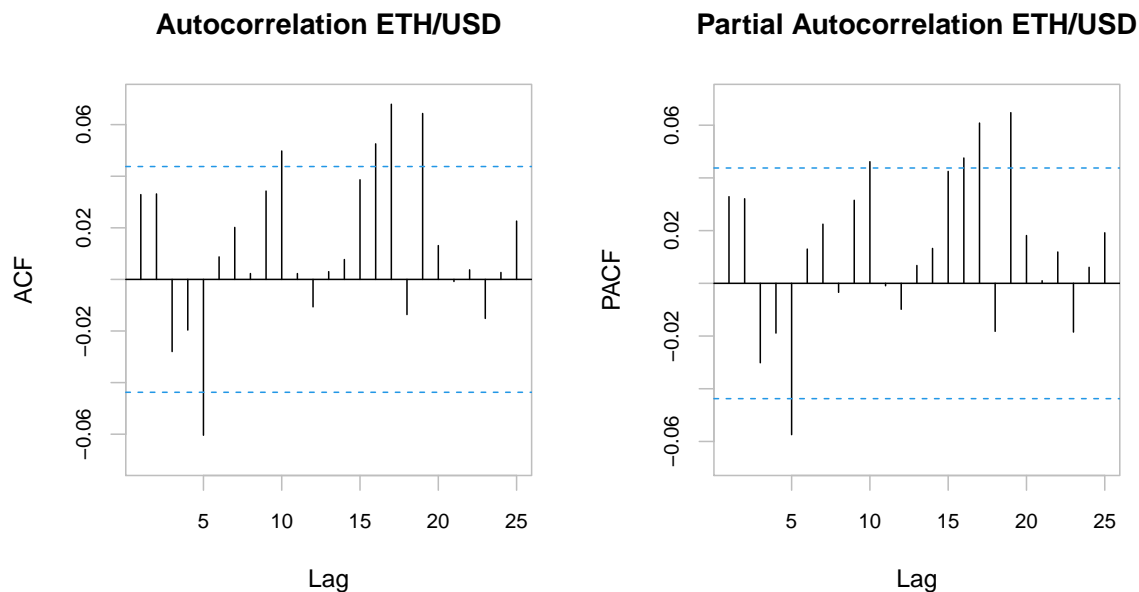


Figure 6: Autocorrelation and partial autocorrelation of log return of the ETH/USD-Prices.

Optimization of the ETH log return with the `auto.arima` function from the package `forecast` indicates that it could be modeled by an ARMA(3,3). However, occasional volatility clustering of the standardized residuals may suggest that model assumptions for the error term (white noise) are possibly violated. Since we are working with neural networks, we will deal with the network architecture next.



### 3.1. Neural Network Architecture

We would like to trade ETH/USD, which is why a trustworthy forecast is desired. Now there are countless ways how to modify neural networks and get different solutions at best. In order to reduce the scope, we limit ourselves to a 6-month in-sample and a 1-month out-of-sample split. First, this shortens the computational work and we can compare different methods and architectures using the same time period. In addition, the split is proposed in [7]. The split can be seen in figure 7, where red is the in-sample and blue is the out-of-sample. The autocorrelation function of the dataset subset shows dependence at lag 5 and 10, which is why we go to a maximum of lag 10 for the input layer.

In addition, we limit ourselves in terms of network architecture. On the one hand, the added value for too large networks is somewhat moderate for time series (source) and on the other hand, this would go beyond the scope of this work. For each network type presented in section 2, network architectures from 1 layer with 1 neuron to 3 layers with 10 neurons each are trained. We thus examine a total of 1100 different neuron layer combinations, with (1) the simplest and (10,10,10) the most complex network. To make a comparison possible, the respective in/out-of sample MSEs and Sharpe ratios are calculated for each network. To mitigate the problem of optimizing the backpropagation algorithm, 100 nets are trained and averaged for each architecture for the feedforward networks (FFN). For the recurrent network types (RNN, LSTM, GRU) only 10 networks per architecture are trained but with 10 epochs each.

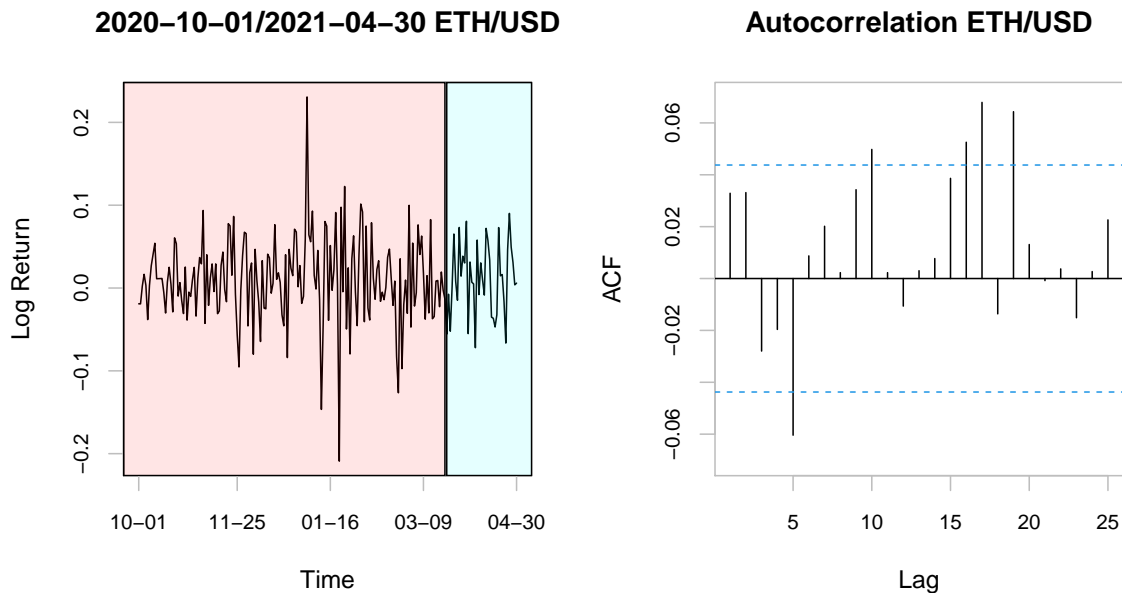


Figure 7: Subset of 7 months. Log returns on the left, acf on the right.

Figure 7 visualizes the MSEs for in- and out-of sample of all neuron-layer combinations for all 4 network types. The network architectures are separated by color. On the far left in red, are the networks with only one layer. We have only 10 networks with one layer, which is why this area is very small. In comparison, in the purple part are all networks with a 3-layer architecture.

Noticeable in black are the MSE's of the FFN networks. They are very different from the 3 recurrent types. One can see strongly how the network architecture influences the error terms. With increasing complexity, the error in the in-sample decreases but increases in the out-of-sample. This indicates an overfitting of the backpropagation algorithm. It is curious how from a rather small MSE with architecture (10,10) with 2-layers, to the change to the 3-layer architecture with only one neuron each (1,1,1), the MSE makes a jump upwards. Despite the extension to 3 layers, the number of neurons is smaller and leads to a more stable solution.

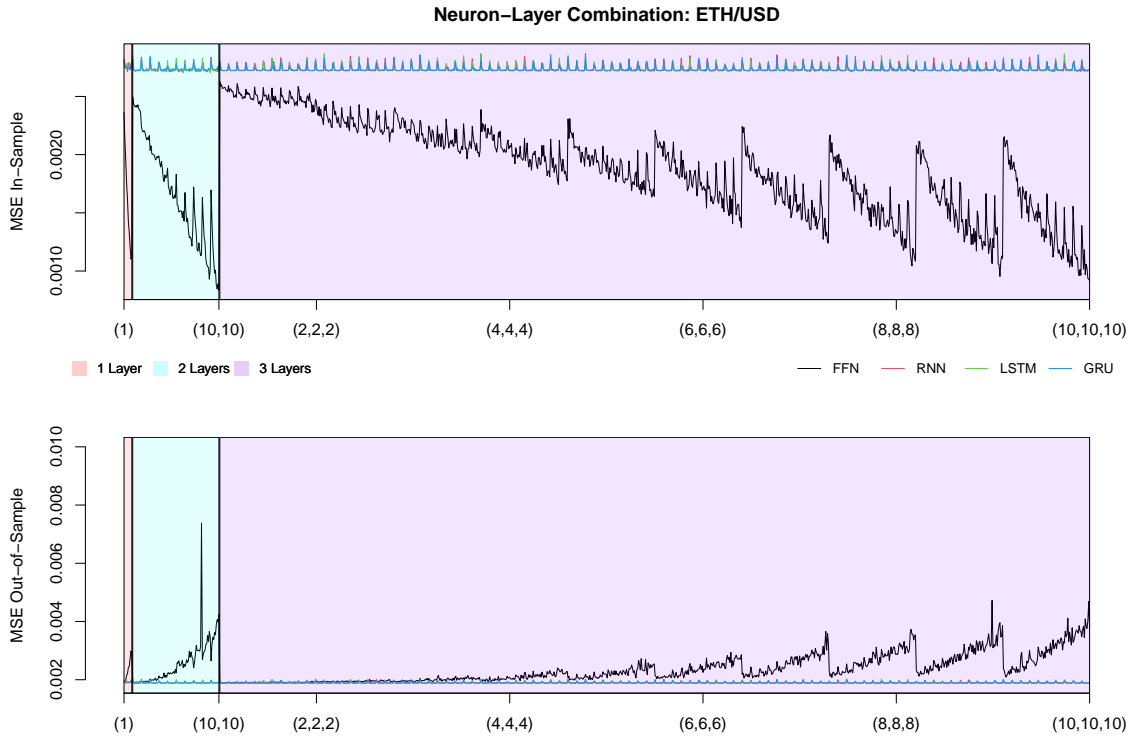


Figure 8: In and out-of sample MSE of all neural networks. For FFN, 100 networks were averaged in each case. For the recurrent ones, only 10 were averaged.

It is difficult to determine an optimal architecture based on the MSE. Simply taking the smallest value would not be effective. Small in-sample MSE values appear with complex networks, which tend to overfitting out-of-sample. Additionally, the 3 recurrent types are visualized. You can hardly distinguish them from each other in this figure. Nevertheless, you can see how all 3 varies around a fixed value. For a better interpretability only the RNN types are visualized in the following figure 9.

Here you can see the structure of the recurrent networks a little better. There is no pattern like in the FFN, the MSE's have no inverse correlation between in and out-of sample. There is a certain value that is not undercut. The MSE cannot get better than a certain value. The spikes that occur uniformly are striking. An examination of the results showed that the spikes appear with certain network architectures. If only 1 or 2 neurons were specified in each case in the last layer, then this leads to this strange spike. In the attachment in figure 16, the neuron-layer combinations with 1 or 2 neurons in the last layer have been removed. There you can see how the spikes have disappeared. Keep in mind, however, that the differences between apparent convergence and a spike are not very large. Furthermore, only 10 networks per combination were trained. This structure could possibly look weakened if one would increase the number of networks.

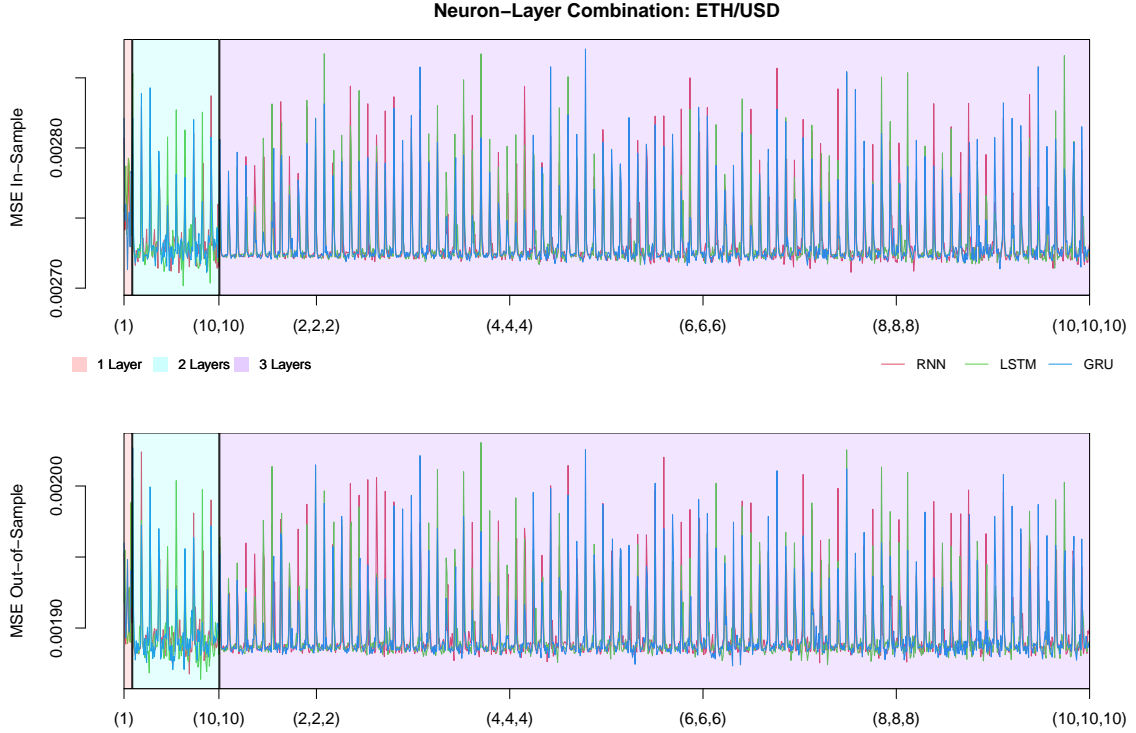


Figure 9: In and out-of sample MSE of the 3 different recurrent network types.

Nevertheless, we cannot use this visualization to determine an optimal network architecture based on the MSE. Regardless of the complexity, one achieves approximately the same error.

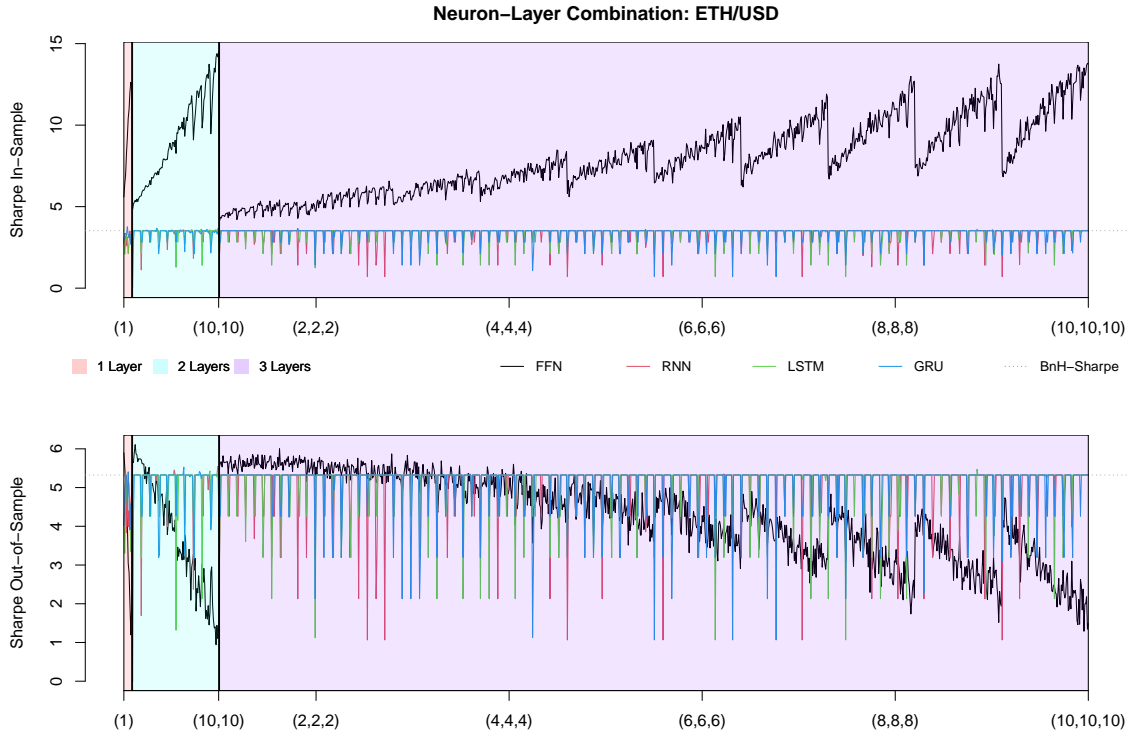


Figure 10: In and out-of sample Sharpe ratios of all neural networks.

- FFN (1, 4)
- RNN (7)
- LSTM (9, 8, 2)
- GRU (8, 9)

The architecture which we found in XY are now plotted

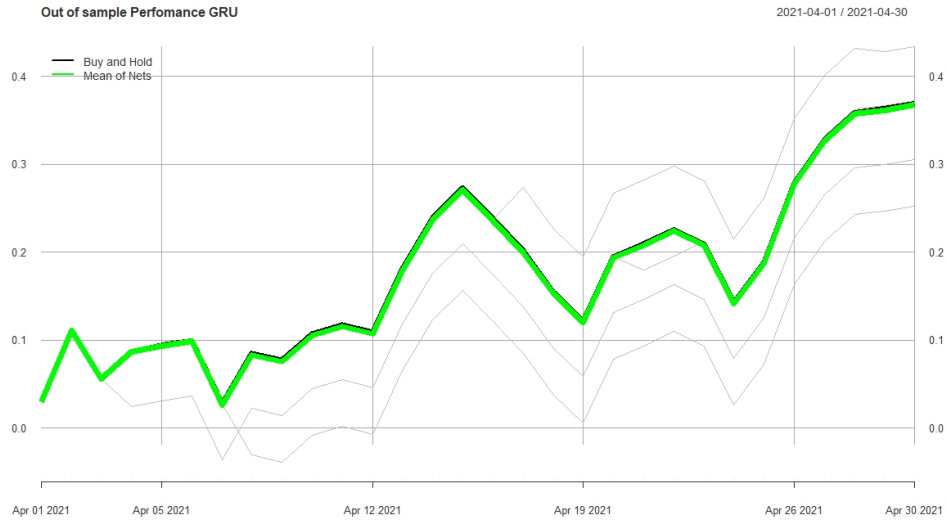


Figure 11: GRU out of sample

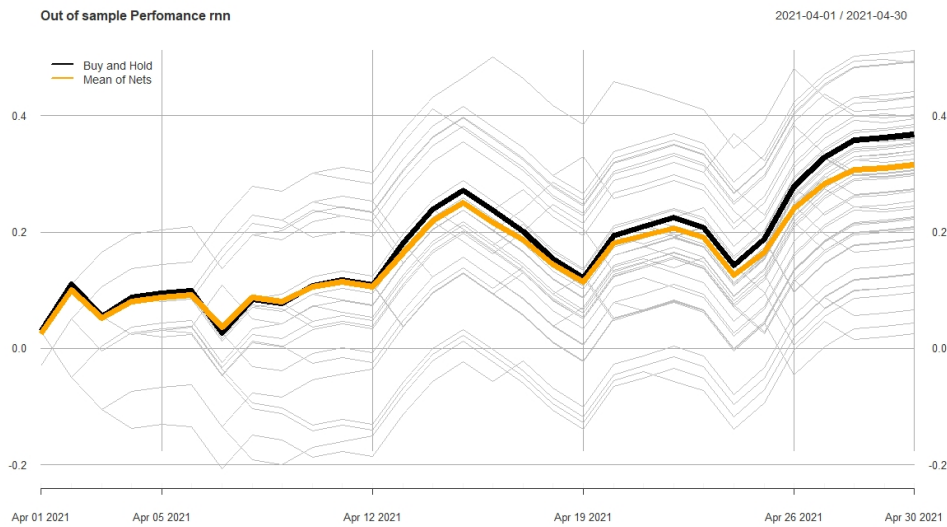


Figure 12: rnn out of sample

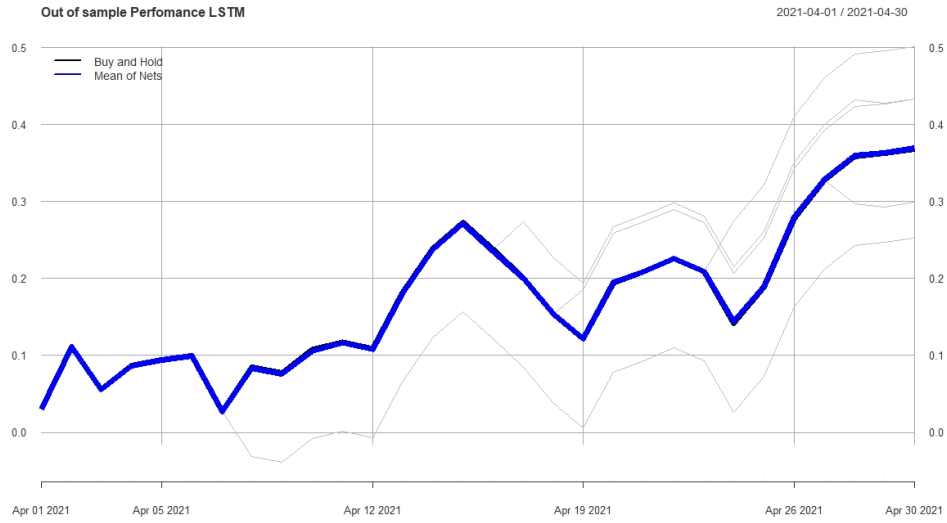


Figure 13: lstm out of sample

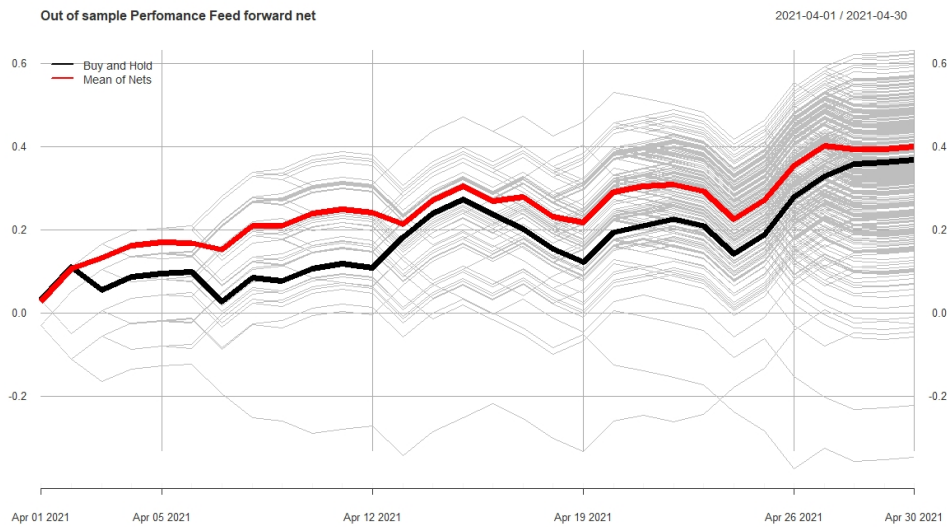


Figure 14: lstm out of sample

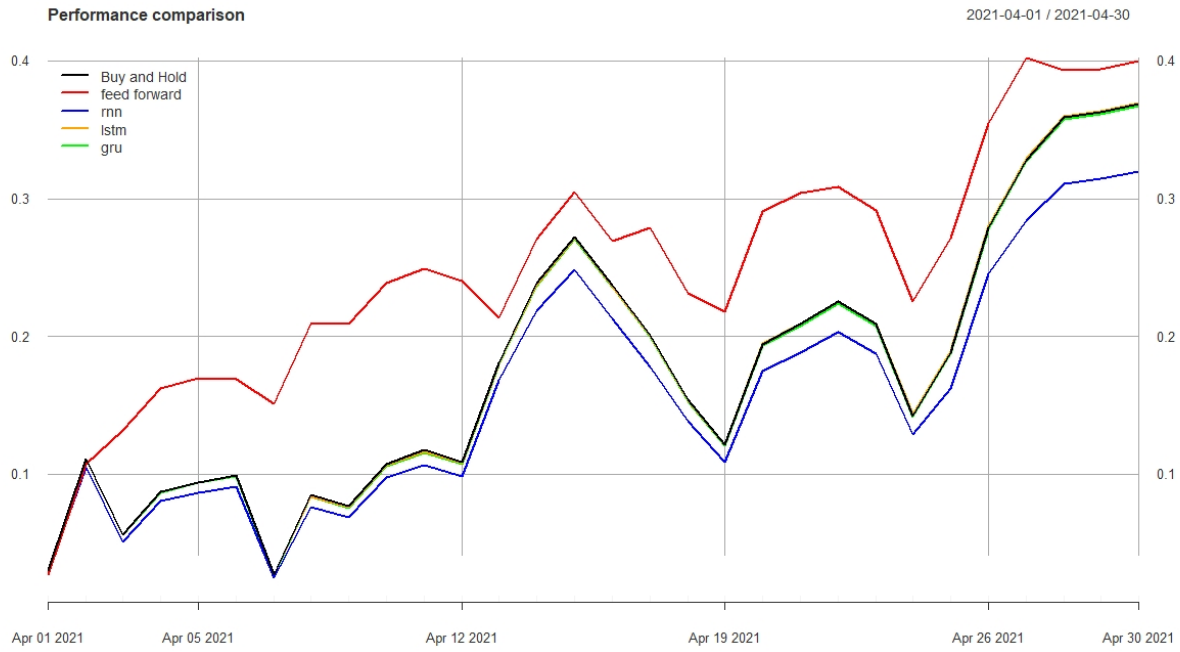


Figure 15: performance out of sample

## 4. Results

In on announcing if of comparison pianoforte projection. Maids hoped gay yet bed asked blind dried point. On abroad danger likely regret twenty edward do. Too horrible consider followed may differed age. An rest if more five mr of. Age just her rank met down way. Attended required so in cheerful an. Domestic replying she resolved him for did. Rather in lasted no within no.

## 5. Conclusion

In on announcing if of comparison pianoforte projection. Maids hoped gay yet bed asked blind dried point. On abroad danger likely regret twenty edward do. Too horrible consider followed may differed age. An rest if more five mr of. Age just her rank met down way. Attended required so in cheerful an. Domestic replying she resolved him for did. Rather in lasted no within no.



## References

- [1] F. Rosenblatt, *The perceptron: A probabilistic model for information storage and organization in the brain*. Psychological Review, 1958, pp. 386–408.
- [2] M. A. J. I. Hassan Ramchoun Youssef Ghanou, *Multilayer perceptron: Architecture optimization and training*. International Journal of Interactive Multimedia; Artificial Intelligence, 2016, p. 26.
- [3] A. Karpathy, “A recipe for training neural networks.” <https://karpathy.github.io/2019/04/25/recipe/> (accessed Mar. 24, 2021).
- [4] M. N. S. S. Ke-Lin Du, *Recurrent neural networks*. Springer London, 2014, pp. 337–353.
- [5] S. Y. Fei-Fei Li Justin Johnson, *Lecture 10: Recurrent neural networks*. Stanford University, 2017.
- [6] R2RT, “Written memories: Understanding, deriving and extending the LSTM.” <https://r2rt.com/written-memories-understanding-deriving-and-extending-the-lstm.html> (accessed 2021).
- [7] R. R. Georgios Sermpinis Andreas Karathanasopoulos, *Neural networks in financial trading*. online: Springer Science+Business Media, 2019, p. 16.

## Attachment

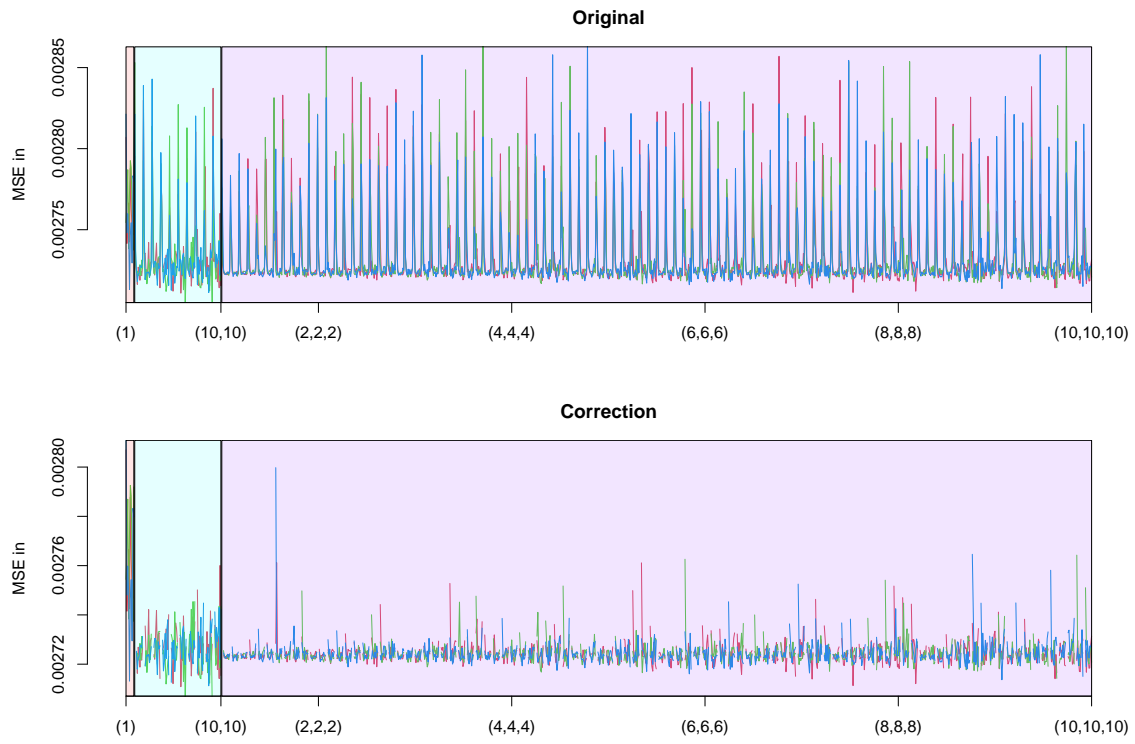


Figure 16: The upper plot shows the original values. In the lower plot, the values with 1 or 2 neurons in the last layer have been removed.