# The Object-Z Specification Language

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# Template for a class definition

# Example 1: Stack ADT – Visibility list and interface

 $\uparrow (Push, Pop, Top)$ 

#### State schema

elements: seq T

 $count: \mathbb{N}$ 

count >= 0

#### Initialization of state

$$\begin{array}{c} INIT \\ elements = \langle \rangle \\ count = 0 \end{array}$$

## **Operation Push**

```
-Push \_
\Delta(elements, count)
el?: T
elements' = \langle el? \rangle \widehat{\ } elements
count' = count + 1
```

## **Operation Pop**

```
 \begin{array}{c} -Pop \\ \Delta(elements, count) \\ el!: T \\ \hline count > 0 \\ el! = head(elements) \\ elements' = tail(elements) \\ count' = count - 1 \end{array}
```

# **Operation Top**

```
Top
el!: T
count > 0
el! = head(elements)
elements' = elements
count' = count
```

```
Stack[T]
(Push, Pop, Top)
 elements: seq T
 count: \mathbb{N}
 count >= 0
 _ INIT _____
 elements = \langle \rangle
 count = 0
_Push _____
 \Delta(elements, count)
 el?:T
 elements' = \langle el? \rangle ^{\frown} elements
 count' = count + 1
_Pop _____
 \Delta(elements, count)
el!:T
count > 0
 el! = head(elements)
 \mathit{elements'} = \mathit{tail}(\mathit{elements})
 count' = count - 1
 _ Top _____
 el!:T
count > 0
el! = head(elements)
 elements' = elements
 count' = count
```

# Instantiating a stack of natural numbers

#### Inheritance

- A class in Object-Z may be specified as a <u>specialization</u> or <u>extension</u> of another class using inheritance.
- A class S can inherit another class P by including the name of the parent class after the visibility list in S.

# Inheritance for specialization

 The subclass is a specialized version of the parent class, and thus satisfies the specification (interface) of the parent class in all relevant aspects, adding any particular behavior through overriding.

#### Inheritance for extension

• A subclass merely adds new behavior and does not modify or alter any of the inherited features.

## Inheritance /cont.

- The subclass inherits every feature (variables, constants, initial state schema and operations), except the visibility list.
- The subclass must define its own visibility list.
- This implies that a feature that is declared private in the parent class may now be declared as visible, and vice versa: A visible feature from the parent class can now be declared as private by not being included in the visibility list of the subclass.

# State and behavior in the presence of inheritance

- State variables in the parent class are merged with those of the subclass.
- The subclass may redefine a state variable, but only in a compatible way, expanding or restricting the type of a variable with the same name, for example restricting an integer variable to one that can hold only positive integers.

# State and behavior in the presence of inheritance /cont.

- If an operation is redefined in the subclass, the declaration of an operation in the parent class is merged with that of the same operation in the subclass.
- An operation's predicate part is conjoined with that of the same operation in the subclass.

# Subclassifying Stack to define BoundedStack Inheritance for *specialization*

$\_BoundedStack[T]$
$\uparrow (Push, Pop, Top)$ Stack[T]
$capacity: \mathbb{N}$
$count \le capacity$
INIT
capacity = 10
Push
count < capacity

## Example 2: Queue ADT

Front of Rear of Queue Queue

$$\Lambda = \langle el_1, el_2, ..., el_n \rangle$$

Head of  $\Lambda$ 

#### Queue ADT – State schema

 $\begin{array}{l} elements: seq \ T \\ count = \mathbb{N} \end{array}$ 

count >= 0

#### Initialization of state

$$\begin{array}{c}
INIT \\
elements = \langle \rangle \\
count = 0
\end{array}$$

### **Operation Enqueue**

### **Operation Dequeue**

# Instantiating a queue of natural numbers

 $. Int Queue \_\_\_$ 

 $items: \overline{Queue(\mathbb{N})}$ 

 $Enqueue \stackrel{\frown}{=} items. Enqueue$ 

Dequeue = items. Dequeue

# Subclassifying Queue to define BoundedQueue Inheritance for *specialization*

```
BoundedQueue[T]
(Enqueue, Dequeue)
Queue[T]
 capacity: \mathbb{N}
 count \le capacity
 capacity = 10
  Enqueue _____
 count < capacity
```

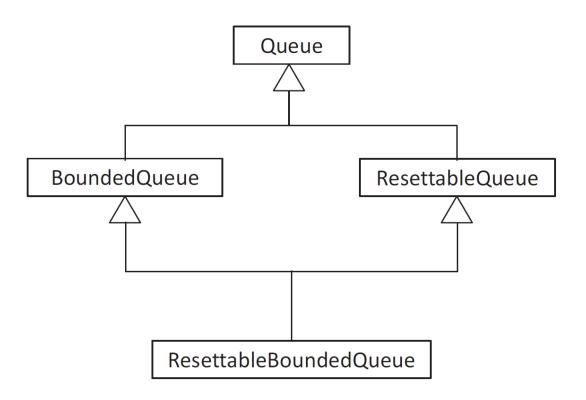
# Subclassifying Queue to define RessetableQueue Inheritance for *extension*

```
 \begin{array}{c|c} ResettableQueue[T] \\ & \upharpoonright (Enqueue, Dequeue, Reset) \\ & Queue[T] \\ & -Reset \\ & \Delta(elements, count) \\ & elements' = \langle \rangle \\ & count' = 0 \\ & \\ \end{array}
```

#### Inheritance for combination

- Object-Z supports multiple inheritance.
- A subclass is formed by combining features from more than one types.

# Multiple inheritance



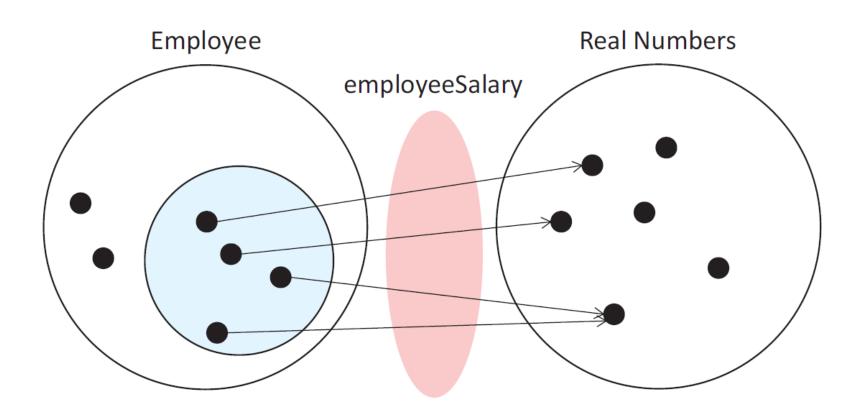
# Class RessetableBoundedQueue Inheritance for *combination*

```
\_ResettableBoundedQueue[T]\_
\uparrow (Enqueue, Dequeue, Reset)
BoundedQueue[T]
ResettableQueue[T]
```

# Handling errors and providing robust specifications

Name
$\uparrow (Op_1)$
$\_Op_1OK$
Success
result!: Report
result! = ok
Error
result!: Report
result! = error
$Op_1 = (Op_1OK \land Success) \oplus Error$
CPI (CPICIT / Duccess) & Ziver

# Example: Managing employees



# Interface, state schema and initialization

```
\uparrow (AddEmployee, DeleteEmployee, ModifySalary)
```

```
employeeSalary: Employee \rightarrow \mathbb{R}
```

 $\forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0$ 

INIT

 $employeeSalary = \varnothing$ 

# Operation AddEmployee

```
 \begin{array}{c} -AddEmployee \\ \Delta(employeeSalary) \\ newEmployee?: Employee \\ salary?: \mathbb{R} \\ \hline salary? > 0.0 \\ newEmployee? \not\in \text{dom } employeeSalary \\ employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\} \end{array}
```

## Operation DeleteEmployee

```
DeleteEmployee \_
\Delta(employeeSalary)
who? : Employee
who? \in dom \ employeeSalary
employeeSalary' = \{who?\} \lessdot employeeSalary
```

# Operation ModifySalary

# Examining the specification: Initial state

 $\forall d: \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark$  Invariant

 $INIT \underline{\hspace{1cm}}$   $employeeSalary = \varnothing$ 

# AddEmployee(Syd, 90)

employeeSalary dom employeeSalary ran employeeSalary { }

 $\forall d: dom \ employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark$  Invariant

 $\Delta (employeeSalary)$ 

newEmployee?: Employee

 $salary?: \mathbb{R}$ 

salary? > 0.0  $\checkmark$   $newEmployee? 
otin doment doment density <math>\checkmark$  Precondition

 $employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}$ 

## AddEmployee(Syd, 90)

```
employeeSalary
                                dom employeeSalary
                                                                 ran employeeSalary
                                        { Syd }
                                                                          { 90 }
   (Syd, 90)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
        \_AddEmployee .
        \Delta(employeeSalary)
         newEmployee?: Employee
         salary?: \mathbb{R}
         salary? > 0.0
                                                                   Postcondition
         newEmployee? \not\in dom \ employeeSalary
         employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}
```

## AddEmployee(David, 100)

```
employeeSalary
                               dom employeeSalary
                                                                ran employeeSalary
                                       { Syd }
                                                                         { 90 }
   (Syd, 90)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
        AddEmployee
        \Delta(employeeSalary)
        newEmployee?: Employee
        salary?: \mathbb{R}
        salary? > 0.0
                                                        Precondition
        newEmployee? \not\in dom\ employeeSalary
        employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}
```

## AddEmployee(David, 100)

```
employeeSalary
                               dom employeeSalary
                                                                ran employeeSalary
                                    { Syd, David }
                                                                       { 90, 100 }
  (Syd, 90),
  (David, 100)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
        \_AddEmployee
        \Delta(employeeSalary)
        newEmployee?: Employee
        salary?: \mathbb{R}
        salary? > 0.0
                                                                  Postcondition
        newEmployee? \not\in dom \ employeeSalary
        employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}
```

## AddEmployee(Roger, 100)

```
employeeSalary
                               dom employeeSalary
                                                                ran employeeSalary
                                                                       { 90, 100 }
                                    { Syd, David }
  (Syd, 90),
  (David, 100)
       \forall d : dom \ employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
        AddEmployee
        \Delta(employeeSalary)
        newEmployee?: Employee
        salary?: \mathbb{R}
        salary? > 0.0
                                                         Precondition
        newEmployee? \not\in dom\ employeeSalary\ \checkmark
        employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}
```

## AddEmployee(Roger, 100)

```
employeeSalary
                               dom employeeSalary
                                                               ran employeeSalary
                                 { Syd, David, Roger }
                                                                      { 90, 100 }
  (Syd, 90),
  (David, 100),
   (Roger, 100)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
        AddEmployee
        \Delta(employeeSalary)
        newEmployee?: Employee
        salary?: \mathbb{R}
        salary? > 0.0
                                                                  Postcondition
        newEmployee? \not\in dom \ employeeSalary
        employeeSalary' = employeeSalary \cup \{newEmployee? \mapsto salary?\}
```

## DeleteEmployee(Syd)

```
employeeSalary
                               dom employeeSalary
                                                                ran employeeSalary
                                 { Syd, David, Roger }
                                                                       { 90, 100 }
   (Syd, 90),
   (David, 100),
   (Roger, 100)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
          DeleteEmployee _____
         \Delta(employeeSalary)
         who?: Employee
         [who? \in dom\ employeeSalary\ \checkmark]
                                                         Precondition
         employeeSalary' = \{who?\} \triangleleft employeeSalary
```

## DeleteEmployee(Syd)

```
employeeSalary
                                  dom employeeSalary
                                                                     ran employeeSalary
                                    { <del>Syd,</del> David, Roger }
                                                                             <del>{ 90,</del> 100 }
  <del>(Syd, 90)</del>,
   (David, 100),
   (Roger, 100)
       \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
          .\,Delete Employee .
          \Delta(employeeSalary)
          who?: Employee
          who? \in dom\ employeeSalary
          employeeSalary' = \{who?\} \triangleleft employeeSalary\}
                                                                     Postcondition
```

## ModifySalary(David, 110)

```
employeeSalary
                                dom employeeSalary
                                                                  ran employeeSalary
                                  { David, Roger }
                                                                          { 100 }
   (David, 100),
   (Roger, 100)
        \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark \text{Invariant}
          ModifySalary
          \Delta(employeeSalary)
          employee?: Employee
          newSalary? : \mathbb{R}
          newSalary? > 0.0
                                                           Precondition
          employee? \in dom \ employeeSalary \checkmark
          employeeSalary' = employeeSalary \oplus \{employee? \mapsto newSalary?\}
```

## ModifySalary(David, 110)

```
employeeSalary
                               dom employeeSalary
                                                                ran employeeSalary
                                 { David, Roger }
                                                                      { 100, 110 }
  (David, 110),
  (Roger, 100)
        \forall d : \text{dom } employeeSalary \bullet employeeSalary(d) > 0.0 \checkmark
          ModifySalary _____
         \Delta(employeeSalary)
          employee?: Employee
         newSalary? : \mathbb{R}
         newSalary? > 0.0
                                                                  Postcondition
          employee? \in dom \ employeeSalary
          employeeSalary' = employeeSalary \oplus \{employee? \mapsto newSalary?\}
```

# Example: CreditCard Visibility list, constants, state and initialization

```
CreditCard _____
\uparrow (Withdraw, Deposit, GetAvailableFunds)
 number: \mathbb{N}
 limit: \mathbb{R}
 limit \in \{1000, 5000, 10000\}
  balance: \mathbb{R}
  balance + limit \ge 0
  balance = 0
```

### **Operation Withdraw**

```
 \begin{array}{c} -Withdraw \\ \Delta(balance) \\ amount?: \mathbb{R} \\ \hline \\ amount? > 0 \\ amount? \leq balance + limit \\ balance' = balance - amount? \end{array}
```

### **Operation Deposit**

### Operation GetAvailableFunds

# Example: CreditCard2 Subclassifying CreditCard

```
CreditCard2
\uparrow (Withdraw, Deposit, GetAvailableFunds)
CreditCard
 with drawals: \mathbb{N}
 INIT
 with drawals = 0
 Withdraw ____
 \Delta(withdrawals)
 withdrawals' = withdrawals + 1
```

# Example: CreditCompany Visibility list, state and initialization

```
CreditCompany ______
\uparrow (AddAccount, DeleteAccount)
 accounts: \mathbb{P} CreditCard
 count: \mathbb{N}
 \forall a_i, a_i : accounts \bullet a_i.number \neq a_j.number
  count = \#accounts
```

### Operation AddAccount

```
\Delta (account)
account?: CreditCard
account? \not\in accounts
accounts' = accounts \cup \{account?\}
count' = count + 1
```

### Operation DeleteAccount

```
DeleteAccount
\Delta(accounts)
account?: CreditCard
account? \in accounts
accounts' = accounts \setminus \{account?\}
count' = count - 1
```

## Inheritance and subtyping

- Each class defines a type and all instances of the class constitute legitimate values of that type.
- Every instance of a subclass is also an instance of a superclass, but not vice-versa.
- The type defined by the subclass is a subset of the type defined by its superclasses as the set of all instances of a subclass is included in the set of all instances of its superclass.

## Polymorphism

In

*account* :↓ *Account* 

variable *account* can hold an instance of *Account* or any of its subclasses.

The declaration

 $accounts : \mathbb{P} \downarrow Account$ 

indicates that *account* is a set of elements from *Account* as well as from any of its subclasses.

# Example: Bank [To be covered in tutorials this week]

Account\_\_\_\_\_ [ (accountNumber, Deposit, Withdraw) SavingsAccount \_\_\_\_\_ [ (accountNumber, balance, Deposit, Withdraw) Account Bank\_\_  $accounts : \mathbb{P} \downarrow Account$  $\forall a_1, a_2 : accounts \bullet a_1.accountNumber = a_2.accountNumber \Leftrightarrow a_1 = a_2$ 

# Cancellation and redefinition of features through renaming

A[T]	
x:T	
$y: \mathbb{P}T$	_
$x \in y$	
<i>Op</i>	
$Dp$ $\Delta(x)$	
x?:T	_
$x? \in y$	
x' = x?	

# Cancellation and redefinition of features through renaming /cont.

```
\begin{array}{c|c}
-B[T] \\
& \upharpoonright (Op) \\
A[y1/y, Op1/Op]
\end{array}

    y: bag T
        x \in y
```

## Explicit redefinition and removal of operations

```
BoundedStack[T][\mathbf{redef}\ Push]
 \Delta(elements, count)
  item?:T
  count < capacity - 1
  elements' = \langle item?, item? \rangle \frown elements
  count' = count + 2
```

## Explicit redefinition and removal of operations /cont.

$$OnlyPushStack[T]$$
  $(Push)$   $Stack[T][\mathbf{remove}\ Pop]$