

---

# COMP 472: Artificial Intelligence

## Machine Learning

### Naive Bayes Classification *video #2*

- Russell & Norvig: Sections 12.2 to 12.6

---

# Today

1. Introduction to ML
2. Naïve Bayes Classification
  - a. Application to Spam Filtering
3. Decision Trees
4. ( Evaluation
5. Unsupervised Learning )
6. Neural Networks
  - a. Perceptrons
  - b. Multi Layered Neural Networks



# Motivation

- How do we represent and reason when there<sup>R</sup> is uncertainly in the necessary knowledge?
  - It might rain tonight
  - If you have red spots on your face, you might have the measles
  - This e-mail is most likely spam
  - I can't read this character, but it looks like a "B"
  - These 2 pictures are very likely of the same person
  - ...
- One way, is to use probability theory

# Remember...

## ■ P is a probability function:

- $0 \leq P(A) \leq 1$
- $P(A) = 0 \Rightarrow$  the event A will never take place
- $P(A) = 1 \Rightarrow$  the event A must take place
- $\sum_i P(A_i) = 1 \Rightarrow$  one of the outcomes A<sub>i</sub> will take place
- $P(A) + P(\sim A) = 1$



## ■ Joint probability

- intersection  $A_1 \cap \dots \cap A_n$  is an event that takes place if all the events A<sub>1</sub>, ..., A<sub>n</sub> take place
- denoted  $P(A \cap B)$  or  $P(A, B)$

## ■ Sum Rule

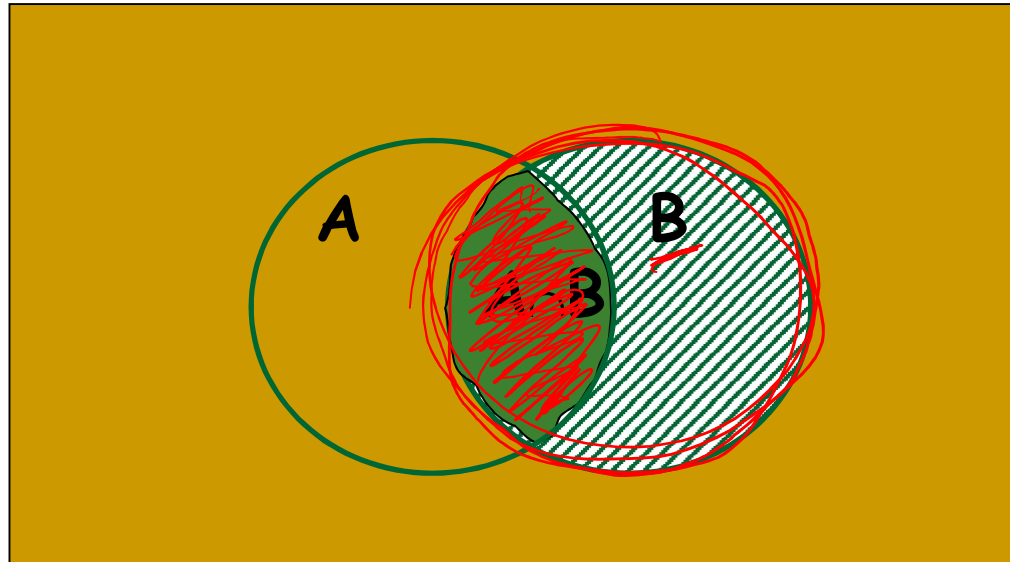
- union  $A_1 \cup \dots \cup A_n$  is an event that takes place if at least one of the events A<sub>1</sub>, ..., A<sub>n</sub> takes place
- denoted  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

# Conditional Probability

- Prior (or unconditional) probability
  - Probability of an event before any evidence is obtained
  - $P(A) = 0.1$                        $P(\text{rain today}) = 0.1$
  - i.e. Your belief about A given that you have no evidence
- Posterior (or conditional) probability
  - Probability of an event given that you know that B is true (B = some evidence)
  - $P(A|B) = 0.8$      $P(\text{rain today} | \text{cloudy}) = 0.8$
  - i.e. Your belief about A given that you know B

# Conditional Probability (con't)

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(A, B)}{P(B)}$$



# Chain Rule

- With 2 events, the probability that  $A$  and  $B$  occur is:

$$P(A, B) = P(A | B) \times P(B)$$

- With 3 events, the probability that  $A$ ,  $B$  and  $C$  occur is:
  - The probability that  $A$  occurs
  - Times, the probability that  $B$  occurs, assuming that  $A$  occurred
  - Times, the probability that  $C$  occurs, assuming that  $A$  and  $B$  have occurred

- With  $n$  events, we can generalize to the Chain rule:

$$P(A_1, A_2, A_3, A_4, \dots, A_n)$$

$$= P(\cap A_i)$$

$$= P(A_1) \times P(A_2 | A_1) \times P(A_3 | A_1, A_2) \times \dots \times P(A_n | A_1, A_2, A_3, \dots, A_{n-1})$$

---

# So what?

- we can do probabilistic inference
  - i.e. infer new knowledge from observed evidence



# Example 1

- Joint probability distribution:

$P(\text{Toothache} \cap \text{Cavity})$

*evidence*

*hypothesis*

	Toothache	$\sim$ Toothache
Cavity	0.04	0.06
$\sim$ Cavity	0.01	0.89

$P(\text{toothache}) = 0.05$      $P(\sim \text{toothache}) = 0.9$      $\Sigma = 1$   
 $P(\text{cavity}) = 0.1$      $P(\sim \text{cavity}) = 0.9$

$$P(H|E) = \frac{P(H \cap E)}{P(E)}$$

$$P(\text{cavity} | \text{toothache}) = \frac{P(\text{cavity} \cap \text{toothache})}{P(\text{toothache})} = \frac{0.04}{0.04 + 0.01} = 0.8$$

# Getting the Probabilities

- in most applications, you just count from a set of observations

$$\underline{P(A)} = \frac{\underline{\text{count\_of\_A}}}{\underline{\text{count\_of\_all\_events}}}$$

$$\underline{P(A|B)} = \frac{\underline{P(A \cap B)}}{\underline{P(B)}} = \frac{\underline{\text{count\_of\_A\_and\_B\_together}}}{\underline{\text{count\_of\_all\_B}}}$$

# Combining Evidence

- Assume now 2 pieces of evidence:
- Suppose, we know that
  - $P(\text{Cavity} \mid \text{Toothache}) = 0.12$
  - $P(\text{Cavity} \mid \text{Young}) = 0.18$
- A patient complains about Toothache and is Young...
  - what is  $P(\text{Cavity} \mid \text{Toothache} \cap \text{Young})$ ?

# Combining Evidence

	Toothache		~Toothache		evidence #1
	Young	~ Young	Young	~ Young	evidence #2
Cavity	0.108	0.012	0.072	0.008	
~Cavity	0.016	0.064	0.144	0.576	

$P(\text{Toothache} \cap \text{Cavity} \cap \text{Young})$

- But how do we get the data ?
- In reality, we may have dozens, hundreds of variables
- We cannot have a table with the probability of all possible combinations of variables
  - Ex. with 16 binary variables, we would need  $2^{16}$  entries

# Independent Events

- In real life:

- some variables are independent...

- eg: living in Montreal & tossing a coin

- $P(\text{Montreal, head}) = P(\text{Montreal}) * P(\text{head})$

- eg: probability of tossing 2 heads in a row

- $P(\text{head, head}) = 1/2 * 1/2 = 1/4$

- some variables are not independent...

- eg: living in Montreal & wearing boots

- $P(\text{Montreal, boots}) \neq P(\text{Montreal}) * P(\text{boots})$

# Independent Events

- Two events A and B are independent:
  - if the occurrence of one of them does not influence the occurrence of the other
  - i.e. A is independent of B if  $P(A) = P(A|B)$
- If A and B are independent, then:
  - $P(A, B) = P(A|B) \times P(B)$  (by chain rule) // see previous slide 7  
     $= P(A) \times P(B)$  (by independence)
- To make things work in real applications, we often assume that events are independent
  - $P(A, B) = P(A) \times P(B)$

# Conditional Independent Events

- Two events  $A$  and  $B$  are conditionally independent given  $C$ :
  - Given that  $C$  is true, then any evidence about  $B$  cannot change our belief about  $A$
  - $P(A, B \mid C) = P(A \mid C) \times P(B \mid C)$ .  
*when  $C$  is True*

# Bayes' Theorem

■ given:

$$P(A|B) = \frac{P(A,B)}{P(B)} \quad \text{so } P(A,B) = P(A|B) \times P(B)$$
$$P(B|A) = \frac{P(A,B)}{P(A)} \quad \text{so } P(A,B) = P(B|A) \times P(A)$$

■ then:

$$P(A|B) \times P(B) = P(B|A) \times P(A)$$

■ and:

$$P(A|B) = \frac{P(B|A) \times P(A)}{P(B)}$$



# So?

- We typically want to know:  $P(\text{Hypothesis}^A \mid \text{Evidence}^B)$ 
  - $P(\text{Disease} \mid \text{Symptoms}) \dots P(\text{meningitis} \mid \text{red spots})$
  - $P(\text{Cause} \mid \text{Side Effect}) \dots P(\text{misaligned brakes} \mid \text{squeaky wheels})$
- But  $P(\text{Hypothesis}^A \mid \text{Evidence}^B)$  is hard to gather
  - ex: out of all people who have red spots... how many have meningitis?
- However  $P(\text{Evidence}^B \mid \text{Hypothesis}^A)$  is easier to gather
  - ex: out of all people who have the meningitis ... how many have red spots?
- So
$$P(\text{Hypothesis} \mid \text{Evidence}) = \frac{P(\text{Evidence} \mid \text{Hypothesis}) \times P(\text{Hypothesis})}{P(\text{Evidence})}$$

*hard to gather* (pointing to the left side of the equation)  
*easy to gather* (pointing to the right side of the equation)  
*easy to gather* (pointing to the denominator)  
*hard to gather* (pointing to the denominator)

# Example 2

Assume we only have 1 hypothesis

Assume:

- $P(\text{spots=yes} \mid \text{meningitis=yes}) = 0.4$

- $P(\text{meningitis=yes}) = 0.00003$

- $P(\text{spots=yes}) = 0.05$

$$P(\text{meningitis=yes} \mid \text{spots=yes})$$

$$= \frac{P(\text{spots=yes} \mid \text{meningitis=yes}) \times P(\text{meningitis=yes})}{P(\text{spots=yes})}$$

$$= \frac{0.4 \times 0.00003}{0.05} = 0.00024$$

→ If you have spots... you are more likely to have meningitis than if we don't know about you having spots

# Example 3

- Predict the weather tomorrow based on tonight's sunset...
- Assume we have 3 hypothesis...
  - $H_1$ : weather will be nice  $P(H_1) = 0.2$
  - $H_2$ : weather will be bad  $P(H_2) = 0.5$
  - $H_3$ : weather will be mixed  $P(H_3) = 0.3$
- And 1 piece of evidence with 3 possible values
  - $E_1$ : today, there's a beautiful sunset
  - $E_2$ : today, there's a average sunset
  - $E_3$ : today, there's no sunset

evidence  
feature

$P(E_2 | H_1)$

$P(E_x   H_i)$	$E_1$	$E_2$	$E_3$
$H_1$	0.7	0.2	0.1
$H_2$	0.3	0.3	0.4
$H_3$	0.4	0.4	0.2

# Example 3

- Observation: average sunset ( $E_2$ )
- Question: how will be the weather tomorrow?
  - $P(H_i | E_2)$  ?
  - predict the weather that maximizes the probability  $P(H_i)$
  - select  $H_i$  such that  $P(H_i | E_2)$  is the greatest

$$P(H_i | E_2) = \frac{P(H_i) \times P(E_2 | H_i)}{P(E_2)}$$

$$P(E_2) = P(H_1) \times P(E_2 | H_1) + P(H_2) \times P(E_2 | H_2) + P(H_3) \times P(E_2 | H_3)$$
$$= .2 \times .2 + .5 \times .3 + .3 \times .4 = .04 + .15 + .12 = 0.31$$

# Example 3

$P(H_1   E_2) = \frac{P(H_1) \times P(E_2   H_1)}{P(E_2)} = \frac{.2 \times .2}{.31} = .129$
$P(H_2   E_2) = \frac{P(H_2) \times P(E_2   H_2)}{P(E_2)} = \frac{.5 \times .3}{.31} = .484$
$P(H_3   E_2) = \frac{P(H_3) \times P(E_2   H_3)}{P(E_2)} = \frac{.3 \times .4}{.31} = .387$

*H<sub>2</sub> will still have the highest score*

*the argument*

⇒ H<sub>2</sub> is the most likely hypothesis, given the evidence

P(H<sub>2</sub> | E<sub>2</sub>) is the highest

Tomorrow the weather will be bad *H<sub>2</sub>*

$$H_{NB} = \underset{H_i}{\operatorname{argmax}} \frac{P(H_i) \times P(E | H_i)}{P(E)}$$

*select H<sub>i</sub> that maximize the function*

*H<sub>2</sub>*

# Bayes' Reasoning

- Out of n hypothesis...
  - we want to find the most probable  $H_i$  given the evidence  $E$
- So we choose the  $H_i$  with the largest  $P(H_i|E)$

$$H_{NB} = \underset{H_i}{\operatorname{argmax}} P(H_i | E) = \underset{H_i}{\operatorname{argmax}} \frac{P(H_i) \times P(E | H_i)}{P(E)}$$

- But...  $P(E)$ 
  - is the same for all possible  $H_i$  (and is hard to gather anyways)
  - so we can drop it
- So Bayesian reasoning:

$$H_{NB} = \underset{H_i}{\operatorname{argmax}} \frac{P(H_i) \times P(E | H_i)}{P(E)} = \underset{H_i}{\operatorname{argmax}} \boxed{P(H_i) \times P(E | H_i)}$$

*prior*

# Representing the Evidence

- The evidence is typically represented by many attributes/features 100's 1000's
  - beautiful sunset? clouds? temperature? summer?, ...
- so often represented as a feature/attribute vector ↔ =

	evidence					hypothesis
	sunset	clouds	temp	summer		weather
	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>		tomorrow
<u>e1</u>	<u>beautiful</u>	<u>no</u>	<u>high</u>	<u>yes</u>		<u>Nice</u>

- e1 = <sunset:beautiful, clouds:no, temp:high, summer:yes>  
features      values

# Combining Evidence

toothache	young	cavity
yes	yes	?

$$P(\text{Cavity} = \text{yes} | \text{Toothache} = \text{yes} \cap \text{Young} = \text{yes}) = ?$$

with Bayes Rule :

$$= \frac{P(\text{Toothache} = \text{yes} \cap \text{Young} = \text{yes} | \text{Cavity} = \text{yes}) \times P(\text{Cavity} = \text{yes})}{P(\text{Toothache} = \text{yes} \cap \text{Young} = \text{yes})}$$

with independence assumption :

$$= \frac{P(\text{Toothache} = \text{yes} | \text{Cavity} = \text{yes}) \times P(\text{Young} = \text{yes} | \text{Cavity} = \text{yes}) \times P(\text{Cavity} = \text{yes})}{P(\text{Toothache} = \text{yes}) \times P(\text{Young} = \text{yes})}$$

with conditional independence assumption :

$$= \frac{P(\text{Toothache} = \text{yes} | \text{Cavity} = \text{yes}) \times P(\text{Young} = \text{yes} | \text{Cavity} = \text{yes}) \times P(\text{Cavity} = \text{yes})}{P(\text{Toothache} = \text{yes}) \times P(\text{Young} = \text{yes})}$$

Now we have decomposed the joint probability distribution into much smaller pieces...



# Combining Evidence

<sup>a<sub>1</sub></sup> <sub>e<sub>1</sub></sub> toothache	<sup>a<sub>2</sub></sup> <sub>e<sub>2</sub></sub> young	cavity
yes	yes	yes? or no?

But since we only care about ranking the hypothesis...

?  $P(\text{Cavity} = \text{yes} \mid \text{Toothache} = \text{yes} \cap \text{Young} = \text{yes})$

$P(\text{Cavity} = \text{no} \mid \text{Toothache} = \text{yes} \cap \text{Young} = \text{yes})$

? 
$$\frac{P(\text{Cavity} = \text{yes}) \times P(\text{Toothache} = \text{yes} \mid \text{Cavity} = \text{yes}) \times P(\text{Young} = \text{yes} \mid \text{Cavity} = \text{yes})}{P(\text{Toothache} = \text{yes}) \times P(\text{Young} = \text{yes})}$$

$$\frac{P(\text{Cavity} = \text{no}) \times P(\text{Toothache} = \text{yes} \mid \text{Cavity} = \text{no}) \times P(\text{Young} = \text{yes} \mid \text{Cavity} = \text{no})}{P(\text{Toothache} = \text{yes}) \times P(\text{Young} = \text{yes})}$$

?  $P(\text{Cavity} = \text{yes}) \times P(\text{Toothache} = \text{yes} \mid \text{Cavity} = \text{yes}) \times P(\text{Young} = \text{yes} \mid \text{Cavity} = \text{yes})$

$P(\text{Cavity} = \text{no}) \times P(\text{Toothache} = \text{yes} \mid \text{Cavity} = \text{no}) \times P(\text{Young} = \text{yes} \mid \text{Cavity} = \text{no})$

$$H_{\text{NB}} = \underset{H_i}{\operatorname{argmax}} \frac{P(H_i) \times P(E \mid H_i)}{P(E)} = \underset{H_i}{\operatorname{argmax}} P(H_i) \times P(E \mid H_i) = \underset{H_i}{\operatorname{argmax}} P(H_i) \times P(\langle a_1, a_2, a_3, \dots, a_n \rangle \mid H_i) = \underset{H_i}{\operatorname{argmax}} P(H_i) \times \prod_{j=1}^n P(a_j \mid H_i)$$

# Example 4

many pieces of evidence

features / attributes

2 hypothesis  
2 classes

Day	Outlook	Temperature	Humidity	Wind	Play Tennis
Day1	Sunny	Hot	High	Weak	No
Day2	Sunny	Hot	High	Strong	No
Day3	Overcast	Hot	High	Weak	Yes
Day4	Rain	Mild	High	Weak	Yes
Day5	Rain	Cool	Normal	Weak	Yes
Day6	Rain	Cool	Normal	Strong	No
Day7	Overcast	Cool	Normal	Strong	Yes
Day8	Sunny	Mild	High	Weak	No
Day9	Sunny	Cool	Normal	Weak	Yes
Day10	Rain	Mild	Normal	Weak	Yes
Day11	Sunny	Mild	Normal	Strong	Yes
Day12	Overcast	Mild	High	Strong	Yes
Day13	Overcast	Hot	Normal	Weak	Yes
Day14	Rain	Mild	High	Strong	No

14 days

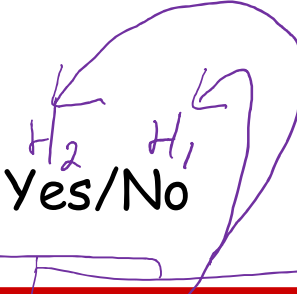
$H_1$  = no tennis  
 $H_2$  = play tennis

$$P(H_2) = \frac{9}{14}$$

$$P(H_1) = \frac{5}{14}$$

# Example 4

- Goal: Given a new instance  $X = \langle a_1, \dots, a_n \rangle$ , classify as Yes/No


$$H_{NB} = \operatorname{argmax}_{H_i} \frac{P(H_i) \times P(E | H_i)}{P(E)} = \operatorname{argmax}_{H_i} P(H_i) \times P(E | H_i) = \operatorname{argmax}_{H_i} P(H_i) \times P(\langle a_1, a_2, a_3, \dots, a_n \rangle | H_i) = \operatorname{argmax}_{H_i} P(H_i) \times \prod_{j=1}^n P(a_j | H_i)$$

- Naïve Bayes: Assumes that the attributes/features are conditionally independent given the hypothesis

# Example 4

- Goal: Given a new instance  $X = \langle a_1, \dots, a_n \rangle$ , classify as Yes/No

$$H_{NB} = \operatorname{argmax}_{H_i} P(H_i) \times \prod_{j=1}^n P(a_j | H_i)$$

1. 1st estimate the probabilities from the training examples:
  - a) For each hypothesis  $H_i$  estimate  $P(H_i)$
  - b) For each attribute value  $a_j$  of each instance (evidence) estimate  $P(a_j | H_i)$

# Example 4

## 1. TRAIN:

- compute the probabilities from the training set

$$P(\text{PlayTennis} = \overset{H_2}{\text{yes}}) = 9/14 = 0.64$$

$$P(\text{PlayTennis} = \text{no}) = 5/14 = 0.36$$

prior probabilities  $P(H_i)$

*feature  $H_1$  value*

$$P(\text{Out} = \text{sunny} \mid \text{PlayTennis} = \overset{H_2}{\text{yes}}) = 2/9 = 0.22$$

$$P(\text{Out} = \text{sunny} \mid \text{PlayTennis} = \overset{H_1}{\text{no}}) = 3/5 = 0.60$$

$$P(\text{Out} = \text{rain} \mid \text{PlayTennis} = \text{yes}) = 3/9 = 0.33$$

$$P(\text{Out} = \text{rain} \mid \text{PlayTennis} = \text{no}) = 2/5 = 0.4$$

*$P(\text{out} = \text{overcast})$*   
...

$$P(\text{Wind} = \text{strong} \mid \text{PlayTennis} = \text{yes}) = 3/9 = 0.33$$

$$P(\text{Wind} = \text{strong} \mid \text{PlayTennis} = \text{no}) = 3/5 = 0.60$$

conditional probabilities

$P(a_j \mid H_i)$

# Example 4

## 2. TEST:

classify the new case:  $X = (\text{Outlook: Sunny, Temp: Cool, Hum: High, Wind: Strong})$

$$H_{NB} = \underset{H_i \in [\text{yes}, \text{no}]}{\operatorname{argmax}} P(H_i) \times P(X | H_i)$$

$$= \underset{H_i \in [\text{yes}, \text{no}]}{\operatorname{argmax}} P(H_i) \times \prod_j P(a_j | H_i)$$

$$= \underset{H_i \in [\text{yes}, \text{no}]}{\operatorname{argmax}} P(H_i) \times P(\text{Outlook} = \text{sunny} | H_i) \times P(\text{Temp} = \text{cool} | H_i)$$

$$\times P(\text{Humidity} = \text{high} | H_i) \times P(\text{Wind} = \text{strong} | H_i)$$

$$1) P(\text{PlayTennis} = \text{yes})$$

$$\times P(\text{Outlook} = \text{sunny} | \text{PlayTennis} = \text{yes}) \times P(\text{Temp} = \text{cool} | \text{PlayTennis} = \text{yes}) \times P(\text{Hum} = \text{high} | \text{PlayTennis} = \text{yes}) \times P(\text{Wind} = \text{strong} | \text{PlayTennis} = \text{yes})$$

$$= 0.0053$$

$$2) P(\text{PlayTennis} = \text{no})$$

$$\times P(\text{Outlook} = \text{sunny} | \text{PlayTennis} = \text{no}) \times P(\text{Temp} = \text{cool} | \text{PlayTennis} = \text{no}) \times P(\text{Hum} = \text{high} | \text{PlayTennis} = \text{no}) \times P(\text{Wind} = \text{strong} | \text{PlayTennis} = \text{no})$$

$$= 0.0206$$

$\Rightarrow$  answer :  $\text{PlayTennis}(X) = \text{no}$

prior

conditional

should have been computed in the previous slide

score  $H_2$

score  $H_1$

# Application of Bayesian Reasoning

## ■ Categorization: $P(\text{Category} \mid \text{Features of Object})$

- Diagnostic systems:  $P(\text{Disease} \mid \text{Symptoms})$
- Text classification:  $P(\text{sports\_news} \mid \text{text})$  *Handwritten: <.t., types, smoke*
- Character recognition:  $P(\text{character} \mid \text{bitmap})$
- Speech recognition:  $P(\text{words} \mid \text{acoustic signal})$
- Image processing:  $P(\text{face\_person} \mid \text{image features})$
- Spam filter:  $P(\text{spam\_message} \mid \text{words in e-mail})$
- ...

Handwritten notes and arrows:  
A box with three arrows pointing to:  
sports  
obituary  
politics



# Digit Recognition

$< 1, 1: 255, 1, 2: 100, \dots \dots \dots$

$28, 28: 255$

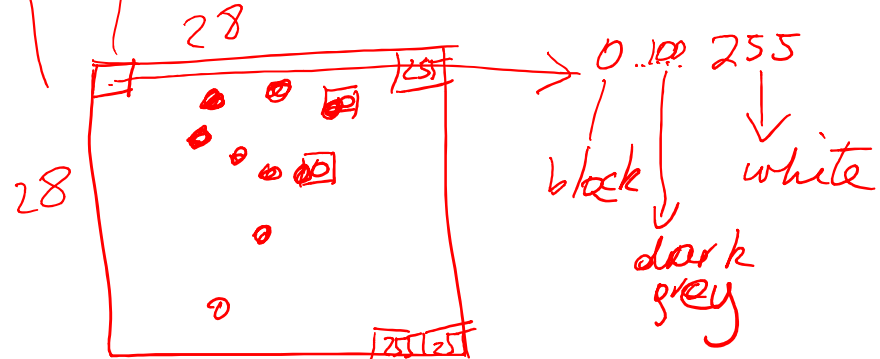
784 features

$H_0 = "0"$   
 $H_1 = "1"$   
 $\dots \dots \dots H_9$   
 10 hyp.

## MNIST dataset

- data set contains handwritten digits from the American Census Bureau employees and American high school students
- 28 x 28 grayscale images
- training set: 60,000 examples
- test set: 10,000 examples.
- Features: each pixel is used as a feature so:
  - there are  $28 \times 28 = 784$  features
  - each feature = 256 grayscale value
- Task: classify new digits into one of the 10 classes

0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
3	3	3	3	3	3	3	3	3	3	3	3	3	3	3
4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
5	5	5	5	5	5	5	5	5	5	5	5	5	5	5
6	6	6	6	6	6	6	6	6	6	6	6	6	6	6
7	7	7	7	7	7	7	7	7	7	7	7	7	7	7
8	8	8	8	8	8	8	8	8	8	8	8	8	8	8
9	9	9	9	9	9	9	9	9	9	9	9	9	9	9





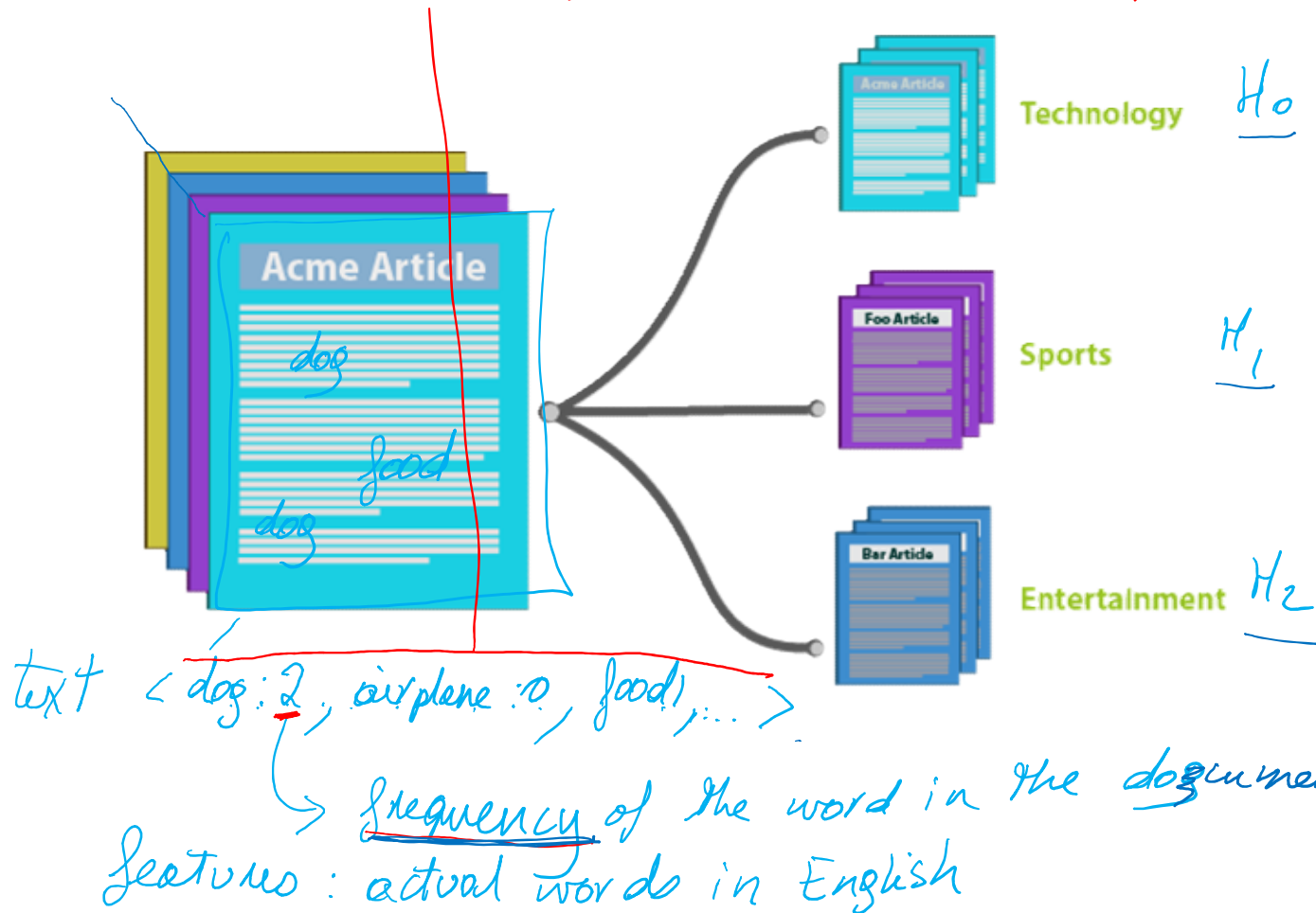
# Postal Code Recognition

BAM BAM  
42 T-REX RD.  
PANGAEA, RB 48016

FRED FLINSTONE  
69 OLD SCHOOL AVE  
BEDROCK, OLDEN-TOWN  
77005

# Text Classification

10 000 features (i.e. 1 feature for each word in the dictionary)



# Comments on Naïve Bayes Classification

- A simple probabilistic classifier based on Bayes' theorem
  - with strong (naive) independence assumption
  - i.e. the features/attributes are conditionally independent given the classes
    - eg: assumes that the word ambulance is conditionally independent of the word accident given the class SPORTS



$$p(\langle E \rangle / H_i) \\ \hookrightarrow \prod p(e_i / H_i)$$

- BUT:

- fast, simple
- gives confidence in its class predictions (i.e., the scores)
- surprisingly very effective on real-world tasks
- basis of many spam filters

$$\begin{aligned} \text{score}(H_1) &= 0.5 \\ \text{score}(H_2) &= 0.00 \\ \text{score}(H_3) &= 0.00001 \end{aligned}$$

# Today

1. Introduction to ML 
2. Naïve Bayes Classification *video #2*
  - a. Application to Spam Filtering *video #3*
3. Decision Trees
4. ( Evaluation
5. Unsupervised Learning )
6. Neural Networks
  - a. Perceptrons
  - b. Multi Layered Neural Networks

---

# Up Next

1. Introduction to ML
2. Naive Bayes Classification
  - a. Application to Spam Filtering
3. Decision Trees
4. ( Evaluation
5. Unsupervised Learning )
6. Neural Networks
  - a. Perceptrons
  - b. Multi Layered Neural Networks