COMP 472 Artificial Intelligence: Adversarial Search part 7 Alpha-Beta Pruning video 2

Russell & Norvig: Chapter 5

Today

- Adversarial Search
 - 1. Minimax
 - 2. Alpha-beta pruning

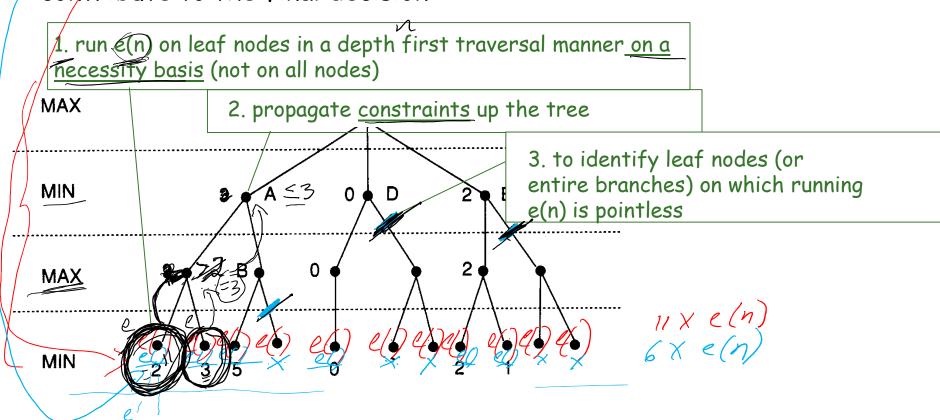


- 3. Other Adversarial Searc.
 - 1. Multiplayer Games
 - 2. Stochastic Games
 - 3. Monte Carlo Tree Search

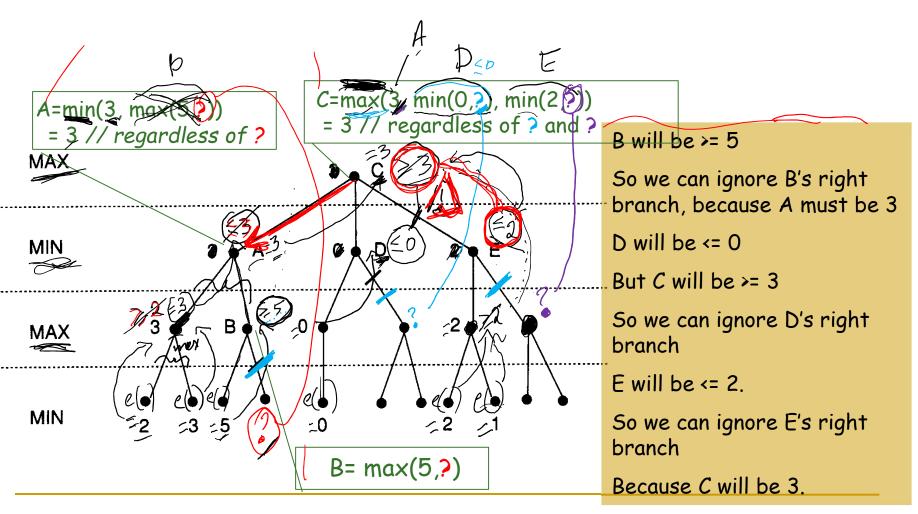
Alpha-Beta Pruning

- Optimization over Minimax, that:
 - ignores (cuts off/prunes) branches of the tree
 that cannot contribute to the solution
 - reduces branching factor
 - allows deeper search with same effort

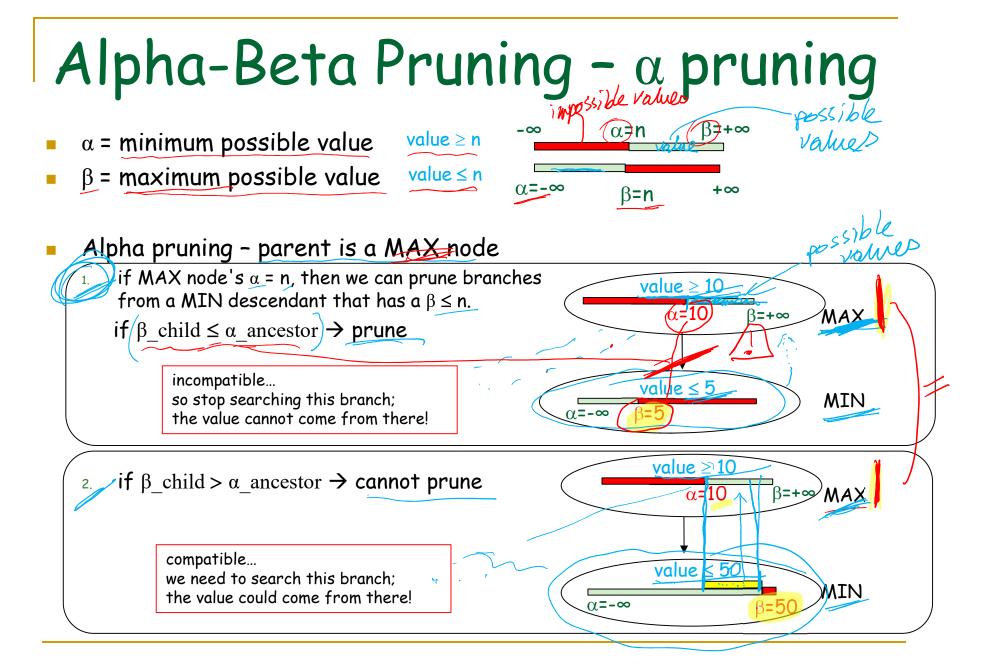
- With Minimax, we look at all nodes at depth n
- With α-β pruning, we ignore branches that could not possibly contribute to the final decision



source: G. Luger (2005)

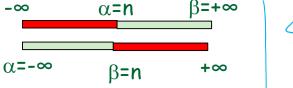


source: G. Luger (2005)



Alpha-Beta Pruning - \beta pruning

- α = minimum possible value
- value ≥ n
- β = maximum possible value
- value ≤ n



Some

Beta pruning - parent is a MIN node

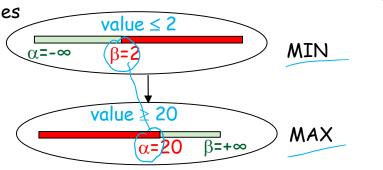
if a MIN node's β = n, then we can prune branches from a MAX descendant that has an $\alpha \ge n$.

if α _child $\geq \beta$ _ancestor \Rightarrow prune

incompatible...

so stop searching this branch;

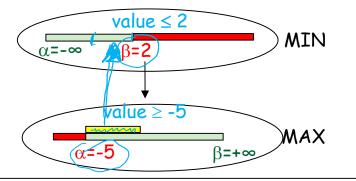
the value cannot come from there!



if $\alpha_{\text{child}} < \beta_{\text{ancestor}} \rightarrow \text{cannot prune}$

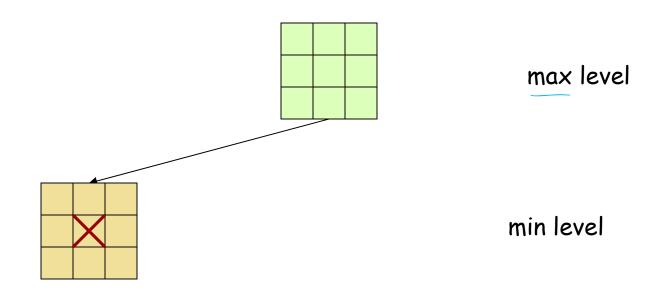
compatible...

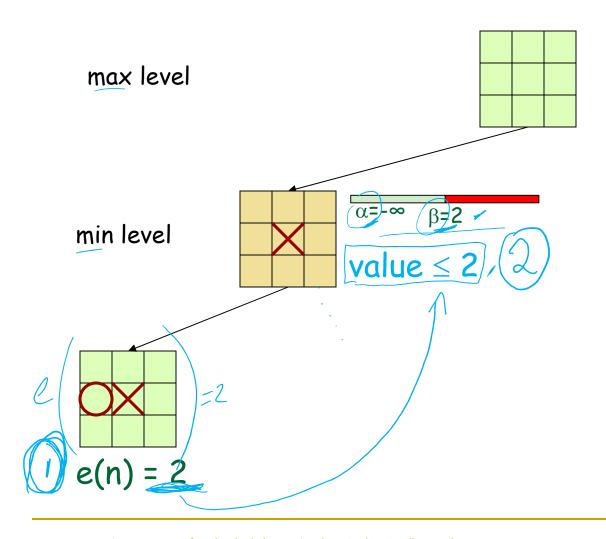
we need to search this branch; the value could come from there!

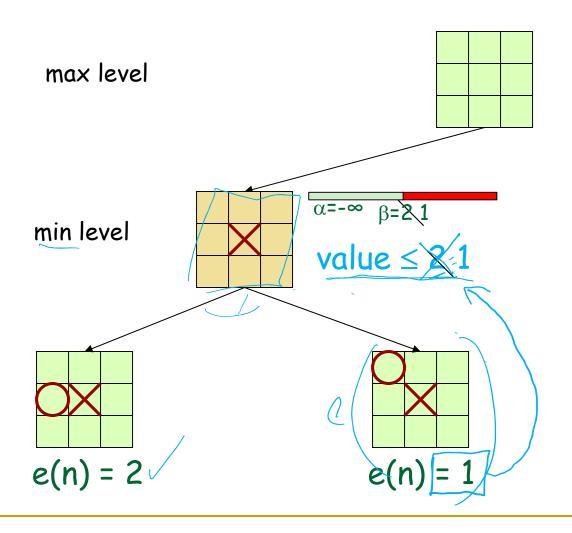


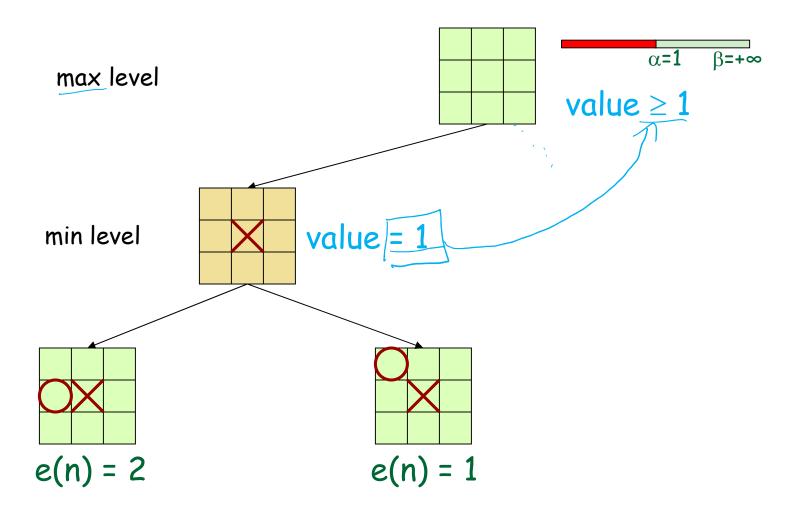
Alpha-Beta Pruning Algorithm

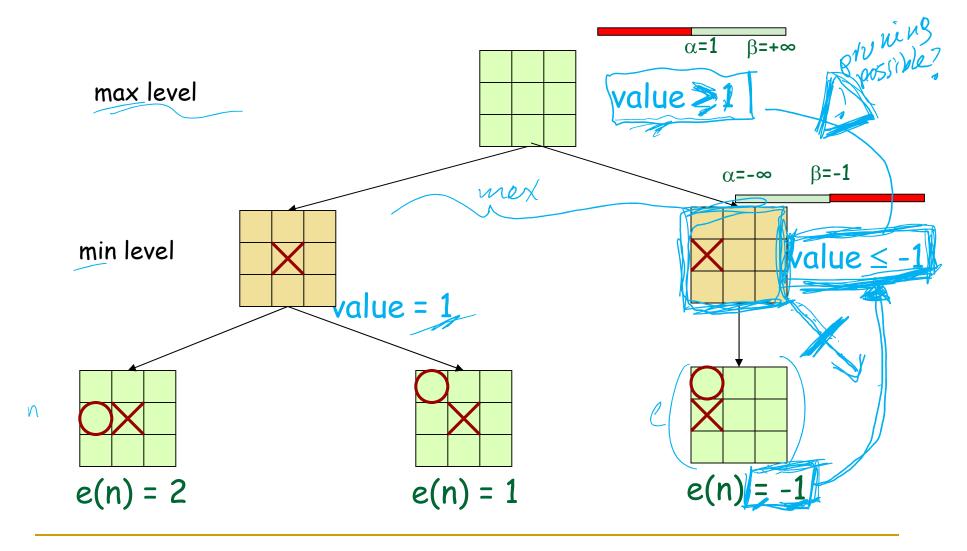
```
01 function alphabeta (node, depth, (\alpha/\beta) maximizing Player)
02
         if depth = 0 or node is a terminal node
03
              return the heuristic value of node
         if maximizingPlayer
04
                                                            Initial call:
0.5
              ∨ := -∞
                                                            alphabeta (origin, depth, -\infty, +\infty, TRUE)
06
              for each child of node
                   v := max(v, alphabeta(child, depth - 1, \alpha, \beta, FALSE))
07
0.8
                   \alpha := \max(\alpha, v)
                  if \beta \leq \alpha
09
                       break (* β cut-off *)
10
11
              return v
12
         else
13
              ∨ := ∞
14
              for each child of node
                   v := min(v, alphabeta(child, depth - 1, \alpha, \beta, TRUE))
15
                   \beta := \min(\beta, v)
16
                   if \beta \leq \alpha
17
                        break (* α cut-off *)
18
19
              return v
```

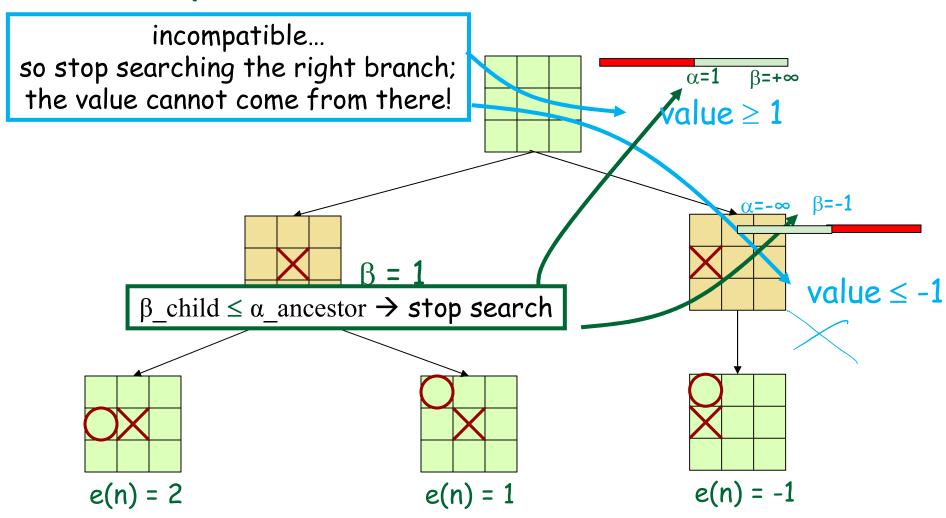


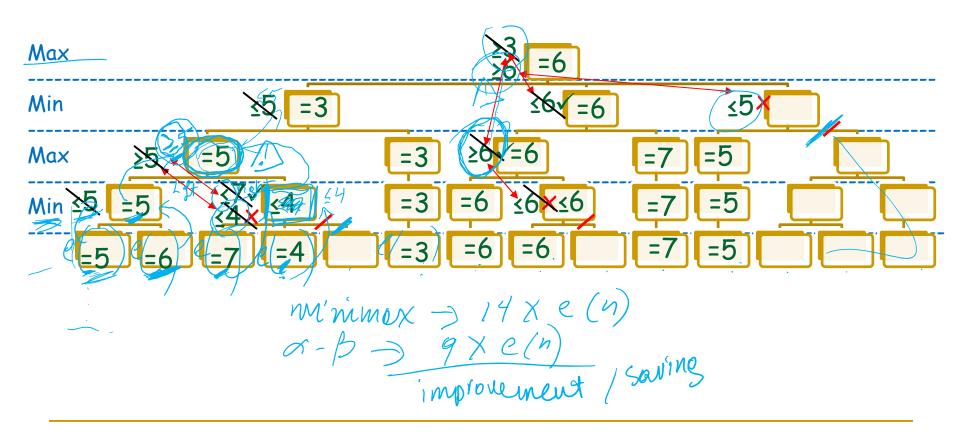


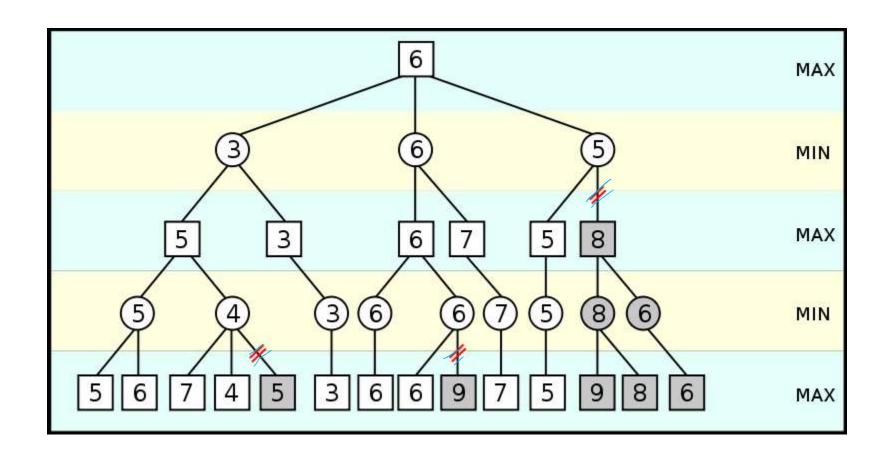


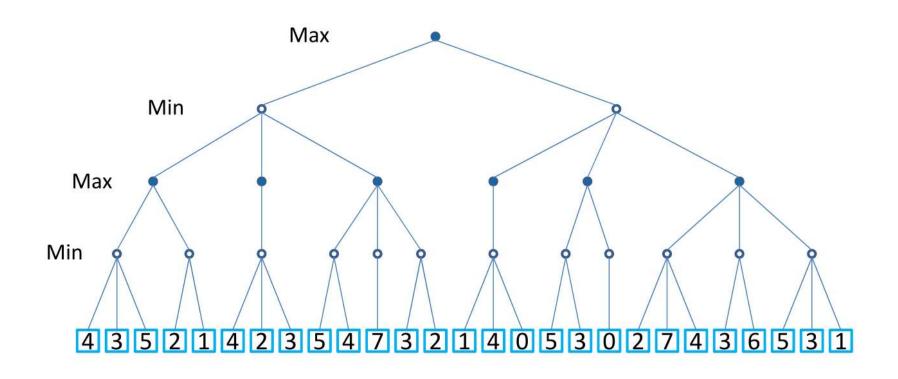


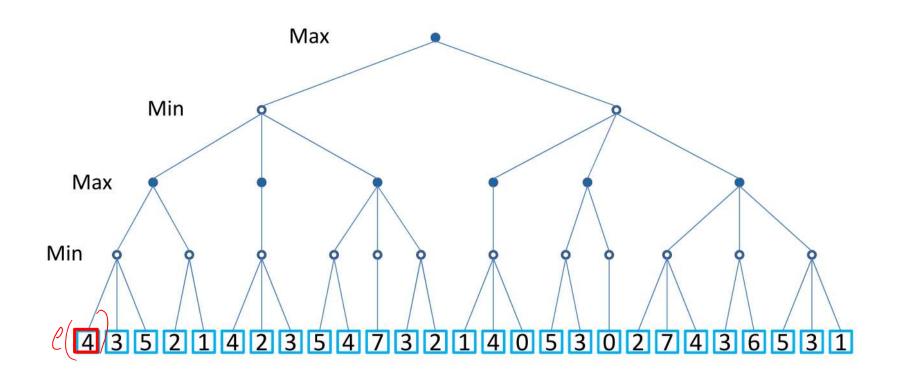


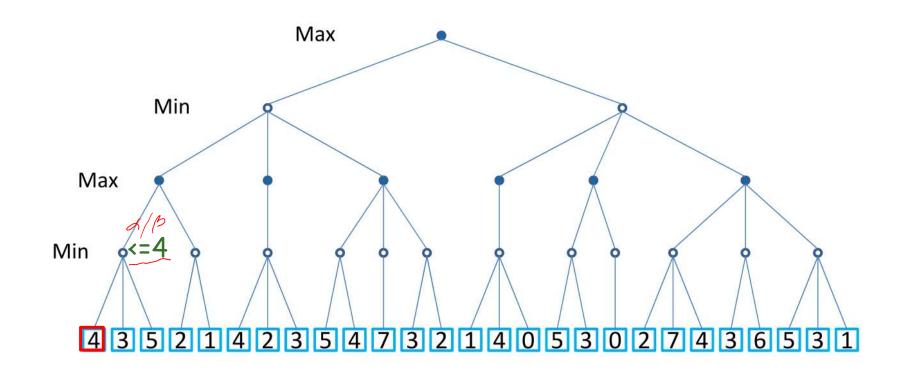


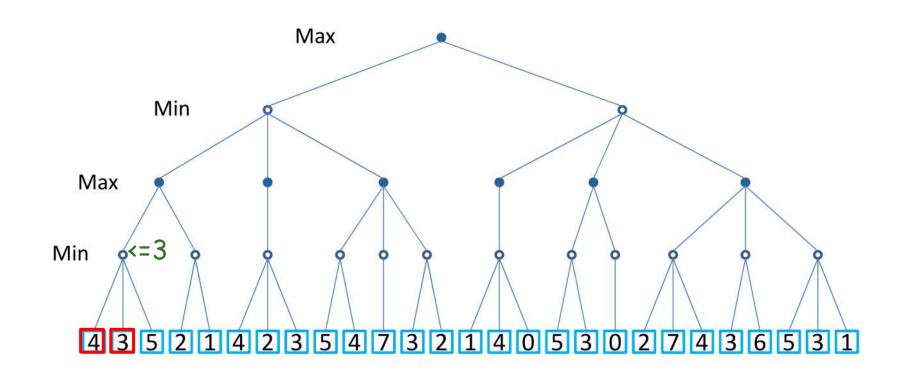


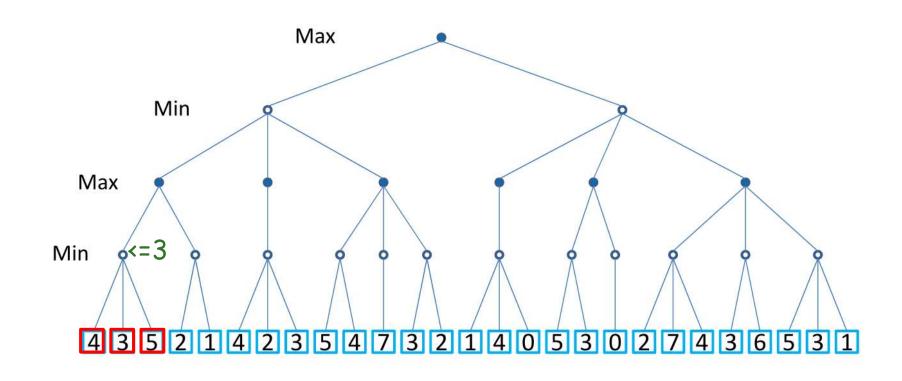


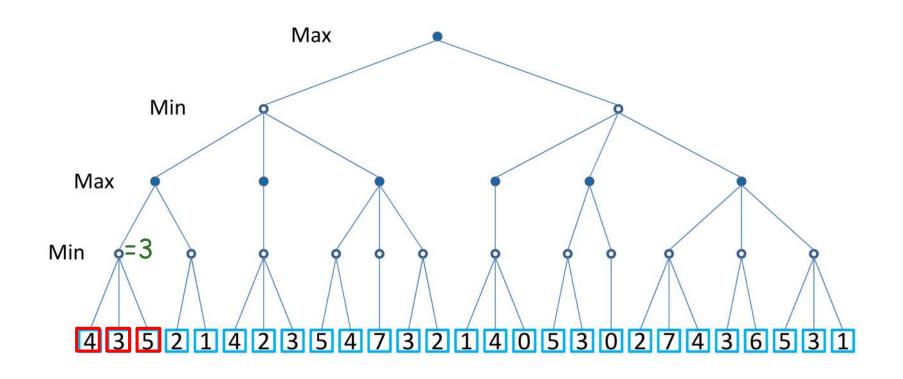


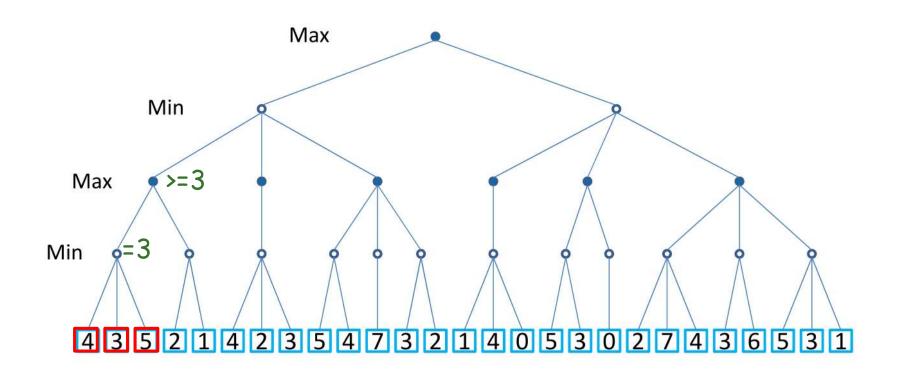


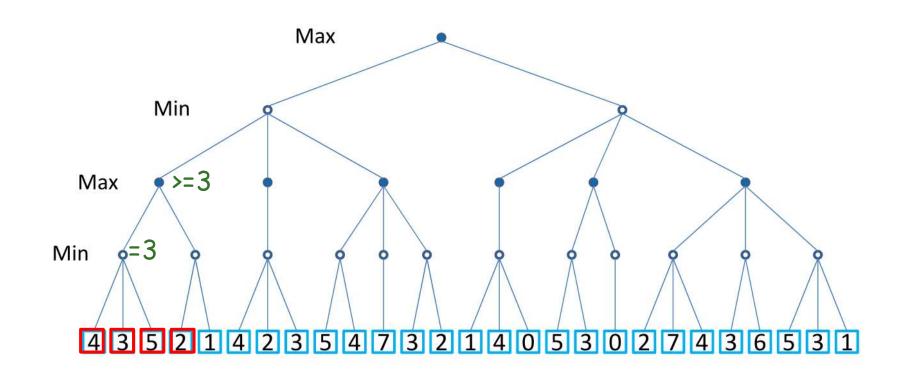


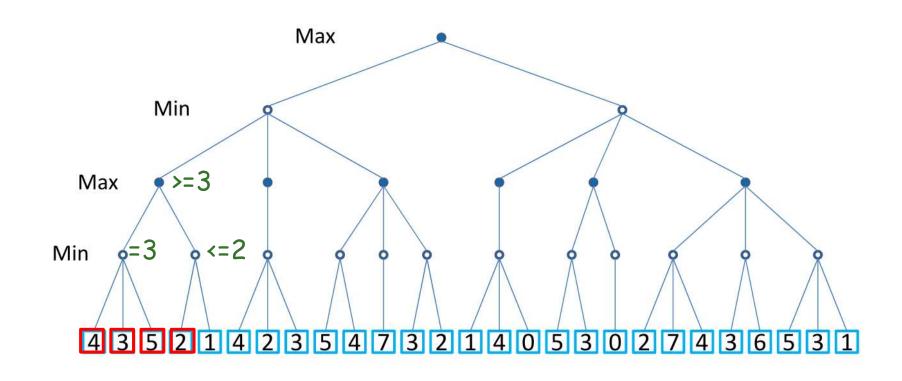


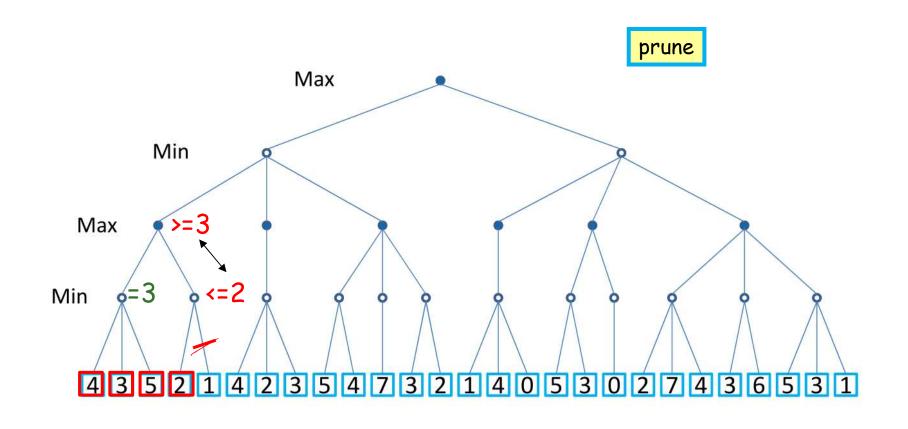


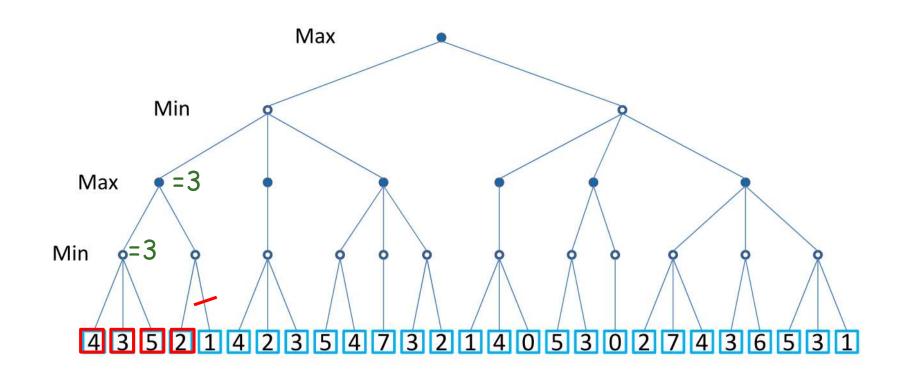


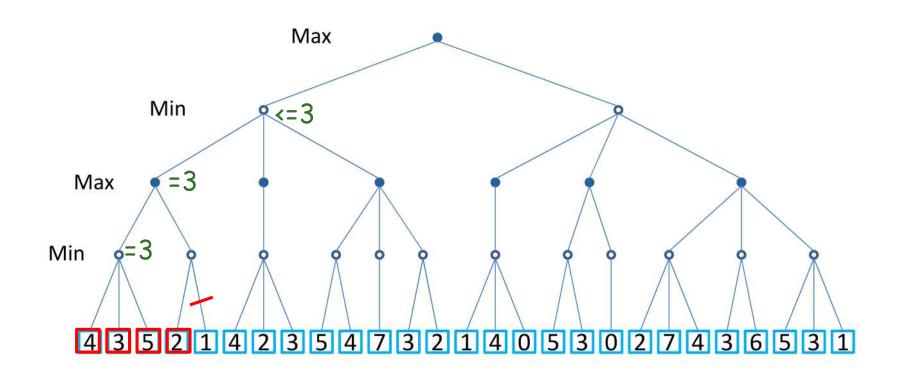


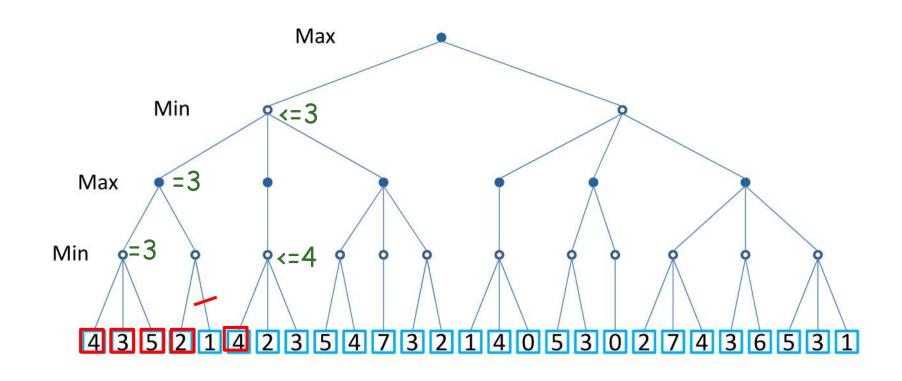


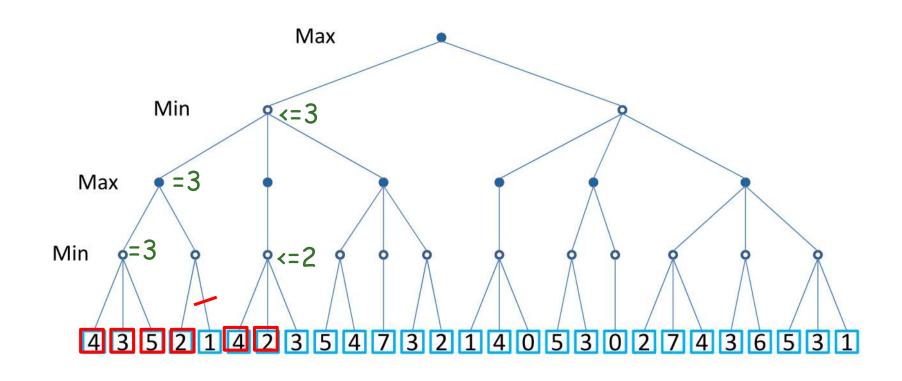


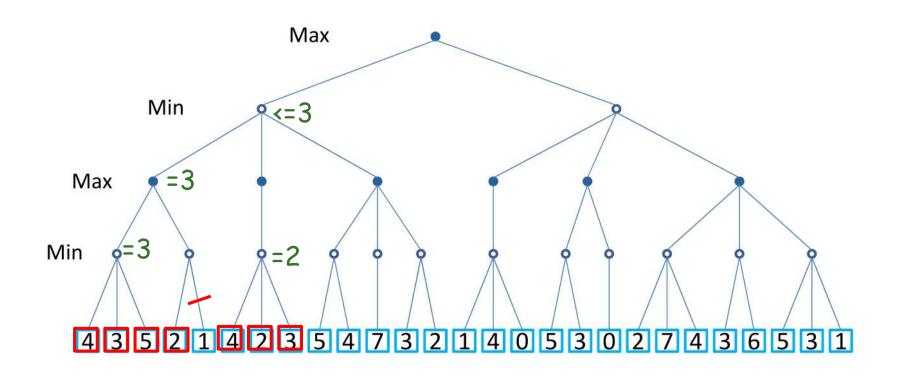


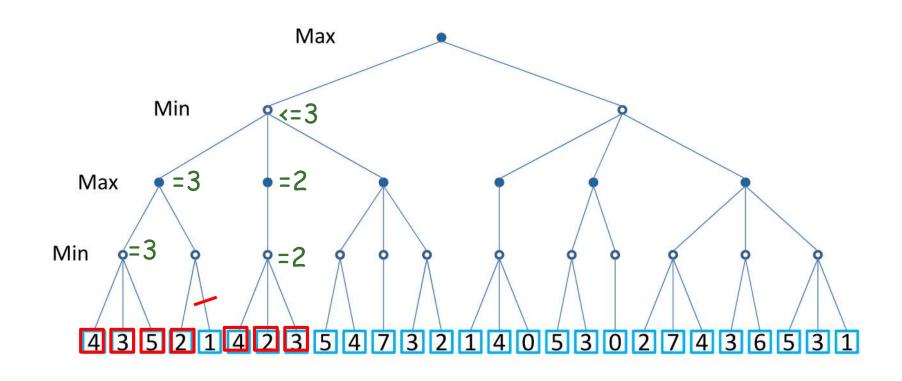


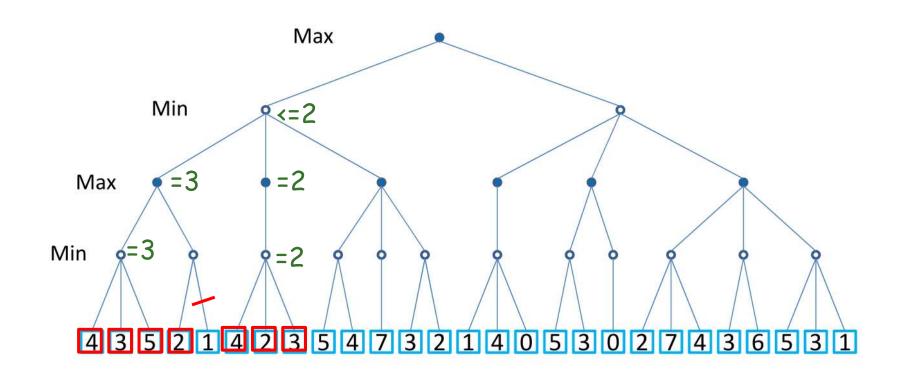


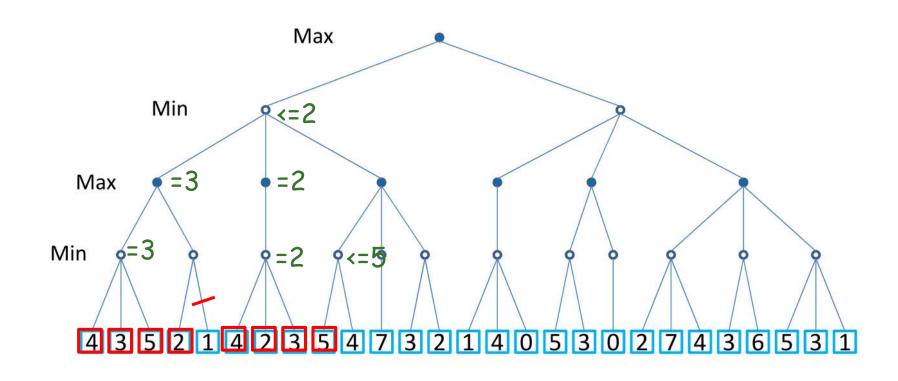


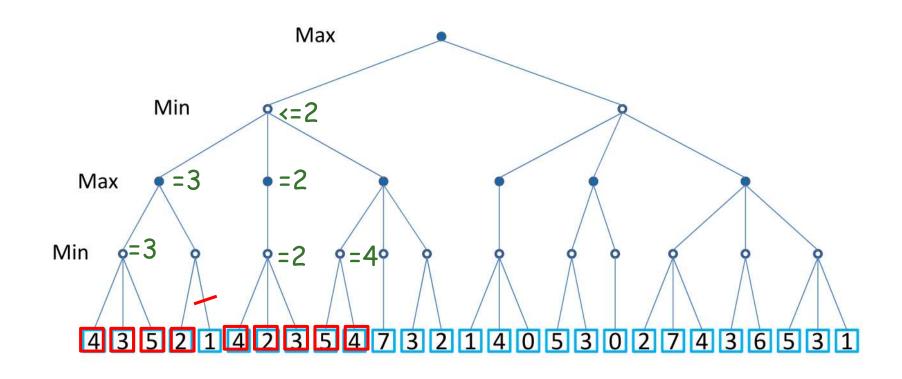


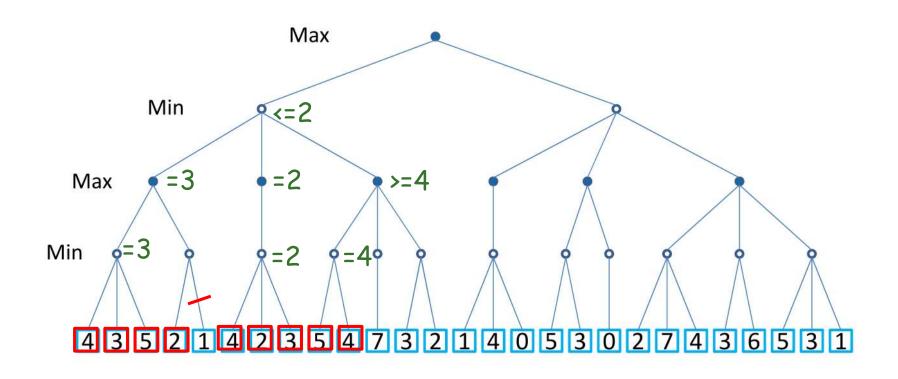


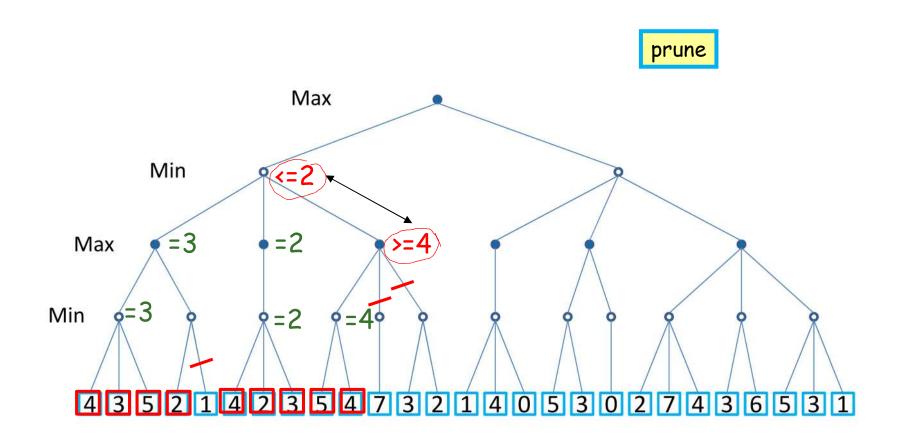


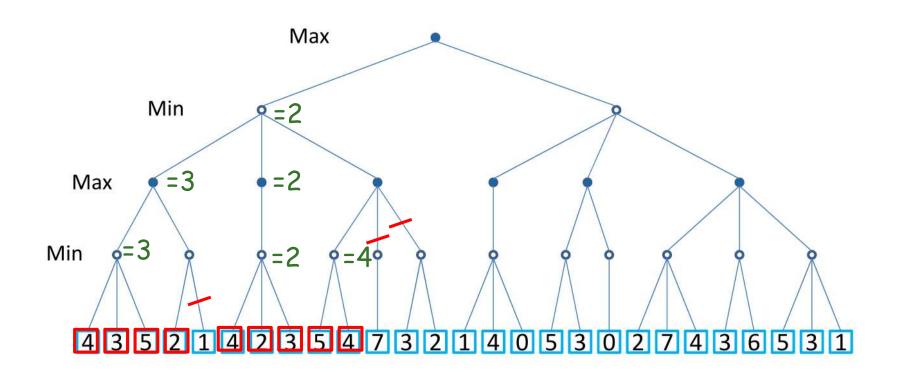


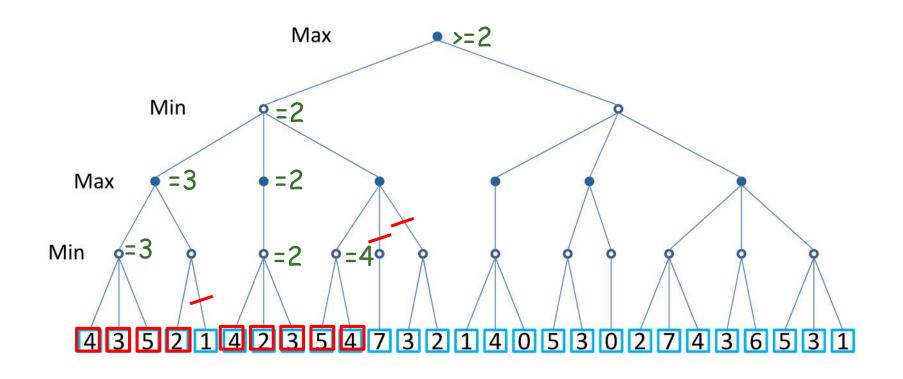


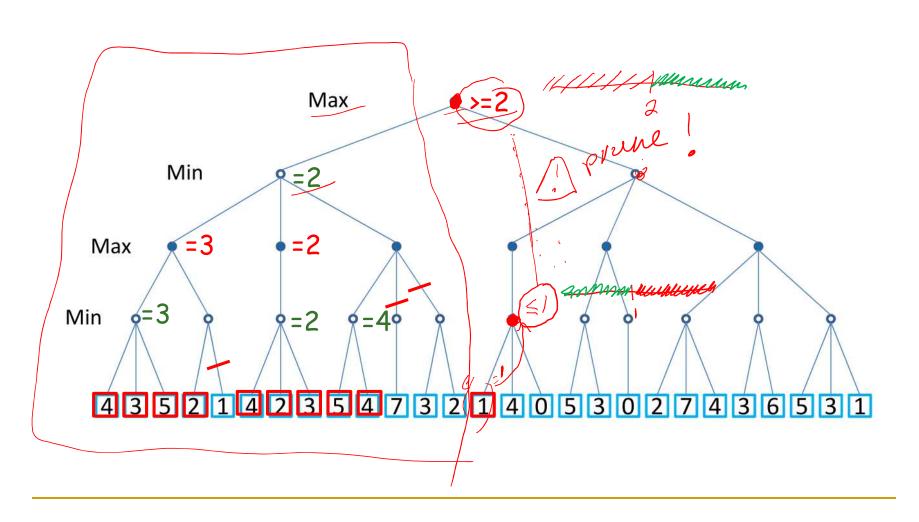




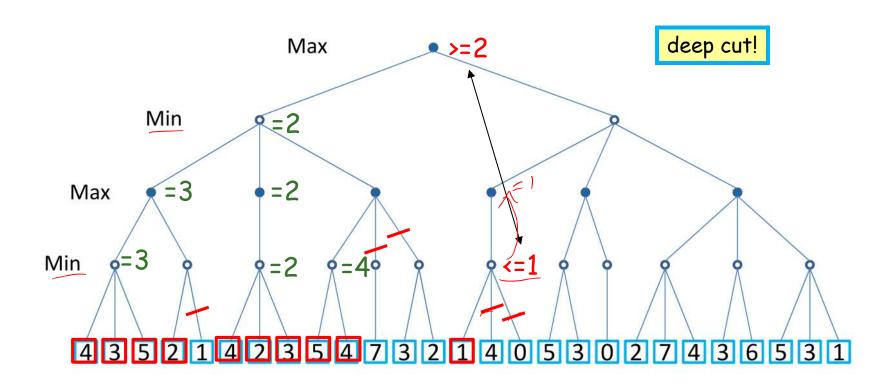


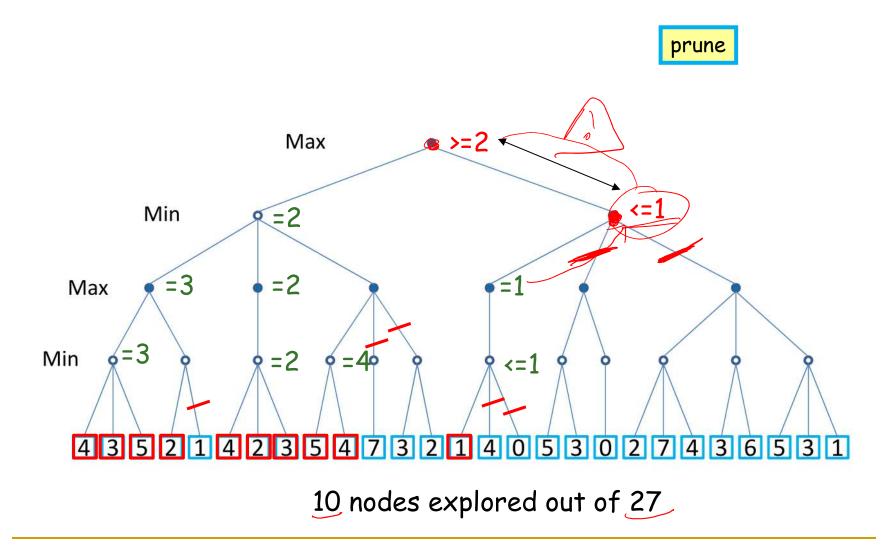






prune





Efficiency of Alpha-Beta Pruning

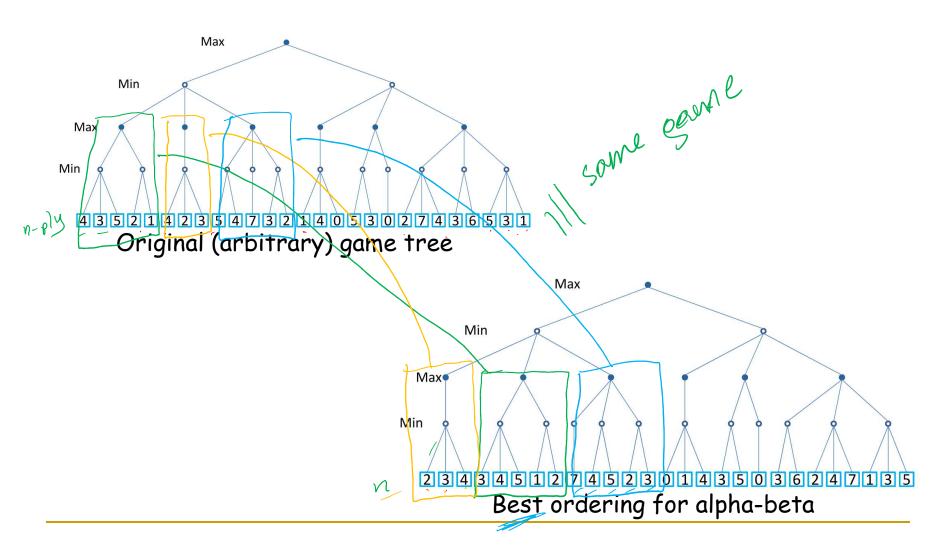
- Depends on the order the siblings
 - which is an arbitrary choice ;-(



- alpha-beta provides no pruning
- plus extra overhead cost ;-(
- In best case:
 - branching factor is reduced to its square root

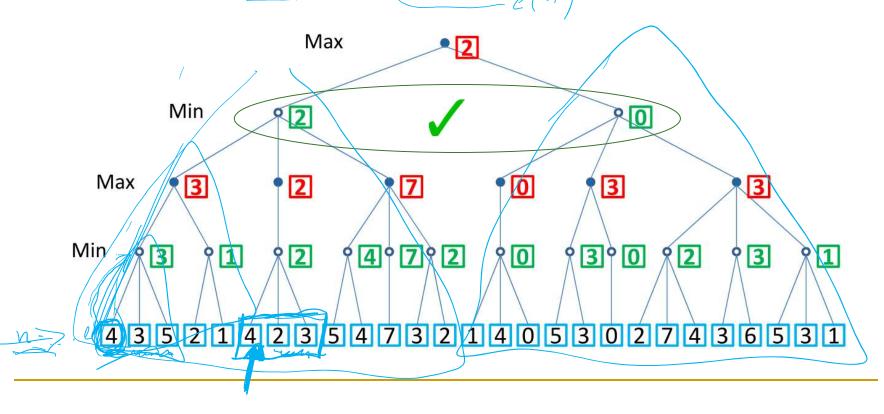
$$36e(n)$$
 $56e(n)$



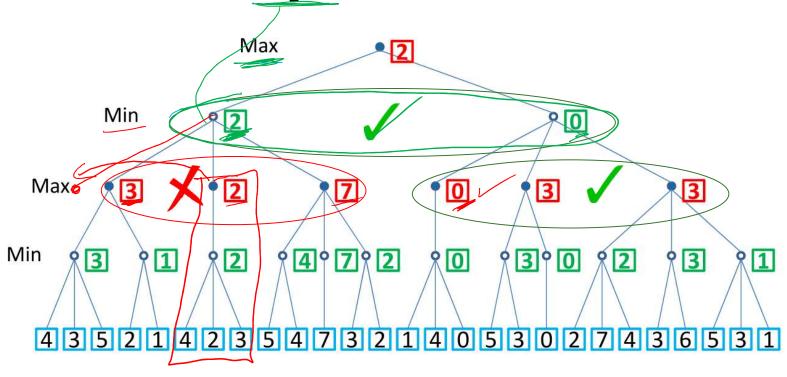


- best ordering:
- Ser girst dield

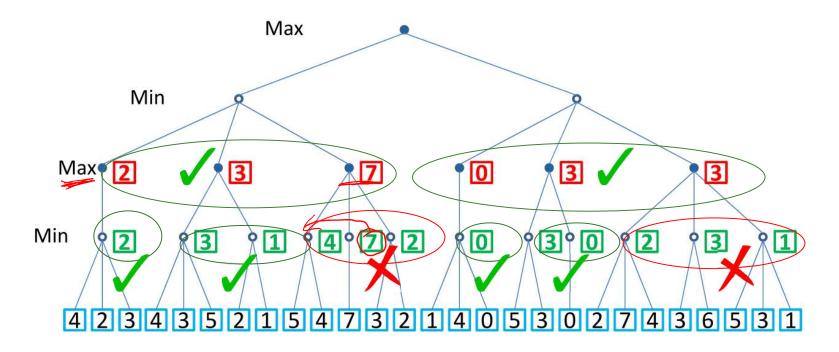
 e/n) strongest constraint placed first, ie:
 - children of MIN: smallest node first
 - children of MAX: largest node first

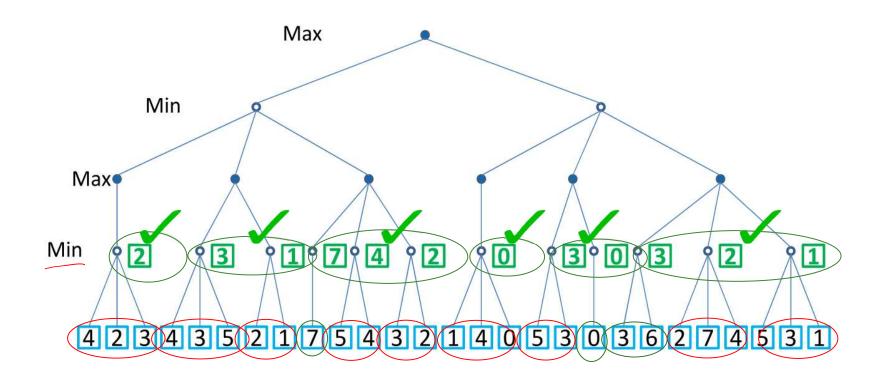


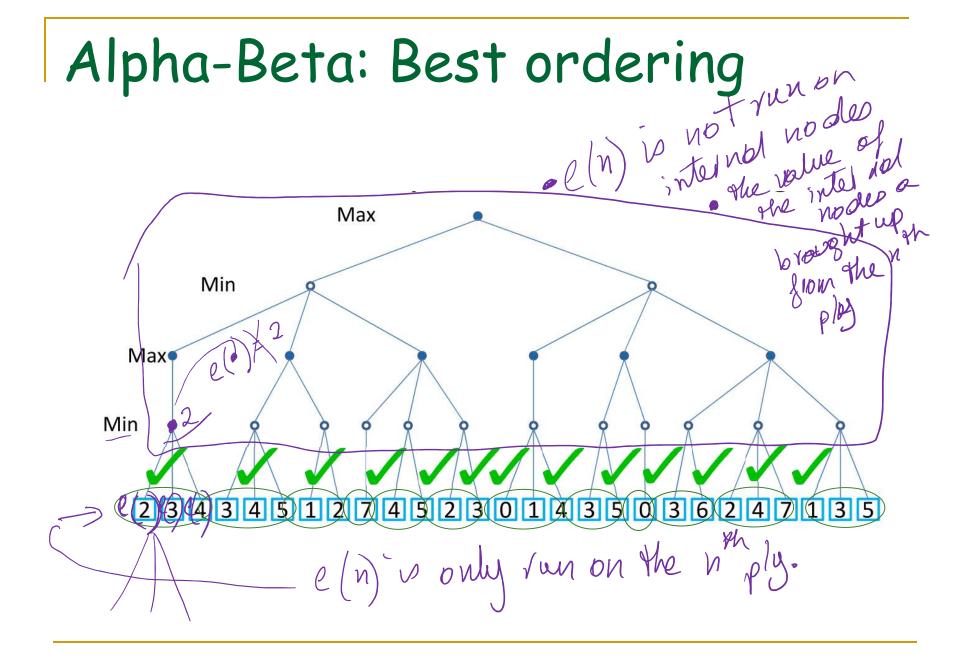
- best ordering:
 - children of MIN: smallest node first
 - 2. children of MAX: largest node first



- best ordering:
 - children of MIN: smallest node first
 - children of MAX: largest node first







Alpha-Beta: Best ordering, Raminder, Raminder hest during > run e(n) test 2 revsions of e(n) 2 revsions of e(n) Leal e(n) to do the G-B seal e(n) find the and find the best next month Max Min e-trivial (n) just 70 Max Min 34345127452300435036247135 8 nodes explored out of 27

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Other Adversarial Search
Multiplayer Games
Stochastic Games
Monte Carlo Tree Search

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