

COMP 472: Artificial Intelligence

State Space Search *part #3*

State Space Representation *video #1*

- Russell & Norvig - Sections 3.1-3.3

Today

1. State Space Representation

2. State Space Search



video #1

a) Overview

b) Uninformed search

1. Breadth-first and Depth-first

2. Depth-limited Search

3. Iterative Deepening

4. Uniform Cost

c) Informed search

1. Intro to Heuristics

2. Hill climbing

3. Greedy Best-First Search

4. Algorithms A & A*

5. More on Heuristics

d) Summary

Motivation

1970

- Many AI problems, can be expressed in terms of going from an initial state to a goal state
 - Ex: to solve a puzzle, to drive from home to Concordia...



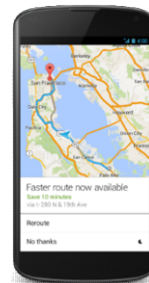
initial

goal

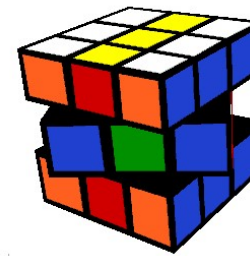
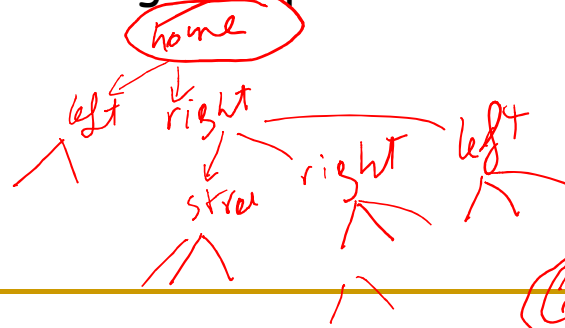
8-puzzle

15 moves

200 moves



Google Maps

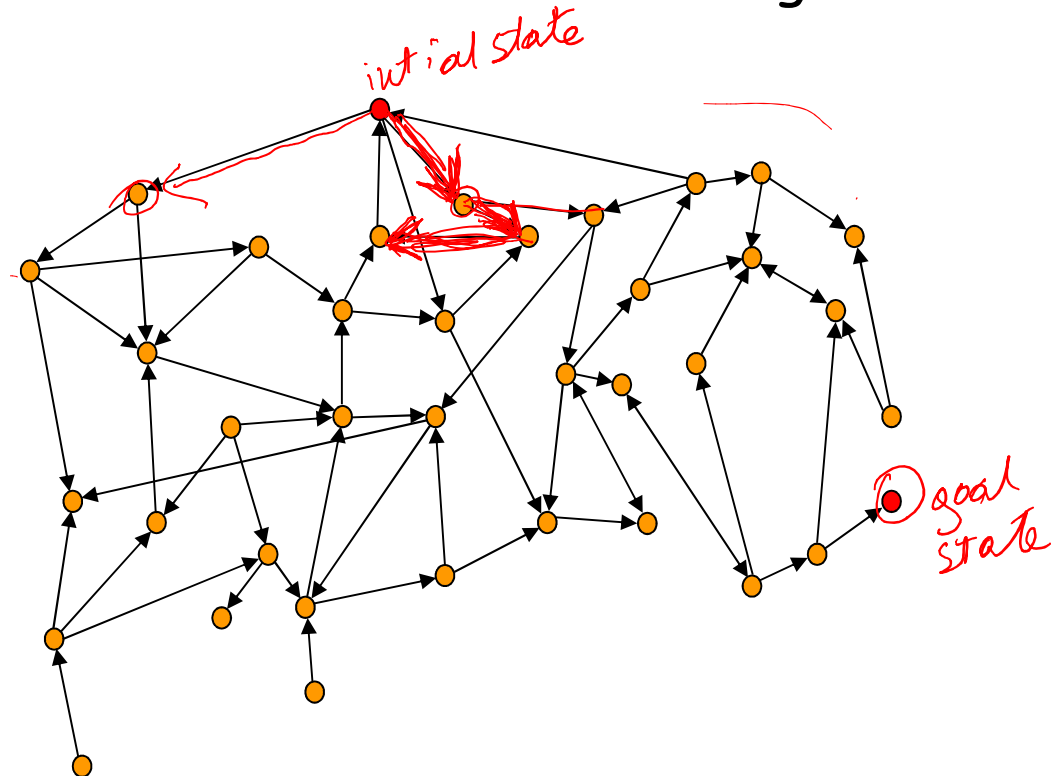
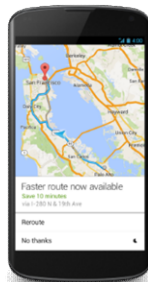


Rubik's cube



Motivation

- Often, there is no direct way to find a solution to go from the initial state to a goal state
- but we can list the possibilities and search through them



Example: 8-Puzzle

State: Any arrangement of 8 numbered tiles and an empty tile on a 3x3 board

8	2	<i>empty</i>
3	4	7
5	1	6

1	2	3
4	5	6
7	8	



Initial state

Goal state



there are several standard goals states for the 8-puzzle

1	2	3
4	5	6
7	8	<i>scribble</i>

1	2	3
8	<i>scribble</i>	4
7	6	5

...

(n^2-1) -puzzle

8	2	
3	4	7
5	1	6

8-puzzle

4

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

15-puzzle

4

■ ■ ■ ■

15-Puzzle

Invented in 1874 by Noyes Palmer Chapman ...
but Sam Loyd claimed he invented it!



Sam Loyd

see Sam Loyd's book of puzzles:

https://archive.org/stream/CyclopediaOfPuzzlesLoyd/Cyclopedia_of_Puzzles_Loyd#mode/2up

State Space

■ Problem is represented by:

1. Initial State

- starting state
- ex. unsolved puzzle, being at home

2. Set of operators / moves / actions

- actions responsible for transition between states

3. Goal test function

- Applied to a state to determine if it is a goal state
- ex. solved puzzle, being at Concordia

4. Path cost function

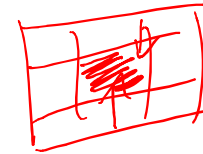
- Assigns a cost to a path to tell if a path is preferable to another

■ State space:

- the set of all states that can be reached from the initial state by any sequence of action

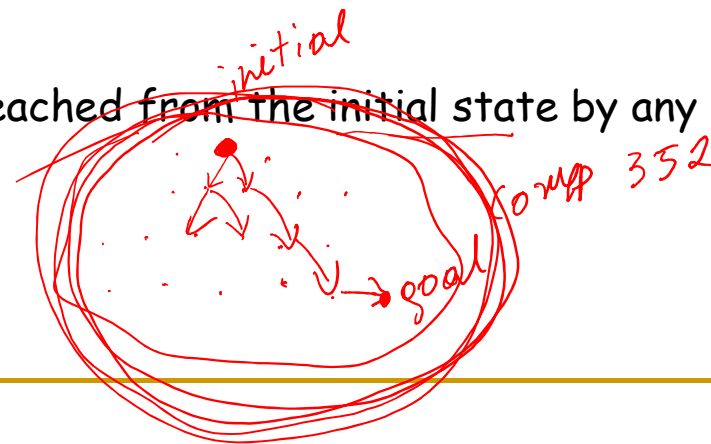
■ Search algorithm:

- how the search space is visited

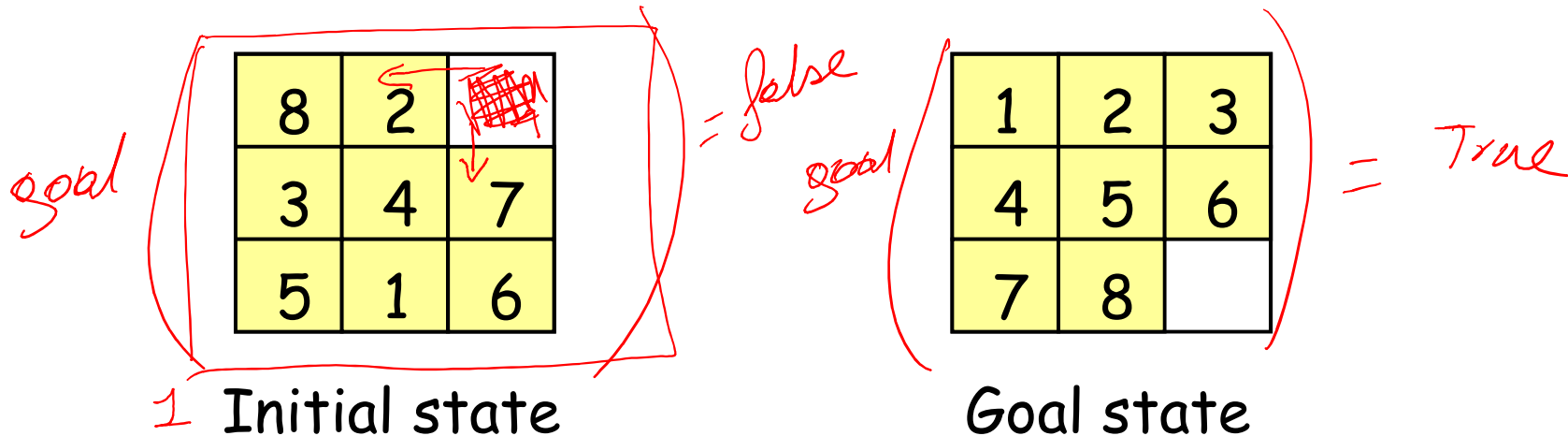


	cost	cost
up	1	3
down	1	1
left	1	2
right	1	4
best nb of moves	lowest cost	

$goal(0) \rightarrow T$
 $goal(\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}) = T$



Example: The 8-puzzle



- 2- Set of operators:
blank moves up, blank moves down, blank moves left, blank moves right
- 3- Goal test function:
state matches the goal state
- 4- Path cost function:
each movement costs 1
so the path cost is the length of the path (the number of moves)

8-Puzzle: Successor Function

{ children

*successor(n)
{ n1,
n2,
n3 }*

node n

8	2	7
3	4	
5	1	6

up

down

left

n1

8	2	
3	4	7
5	1	6

n2

8	2	7
3	4	6
5	1	

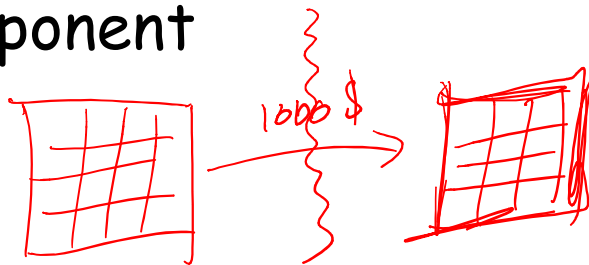
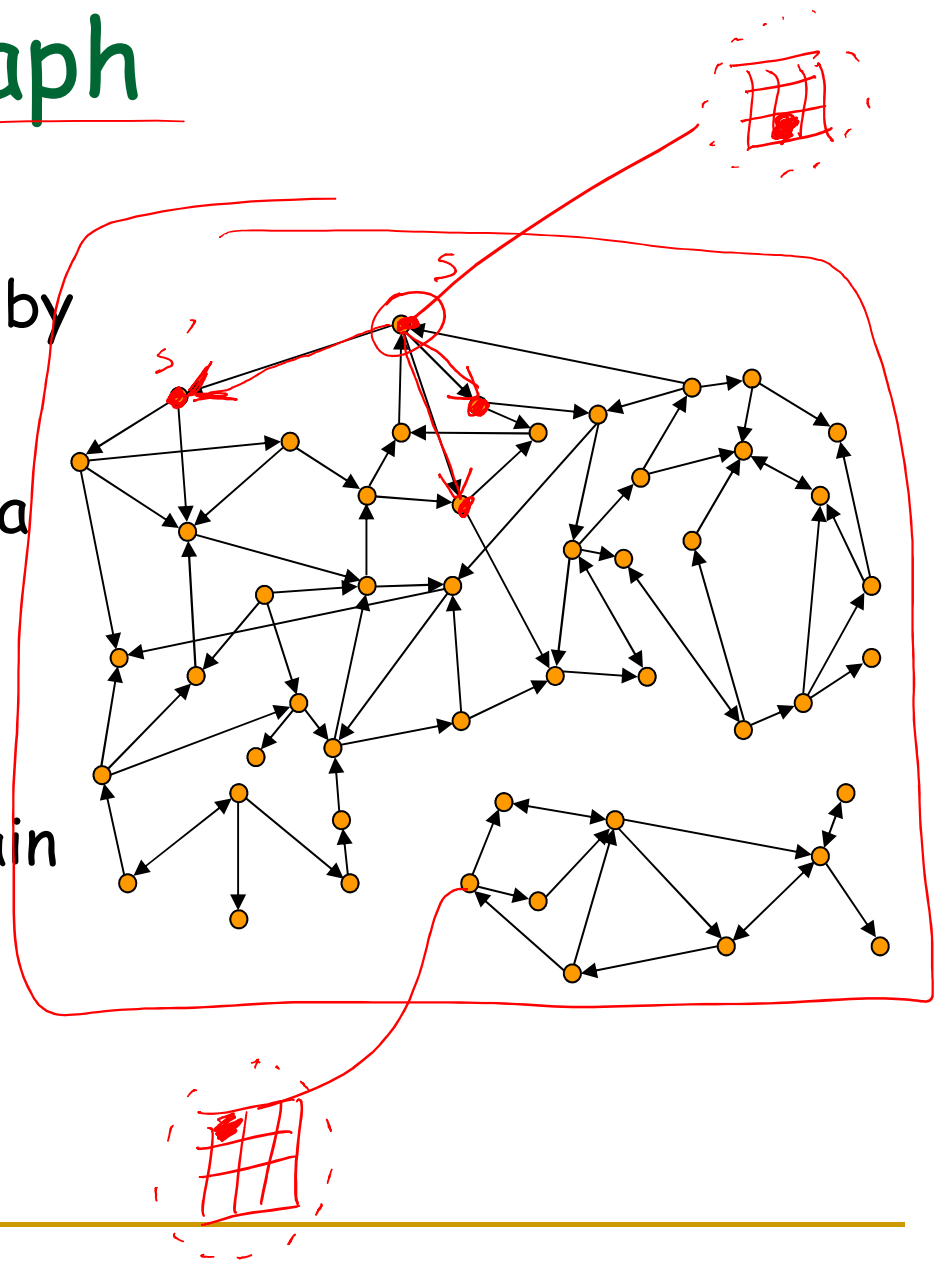
n3

8	2	7
3		4
5	1	6

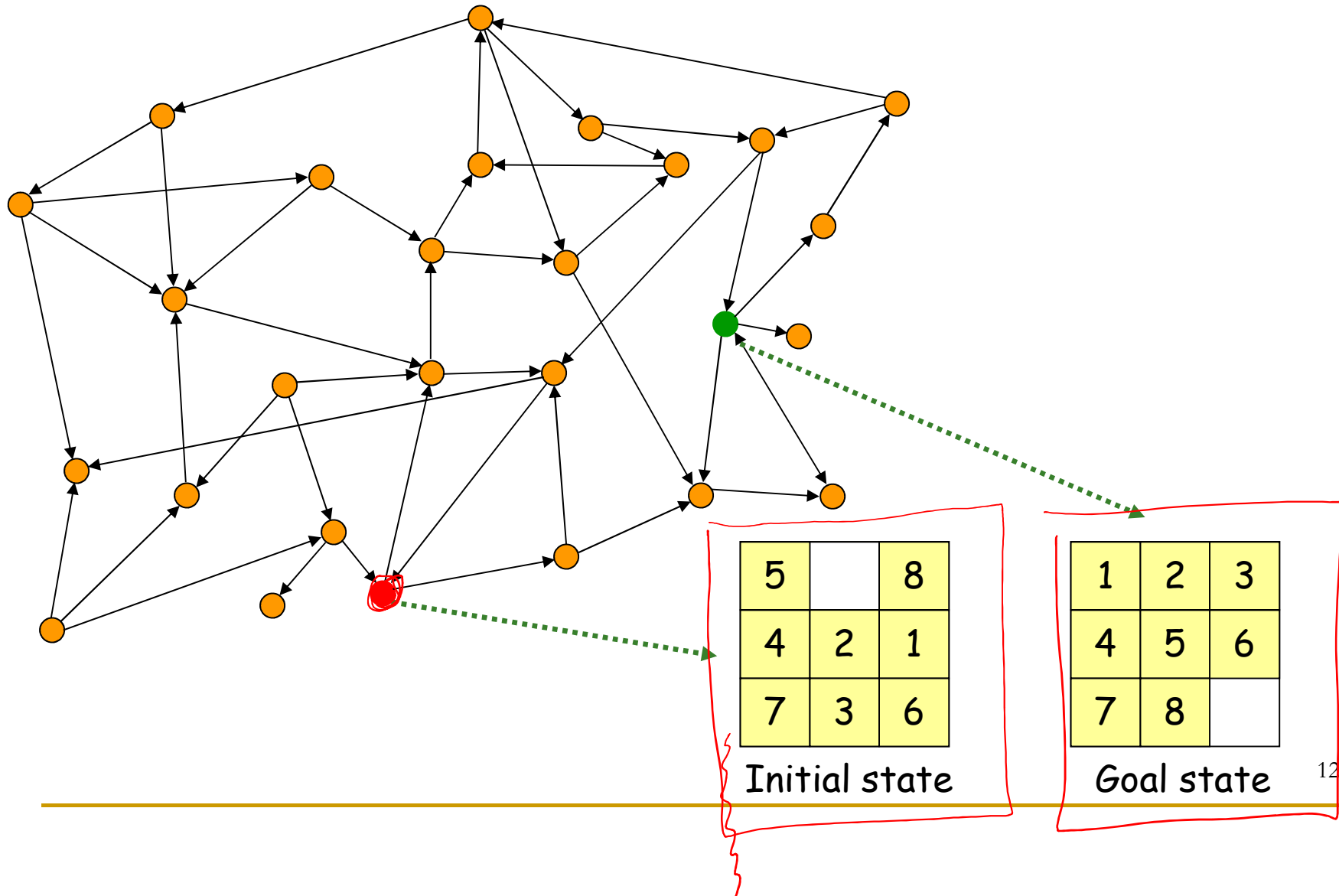
Search is about the exploration of alternatives

State Space Graph

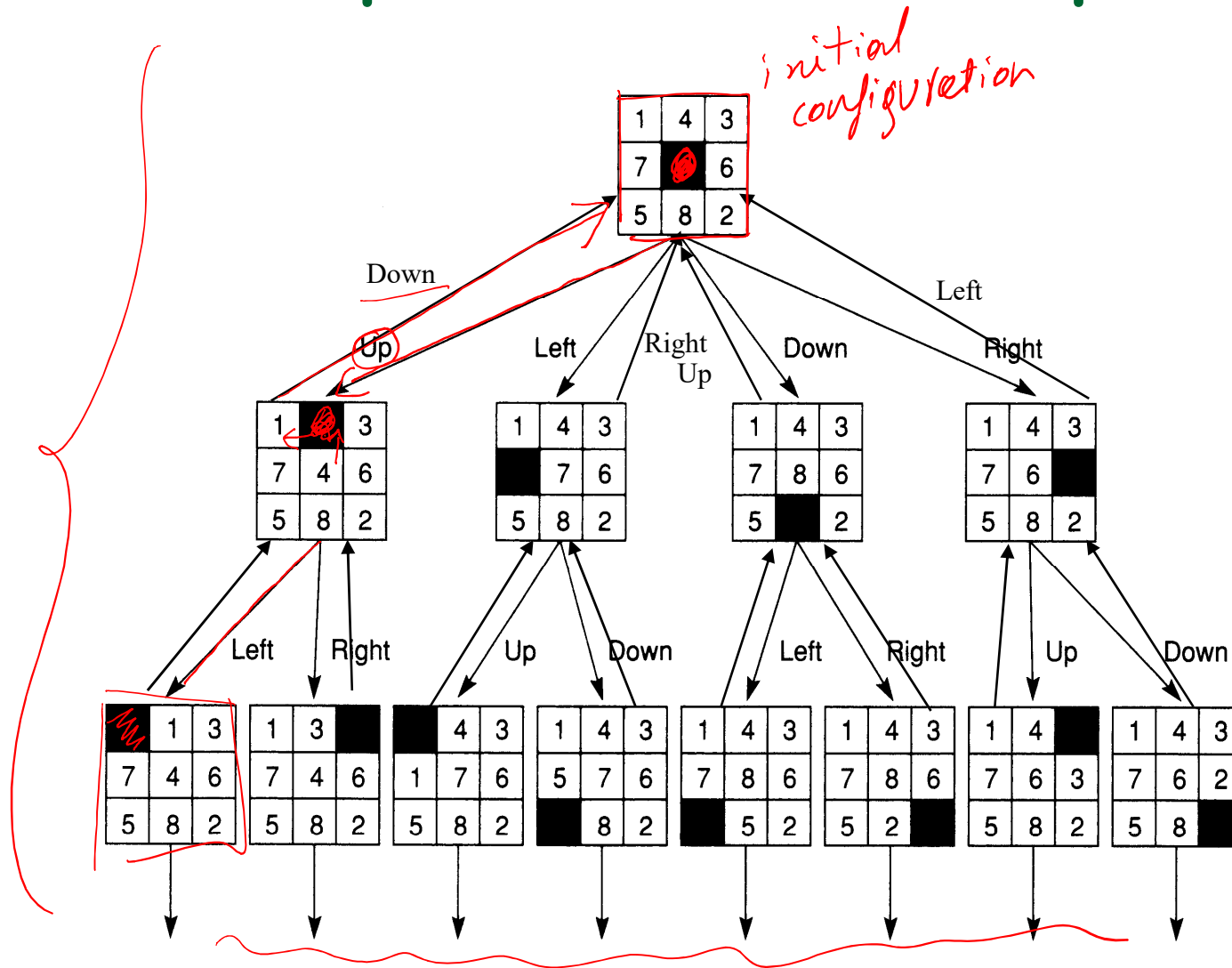
- Each state is represented by a distinct node
- An arc (or edge) connects a node s to a node s' if $s' \in \text{SUCCESSOR}(s)$
- The state graph may contain more than one connected component



Just to make sure we're clear...



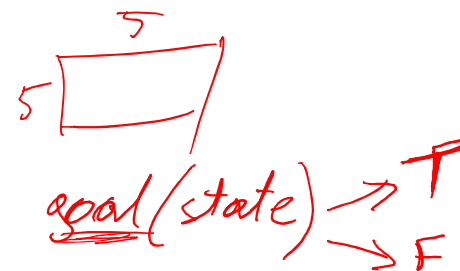
State Space for the 8-puzzle



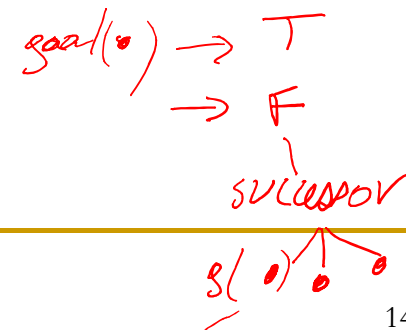
source: G. Luger (2005)

Size of state spaces

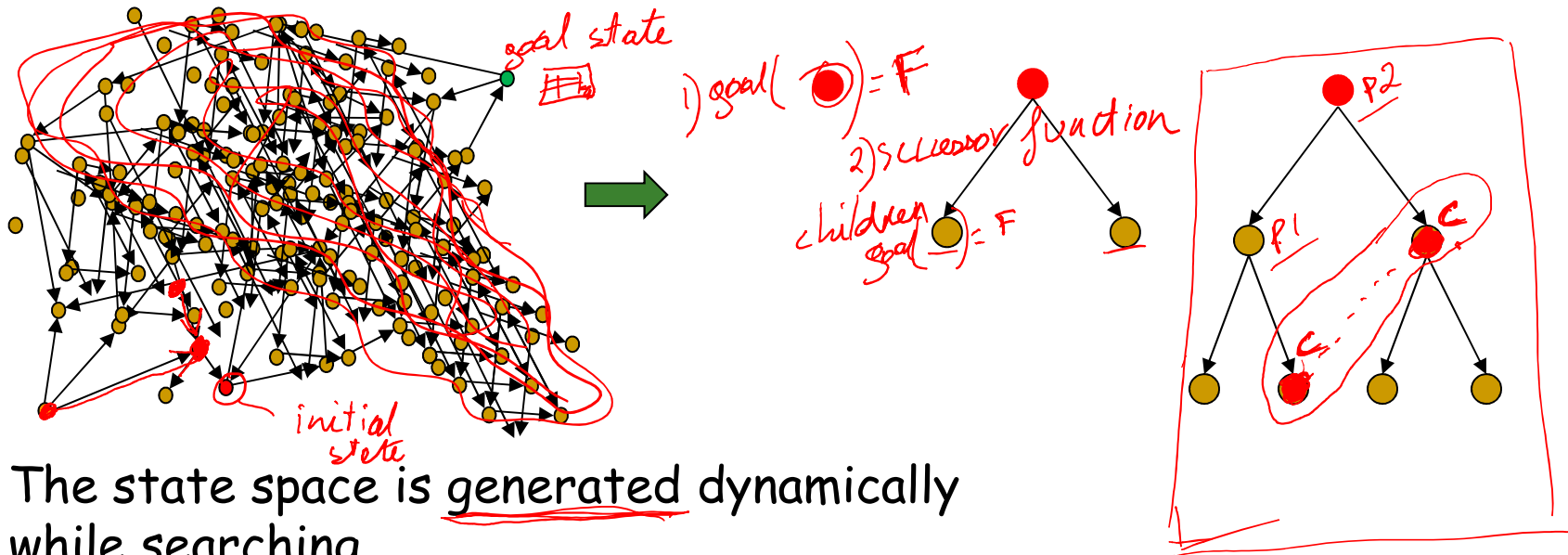
- For the (n-1)-puzzle:
 - Nb of states:
 - 8-puzzle --> $9! = 362,880$ states
 - 15-puzzle --> $16! \sim 2.09 \times 10^{13}$ states
 - 24-puzzle --> $25! \sim 10^{25}$ states
 - At 100 millions states/sec:
 - 8-puzzle --> 0.036 sec
 - 15-puzzle --> ~ 55 hours
 - 24-puzzle --> $> 10^9$ years



- For real problems:
 - state spaces are way too large to be generated in advance and searched after
 - so it is generated dynamically while searching.



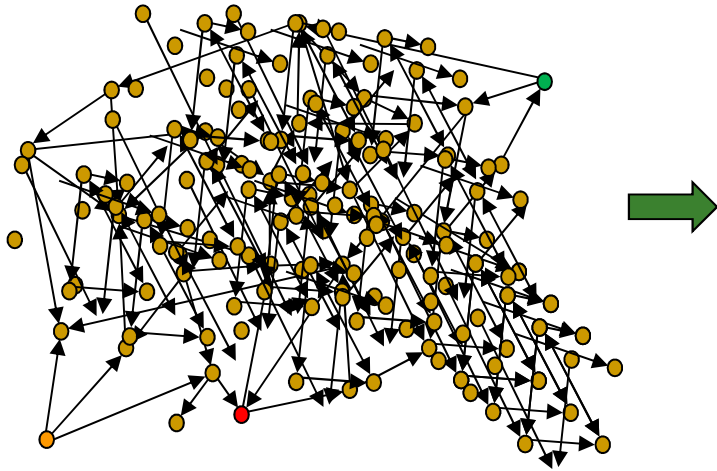
State Space Graph as a Search Tree



- The state space is generated dynamically while searching.
 - we explore a node:
 - if it the goal, stop and trace back the path / s from the initial node
 - if it is not the goal, then generating its successors/children and explore these recursively
 - to avoid cycles, the search algorithm will check for duplicate nodes.

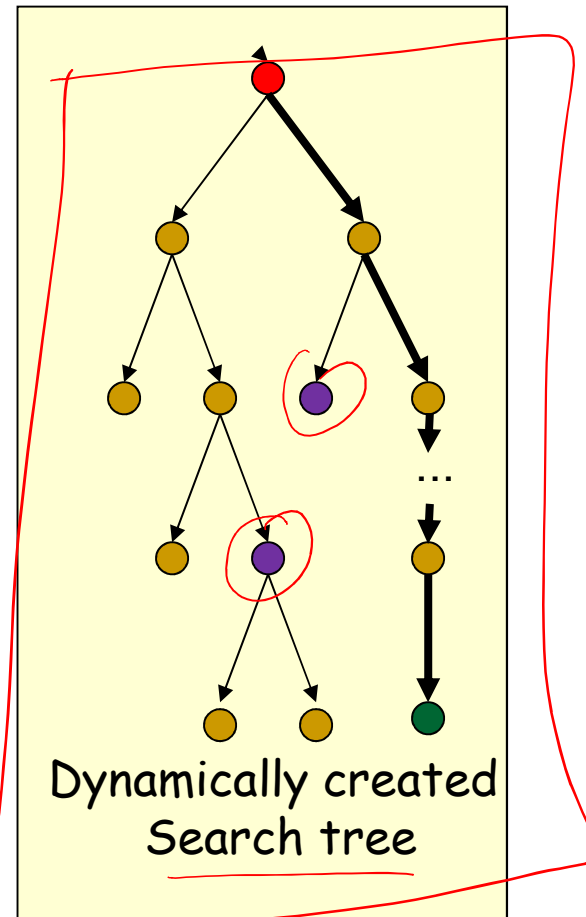
Search tree

State Space Graph as a Search Tree



Theoretical State Space Graph

So now, we just need an efficient search algorithm



Dynamically created
Search tree

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Up Next

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