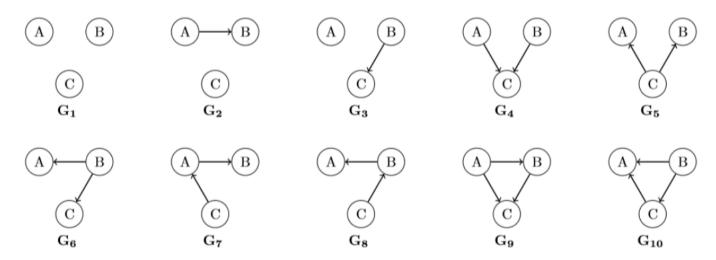
吴传递 51737091025

Homework 7 Written

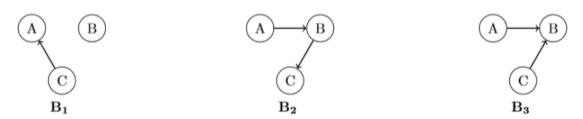
July 8th, 2020 at 11:59pm

Bayes' Net: Representation

Assume we are given the following ten Bayes' nets, labeled G_1 to G_{10} :



Assume we are also given the following Bayes' nets, labeled G_1 to G_3 :



- 1. Assume we know that a joint distribution d_1 (over A,B,C) can be represented by Bayes' net $\mathbf{B_1}$. Mark all of the following Bayes' nets that are guaranteed to be able to represent d_1 .
 - \Box G_2 G_1

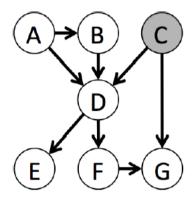
- G_6
- lacksquare G_7 \Box G_8 lacksquare G_9 lacksquare G_{10}

None of the above.

2.				_					. ,	can be represented by Bayes' net $\mathbf{B_2}$. be able to represent d_2 .	
		$\mathbf{G_1}$		G_2		G_3		G_4		G_5	
	∀∕	${ m G}_6$		G_7		\mathbf{G}_{8}		G_9		${ m G}_{10}$	
		None of	the	above.							
3.	3. Assume we know that a joint distribution d_3 (over A,B,C) can be represented by Bayes' new Mark all of the following Bayes' nets that are guaranteed to be able to represent d_3 .										
		$\mathbf{G_1}$		$\mathbf{G_2}$		G_3		$\mathbf{G_4}$		${ m G}_5$	
		${ m G_6}$		G_7		G_8	D	G_9	7	${f G_{10}}$	
		None of	the	above.							
4.	Assume we know that a joint distribution d_4 (over A,B,C) can be represented by Bayes' net $\mathbf{B_1B_2}$ and $\mathbf{B_3}$. Mark all of the following Bayes' nets that are guaranteed to be able to represent d_4 .										
		$\mathbf{G_1}$		G_2		G_3		G_4		${ m G}_5$	
		${ m G_6}$		G_7		G_8		G_9		G_{10}	
		None of	the	above.							

2 Variable Elimination

For the Bayes' net below, we are given the query P(A, E|+c). All variables have binary domains. Assume we run variable elimination to compute the answer to this query, with the following variable elimination ordering: B, D, G, F.



Complete the following description of the factors generated in this process:

After inserting evidence, we have the following factors to start out with:

Solution:

$$P(A), P(B \mid A), P(+c), P(D \mid A, B, +c), P(E \mid D), P(F \mid D), P(G \mid +c, F)$$

When eliminating B we generate a new factor f_1 as follows:

Solution:

$$f_1(A, +c, D) = \sum_b P(b \mid A) P(D \mid A, b, +c)$$

This leaves us with the factors:

Solution:

$$P(A), P(+c), P(E \mid D), P(F \mid D), P(G \mid +c, F), f_1(A, +c, D)$$

When eliminating D we generate a new factor f_2 as follows:

Solution: ...
$$f_2(A, +C, E, F) = \sum_{d} P(E|d) P(F|d) f_1(A, +c, d)$$

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This leaves us with the factors:

Solution: ...
$$P(A)$$
, $P(+c)$, $P(G|+c,F)$, $f_2(A,+c,E,F)$

When eliminating G we generate a new factor f_2 as follows:

Solution: ...
$$f_3(tc, F) = \sum (P(g|tc, F))$$

This leaves us with the factors:

Solution: ...
$$P(A)$$
, $P(+C)$, $f_2(A,+C,E,F)$, $f_3(+C,F)$

When eliminating F we generate a new factor f_4 as follows:

Solution: ...
$$f_4(A, +C, E) = \sum_f f_2(A, +C, E, f) f_3(+C, f)$$

This leaves us with the factors:

Solution: ...
$$P(A)$$
, $P(+c)$, $f_4(A)$, $+c$, E)

(b) Write a formula to compute P(A, E|+c) from the remaining factors.

Solution: ...
$$P(A,E|+c) = \frac{P(A)P(+c)f_4(A,+c,E)}{\sum_{a,c}P(a)P(+c)f_4(a,+c,e)}$$

(c) Among f_1, f_2, f_3, f_4 , which is the largest factor generated, and how large is it? Assume all variables have binary domains and measure the size of each factor by the number of rows in the table that would represent the factor.

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(d) Find a variable elimination ordering for the same query, i.e., for P(A, E|+c), for which the maximum size factor generated along the way is smallest. Hint: the maximum size factor generated in your solution should have only 2 variables, for a size of $2^2 = 4$ table. Fill in the variable elimination ordering and the factors generated into the table below.

Variable Eliminated	Factor Generated
B	f, (A, +C, D)
G	fz(+c,F)
F	f3(tC,D)
	f4 (A,+C,E)

For example, in the naive ordering we used earlier, the first row in this table would have had the following two entries: B, $f_1(A, +c, D)$.