VE 492 Homework9

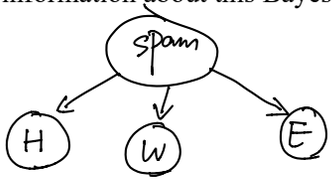
Due: 23:59, July. 22th

Q1. Naive Bayes

Your friend claims that he can write an effective Naive Bayes spam detector with only three features: the hour of the day that the email was received ($H \in \{1,2,...,24\}$), whether it contains the word 'viagra' ($W \in \{yes,no\}$), and whether the email address of the sender is Known in his address book, Seen before in his inbox, or Unseen before ($E \in \{K,S,U\}$).

(a) Flesh out the following information about this Bayes net:

Graph structure:



Parameters:

θ_{spam}, $\theta_{H,i,c}$, $\theta_{W,c}$, $\theta_{E,j,c}$, where $i \in \{1,2,\cdots,23\}$, $j \in \{K,S\}$, $c \in \{spam, ham\}$

Size of the set of parameters:

53

Suppose now that you labeled three of the emails in your mailbox to test this idea:

spam or ham?	H	W	E
spam	3	yes	S
ham	14	no	K
ham	15	no	K

(b) Use the three instances to estimate the maximum likelihood parameters.

$\theta_{spam} = \frac{1}{3}$, $\theta_{H,3,spam} = 1$, $\theta_{H,14,ham} = \frac{1}{2}$, $\theta_{H,15,ham} = \frac{1}{2}$, $\theta_{W,spam} = 1$, $\theta_{E,S,spam} = 1$, $\theta_{E,K,ham} = 1$

(c) Using the maximum likelihood parameters, find the predicted class of a new datapoint with $H = 3, W = no, E = U$.

None of the predicted class can be found.

(d) $\theta_{spam} = \frac{3}{7}$, $\theta_{H,3,spam} = \frac{3}{49}$, $\theta_{H,other,spam} = \frac{3}{49}$, $\theta_{H,14,ham} = \frac{3}{50}$, $\theta_{H,15,ham} = \frac{3}{50}$, $\theta_{H,other,ham} = \frac{2}{50}$, $\theta_{W,spam} = \frac{3}{5}$, $\theta_{W,ham} = \frac{2}{6}$, $\theta_{E,S,spam} = \frac{3}{7}$, $\theta_{E,other,spam} = \frac{1}{7}$, $\theta_{E,K,ham} = \frac{1}{2}$, $\theta_{E,other,ham} = \frac{1}{4}$

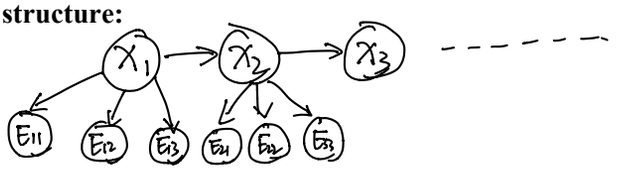
(d) Now use the three to estimate the parameters using Laplace smoothing and $k = 2$. Do not forget to smooth both the class prior parameters and the feature values parameters.

(e) Using the parameters obtained with Laplace smoothing, find the predicted class of a new datapoint with $H = 3, W = no, E = U$.

ham

(f) You observe that you tend to receive spam emails in batches. In particular, if you receive one spam message, the next message is more likely to be a spam message as well. Explain a new graphical model which most naturally captures this phenomena.

Graph structure:



Parameters:

θ_{spam}, $\theta_{H,i,c}$, $\theta_{W,c}$, $\theta_{E,j,c}$, where $i \in \{1,2,\cdots,23\}$, $j \in \{K,S\}$, $c \in \{spam, ham\}$, $\theta_{spam,ham}$, $\theta_{ham,spam}$

Size of the set of parameters:

55

Q2. Perceptron

A (a) Suppose you have a binary perceptron in 2D with weight vector $\boldsymbol{w} = r\,[w_1, w_2]^T$. You are given w_1 and w_2, and are given that r > 0, but otherwise not told what r is. *Assume that ties are broken as positive*. Can you determine the perceptron's classifification of a new example x with known feature vector f(x)?

A. Always
B. Sometimes
C. Never

(b) Now you are learning a multi-class perceptron between 4 classes. The weight vectors are currently $[1,0]^T,[0,1]^T,[-1,0]^T,[0,-1]^T$ for the classes A, B, C, and D. The next training example *x* has a **label of A** and feature vector *f*(*x*).

For the following questions, *do not make any assumptions about tie-breaking.* (Do not write down a solution that creates a tie.)

If the answer does not exist, write down **Not possible**

$f(x) = \begin{bmatrix} & \\ & \end{bmatrix}$ ○ Not possible

(i) Write down a feature vector in which no weight vectors will be updated. $f(x) = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$

(ii) Write down a feature vector in which **only** $\mathbf{w}_A$ will be updated by the perceptron. None

(iii) Write down a feature vector in which **only** $\mathbf{w}_A$ and $\mathbf{w}_B$ will be updated by the perceptron. $f(x) = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$

(iv) Write down a feature vector in which **only** $\mathbf{w}_A$ and $\mathbf{w}_C$ will be updated by the perceptron. $f(x) = \begin{bmatrix} -1 \\ 0 \end{bmatrix}$

The weight vectors are the same as before, but now there is a bias feature with value of 1 for all *x* and the weight of this bias feature is 0, -2, 1, - 1 for classes A, B, C, and D respectively. As before, the next training example *x* has a **label of A** and a feature vector *f*(*x*). The always "1" bias feature is the first entry in *f*(*x*).

If the answer does not exist, write down **Not possible**

$f(x) = \begin{bmatrix} 1 & \\ & \\ & \end{bmatrix}$ ○ Not possible

(v) Write down a feature vector in which **only** $\mathbf{w}B$ and $\mathbf{w}C$ will be updated by the perceptron. None

(vi) Write down a feature vector in which **only** $\mathbf{w}A$ and $\mathbf{w}C$ will be updated by the perceptron.

$f(x) = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$