



# Estimation of Actuation Configuration for a Multi-Actuated Blimp

Final Presentation (Semester Thesis)

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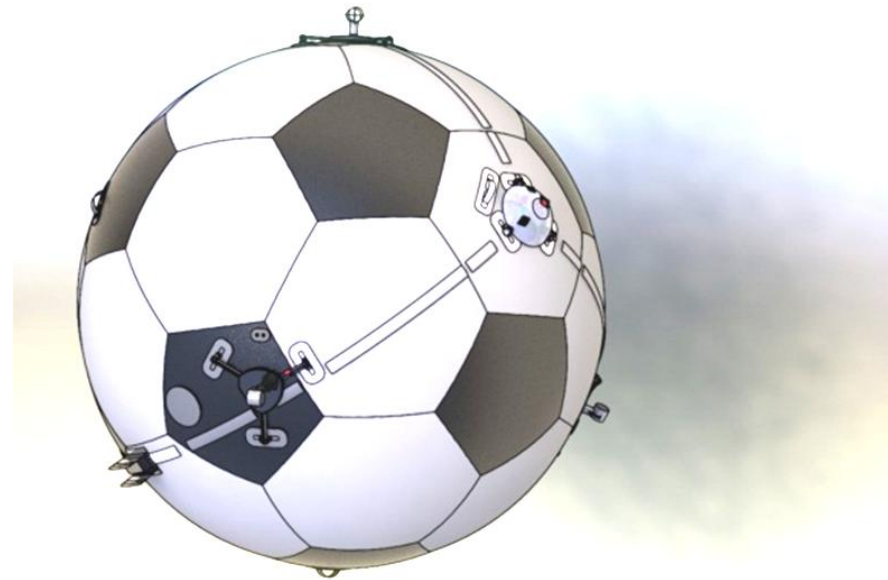
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# Content

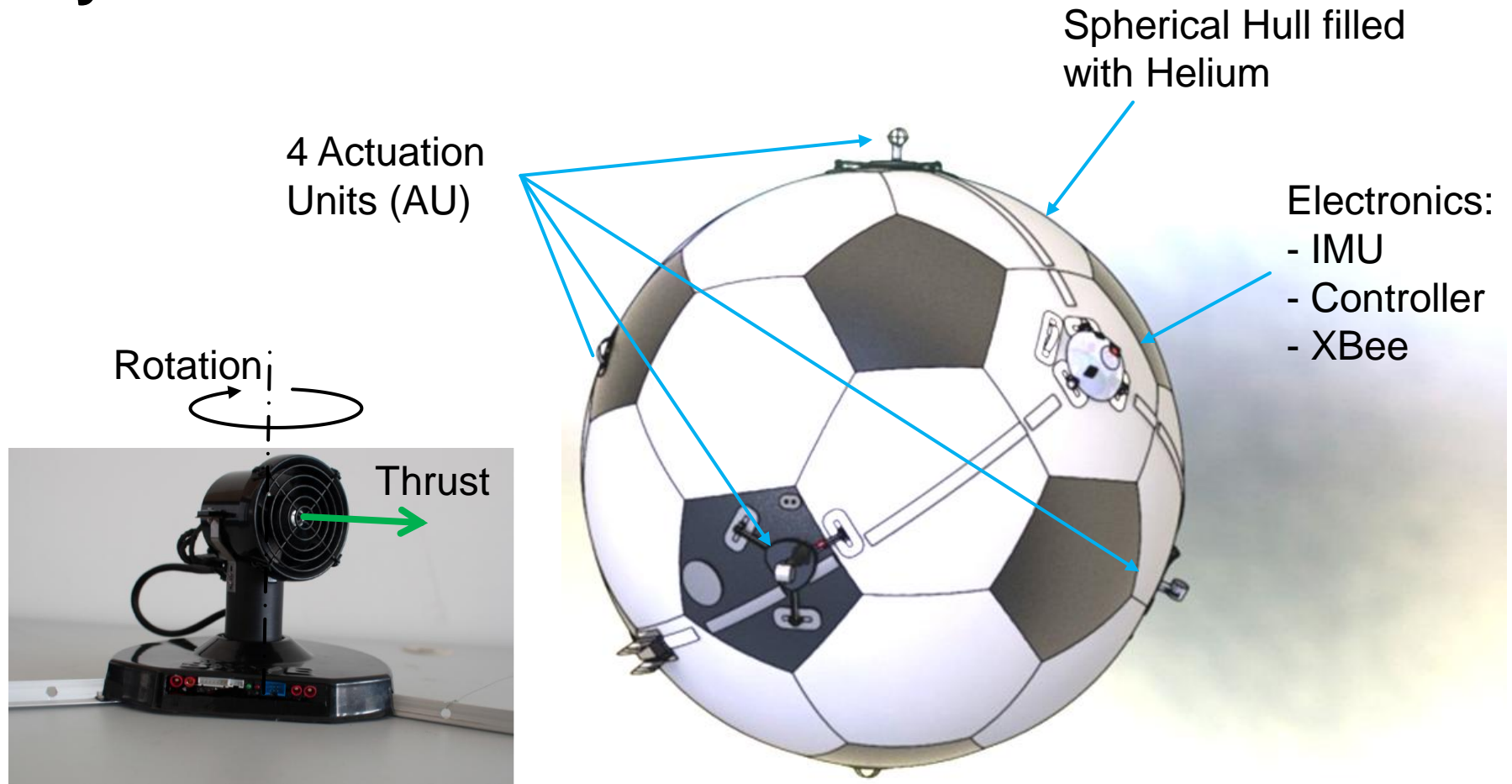
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# Motivation

- FANCY SLIDE
- Parameters



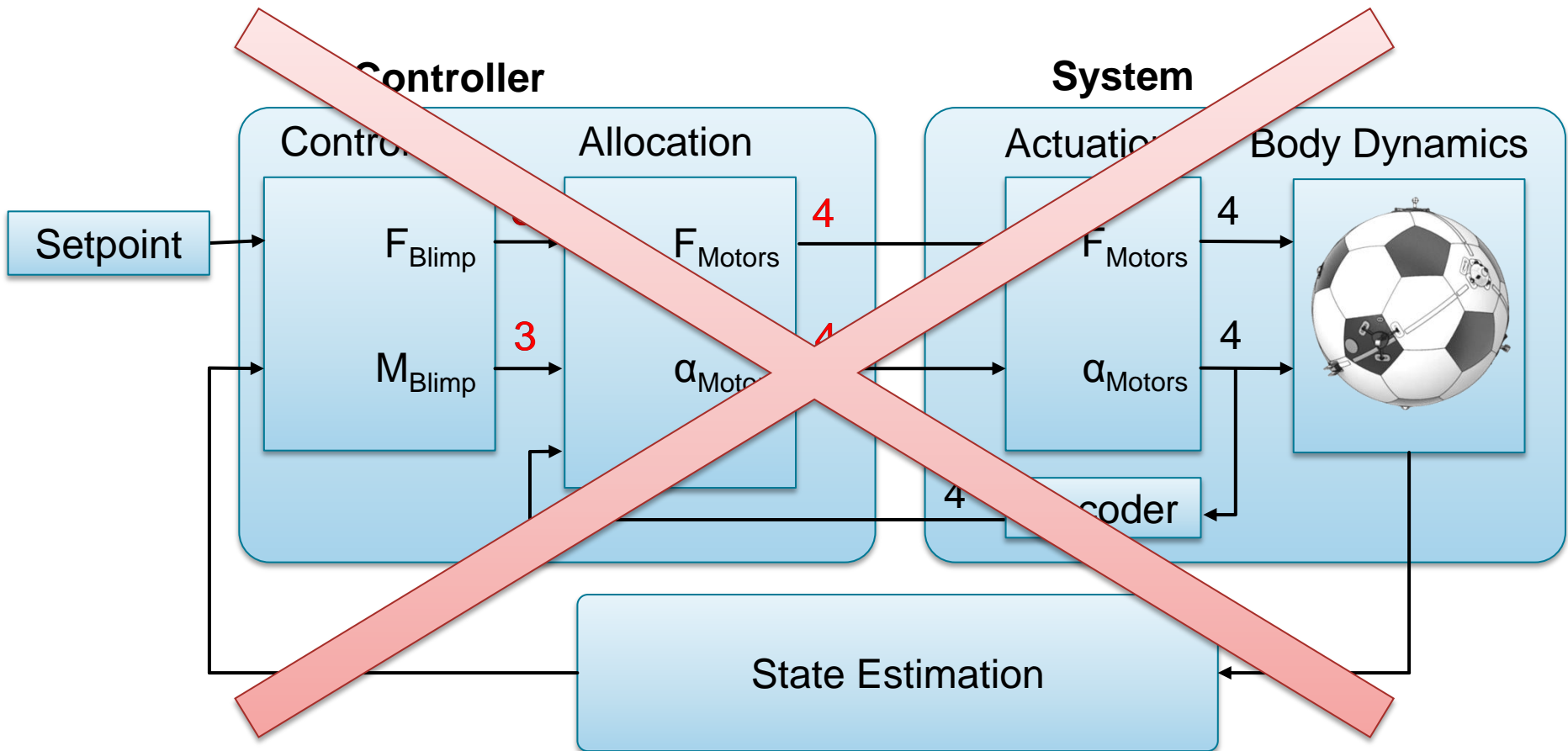
# System Overview



# System Overview



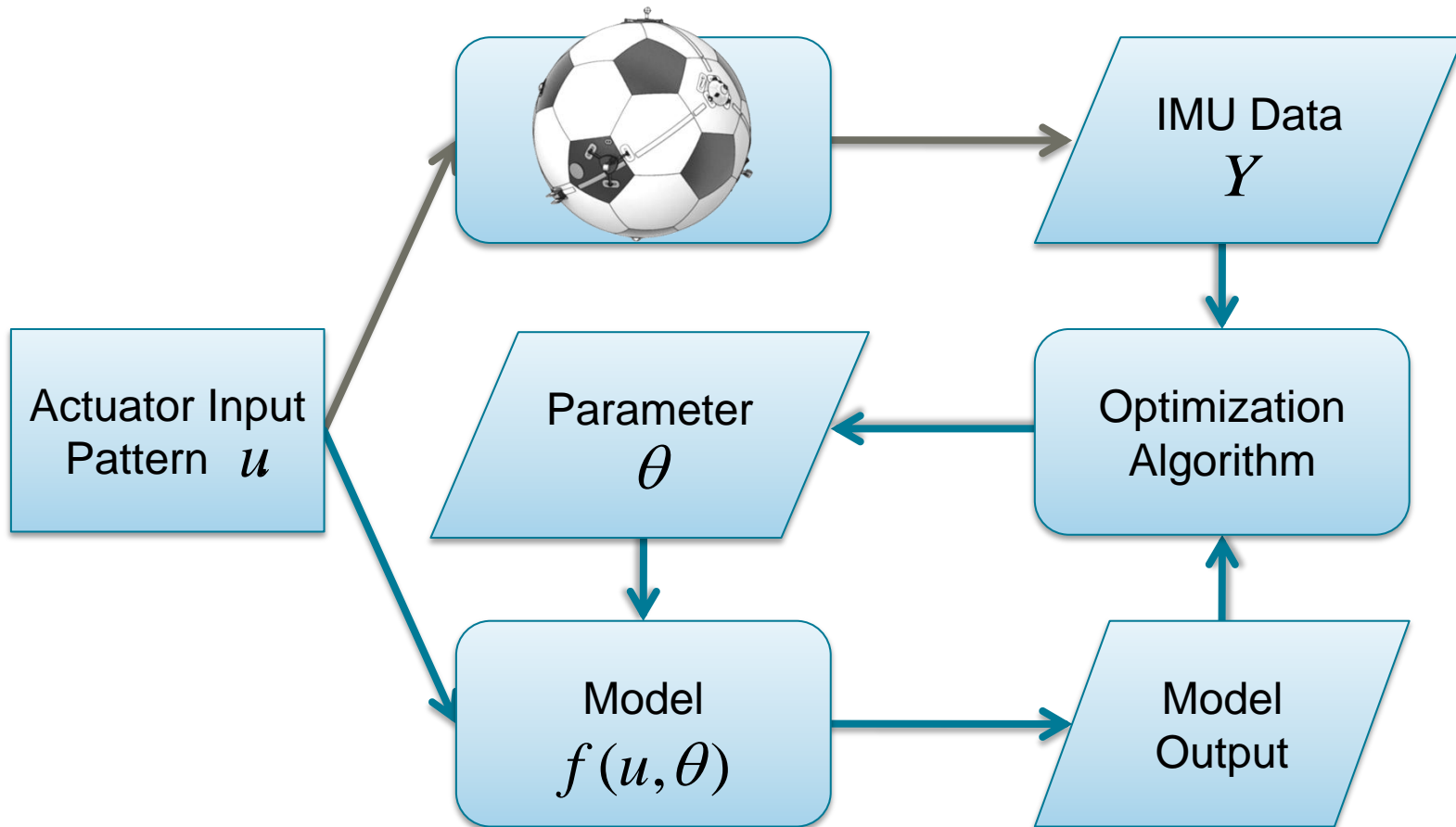
# System Overview



# Goals



# Problem Formulation





# Problem Formulation: System Model

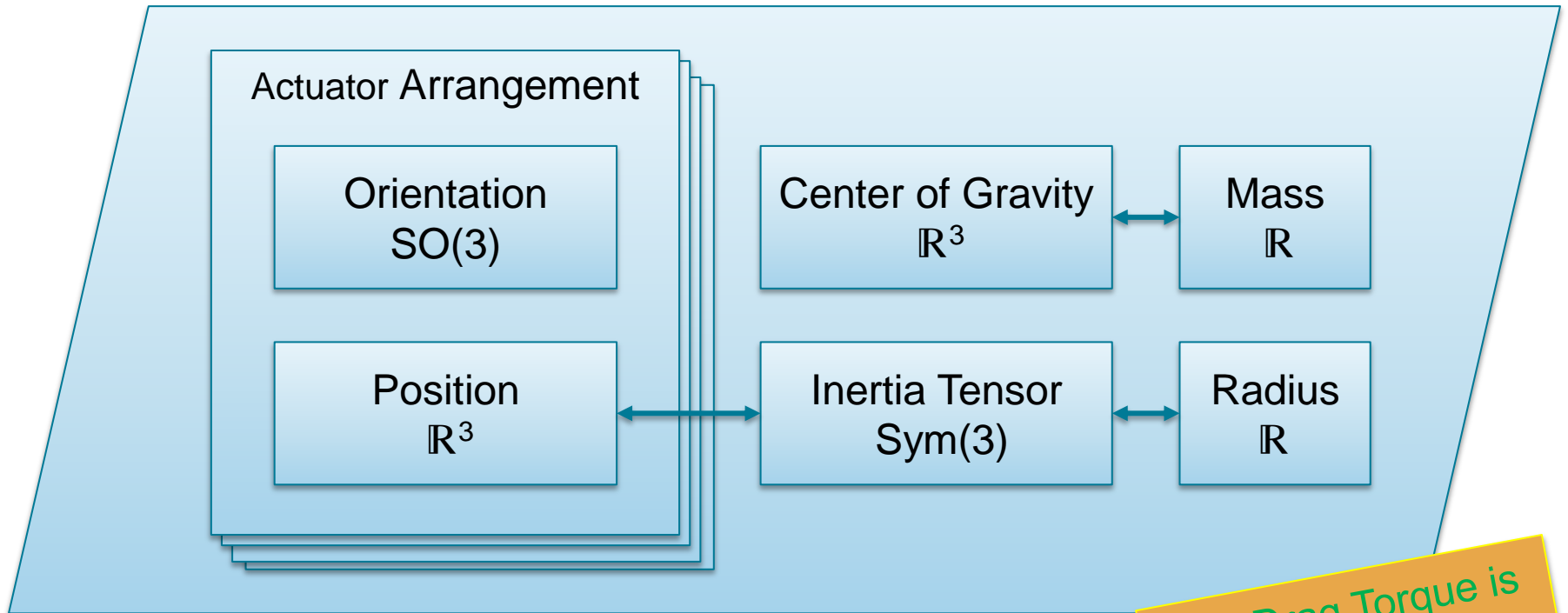
- Angular Acceleration

$$\mathbf{f}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) = \hat{\boldsymbol{\alpha}}_b = \mathbf{J}_b^{-1}(\mathbf{M}_b - \boldsymbol{\omega}_b \times \mathbf{J}_b \boldsymbol{\omega}_b)$$

$$\mathbf{M}_b = \underbrace{\sum_{k=1}^N [\mathbf{C}_{b,m_k} (\mathbf{p}_{m_k}^{m_k, cog} \times \mathbf{F}_{m_k})]}_{\mathbf{M}_{actuation}} - \underbrace{\left( \mathbf{p}_b^{cob, cog} \times (\mathbf{C}_{b,w} m \mathbf{g}_w) \right)}_{\mathbf{M}_{gravity}}$$

- Neglect aerodynamic effects on rotation

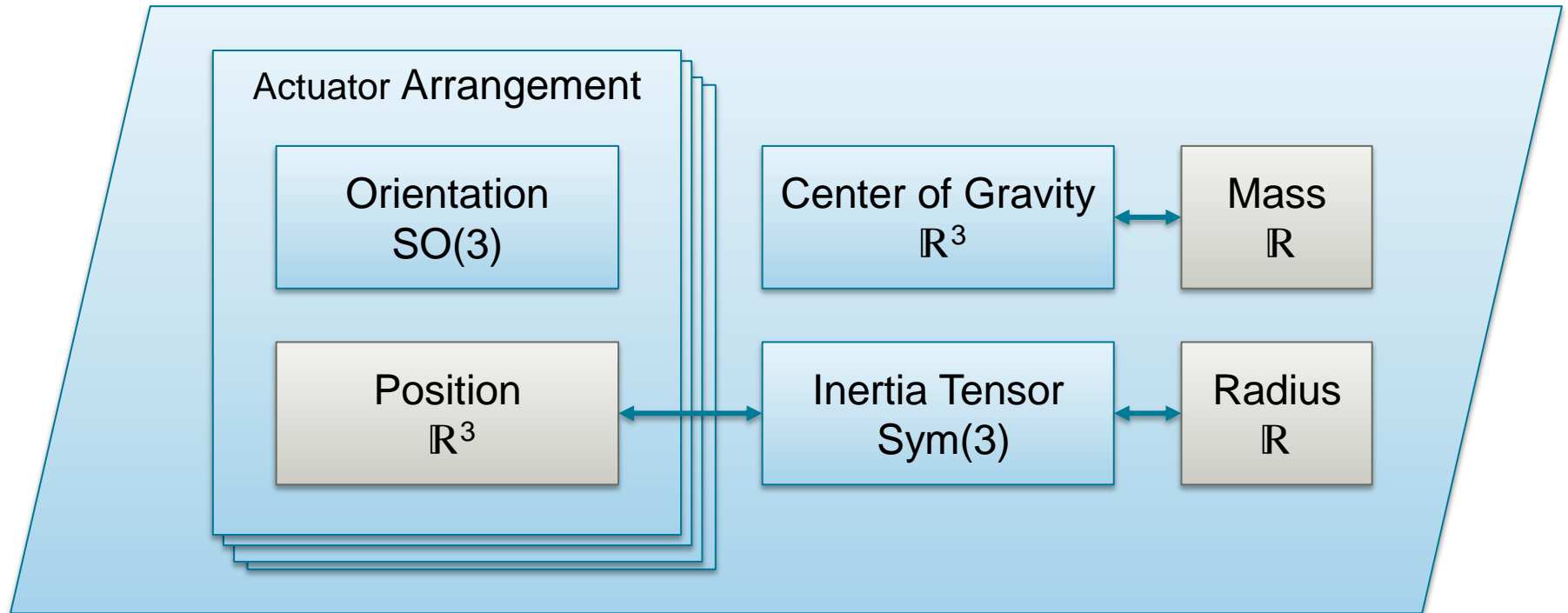
# Problem Formulation: Parameters



Full Parameter set is only jointly observable

e.g. Drag Torque is  
another jointly  
observable param

# Problem Formulation: Parameters



Position is assumed to be on sphere

Radius and mass are fixed (they don't influence result)

# Problem Formulation: System Model

- Angular Acceleration

$$\mathbf{f}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) = \hat{\boldsymbol{\alpha}}_b = \mathbf{J}_b^{-1} (\mathbf{M}_b - \boldsymbol{\omega}_b \times \mathbf{J}_b \boldsymbol{\omega}_b)$$

$$\mathbf{M}_b = \underbrace{\sum_{k=1}^N [\mathbf{C}_{b,m_k} (\mathbf{p}_{m_k}^{m_k, cog} \times \mathbf{F}_{m_k})]}_{\mathbf{M}_{actuation}} - \underbrace{(\mathbf{p}_b^{cob, cog} \times (\mathbf{C}_{b,w} m \mathbf{g}_w))}_{\mathbf{M}_{gravity}}$$

- Assume perfect knowledge of actuator force (in steady state)

# Problem Formulation: Optimization

- Nonlinear Least Squares

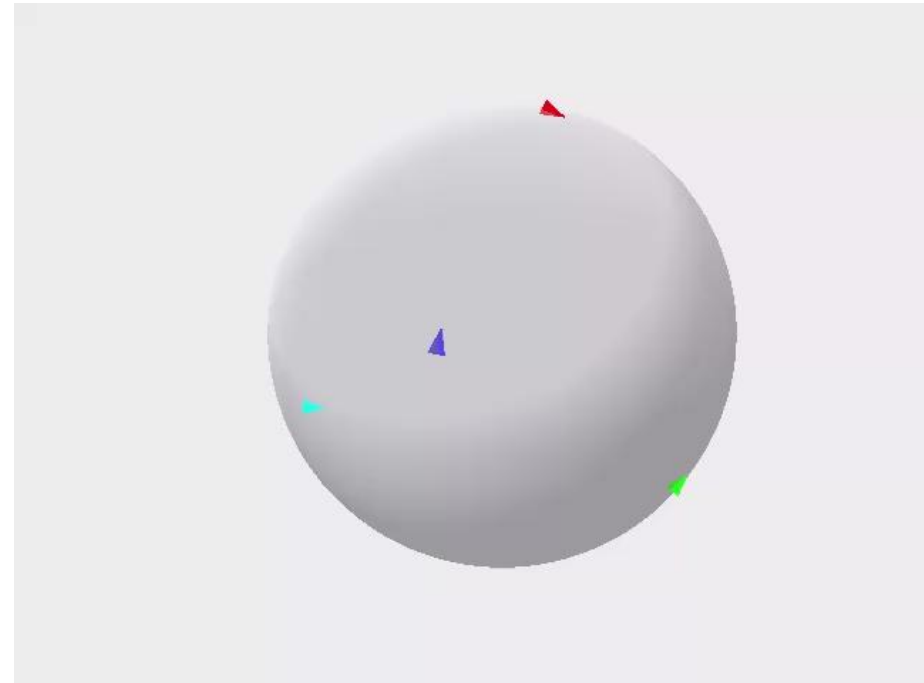
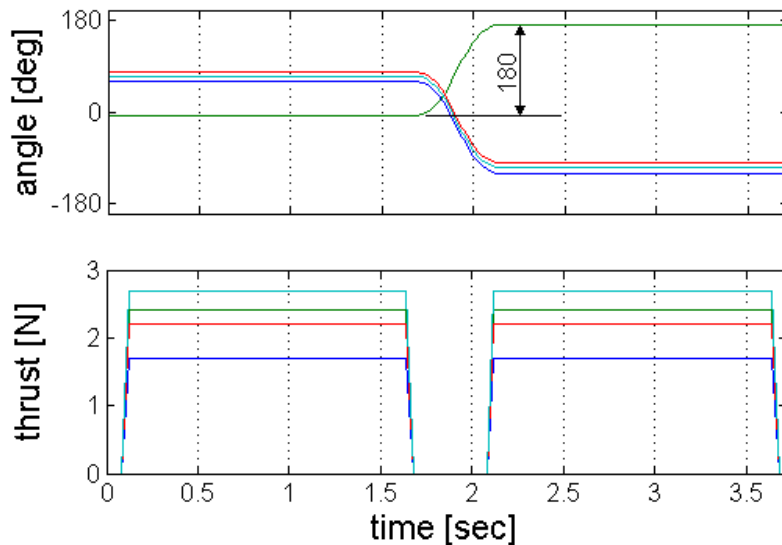
$$S(\boldsymbol{\theta}) = \sum_{i=1}^N \|\mathbf{y}_i - \mathbf{f}(\mathbf{x}_i, \boldsymbol{\theta})\|^2$$

- Levenberg-Marquardt
  - Robust and fast gradient based minimization

$$(\mathbf{J}^\top \mathbf{J} + \lambda \text{diag}(\mathbf{J}^\top \mathbf{J})) \boldsymbol{\delta} = \mathbf{J}^\top [\mathbf{y} - \mathbf{f}(\boldsymbol{\theta})]$$

# Problem Formulation: Input Pattern

- Inputs must be **applicable** and **sufficiently excited**
  - Apply sequence of **forward/backward** force patterns in **varying directions** for all actuation units
  - Steady state motor dynamics



# Simulator



# Results

- Simulation Results
  - Confidence Region
  - Convergence Region
  - Casestudies (no drag; 1AU; 5AU; COG offset;)
- Experimental Results
- Groundtruth with Leica



# Simulation: Confidence Region

- Zeige Konvergenz & Anzahl Iterationen mit LMA

# Simulation: Case studies

mean	AU4 x	AU4 y	J	cog
Default	6.18e-04	7.66e-04	6.12e-02	6.94e-05
No drag	-4.89e-04	1.38e-03	5.16e-02	1.81e-05
std	AU4 x	AU4 y	J	cog
Default	3.65e-03	7.19e-03	3.00e-02	1.35e-04
No drag	4.29e-03	7.96e-03	3.35e-02	1.21e-04

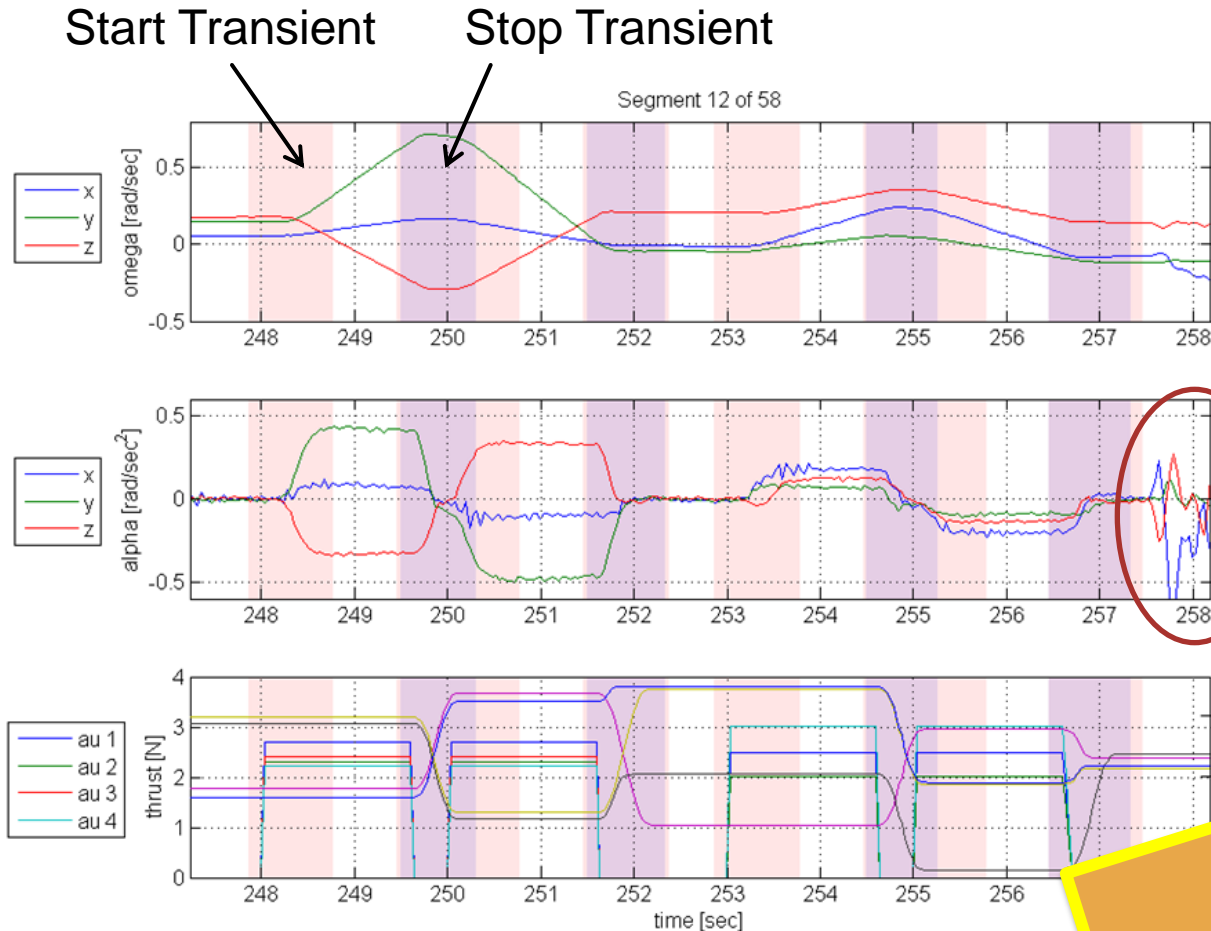
Resnorm [rad/s <sup>2</sup> ]
6.73e-04
6.88e-04

32 simulations à 2000 raw datapoints

# Problem Formulation: Input Pattern



# Data Acquisition (Preprocessing)

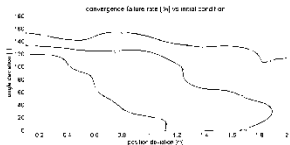
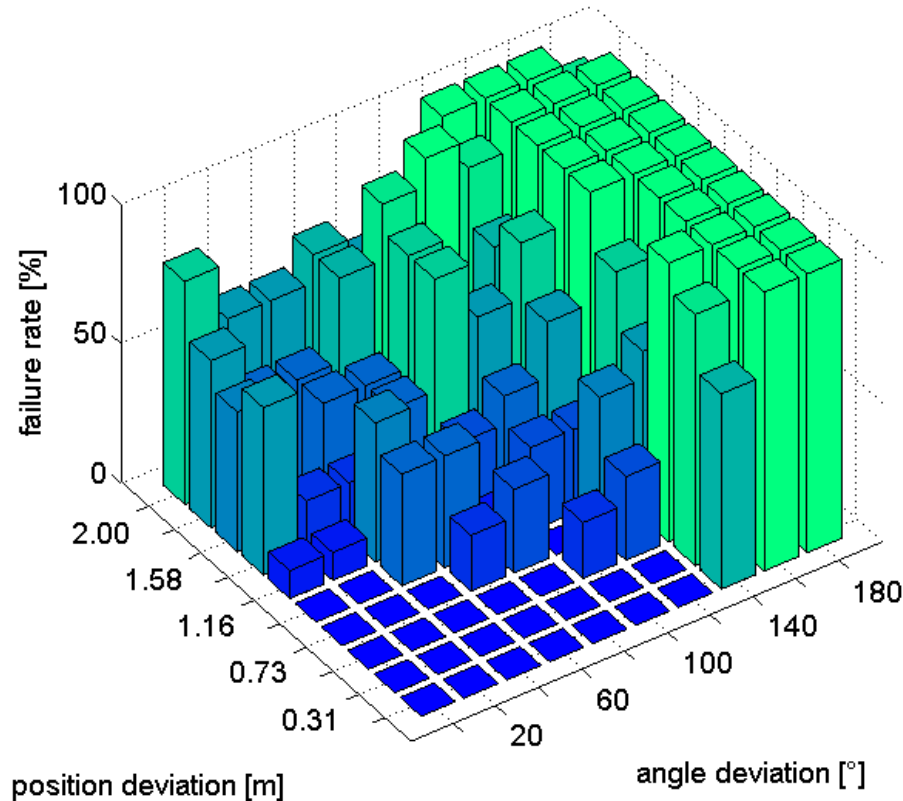


**Disturbance:**  
Remove  
manually

**ZOOM**

# Results: Experiments

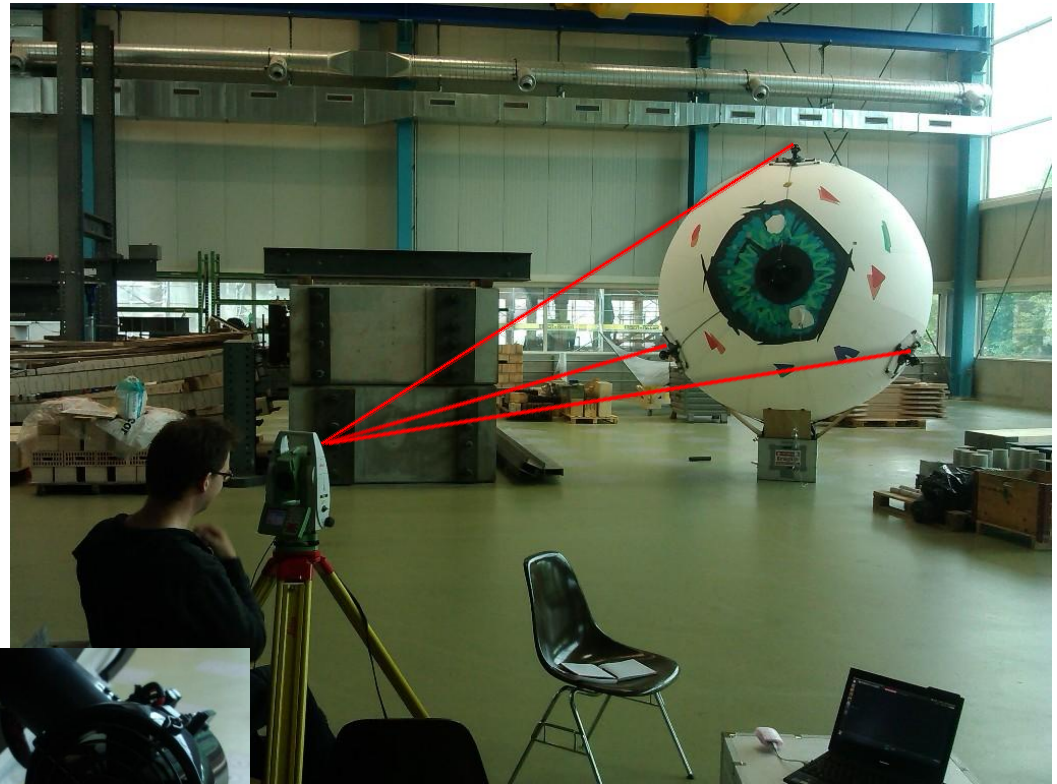
# Simulation: Convergence Region



Initial Parameters can be about **1m or 120°** apart of the true value

## Results: „Ground Truth“ (Leica)

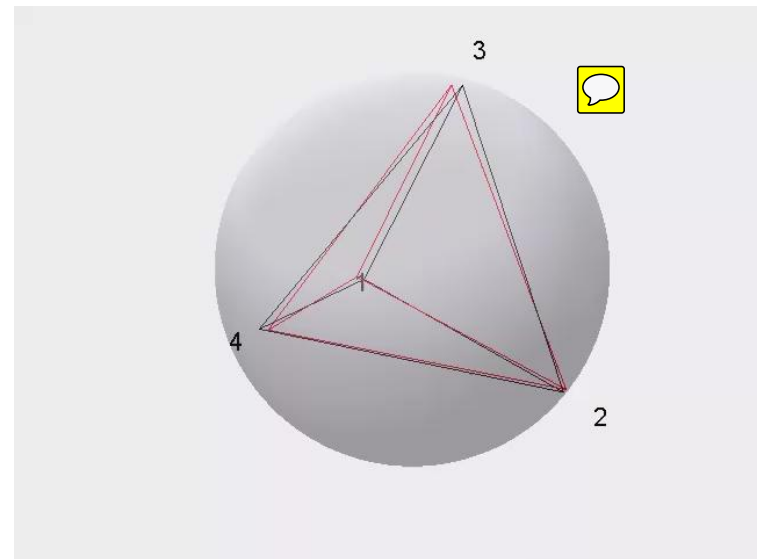
- 3 AU's visible at once
- Use different views
- Fit data to get tetrahedral's edge length
  - Residual below 0.01m



# Results: Compare Leica and Batch Solution

- Compare tetrahedral edge length

Relative error of batch solution			
%	AU2	AU3	AU4
AU1	1.68	0.86	2.76
AU2		0.67	2.47
AU3			3.78



Leica  
Batch



# Discussion



# Outlook