



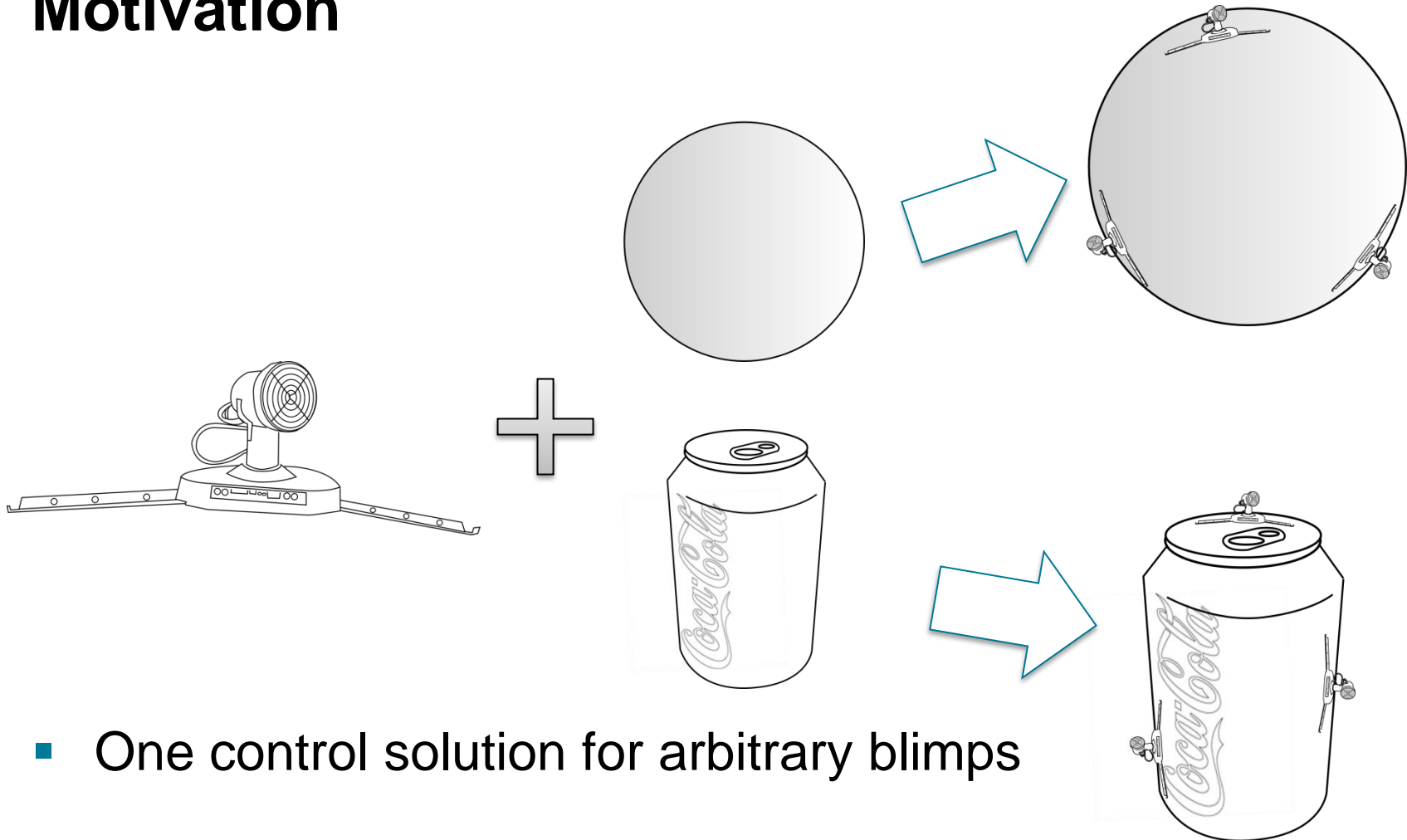
Estimation of Actuation Configuration for a Multi-Actuated Blimp

Final Presentation (Semester Thesis)

Students: Matthias Krebs
Simon Laube

Advisors: Kostas Alexis
Markus Achtelik

Motivation



- One control solution for arbitrary blimps

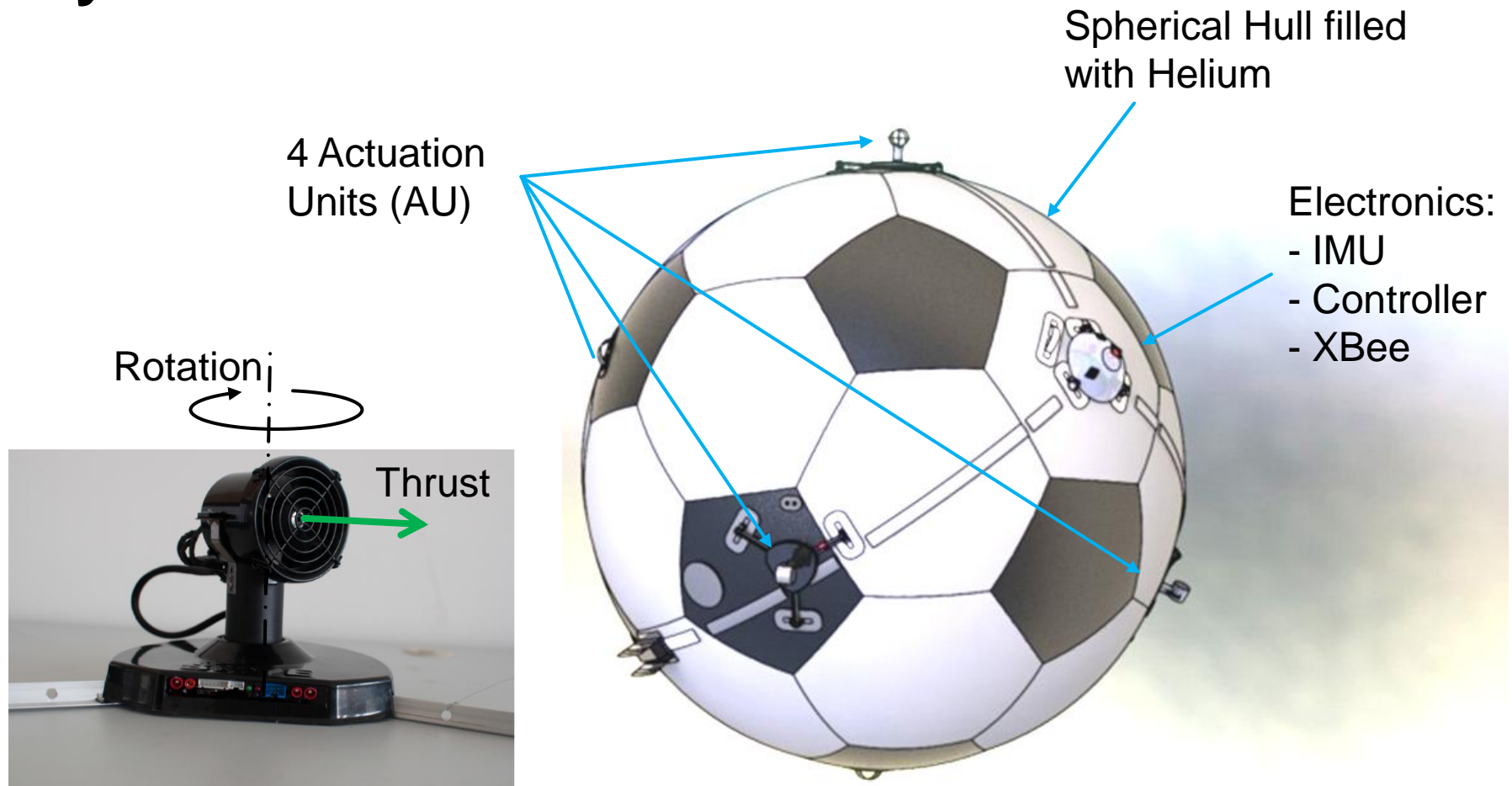
Goal

- Find Blimp model parameters
- Use IMU measurements

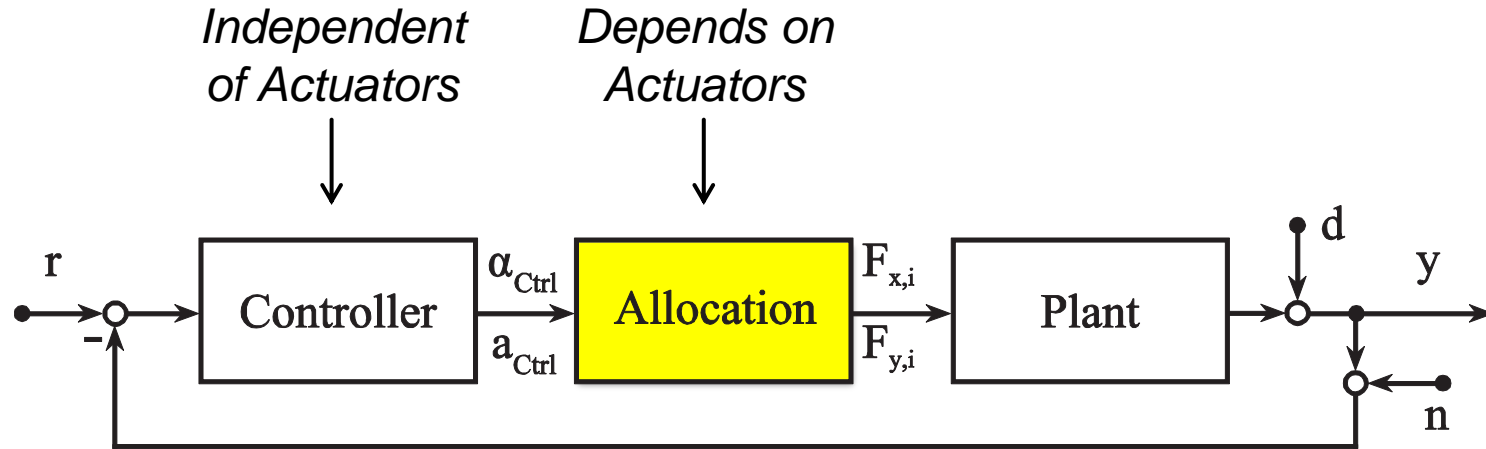
Content

- System Overview
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- Results
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 - Experimental Results
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- Conclusion & Outlook

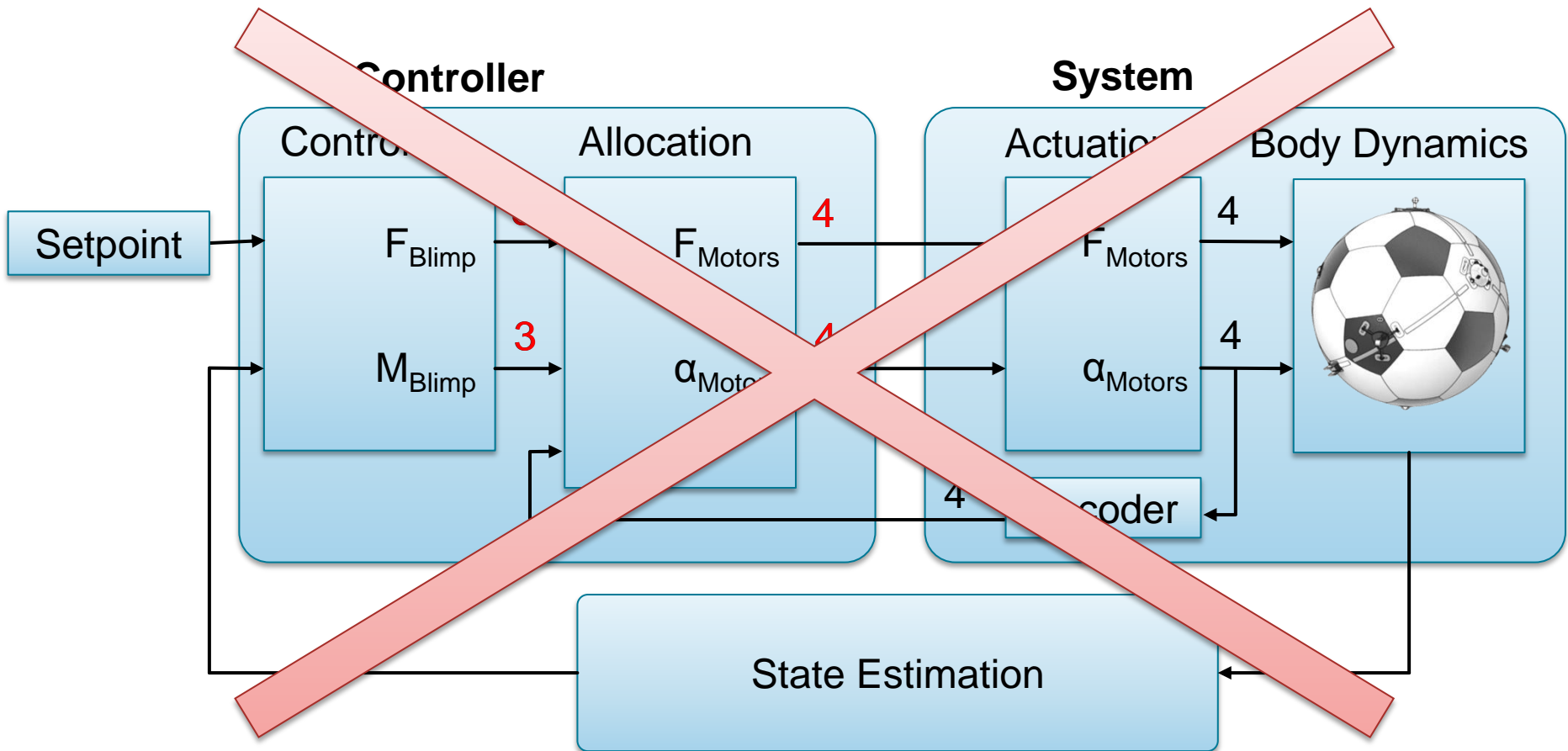
System Overview



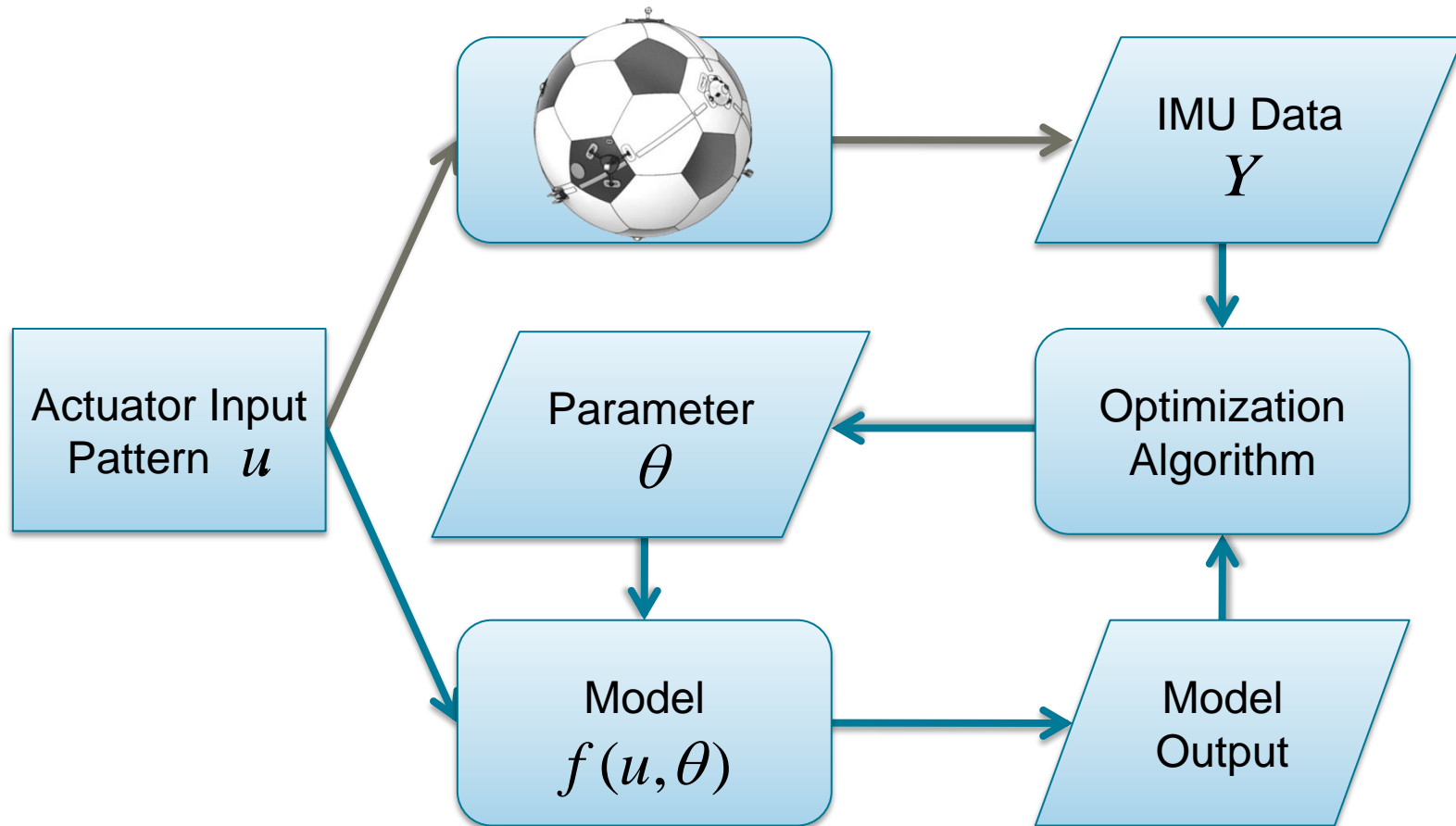
System Overview: Control



System Overview



Problem Formulation



Problem Formulation: System Model

- Angular Acceleration

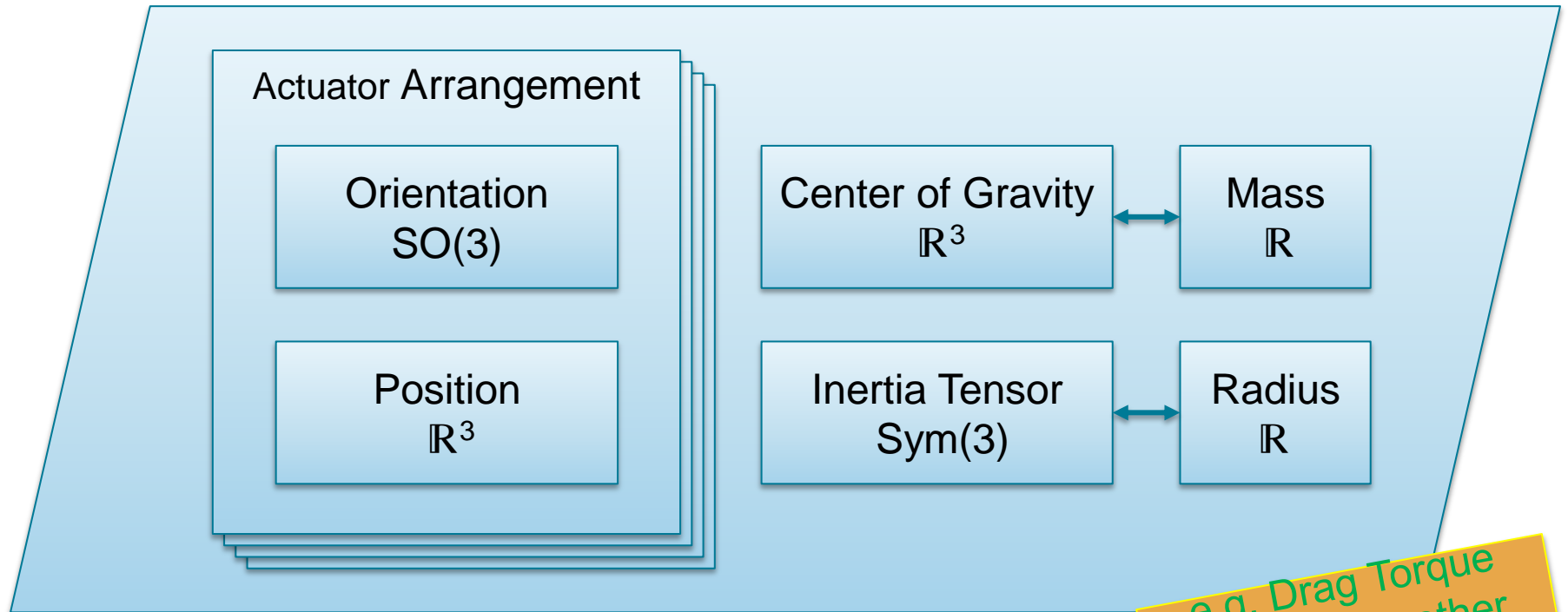
$$\mathbf{f}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) = \hat{\boldsymbol{\alpha}}_b = \mathbf{J}_b^{-1}(\mathbf{M}_b - \boldsymbol{\omega}_b \times \mathbf{J}_b \boldsymbol{\omega}_b)$$

with

$$\mathbf{M}_b = \underbrace{\sum_{k=1}^N [\mathbf{C}_{b,m_k} (\mathbf{p}_{m_k}^{m_k, cog} \times \mathbf{F}_{m_k})]}_{\mathbf{M}^{actuation}} - \underbrace{\left(\mathbf{p}_b^{cob, cog} \times (\mathbf{C}_{b,w} m \mathbf{g}_w) \right)}_{\mathbf{M}^{gravity}}$$

- Aerodynamic effects on rotation neglected ($\mathbf{M}^{aero} \ll \mathbf{M}^{actuation}$)

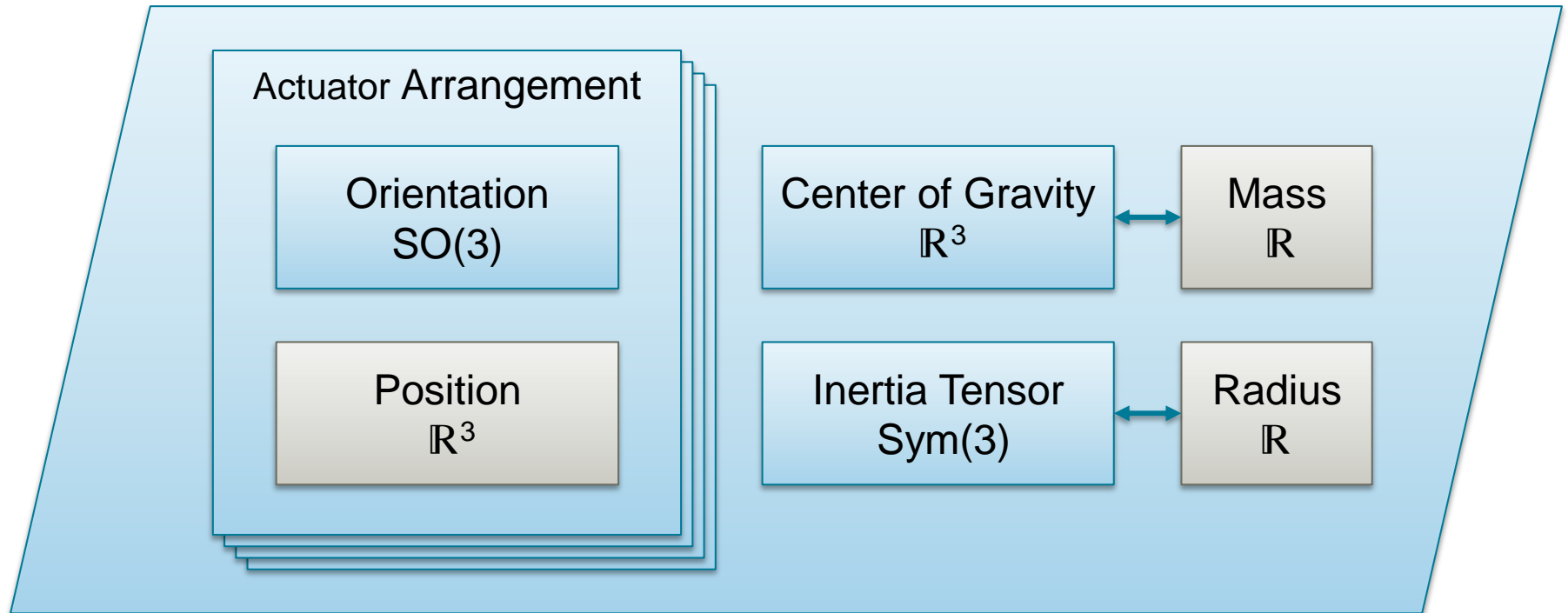
Problem Formulation: Parameters



- Full Parameter set is only jointly observable

e.g. Drag Torque
would be another
jointly observable
param

Problem Formulation: Parameters



- **Position** is assumed to be on sphere
- **Radius** and **mass** are assumed to be known (scales J & cog)

Problem Formulation: System Model

- Angular Acceleration

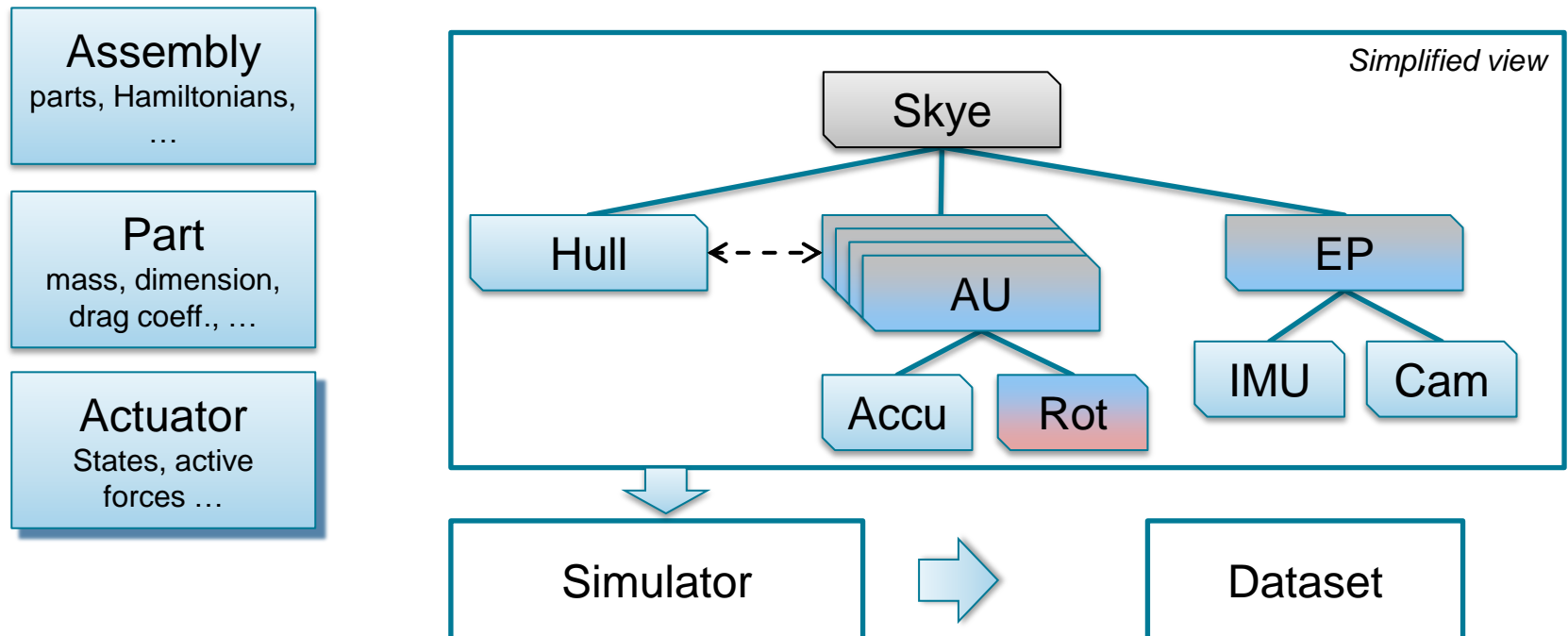
$$\mathbf{f}(\mathbf{x}, \mathbf{u}, \boldsymbol{\theta}) = \hat{\boldsymbol{\alpha}}_b = \mathbf{J}_b^{-1} (\mathbf{M}_b - \boldsymbol{\omega}_b \times \mathbf{J}_b \boldsymbol{\omega}_b)$$

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Simulator

- Object oriented simulator in MATLAB
- Modular concept for (almost) arbitrary blimps



Problem Formulation: Optimization

- Nonlinear Least Squares

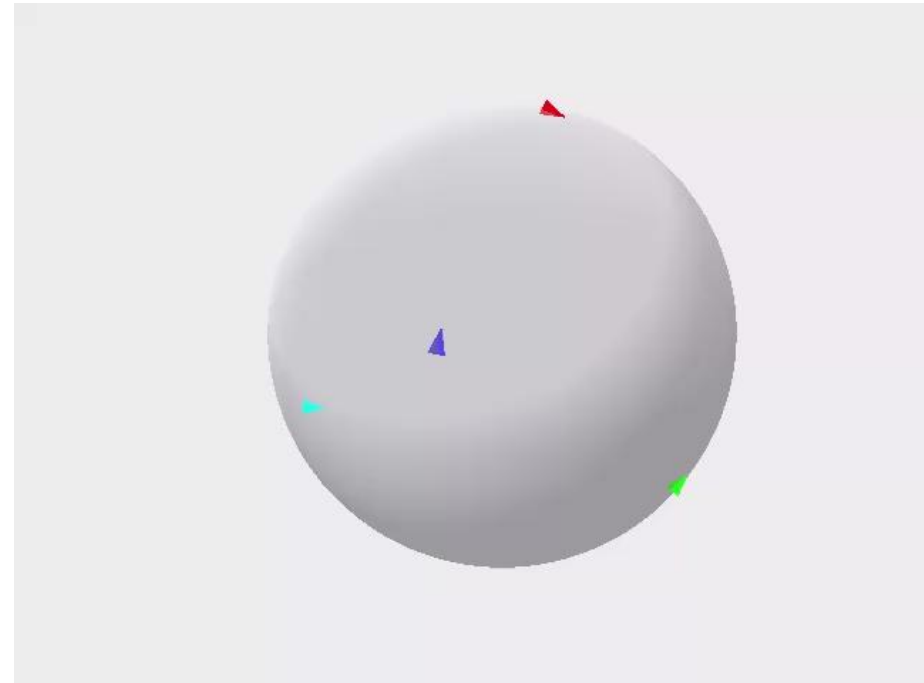
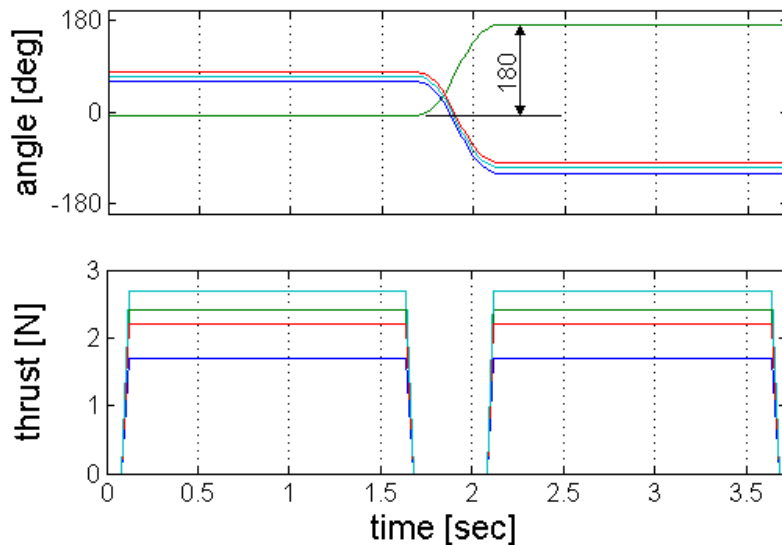
$$S(\boldsymbol{\theta}) = \sum_{i=1}^N \|\mathbf{y}_i - \mathbf{f}(\mathbf{x}_i, \boldsymbol{\theta})\|^2$$

- Levenberg-Marquardt
 - Gradient based minimization
 - Robust and fast convergence

$$(\mathbf{J}^\top \mathbf{J} + \lambda \text{diag}(\mathbf{J}^\top \mathbf{J})) \boldsymbol{\delta} = \mathbf{J}^\top [\mathbf{y} - \mathbf{f}(\boldsymbol{\theta})]$$

Problem Formulation: Input Pattern

- Inputs must be **applicable** and **sufficiently excited**
 - Apply sequence of **forward/backward** force patterns in **varying directions** for all actuation units
 - Steady state motor dynamics



Results

- Simulation Results
 - Confidence Region
 - Convergence Region
 - Casestudies
- Experimental Results
- Groundtruth with Leica

Simulation: Confidence Region

- Zeige Konvergenz & Anzahl Iterationen mit LMA

Simulation: Casestudies

| mean | AU4 x | AU4 y | J | cog |
|-----------|-----------|----------|----------|----------|
| 4 AUs | 6.18e-04 | 7.66e-04 | 6.12e-02 | 6.94e-05 |
| No drag | -4.89e-04 | 1.38e-03 | 5.16e-02 | 1.81e-05 |
| Single AU | | | | |
| | | | | |
| std | AU4 x | AU4 y | J | cog |
| 4 AUs | 3.65e-03 | 7.19e-03 | 3.00e-02 | 1.35e-04 |
| No drag | 4.29e-03 | 7.96e-03 | 3.35e-02 | 1.21e-04 |
| | | | | |
| | | | | |

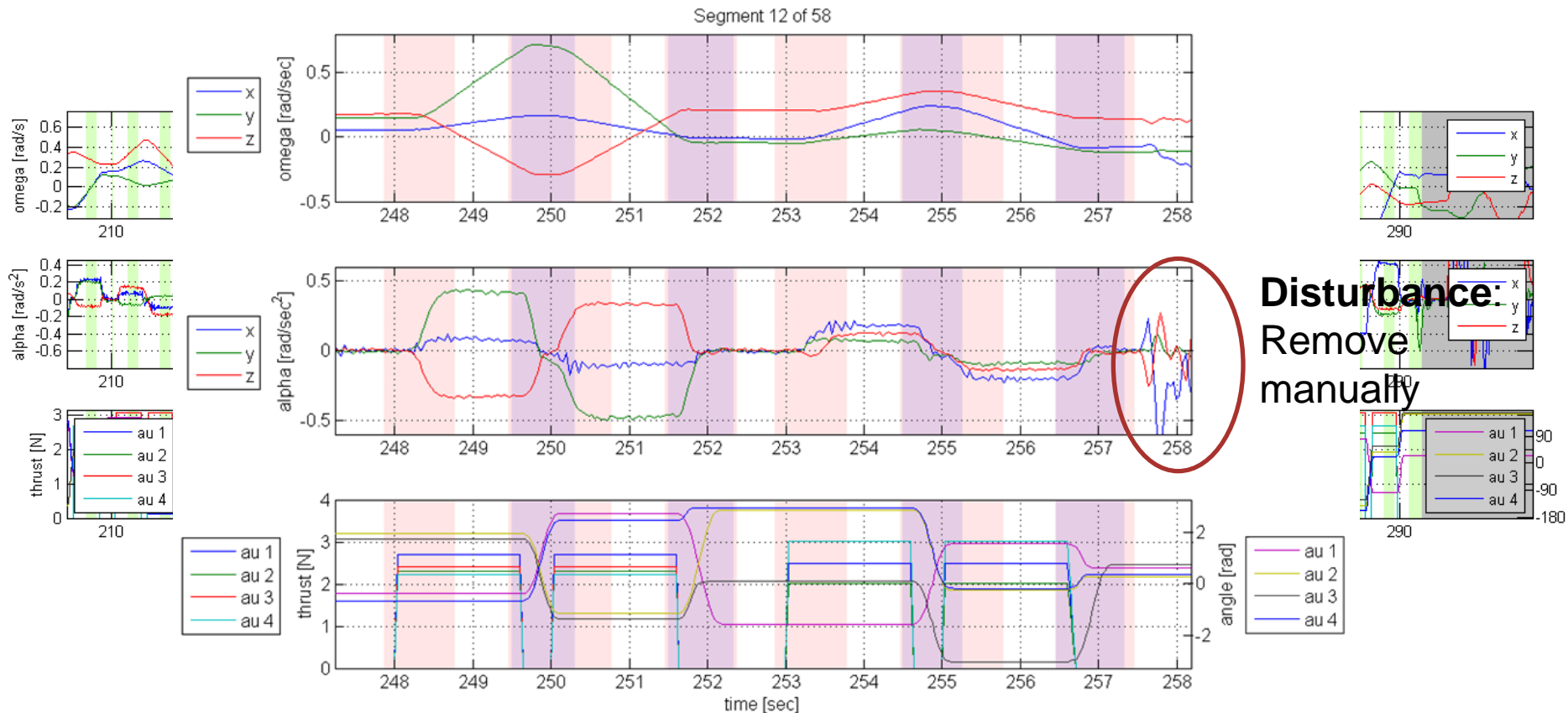
| Resnorm [rad/s ²] |
|-------------------------------|
| 6.73e-04 |
| 6.88e-04 |
| |
| |

32 simulations à 2000 raw datapoints

Problem Formulation: Input Pattern

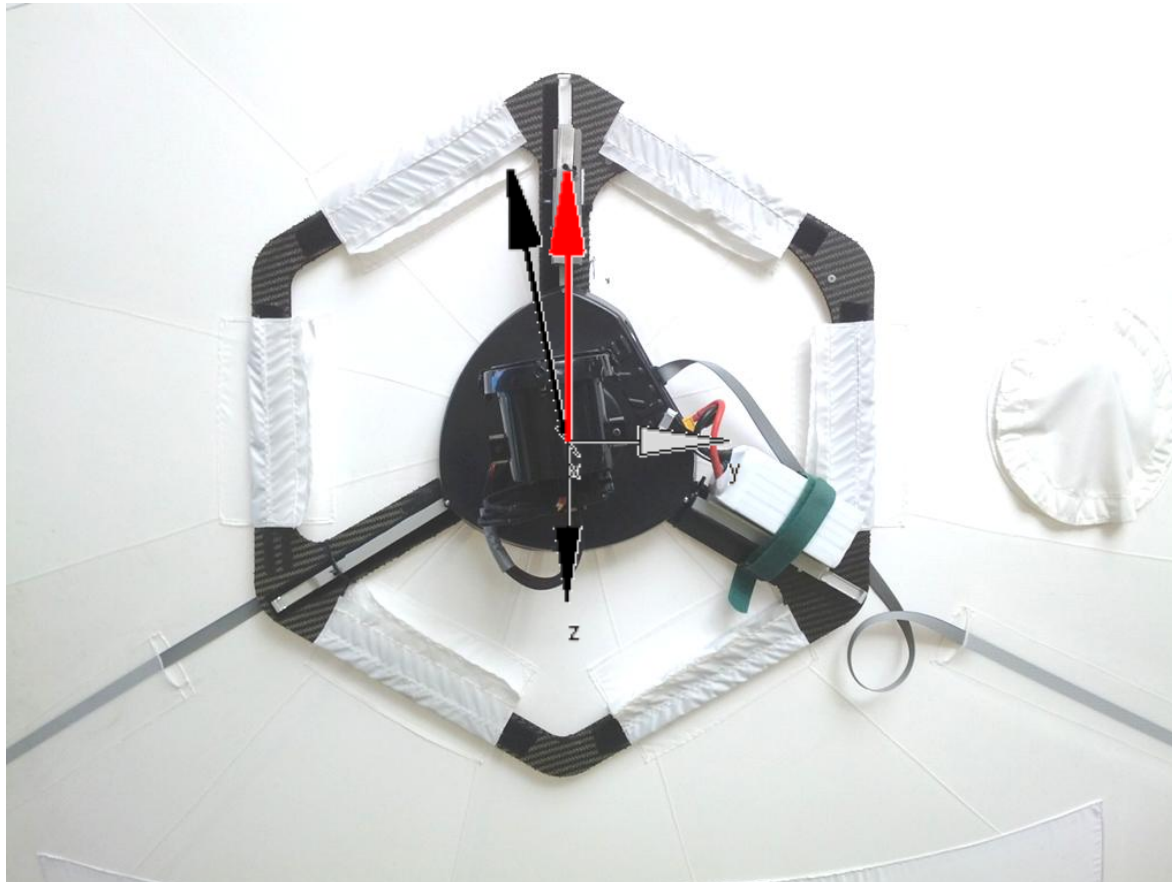


Data Acquisition (Preprocessing)

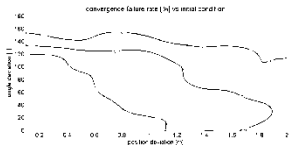
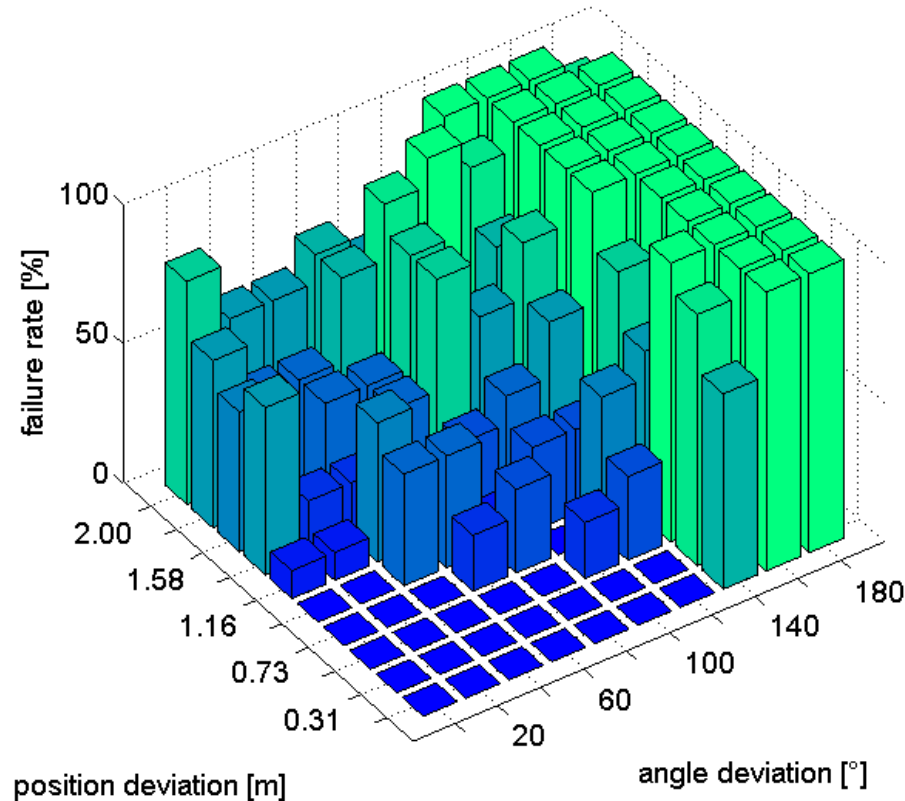


Results: Experiments

Experiments

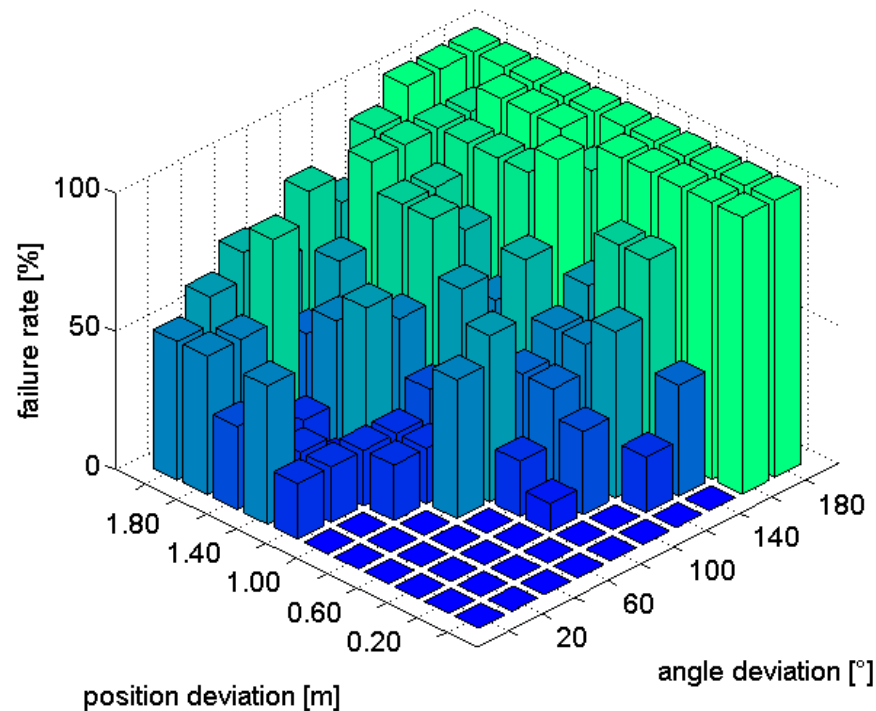


Simulation: Convergence Region



Initial Parameters can be about **1m or 120°** apart of the true value

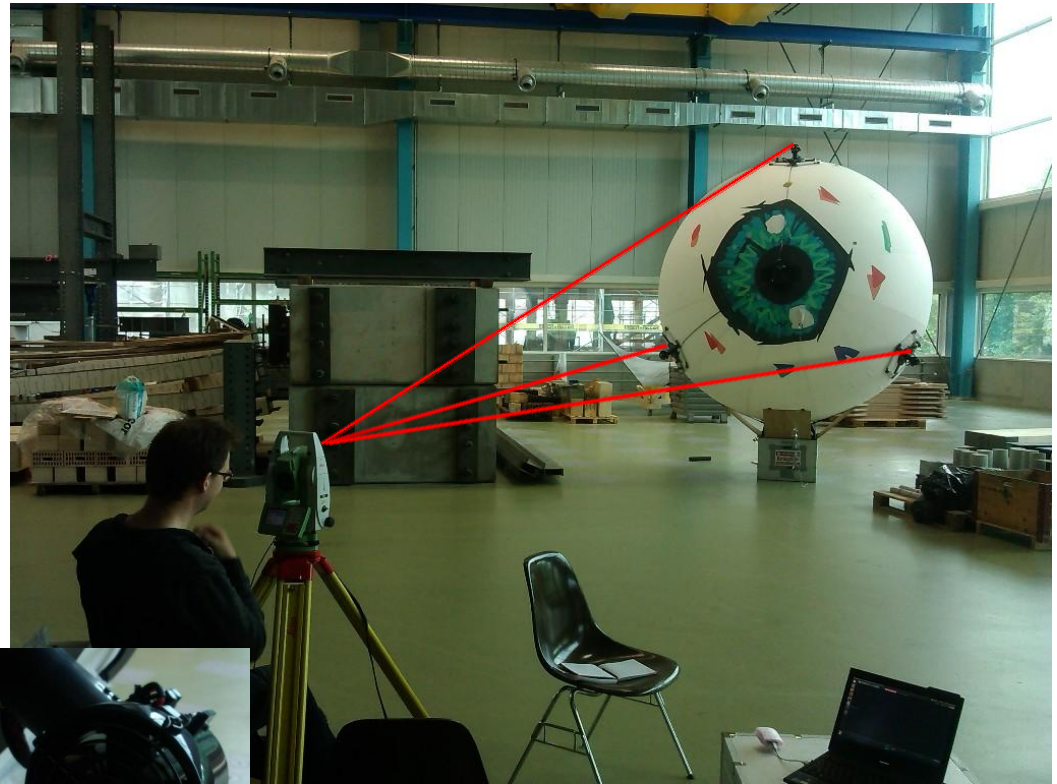
Experiment: Convergence Region



Initial Parameters can be about **1m or 120°** apart of the true value

Results: „Ground Truth“ (Leica)

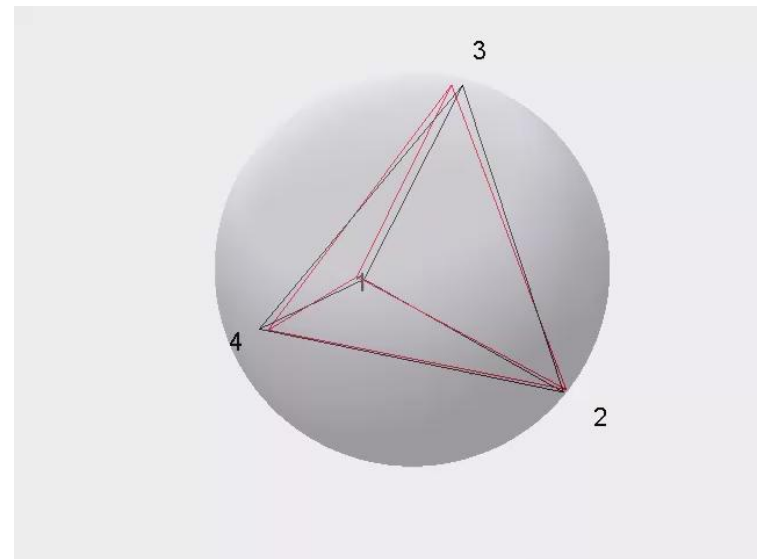
- 3 AU's visible at once
- Use different views
- Fit data to get tetrahedral's edge length
 - Residual below 0.01m



Results: Compare Leica and Batch Solution

- Compare tetrahedral edge length

| Relative error of batch solution | | | |
|----------------------------------|------|------|------|
| % | AU2 | AU3 | AU4 |
| AU1 | 1.68 | 0.86 | 2.76 |
| AU2 | | 0.67 | 2.47 |
| AU3 | | | 3.78 |



Leica
Batch

Discussion

- To be done!
- How can data be used

Outlook

- To be done
- Use data for allocation
- Best length of input patterns
- Use it for different Blimps