

```
In [1]: import warnings
warnings.filterwarnings("ignore")
```

```
In [2]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

```
In [3]: from statsmodels.tsa.statespace.sarimax import SARIMAX
from pmdarima import auto_arima
from statsmodels.tsa.seasonal import seasonal_decompose
```

```
In [7]: from sklearn.metrics import mean_absolute_percentage_error, mean_sq
```

```
In [8]: import scipy.stats as stats
```

```
In [9]: df=pd.read_csv('RestaurantVisitors.csv',index_col='date',parse_date
```

```
In [10]: df
```

```
Out[10]:
```

	weekday	holiday	holiday_name	rest1	rest2	rest3	rest4	total
date								
2016-01-01	Friday	1	New Year's Day	65.0	25.0	67.0	139.0	296.0
2016-01-02	Saturday	0	na	24.0	39.0	43.0	85.0	191.0
2016-01-03	Sunday	0	na	24.0	31.0	66.0	81.0	202.0
2016-01-04	Monday	0	na	23.0	18.0	32.0	32.0	105.0
2016-01-05	Tuesday	0	na	2.0	15.0	38.0	43.0	98.0
...	...	...	...	...	...	...	...	...
2017-05-27	Saturday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-28	Sunday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-29	Monday	1	Memorial Day	NaN	NaN	NaN	NaN	NaN
2017-05-30	Tuesday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-31	Wednesday	0	na	NaN	NaN	NaN	NaN	NaN

517 rows × 8 columns

In [11]:

```
df.index.freq='D'
```

In [12]:

```
df.tail()
```

Out [12]:

	weekday	holiday	holiday_name	rest1	rest2	rest3	rest4	total
date								
2017-05-27	Saturday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-28	Sunday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-29	Monday	1	Memorial Day	NaN	NaN	NaN	NaN	NaN
2017-05-30	Tuesday	0	na	NaN	NaN	NaN	NaN	NaN
2017-05-31	Wednesday	0	na	NaN	NaN	NaN	NaN	NaN

In [13]:

```
df1=df.dropna()
df1.tail()
```

Out [13]:

	weekday	holiday	holiday_name	rest1	rest2	rest3	rest4	total
date								
2017-04-18	Tuesday	0	na	30.0	30.0	13.0	18.0	91.0
2017-04-19	Wednesday	0	na	20.0	11.0	30.0	18.0	79.0
2017-04-20	Thursday	0	na	22.0	3.0	19.0	46.0	90.0
2017-04-21	Friday	0	na	38.0	53.0	36.0	38.0	165.0
2017-04-22	Saturday	0	na	97.0	20.0	50.0	59.0	226.0

In [14]: df1.info()

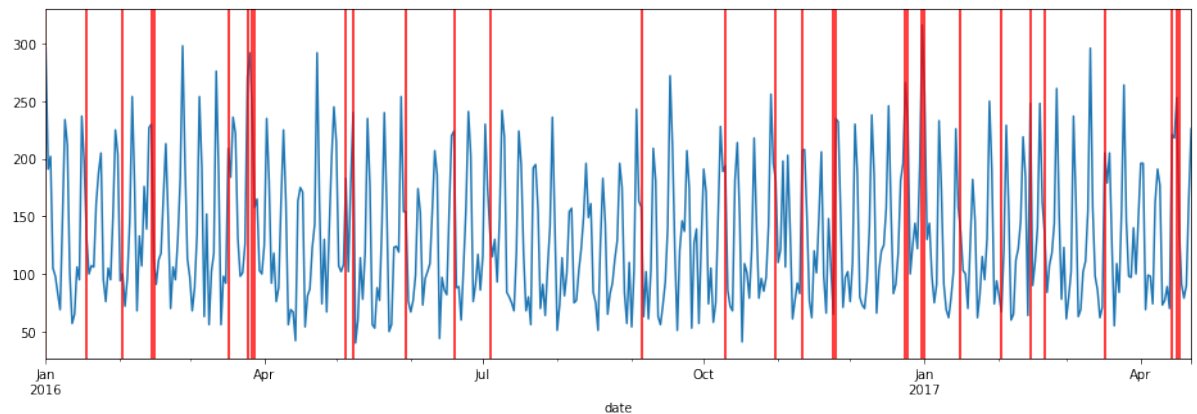
```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 478 entries, 2016-01-01 to 2017-04-22
Freq: D
Data columns (total 8 columns):
#   Column          Non-Null Count  Dtype
---  -
0   weekday         478 non-null    object
1   holiday         478 non-null    int64
2   holiday_name    478 non-null    object
3   rest1          478 non-null    float64
4   rest2          478 non-null    float64
5   rest3          478 non-null    float64
6   rest4          478 non-null    float64
7   total          478 non-null    float64
dtypes: float64(5), int64(1), object(2)
memory usage: 33.6+ KB
```

In [17]: cols=['rest1','rest2','rest3','rest4','total']  
for col in cols:  
df1[col]=df1[col].astype(int)

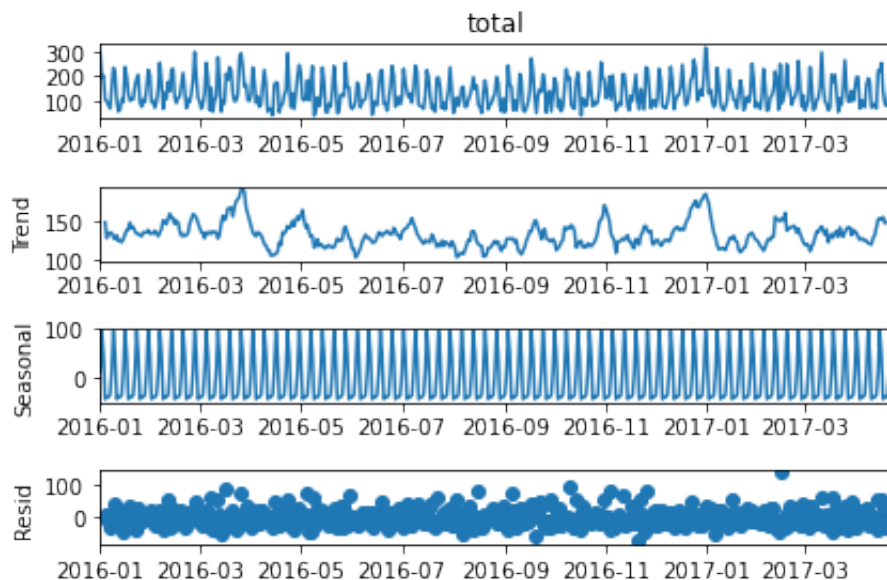
In [18]: df1.info()

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 478 entries, 2016-01-01 to 2017-04-22
Freq: D
Data columns (total 8 columns):
#   Column          Non-Null Count  Dtype
---  -
0   weekday         478 non-null    object
1   holiday         478 non-null    int64
2   holiday_name    478 non-null    object
3   rest1          478 non-null    int64
4   rest2          478 non-null    int64
5   rest3          478 non-null    int64
6   rest4          478 non-null    int64
7   total          478 non-null    int64
dtypes: int64(6), object(2)
memory usage: 33.6+ KB
```

```
In [19]: ax=df1['total'].plot(figsize=(16,5))
for x in df1.query('holiday==1').index:
    ax.axvline(x=x,color='r')
```



```
In [20]: result=seasonal_decompose(df1['total'])
result.plot();
```



```
In [21]: auto_arima(df1['total'],seasonal=True,m=7,trace=True).summary()
```

Performing stepwise search to minimize aic

ARIMA(2,0,2)(1,0,1)[7]	intercept	: AIC=inf, Time=1.03 sec
ARIMA(0,0,0)(0,0,0)[7]	intercept	: AIC=5269.484, Time=0.01 sec
ARIMA(1,0,0)(1,0,0)[7]	intercept	: AIC=4916.749, Time=0.34 sec
ARIMA(0,0,1)(0,0,1)[7]	intercept	: AIC=5049.644, Time=0.20 sec
ARIMA(0,0,0)(0,0,0)[7]		: AIC=6126.084, Time=0.01 sec
ARIMA(1,0,0)(0,0,0)[7]	intercept	: AIC=5200.790, Time=0.06 sec
ARIMA(1,0,0)(2,0,0)[7]	intercept	: AIC=4845.442, Time=0.89 sec
ARIMA(1,0,0)(2,0,1)[7]	intercept	: AIC=inf, Time=1.14 sec
ARIMA(1,0,0)(1,0,1)[7]	intercept	: AIC=4816.600, Time=0.53 sec
ARIMA(1,0,0)(0,0,1)[7]	intercept	: AIC=5058.642, Time=0.25 sec
ARIMA(1,0,0)(1,0,2)[7]	intercept	: AIC=4951.803, Time=0.97 sec
ARIMA(1,0,0)(0,0,2)[7]	intercept	: AIC=4982.776, Time=0.45 sec

```

ARIMA(1,0,0)(2,0,2)[7] intercept : AIC=inf, Time=1.24 sec
ARIMA(0,0,0)(1,0,1)[7] intercept : AIC=4770.490, Time=0.49 sec
ARIMA(0,0,0)(0,0,1)[7] intercept : AIC=5093.130, Time=0.09 sec
ARIMA(0,0,0)(1,0,0)[7] intercept : AIC=4926.360, Time=0.23 sec
ARIMA(0,0,0)(2,0,1)[7] intercept : AIC=4975.347, Time=1.11 sec
ARIMA(0,0,0)(1,0,2)[7] intercept : AIC=4968.926, Time=0.74 sec
ARIMA(0,0,0)(0,0,2)[7] intercept : AIC=5010.582, Time=0.29 sec
ARIMA(0,0,0)(2,0,0)[7] intercept : AIC=4859.638, Time=1.22 sec
ARIMA(0,0,0)(2,0,2)[7] intercept : AIC=inf, Time=1.07 sec
ARIMA(0,0,1)(1,0,1)[7] intercept : AIC=inf, Time=0.62 sec
ARIMA(1,0,1)(1,0,1)[7] intercept : AIC=inf, Time=0.73 sec
ARIMA(0,0,0)(1,0,1)[7] intercept : AIC=inf, Time=0.14 sec

```

Best model: ARIMA(0,0,0)(1,0,1)[7] intercept  
 Total fit time: 13.897 seconds

Out [21]:

SARIMAX Results

<b>Dep. Variable:</b>	y	<b>No. Observations:</b>	478
<b>Model:</b>	SARIMAX(1, 0, [1], 7)	<b>Log Likelihood</b>	-2381.245
<b>Date:</b>	Tue, 26 Apr 2022	<b>AIC</b>	4770.490
<b>Time:</b>	06:55:33	<b>BIC</b>	4787.169
<b>Sample:</b>	0	<b>HQIC</b>	4777.048
	- 478		
<b>Covariance Type:</b>	opg		

	coef	std err	z	P> z	[0.025	0.975]
<b>intercept</b>	4.0723	1.600	2.545	0.011	0.936	7.209
<b>ar.S.L7</b>	0.9680	0.012	81.909	0.000	0.945	0.991
<b>ma.S.L7</b>	-0.7313	0.051	-14.451	0.000	-0.830	-0.632
<b>sigma2</b>	1248.4033	75.522	16.530	0.000	1100.384	1396.423

<b>Ljung-Box (L1) (Q):</b>	14.32	<b>Jarque-Bera (JB):</b>	59.98
<b>Prob(Q):</b>	0.00	<b>Prob(JB):</b>	0.00
<b>Heteroskedasticity (H):</b>	0.87	<b>Skew:</b>	0.71
<b>Prob(H) (two-sided):</b>	0.38	<b>Kurtosis:</b>	4.01

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

```
In [22]: train=df1.iloc[:436]
test=df1.iloc[436:]
len(test)
```

Out [22]: 42

```
In [23]: model=SARIMAX(train['total'],order=(0,0,0),seasonal_order=(1,0,1,7)
model.summary()
```

RUNNING THE L-BFGS-B CODE

\* \* \*

Machine precision = 2.220D-16

N = 3 M = 10

At X0 0 variables are exactly at the bounds

At iterate 0 f= 5.01719D+00 |proj g|= 8.65114D-02

At iterate 5 f= 4.98913D+00 |proj g|= 3.10711D-02

At iterate 10 f= 4.97484D+00 |proj g|= 1.66063D-02

At iterate 15 f= 4.96669D+00 |proj g|= 5.66525D-04

At iterate 20 f= 4.96644D+00 |proj g|= 2.66764D-06

\* \* \*

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

\* \* \*

N	Tit	Tnf	Tnint	Skip	Nact	Projg	F
3	20	24	1	0	0	2.668D-06	4.966D+00

F = 4.9664421023955105

CONVERGENCE: NORM\_OF\_PROJECTED\_GRADIENT\_<=\_PGTOL

This problem is unconstrained.

Out [23]: SARIMAX Results

Dep. Variable: total No. Observations: 436

Model: SARIMAX(1, 0, [1], 7) Log Likelihood -2165.369

<b>Date:</b>	Tue, 26 Apr 2022	<b>AIC</b>	4336.738
<b>Time:</b>	06:55:45	<b>BIC</b>	4348.970
<b>Sample:</b>	01-01-2016	<b>HQIC</b>	4341.565
	- 03-11-2017		
<b>Covariance Type:</b>	opg		

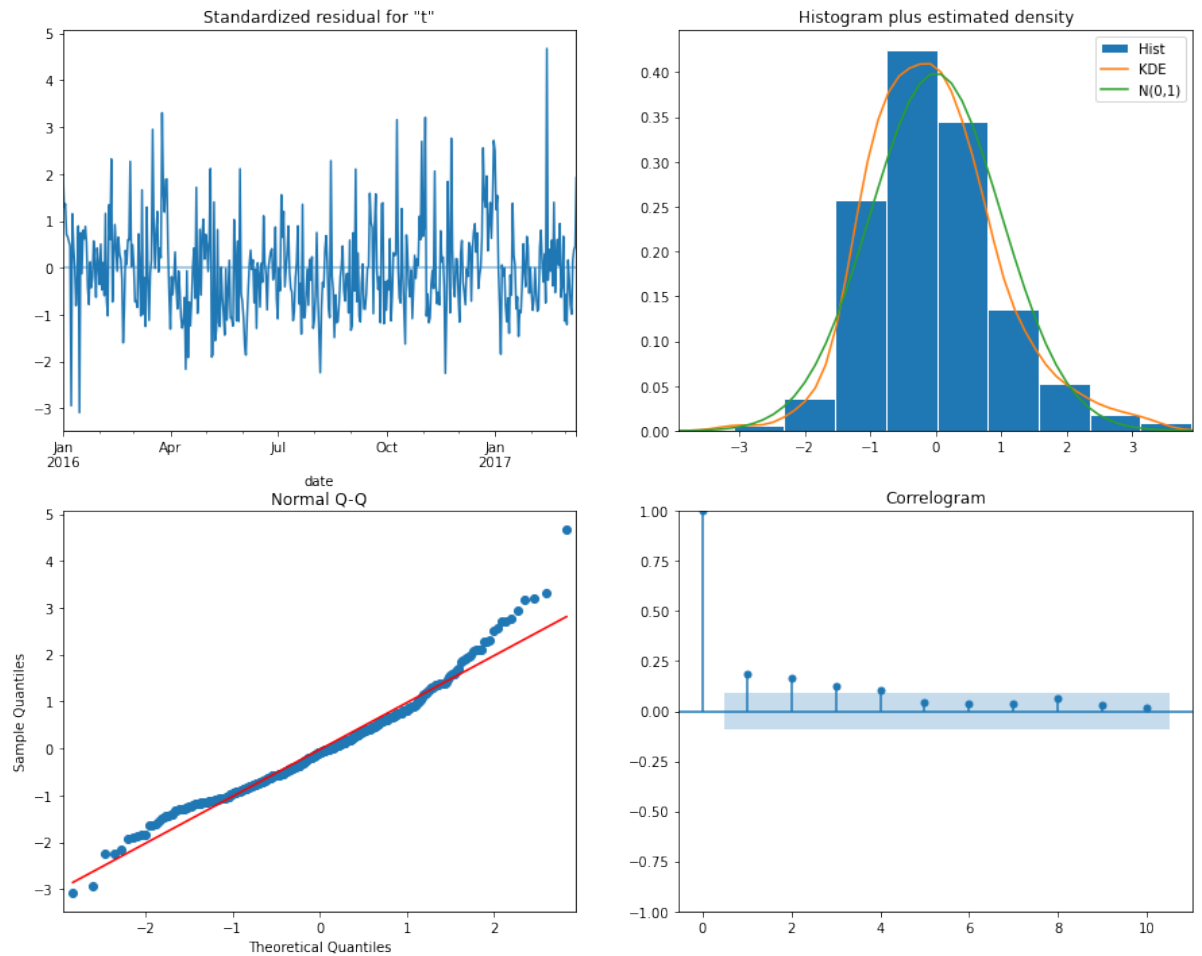
	coef	std err	z	P> z	[0.025	0.975]
<b>ar.S.L7</b>	0.9999	9.58e-05	1.04e+04	0.000	1.000	1.000
<b>ma.S.L7</b>	-0.9383	0.024	-39.198	0.000	-0.985	-0.891
<b>sigma2</b>	1111.8065	58.739	18.928	0.000	996.680	1226.932

<b>Ljung-Box (L1) (Q):</b>	15.40	<b>Jarque-Bera (JB):</b>	83.56
<b>Prob(Q):</b>	0.00	<b>Prob(JB):</b>	0.00
<b>Heteroskedasticity (H):</b>	0.96	<b>Skew:</b>	0.72
<b>Prob(H) (two-sided):</b>	0.81	<b>Kurtosis:</b>	4.59

Warnings:

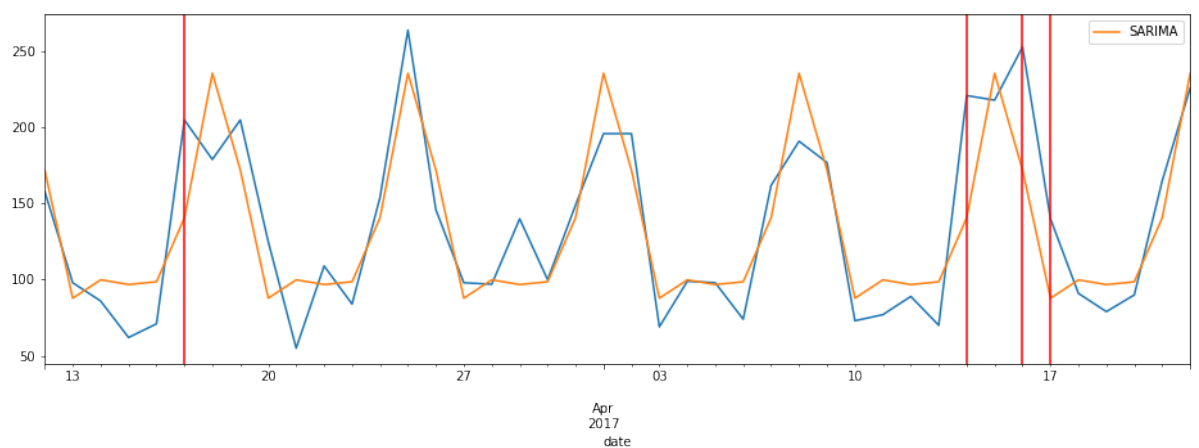
[1] Covariance matrix calculated using the outer product of gradients (complex-step).

```
In [24]: model.plot_diagnostics(figsize=(15,12));
```



```
In [25]: start=len(train)
end=start+len(test)-1
predictions=model.predict(start=start,end=end,dynamic=False).rename
```

```
In [26]: ax=test['total'].plot(figsize=(16,5))
predictions.plot(legend=True)
for x in test.query('holiday==1').index:
    ax.axvline(x=x,color='r')
```





```
In [28]: mean_absolute_percentage_error(test['total'], predictions)
```

```
Out[28]: 0.20157016526303326
```

```
In [29]: modelExog=SARIMAX(train['total'], exog=train['holiday'], order=(0,0,0)
modelExog.summary())
```

This problem is unconstrained.

RUNNING THE L-BFGS-B CODE

\* \* \*

Machine precision = 2.220D-16

N = 4 M = 10

At X0 0 variables are exactly at the bounds

At iterate 0 f= 5.24304D+00 |proj g|= 7.49269D-02

At iterate 5 f= 5.09816D+00 |proj g|= 9.66459D-03

At iterate 10 f= 4.81986D+00 |proj g|= 1.11454D-02

At iterate 15 f= 4.81298D+00 |proj g|= 2.51383D-04

At iterate 20 f= 4.81287D+00 |proj g|= 8.62111D-05

\* \* \*

Tit = total number of iterations

Tnf = total number of function evaluations

Tnint = total number of segments explored during Cauchy searches

Skip = number of BFGS updates skipped

Nact = number of active bounds at final generalized Cauchy point

Projg = norm of the final projected gradient

F = final function value

\* \* \*

N	Tit	Tnf	Tnint	Skip	Nact	Projg	F
4	23	27	1	0	0	4.105D-06	4.813D+00
F =	4.8128709766911708						

CONVERGENCE: NORM\_OF\_PROJECTED\_GRADIENT\_<=\_PGTOL

```
Out [29]: SARIMAX Results
```

<b>Dep. Variable:</b>	total	<b>No. Observations:</b>	436
<b>Model:</b>	SARIMAX(1, 0, [1], 7)	<b>Log Likelihood</b>	-2098.412
<b>Date:</b>	Tue, 26 Apr 2022	<b>AIC</b>	4204.823

**Time:** 06:56:42 **BIC** 4221.134  
**Sample:** 01-01-2016 **HQIC** 4211.260  
 - 03-11-2017  
**Covariance Type:** opg

	coef	std err	z	P> z	[0.025	0.975]
<b>holiday</b>	69.6423	3.968	17.550	0.000	61.865	77.420
<b>ar.S.L7</b>	0.9999	7.57e-05	1.32e+04	0.000	1.000	1.000
<b>ma.S.L7</b>	-0.9429	0.023	-40.396	0.000	-0.989	-0.897
<b>sigma2</b>	813.5453	47.380	17.171	0.000	720.681	906.409

**Ljung-Box (L1) (Q):** 15.58 **Jarque-Bera (JB):** 20.71

**Prob(Q):** 0.00 **Prob(JB):** 0.00

**Heteroskedasticity (H):** 1.00 **Skew:** 0.23

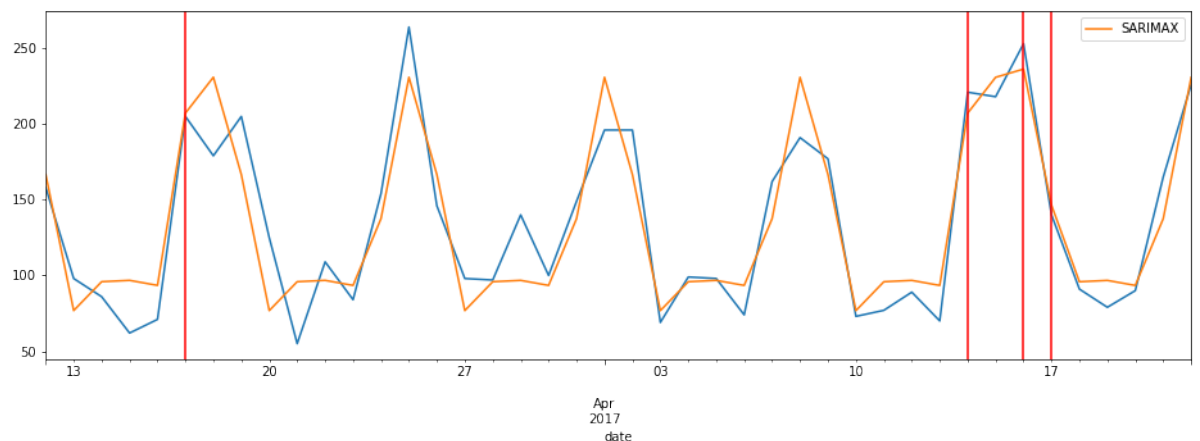
**Prob(H) (two-sided):** 1.00 **Kurtosis:** 3.96

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

```
In [30]: predictionsExog=modelExog.predict(start=start,end=end,exog=test['ho
```

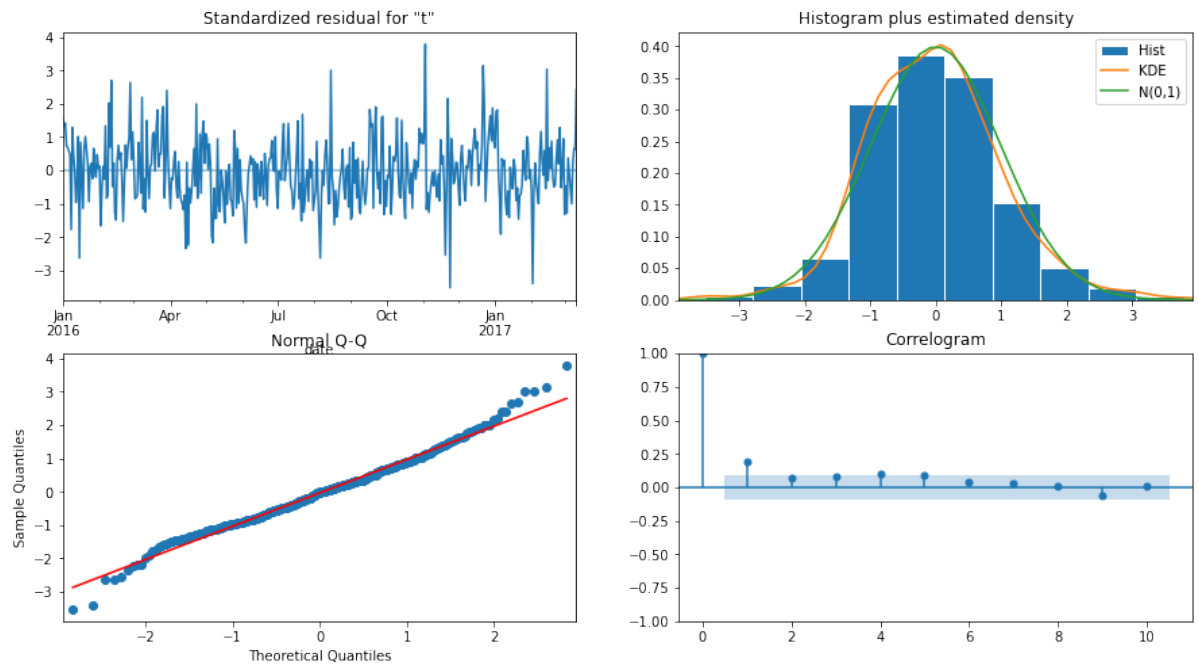
```
In [31]: ax=test['total'].plot(figsize=(16,5))
          predictionsExog.plot(legend=True)
          for x in test.query('holiday==1').index:
              ax.axvline(x=x,color='r')
```



In [32]:

```
mean_absolute_percentage_error(test['total'], predictionsExog)
```

Out[32]: 0.16142983735081276

In [33]: `modelExog.plot_diagnostics(figsize=(15,8));`

In [ ]: