

Warshel, A., & Levitt, M. (1976). Theoretical Studies of Enzymic Reactions - Dielectric, Electrostatic and Steric Stabilization of the Carbonium Ion in the Reaction of Lysozyme. *Journal of Molecular Biology*, 103(2), 227-249.

Background

- ❖ *Enzymes* are large biological molecules responsible for thousands of metabolic processes that sustain life, including food digestion and DNA synthesis.
 - They are highly selective catalysts that greatly accelerate the *rate* and *specificity* of metabolic reactions.
 - Most enzymes are *proteins* and they adopt a specific three-dimensional structure.
 - Enzymes may employ organic or inorganic *cofactors* to assist in catalysis.
- ❖ *Cofactors* are non-protein compounds that are bound to a protein and are required for the protein's biological activity.
 - "Helper molecules" that assist in biochemical transformations.
 - Organic cofactors include biotin, flavin and heme. They can be further classified as:
 - *Coenzymes* → loosely bound cofactors that refer to the functional properties of a protein.
 - *Prosthetic groups* → tightly bound (covalent) cofactors that refer to a structural property.
 - Inorganic cofactors include:
 - *Metal ions* → metalloproteins
 - *Iron-sulfur clusters* → sulphide-linked di-, tri- and tetra-iron centres in variable oxidation states
- ❖ *Substrates* are molecules upon which an enzyme acts.
 - For a single substrate, an *enzyme-substrate complex* forms when the substrate bonds with the enzyme active site.
 - *Active sites* → small areas of an enzyme where substrates bind and undergo a chemical reaction.
 - *Binding* → usually enzymes have only one active site which fits with one specific type of substrate.
- ❖ Enzymes can be *denatured* at high temperatures or extreme pH values.
 - This causes the active site to change shape and the substrate molecules to no longer fit.
 - The *efficiency* of a reaction is believed to increase when there is a tighter fit between the active site and the substrate.
- ❖ *Solvation* is the interaction of molecules of a *solvent* with ions of a *solute* which leads to the stabilisation of the solute species in the solution.
 - Ions spread out and dissolve in a solvent and become surrounded by solvent molecules.
- ❖ *Dielectrics* are electrical insulators that can be polarized by an applied electric field.
 - Electrical charges do not flow through dielectric material when it is placed in an electric field.
 - Instead, there is a slight shift in average equilibrium positions causing dielectric polarization.

- ❖ *Solvation energy* resulting from polarization is quite considerable and must be accounted for when studying enzyme reactions. This allows:
 - Acidic groups to become ionized.
 - Charge distribution on substrate to be reasonable.
- ❖ *Bond cleavage* is the process of breaking down large molecules by splitting their internal bonds.
- ❖ *Charge distribution (density)* in quantum mechanics is summarised by the following equations.
 - $\rho_q(\mathbf{r}) = q|\psi(\mathbf{r})|^2 \rightarrow$ related to wavefunction
 - q = charge of the particle
 - $|\psi(\mathbf{r})|^2 = \psi^*(\mathbf{r})\psi(\mathbf{r})$ = probability density function \rightarrow probability per unit volume of a particle located at (\mathbf{r})
 - $Q = \int_R q|\psi(\mathbf{r})|^2 d^3\mathbf{r} \rightarrow$ when wavefunction is normalized
 - Q = the average charge in the region $\mathbf{r} \in R$
 - $d^3\mathbf{r}$ = the integration measure over 3-D space

Outline

- ❖ Aim: To develop a theoretical method for studying the reactions of enzymes, with particular emphasis on the factors that affect reaction pathways.
- ❖ Scope:
 - The system includes the entire enzyme-substrate (E-S) complex and its solvent (water).
 - The reaction examined is the cleavage of the glycosidic bond of *lysozyme*, focusing on the factors that affect the stability of the carbocation intermediate formed.
 - Classical approaches use *empirical energy functions* to study the conformation of E-S complexes \rightarrow based on bond stretching, angle-bending, twisting and non-bonded interactions.
 - Quantum mechanical (QM) approaches can study the mechanism and energetics of enzyme reactions, although it has several limitations:
 - Model is oversimplified, including only a small fraction of atoms involved in the reaction.
 - Reactions are treated within an isolated system (vacuum) and are not able to account for “dielectric effects” (polarizability of atoms) which affect the energy contributions from electrostatic interactions.
- ❖ Method:
 - The complete enzyme-substrate-solvent system examined includes all the energy factors that might contribute to the reaction mechanism, including:
 - *QM energy factors*:
 - Bond cleavage (rearrangement of bonds)
 - Charge redistribution (density) of the substrate
 - *Classical energy factors*:
 - Steric interactions (substrate strain on binding to the enzyme)
 - Electrostatic interactions (between substrate and enzyme)
 - *Dielectric effects*:
 - Polarization of the enzyme atoms
 - Dipole orientation of water molecules

❖ Model:

- The proposed *hybrid classical/QM* model evaluates:
 - *Energy and charge distribution* of the atoms that directly participate in the reaction (QM methods).
 - *Potential energy surface* of the rest of the system, which includes steric and electrostatic interactions (classical methods).
 - *Dielectric effects* from induced dipoles and polarization (QM/classical).

❖ Analysis:

➤ *Potential energy partition*

- The model partitions the potential energy surface into classical and quantum mechanical components, as well as a “coupling” term.
- $V = V_{\text{quantum}} + V_{\text{classical}} + V_{\text{quantum|classical}}$
- The combined coupling term accounts for:
 - Induced dipoles in the classical region
 - Electrostatic and van der Waals interactions between atoms in the quantum and classical regions.
- $$V_{\text{classical}} = \sum_i K_b (b_i - b_0)^2 + \sum_i K_\theta (\theta_i - \theta_0)^2 + \sum_i K_\phi \cos\{n(\phi_i - \phi_0)\} \\ + \sum_{i>j} \epsilon_{ij} \{(r_{ij}^0/r_{ij})^{12} - 2(r_{ij}^0/r_{ij})^6\} + \sum_i Q_i Q_j / r_{ij}$$
- V_{quantum} = obtained by an extended form of *QCFF/PI* (quantum-mechanical consistent force field method for pi-electron systems) that includes all valence electrons → referred to as *QCFF/ALL*
- $$V_{\text{quantum|classical}} = \sum_{i,j} Q_i Q_j / r_{ij} + \sum_{i,j} \epsilon_{ij} \{(r_{ij}^0/r_{ij})^{12} - 2(r_{ij}^0/r_{ij})^6\} \\ + V_{\text{ind}}^E + V_{\text{ind}}^W$$

➤ *Induced dipoles and the effective dielectric*

➤ *Substrate conformational changes*

❖ Results:

- *Steric effects in the ground state*
- *Equilibrium conformation of the carbonium ion*
- *Charge stabilization and dielectric effect*

❖ Conclusions:

- By incorporating the polarizability of atoms into the hybrid model through dielectric effects, a more accurate description of electrostatic interactions and its energy contributions is achieved.
- Electrostatic interaction is a major factor in the reaction rate leading to carbocation intermediate formation.
- Steric strain was found to be of minor importance.