



## 21L-S648- Assignment 4

AI:-

State of the vehicle can be represent with coordinates  $x, y$ .

will add  $f = g + h$  heuristic path cost

b)

We can use Manhattan distance as well as euclidian distance to calculate our heuristic cost.

c)

We will use manhattan distance

Open list: [ ]

Close list: [ ]

We will expand the node with lowest cost

$$f = g + h$$

Manhattan dist from G to all other nodes

$$\text{dist}(A, G) = 3 \quad \because |2-0| + |(0-1)| = 2 + 1 = 3. \quad f(2,0) = (0,1)$$

$$\text{dist}(B, G) = 2$$

$$\text{dist}(S, G) = 3$$

$$\text{dist}(C, G) = 4$$

$$\text{dist}(H, G) = 3$$

$$\text{dist}(D, G) = 2$$

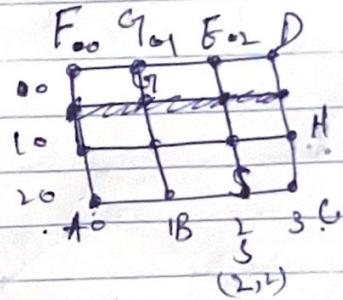
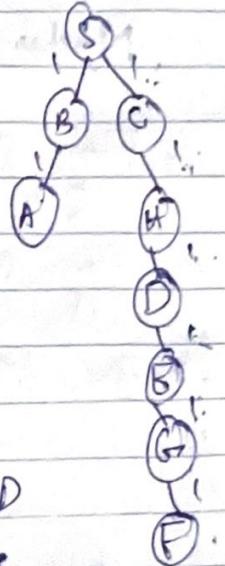
$$\text{dist}(E, G) = 1$$

$$\text{dist}(F, G) = 1$$

Expand {S, B, A, C, H, D, E, G}.

Total 7 moves  
Path cost: 5

Visited ((2,1), (2,0), (2,3), (1,3), (0,3), (0,2), (0,1))



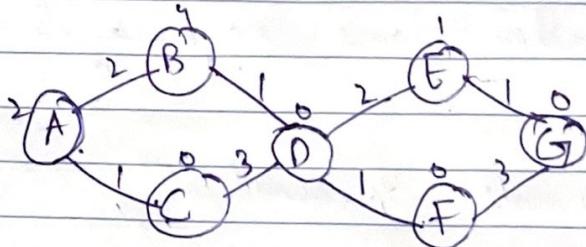


Q2

## Nodes Expanded by A\* BFS DFS:

- For DFS we will expand ~~13~~ nodes if we consider S to G too.
- For BFS since it is level by level it will traverse all nodes  $7 \times 7 = 49$ .
- For A\* it will expand nodes with lower cost.  
 = path nodes + additional explore nodes.  
 $\approx 13 - 20$ .

Q2.2:



Total Cost = 6.

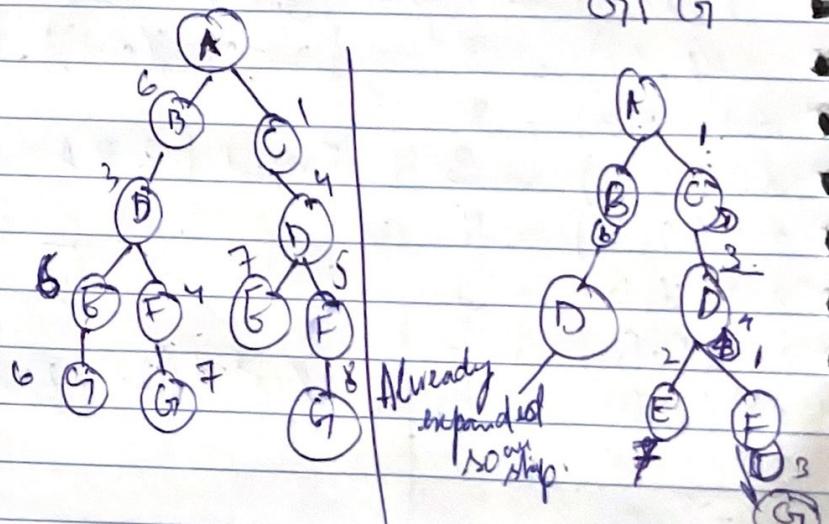
A	2
B	4
C	0
D	0
E	0
F	0
G	0

Path:

A → B → D → E → G.

State: —

AGDFBDFFEG.





Foundation for Advancement  
of Science & Technology

(c) E will be in the frontier queue.



(d) The path will be. A → G → D → F → B.  
but it is not optimal path.

(e) In this algo we will expand A → G → D → F → G  
G is in successor list of F and we will not move  
from F to other lower cost which is B.  
It will end there.  
It will not be optimal because cost is 8  
but it is complete!

Q3 :

### Knapsack

n = 100 array.

①

0 if not included

1 if included.

Total search space =  $2^{100}$ .

Reason: Each of the item can be either in the  
Knapsack or not.

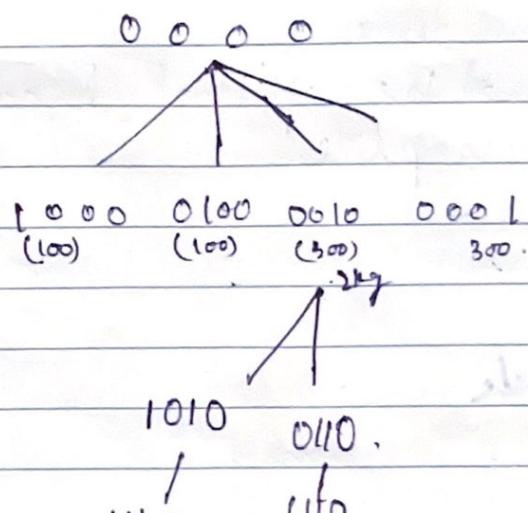
②

The state has 100 bits so it can have  
possible success at each level. because each  
bit can be use to generate a new successor.

(Q1):-

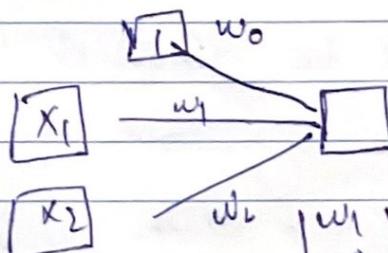
The suitable function will be to maximize the ~~weight~~ and minimize the weight where we will get <sup>cost</sup> as many value within the provided threshold.

(Q2):



Both will give  $4K \text{ Kg} \approx 500$ .

(Q4)



$$y = \begin{cases} 1 & \text{if } f(x) \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

$$1 \text{ if } x_2 \geq r_1$$

	$w_1$	$w_2$	$x_1$	$x_2$	$y$
-2	6		0		
-2	0		0	1	1
-2	0		-1	1	-1
-2	0		1	-1	-1



For all of these weights our output will be 2 pos & 2 neg according to the X value.

$x_1$	$x_2$	$y$
0	1	1
-1	1	1
1	0	-1
1	-1	-1

$\exists \text{ for } E=2:$

$$[1 0 1] [-1 -1 0] = -1 \neq 1$$

update weights.

$$\begin{array}{r} -1 -1 0 \\ 1 0 1 \\ \hline 0 -1 1 \end{array} \quad \text{new weight.}$$

$\exists \text{ for } X=2.$

$$[1 -1 1] [0 -1 1] = 2 f(2) = 1 \checkmark$$

$\exists \text{ for } X=3:$

$$\begin{aligned} & [1 1 0] [0 -1 1] \\ & (-1) = -1 \checkmark \\ & x=4 \quad [1 -1 1] [0 -1 1] = [-1 1] = -2 \end{aligned}$$

Initial weigh = [0 0 0].

For 1 epoch:-

$x_1:$

$$[1 0 1] \times [0 0 0]$$

$$= 0 f(0) = 1 \text{ (No weights)}$$

$\exists \text{ for } X=2:$

$$[1 -1 1] [0 0 0]$$

$$= 0 \Rightarrow f(0) = 1$$

$\exists \text{ for } X=3.$

$$[1 1 0] [0 0 0] = 1 \neq -1$$

update weights.

$$[0 0 0]$$

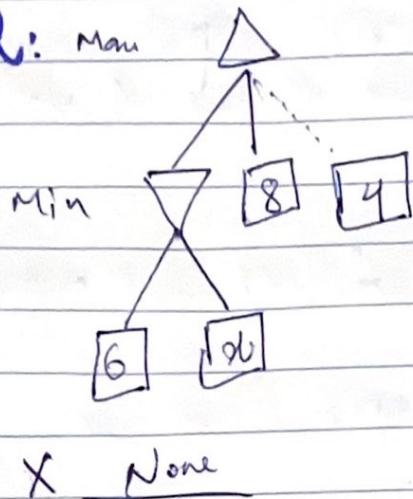
$$\begin{array}{r} 1 1 0 \\ -1 -1 0 \\ \hline \end{array}$$

$\exists \text{ for } X=4$

$$[1 1 -1] [-1 -1 0]$$

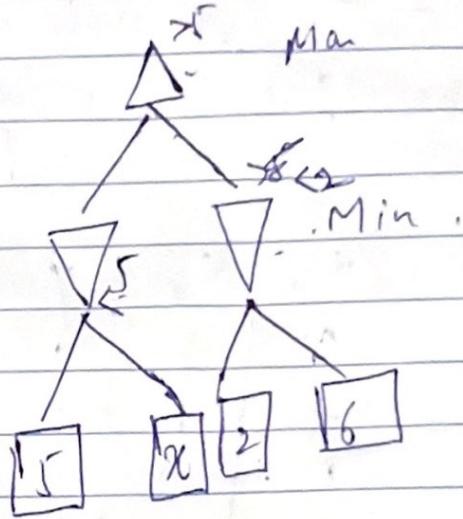
$$= [-1 -1] = -2 = -1.$$

Q: Max

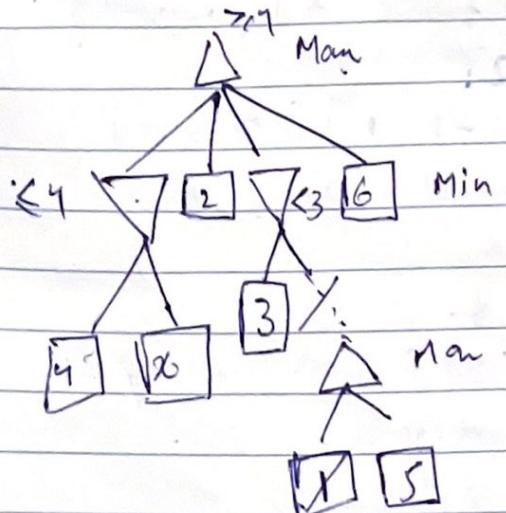


X None

Max



Min.

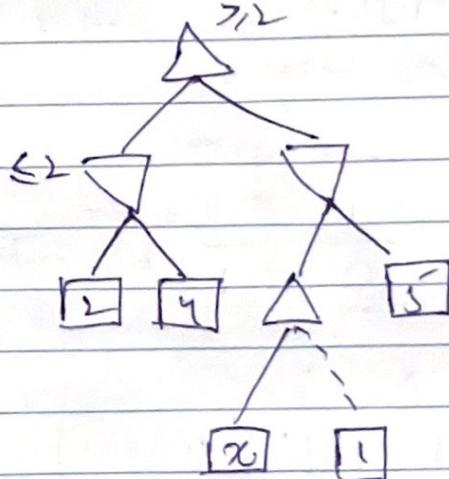


X = 5, 6, 7 ( $x > 7$ )

If will prune.

(All) if ignore x6.

X = 4, 5, 6 ( $val > 2$ )  
(All) if ignore x.



X = None



	$C_1 = (2, 10)$	$C_2 = (5, 8)$	$C_3 = (1, 2)$	Clusters.
A1 (2, 10)	0	-	-	$C_1$
A2 (5, 8)	5	4.24	3.16	$C_3$ .
A3 (8, 4)	8.4	.5	7.28	$C_2$
A4 (5, 8)	-	0	-	$C_2$
A6 (6, 4)	7.2	4.12	5.38	$C_2$
A7 (1, 2)	8.06	7.21	0	$C_3$ .
A8 (4, 9)	2.23	1.41	7.81	$C_2$
A5 (7, 5)	7.07	3.6	6.7	$C_2$

Pin in 1st C  
(2, 10)

Pin in 2nd C  
(8, 4), (5, 8), (6, 4)  
(4, 9), (7, 5)

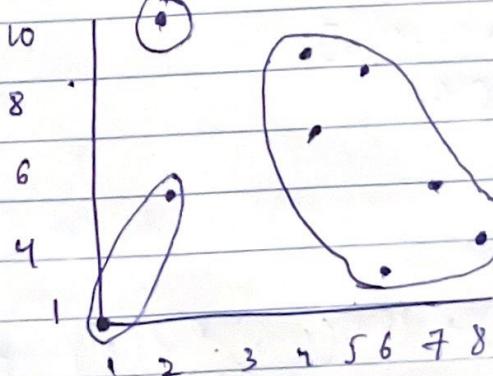
Pin in 3rd C  
(2, 5)  
(1, 2)

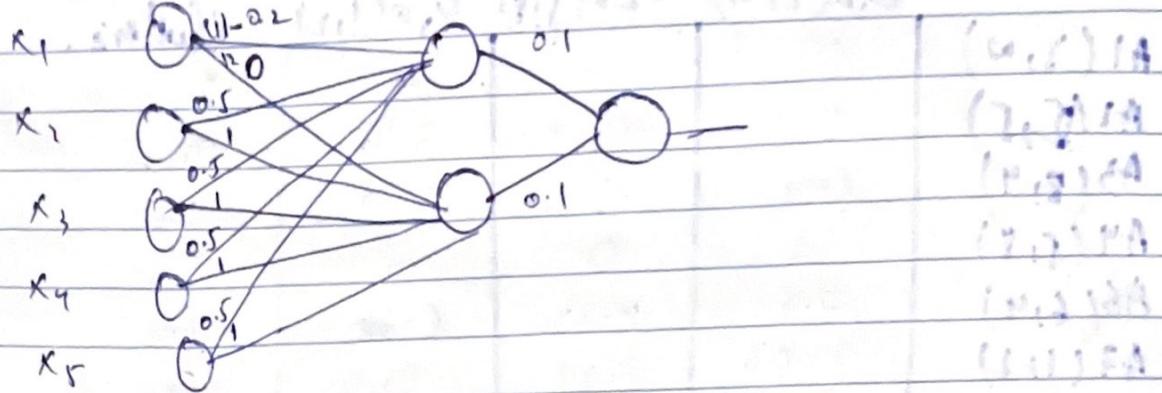
③ :-

$C_1 (2, 10)$

$C_2 \frac{8+5+6+4+7}{5},$   
 $\frac{4+8+9+5}{5}$

6.9, 7.6.





(a)

To train the data we will label it as.

# of Projects	Avg Success Ratio	Avg Comp Time	Skill	Exp (Grade)
---------------	-------------------	---------------	-------	-------------

(b).

For Empl:

$$h_1 = [5 \ -0.4 \ 0.8 \ 0.1 \ 0.3] [-0.2 \ 0.5 \ 0.5 \ 0.5 \ 0.5] + 0.1 = (-0.6)$$

$$= [-1 \ -0.2 \ 0.4 \ 0.05 \ 0.15] = (-0.6)$$

$$= -0.7$$

$$h_2 = [5 \ -0.2 \ 0.8 \ -0.1 \ 0.3] [0 \ 1 \ 1 \ 1]$$

$$= [0 \ -0.4 + 0.8 + 0.1 + 0.3].$$

$$= \cancel{+0.6} = 0.6.$$

Output layer.

$$\hat{y} = (0.1)(-0.7) + (0.1)(0.6) + 2(0) = -0.01$$

$$= \cancel{+0.6} = 0.49.$$



For Emp 2:

$u_1$

$$x [1 \ 0.4 \ 0.1 \ 1 \ -0.5] [-0.2 \ 0.5 \ 0.5 \ 0.5 \ 0.5]$$

$$= -0.075 = -0.075.$$

$$u_2 = [1 \ 0.4 \ 0.1 \ 1 \ -0.5] [0 \ 1 \ 1 \ 1 \ 1]$$

$$= [1] = 1$$

$$y = (2)(0) + (-0.075)(0.1) + (1)(0.1)$$

$$= 0.09 \Rightarrow \frac{1}{1+e^{-0.09}}$$

$$\underline{= 0.511}$$

(Part C)

$$x [4 \ -0.5 \ 0.3 \ -0.2 \ 0.5]$$

$$u_1 = x u_1 = -0.75$$

$$u_2 = x u_2 = 0.1 = 0.1$$

$$y = (2)(0) + (-0.75)(0.1) + (0.1)(0.1)$$

$$= -0.06 = 0.517.$$

$$\text{error at } y = 1 - 0.517 = 0.49.$$

$$= \cancel{0.517} (0.517)(1-0.517)(0.49)$$

$$= 0.122.$$



error at  $w_1$ :-

$$(-0.75)(1+0.75)((0.1)(0.123)) \\ = -0.016.$$

error at  $w_2$ :-

$$\begin{aligned} & \cancel{(0.514)} \cancel{(+0.514)} \cancel{((0.1)(0.123))} \\ & = \cancel{-0.0003} = (0.1)(1-0.1)(0.1)(0.123) \\ & = 0.001 \end{aligned}$$

Computing new weights.

at  $\gamma$ :

$$LR=1$$

$$\begin{aligned} Y_1 &= (1)(-0.75)(0.123) \\ &= -0.09 + 0.1 \\ &= 0.01 \end{aligned}$$

$$Y_2 = (1)(0.123)(0.1) = 0.0123 + 0.1 \\ = 0.11$$

New weights at  $\gamma_1$

$$X_{11} = (1)(\cancel{0.2})(1)(4)(-0.016) = \boxed{-0.26}$$

$$X_{21} = (1)(-0.5)(-0.016) + 0.5 = 0.508$$

$$\Rightarrow (1)(0.3)(-0.016) + 0.5 = 0.495$$

$$(1)(-0.2)(-0.016) + 0.5 = 0.503$$

$$(1)(0.5)(-0.016) + 0.5 = 0.492$$

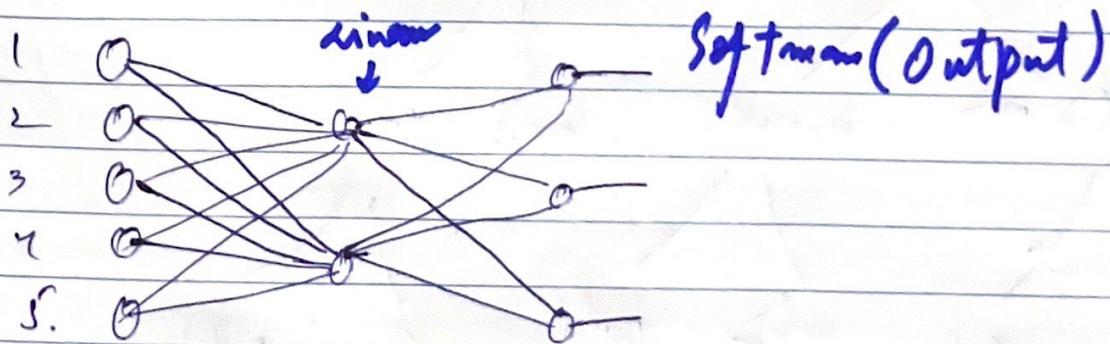
For  $h_2$  :-

$$\begin{array}{ll}
 X_{12} = (1)(0.001)(9) & +0 = 0.004 \\
 X_{22} = (1)(0.001)(-0.5) & +1 = 0.99 \\
 X_{32} = (1)(0.001)(0.3) & +1 = 1.0003 \\
 X_{42} = (1)(0.001)(-0.2) & +1 = 0.99 \\
 X_{52} = (1)(0.001)(0.5) & +1 = 1.0005
 \end{array}$$

(a):

We will use 3 neurons instead of 1 which will represent Good AVG Bad.

→ Also we will apply Softmax instead of Sigmoid.  
To convert data into probabilities.



(Q#6)

$$\textcircled{a} \quad 1^{\text{st}} \text{ level} = 5 = 5.$$

$$2^{\text{nd}} \text{ level} = 5 \times 5 = 25.$$

$$3^{\text{rd}} \text{ level} = 5 \times 5 \times 5 = 125.$$

Total is  $7 \times 6 = 42$  level.

$$\text{use geometric series formula} = \frac{b^{d+1}-1}{b-1} = \frac{5^{7+1}-1}{5-1}$$

$$= 9.86 \times 10^{23}$$

