
Gradient Rewiring for Editable Graph Neural Network Training

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Abstract

Deep neural networks are ubiquitously adopted in many applications, such as computer vision, natural language processing, and graph analytics. However, well-trained neural networks can make prediction errors after deployment as the world changes. *Model editing* involves updating the base model to correct prediction errors with less accessible training data and computational resources. Despite recent advances in model editors in computer vision and natural language processing, editable training in graph neural networks (GNNs) is rarely explored. The challenge with editable GNNs training lies in the inherent information aggregation across neighbors, which can lead model editors to affect the predictions of other nodes unintentionally. In this paper, we first observe the gradient of cross-entropy loss for the target node and training nodes with significant inconsistency, which indicates that directly fine-tuning the base model using the loss on the target node deteriorates the performance on training nodes. Motivated by the gradient inconsistency observation, we propose a simple yet effective Gradient Rewiring method for Editable graph neural network training, named GRE. Specifically, we first store the anchor gradient of the loss on training nodes to preserve the locality. Subsequently, we rewire the gradient of the loss on the target node to preserve performance on the training node using anchor gradient. Experiments demonstrate the effectiveness of GRE on various model architectures and graph datasets in terms of multiple editing situations.

1 Introduction

Graph Neural Networks (GNNs) have demonstrated exemplary performance for graph learning tasks, such as recommendation, link prediction, molecule property analysis [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]. With message passing, GNNs learn node representations by recursively aggregating the neighboring nodes' representations. Once trained, GNN models are deployed to handle various high-stake tasks, such as credit risk assessment in financial networks [11] and fake news detection in social networks [12]. However, the impact of erroneous decisions in such influential applications can be substantial. For instance, misplaced credit trust in undetected fake news can lead to severe financial loss.

An ideal approach to tackle such errors should possess the following properties: 1) the ability to rectify severe errors in the model's predictions, 2) the capacity to generalize these corrections to other similar instances of misclassified samples, and 3) the ability to preserve the model's prediction accuracy for all other unrelated inputs. To achieve these goals, various model editing frameworks have been developed to rectify errors by dynamically adjusting the model's behavior when errors are detected [13, 14]. The core principle is to implement minimal changes to the model to correct the error while keeping the rest of the model's behavior intact. However, model editing is not a simple plug-and-play solution. These frameworks often require an additional training phase to prepare for

37 editing before they can be used effectively for editing [13, 14, 15, 16]. Although model editing
 38 techniques have [show significant](#) utility in computer vision and language models, there is only one
 39 work [17], to the best of our knowledge, [focused on](#) rectifying critical errors in graph data. The unique
 40 challenge arises from the inherent message-passing mechanism in GNNs when edits [involve](#) densely
 41 interconnected nodes. Specifically, editing the behavior of a single node can [unintentionally](#) induce
 42 a ripple effect, causing changes [that](#) propagate [throughout](#) the entire graph. [17] theoretically and
 43 empirically demonstrate [the complexity of editing GNNs through the lens of the loss landscape of the](#)
 44 [Kullback-Liebr divergence between the pre-trained node features and edited final node embeddings](#).
 45 Moreover, a simple yet effective model structure, named EGNN, is proposed with stitched peer
 46 multi-layer perception (MLP), [where only the stitched MLP is trained during model editing](#).

47 In this work, we investigate the model editing problem for GNNs from a *brand-new gradient*
 48 *perspective*, [which is compatible with existing work \[17\]](#). Specifically, we first found a considerable
 49 inconsistency between the gradients of the cross-entropy loss for the target node and the training
 50 nodes for GNNs. Such inconsistency implies that direct fine-tuning of the base model using the loss
 51 of the target node can lead to a deterioration in the performance [on](#) the training nodes. Motivated
 52 by the above observation, we propose a simple yet effective Gradient Rewiring method for Editable
 53 graph neural network training, named **GRE**. Specifically, we first calculate and store the anchor
 54 gradient of the loss [on](#) the training nodes. This anchor gradient represents the original learning
 55 direction that we wish to preserve. Then, during the editing process, we adjust the gradient of the loss
 56 [on](#) the target node based on the stored anchor gradient. This adjustment, or “rewiring”, ensures that
 57 the changes made to the target node do not adversely affect the performance [on](#) the training nodes.
 58 Experiments demonstrate the effectiveness of our proposed method for various model structures and
 59 graph datasets. Moreover, the proposed method is compatible with the existing EGNN baseline and
 60 further improves the performance.

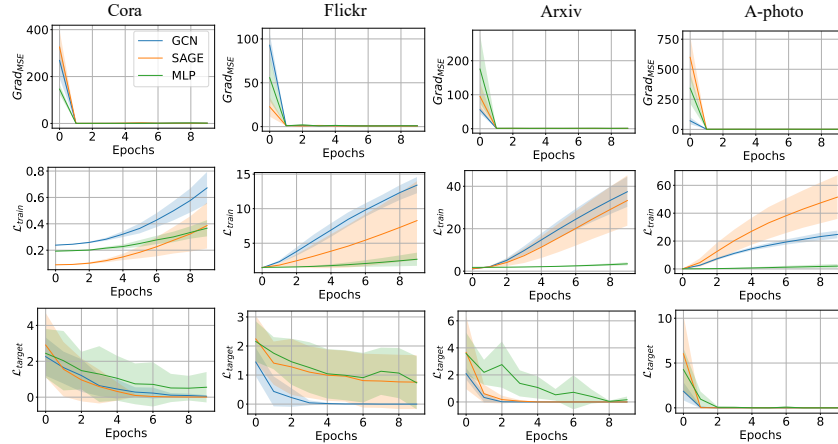


Figure 1: (a) Top: RMSE distance between the gradients of cross-entropy loss over training datasets and over the targeted sample for different architectures. (b) Middle: Cross-entropy loss over training datasets when the model is updated using target loss. (c) Bottom: Cross-entropy loss over the targeted sample when the model is updated using target loss.

61 2 Preliminary and Related Work

62 We first introduce the notations used throughout this paper. A graph is given by $\mathcal{G} = (\mathcal{V}, \mathcal{E})$, where
 63 $\mathcal{V} = (v_1, \dots, v_N)$ is the set of nodes indexed from 1 to n , and $\mathcal{E} = (e_1, \dots, e_m) \subseteq \mathcal{V} \times \mathcal{V}$ is the set
 64 of edges. $n = |\mathcal{V}|$ and $m = |\mathcal{E}|$ are the numbers of nodes and edges, respectively. Let $\mathbf{X} \in \mathbb{R}^{n \times d}$ be
 65 the node feature matrix, where d is the dimension of node features. $\mathbf{A} \in \mathbb{R}^{n \times n}$ is the graph adjacency
 66 matrix, where $A_{i,j} = 1$ if $(v_i, v_j) \in \mathcal{E}$ else $A_{i,j} = 0$. $\tilde{\mathbf{A}} = \tilde{\mathbf{D}}^{-\frac{1}{2}}(\mathbf{A} + \mathbf{I})\tilde{\mathbf{D}}^{-\frac{1}{2}}$ is the normalized
 67 adjacency matrix, where $\tilde{\mathbf{D}}$ is the degree matrix of $\mathbf{A} + \mathbf{I}$. The node label is defined as y_i for node
 68 v_i . We consider node classification tasks with C classes in this paper.

69 2.1 Graph Neural Networks

70 Most graph neural networks follow a neighborhood aggregation procedure to learn node representation
 71 via propagating representations of neighbors and then follow up with feature transformation [18].
 72 The l -th layer of graph neural networks is given by:

$$\begin{aligned} \mathbf{a}_i^{(l)} &= \text{PROPAGATION}^{(l)}\left(\{\mathbf{x}_i^{(l-1)}, \mathbf{x}_j^{(l-1)} | j \in \mathcal{N}_i\}\right), \\ \mathbf{x}_i^{(l)} &= \text{TRANSFORMATION}^{(l)}\left(\mathbf{a}_i^{(l)}\right), \end{aligned}$$

73 where $\mathbf{x}_i^{(l)}$ is the representation of node v_i at l -th layer and $\mathbf{x}_i^{(0)}$ is initialized as node feature \mathbf{x}_i ,
 74 i.e., the i -th row at node feature matrix \mathbf{X} . Many GNNs, such as GCN [19], GraphSAGE [20], and
 75 GAT [21], can be defined under this computation paradigm via adopting the different propagation
 76 and transformation operations. For example, the l -th layer in GCN can be defined as:

$$\mathbf{X}^{(l)} = \sigma(\tilde{\mathbf{A}}\mathbf{X}^{(l-1)}\mathbf{W}^{(l)}), \quad (1)$$

77 where $\mathbf{X}^{(l)} \in \mathbb{R}^{n \times d}$ and $\mathbf{X}^{(l-1)} \in \mathbb{R}^{n \times d}$ are the node representation matrix containing the \mathbf{h}_v for
 78 each node v at the layer l and layer $l-1$, respectively. $\mathbf{W}^{(l)} \in \mathbb{R}^{d \times d}$ is a layer-specific trainable
 79 weight matrix, and $\sigma(\cdot)$ is a non-linear activation function (e.g., ReLU).

80 2.2 Model Editing

81 Model editing aims to modify a base model’s responses for a misclassified sample x_{tg} and its analogs.
 82 This is typically achieved by fine-tuning the model using only a single pair of input x_{tg} and the
 83 desired output y_{tg} , while preserving the model’s responses to unrelated inputs [13, 14, 15, 17].
 84 Our contribution **lies in** the novel application of model editing to graph data, a **domain** where
 85 misclassifications on a **few** pivotal nodes can trigger substantial financial losses, fairness issues, or
 86 even the propagation of adversarial attacks. Consider the scenario of node classification where a
 87 well-trained GNN **incorrectly** predicts a particular node. Model editing **can be employed to rectify**
 88 **this erroneous** prediction. **By leveraging** the node’s characteristics and the desired label, **the model**
 89 **can be updated** to correct such behavior. The ideal outcome of model editing is twofold: first, the
 90 updated model should correctly predict the specific node and its similar **instances**; second, the model
 91 should maintain its original behavior **on** unrelated inputs. **It is important to note that** some model
 92 editors require a **preparatory** training phase **before they can be applied effectively** [13, 16, 15, 14].
 93 This crucial **step** ensures that the model editing process is both precise and effective in its application.

94 3 Methodology

95 In this section, we first provide the preliminary experimental results as the motivation to rewire
 96 gradients **for** model editing. Subsequently, we propose our gradient rewiring method for editable
 97 graph neural networks training (GRE) and **an** advanced version (GRE+) to improve the effectiveness
 98 of model editing, respectively.

99 3.1 Motivation

100 In the preliminary experiments, **we first pre-train GCN, GraphSAGE, and MLP on the training**
 101 **dataset \mathcal{V}_{train}** (e.g., Cora, Flickr, ogbn-arxiv, and Amazon Photo datasets) using cross-entropy loss.
 102 Subsequently, we find the misclassified samples in the validation dataset and randomly select one
 103 sample as the target sample $(\mathbf{x}_{tg}, y_{tg})$. During the model editing, **we update the pre-trained model**
 104 **using cross-entropy loss over target sample using gradient descent**, i.e., *the models are trained*
 105 *inductively*. Following previous work [13, 15, 17], we perform 50 independent edits and report the
 106 averaged metrics.

107 **It is well-known that model editing incurs training performance degradation** [14, 13, 15] ¹ for
 108 many model architectures. To deeply delve into the underlying reason, we investigate performance
 109 degradation from **a** model gradient perspective. We further define **the** training loss as $\mathcal{L}_{train} =$

¹The reason for focusing on the training set is that during model editing, we can only use the training set and not the test set.

110 $\frac{1}{|\mathcal{V}_{train}|} \sum_{i \in \mathcal{V}_{train}} CE(f_{\theta}(\mathbf{x}_i), y_i)$, where $f_{\theta}(\cdot) \in \mathbb{R}^C$ is a prediction model parameterized with
 111 $\theta \in \mathbb{R}^L$, C and L are the number of classes and model parameters, $CE(\cdot, \cdot)$ is the cross-entropy loss,
 112 the target loss is given by $\mathcal{L}_{tg} = CE(f_{\theta}(\mathbf{x}_{tg}), y_{tg})$. For example, model $f_{\theta}(\cdot)$ can be instantiated by
 113 GNNs with the number of layers defined in Eq. (1) or a simple MLP. For model editing, the gradient
 114 for training and target loss is given by $g_{train} = \frac{\partial \mathcal{L}_{train}}{\partial \theta} \in \mathbb{R}^L$ and $g_{tg} = \frac{\partial \mathcal{L}_{tg}}{\partial \theta} \in \mathbb{R}^L$, respectively.
 115 To investigate why the model editing leads to training performance degradation, we use gradient
 116 RMSE (Root-Mean-Squared-Error), i.e., $\text{Grad}_{RMSE} = \sqrt{\|g_{train} - g_{tg}\|_2^2}$, to measure the model
 117 editing discrepancy for training datasets and target sample.

118 The model editing curves for gradient RMSE², training loss, and target loss across various model
 119 architectures (GCN, GraphSAGE, and MLP) are shown in Figure 1. Although the gradient RMSE
 120 for training datasets and target sample is close to 0, the model parameters demonstrate significant
 121 inconsistent behavior in terms of training loss due to large gradient discrepancy in the initial editing
 122 stage. We observe that: 1) Even though the target loss decreases during model editing, the training
 123 loss increases significantly. 2) The increasing rates of training loss for GCN and GraphSAGE are
 124 significantly higher than that of MLP. The above observations imply that editing training for graph
 125 neural networks is more challenging due to higher gradient discrepancy between the training dataset
 126 and the target sample.

127 3.2 Gradient Rewiring Approach

128 Preliminary results show a high discrepancy in training loss and target loss for GNNs, which implies
 129 that the vanilla model editing hampers the performance on the overall training dataset and thus results
 130 in a high accuracy drop for node classification tasks. Therefore, we aim to tackle the training dataset
 131 performance degradation from the gradient rewiring approach.

132 **GRE** We propose a simple yet effective gradient rewiring approach for editable graph neural
 133 network training, named GRE. We first formulate a constrained optimization problem to regulate
 134 model editing and then solve the constrained optimization problem via gradient rewiring.

135 Note that the model editing aims to correct the prediction on the target sample while preserving the
 136 prediction results on training nodes. We constrain the model prediction differences after the model
 137 editing within a pre-defined range. Meanwhile, the training loss is regulated as not being larger than
 138 the loss before model editing. Define θ_0 and θ' as the model parameters before and after model
 139 editing. Then we have the following constrained optimization problem:

$$\min_{\theta} \quad \mathcal{L}_{tg}(f_{\theta}(\mathbf{x}_{tg}), y_{tg}) \quad (2)$$

$$\text{s.t.} \quad \mathcal{L}_{train}(f_{\theta'}, \mathcal{V}_{train}) \leq \mathcal{L}_{train}(f_{\theta_0}, \mathcal{V}_{train}) \quad (3)$$

$$\left\| \frac{1}{|\mathcal{V}_{train}|} \sum_{i \in \mathcal{V}_{train}} f_{\theta'}(\mathbf{x}_i) - f_{\theta_0}(\mathbf{x}_i) \right\|^2 \leq \delta', \quad (4)$$

140 where the hyperparameter δ' represents the maximum average prediction difference on training
 141 nodes. Notice that the model parameters update adopts gradient descent using target loss without any
 142 constraints, i.e., $\theta' = \theta_0 - \alpha g_{tg}$, where α is step size in model editing. The key idea of our proposed
 143 solution is to rewire gradient g_{tg} as g , which is obtained by satisfying the involved constraints. Note
 144 that the model editing usually corrects the model prediction on the target sample within a few steps,
 145 i.e. there are no significant model parameter differences, thus we adopt Taylor expansion to tackle
 146 such constrained optimization problem. For target loss \mathcal{L}_{tg} , we can approximate it as:

$$\begin{aligned} \mathcal{L}_{tg}(f_{\theta'}(\mathbf{x}_{tg}), y_{tg}) &\approx \mathcal{L}_{tg}(f_{\theta_0}(\mathbf{x}_{tg}), y_{tg}) + g_{tg}^{\top}(\theta' - \theta_0) \\ &= \mathcal{L}_{tg}(f_{\theta_0}(\mathbf{x}_{tg}), y_{tg}) - \alpha g_{tg}^{\top} g. \end{aligned} \quad (5)$$

147 To optimize the objective function Eq. (2), it is easy to conclude that the gradient cosine similarity
 148 $g_{tg}^{\top} g$ should be maximized. Given the gradient before/after model editing is fixed, the maximization
 149 of gradient cosine similarity $g_{tg}^{\top} g$ is equivalent to the minimization of $\|g_{tg} - g\|^2$. To satisfy Eq. (3),

²There is no variance for gradient estimation since gradient calculation is based on backpropagation. The large variance in model performance and gradient discrepancy derives from the randomly selected target node.

we also adopt Taylor expansion on \mathcal{L}_{train} and it is easy to obtain that the gradient cosine similarity should be positive, i.e., $g_{tg}^\top g \geq 0$. As for the constraint in Eq. (4), similarly, we also have:

$$\left\| \frac{1}{|\mathcal{V}_{train}|} \sum_{i \in \mathcal{V}_{train}} f_{\theta'}(\mathbf{x}_i) - f_{\theta_0}(\mathbf{x}_i) \right\|^2 \approx \|\hat{g}_{train}^\top (-\alpha g)\|^2 \leq \delta', \quad (6)$$

where gradient for a model prediction is defined as $\hat{g}_{train} = \frac{\partial \frac{1}{|\mathcal{V}_{train}|} \sum_{i \in \mathcal{V}_{train}} f_{\theta_0}(\mathbf{x}_i)}{\partial \theta} \Big|_{\theta=\theta_0} \in \mathbb{R}^{L \times C}$. Therefore, the model prediction difference constraint can be transformed into $\|\hat{g}_{train}^\top g\|^2 \leq \delta$, where $\|\cdot\|_{spect}$ represents matrix spectrum norm and $\|\hat{g}_{train}\|_{spect}$ is fixed in model editing, and $\delta = \frac{\delta'}{\alpha^2}$. In a nutshell, our goal is to correct the target sample (i.e., minimize $\|g_{tg} - g\|^2$) and minimize gradient discrepancy for model prediction among training dataset and target sample (i.e., $\|g\|^2$), while guaranteeing non-increased training loss (i.e., $g_{train}^\top g \geq 0$). The original constraint optimization problem is simplified as gradient rewiring, i.e.,

$$\min_g \frac{1}{2} \|g - g_{tg}\|^2 + \frac{\lambda}{2} \|g\|^2 = \min_g \frac{1+\lambda}{2} g^\top g - g_{tg}^\top g + \frac{1}{2} g_{tg}^\top g_{tg} \quad \text{s.t.} \quad g_{train}^\top g \geq 0, \quad (7)$$

where $\lambda \geq 0$ is the hyperparameter to control the balance between target sample correction and gradient discrepancy for model prediction. It is easy to obtain that Eq.(7) is a quadratic program (QP) in L -variables (the number of model parameters and usually high in neural networks). Fortunately, we can effectively solve this problem in the dual space via transforming as a smaller QP problem with only one variable v [22], where the relation between primal and dual variable is $g_{train}v - (1+\lambda)g = -g_{tg}$. Then we have the following problem:

$$\min_v \frac{(1+\lambda)^{-1}}{2} (g_{train}v + g_{tg})^\top (g_{train}v + g_{tg}) \quad \text{s.t.} \quad v \geq 0. \quad (8)$$

It is easy to obtain the optimal dual variable $v^* = -\min\{\frac{g_{train}^\top g_{tg}}{g_{train}^\top g_{train}}, 0\}$ and the optimal rewired gradient $g^* = (1+\lambda)^{-1}(g_{tg} - v^* g_{train})$. In other words, the gradient rewiring procedure is quite simple: for the gradient of the target loss g_{tg} , reduce its projection component on g_{train} and then scale it by $(1+\lambda)^{-1}$.

Additionally, we highlight that the gradient for training loss g_{train} is required to be stored before model editing. In this way, the gradient rewiring can be conducted to remove the harmful gradient component on target loss that increases training loss. Since shallow GNNs model performs well in practice [23], the model size of GNNs are small and the memory cost $O(L)$ for storing anchor gradient is negligible.

Table 1: The results on four small-scale datasets after applying one single edit. The reported number is averaged over 50 independent edits. **SR** is the edit success rate, **Acc** is the test accuracy after editing, and **DD** are the test drawdown, respectively. “OOM” is the out-of-memory error. The best/second-best results are highlighted in **boldface**/underlined, respectively.

Editor	Cora			A-computers			A-photo			Coauthor-CS			
	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	
MLP	GD	68.15 \pm 0.33	3.85 \pm 0.33	0.98	73.22 \pm 0.48	6.78 \pm 0.48	1.00	83.19 \pm 0.91	6.81 \pm 0.91	1.00	<u>93.59</u> \pm 0.05	<u>0.41</u> \pm 0.05	1.00
	ENN	37.16 \pm 3.80	52.24 \pm 4.76	1.00	15.51 \pm 10.99	72.36 \pm 10.87	1.00	16.71 \pm 14.81	77.07 \pm 15.20	1.00	4.94 \pm 3.78	89.43 \pm 3.34	1.00
	GRE	<u>69.41</u> \pm 0.44	<u>2.59</u> \pm 0.44	0.96	61.21 \pm 1.26	18.79 \pm 1.26	1.00	73.56 \pm 1.41	16.44 \pm 1.41	1.00	93.27 \pm 0.09	0.73 \pm 0.09	1.00
	GRE+	71.19 \pm 0.28	0.61 \pm 0.28	0.96	61.27 \pm 1.15	18.73 \pm 1.15	1.00	78.26 \pm 1.15	11.74 \pm 1.15	1.00	93.73 \pm 0.07	0.27 \pm 0.07	1.00
GCN	GD	84.37 \pm 5.84	5.03 \pm 6.40	1.00	44.78 \pm 22.41	<u>43.09</u> \pm 22.32	1.00	28.70 \pm 21.26	65.08 \pm 20.13	1.00	<u>91.07</u> \pm 3.23	<u>3.30</u> \pm 2.22	1.00
	ENN	37.16 \pm 3.80	52.24 \pm 4.76	1.00	15.51 \pm 10.99	72.36 \pm 10.87	1.00	16.71 \pm 14.81	77.07 \pm 15.20	1.00	4.94 \pm 3.78	89.43 \pm 3.34	1.00
	GRE	<u>84.98</u> \pm 0.47	<u>4.02</u> \pm 0.47	0.96	<u>46.28</u> \pm 3.47	51.72 \pm 3.47	0.98	<u>35.88</u> \pm 2.26	<u>58.12</u> \pm 2.26	0.99	89.46 \pm 0.29	4.54 \pm 0.29	1.00
	GRE+	88.84 \pm 0.35	0.56 \pm 0.35	0.98	47.75 \pm 0.45	40.25 \pm 0.45	1.00	50.13 \pm 1.36	48.87 \pm 1.36	1.00	91.99 \pm 0.30	2.01 \pm 0.30	1.00
Graph-SAGE	GD	82.06 \pm 4.33	4.54 \pm 5.32	1.00	<u>21.68</u> \pm 20.98	<u>61.15</u> \pm 20.33	1.00	38.98 \pm 30.24	55.32 \pm 29.35	1.00	90.15 \pm 5.58	5.01 \pm 5.32	1.00
	ENN	33.16 \pm 1.45	53.44 \pm 2.23	1.00	16.89 \pm 16.98	65.94 \pm 16.75	1.00	15.06 \pm 11.92	79.24 \pm 11.25	1.00	13.71 \pm 2.73	81.45 \pm 2.11	1.00
	GRE	<u>83.64</u> \pm 0.20	<u>3.36</u> \pm 0.20	1.00	20.11 \pm 2.30	62.89 \pm 2.30	0.96	<u>41.96</u> \pm 1.57	<u>52.04</u> \pm 1.57	0.98	<u>91.07</u> \pm 0.44	<u>3.93</u> \pm 0.44	1.00
	GRE+	86.59 \pm 0.07	0.41 \pm 0.07	1.00	22.23 \pm 1.60	60.77 \pm 1.60	0.97	44.05 \pm 0.83	50.32 \pm 0.83	1.00	91.75 \pm 0.43	3.25 \pm 0.43	1.00
EGNN-GCN	GD	87.58 \pm 0.31	<u>1.42</u> \pm 0.31	1.00	87.27 \pm 0.14	<u>0.73</u> \pm 0.14	0.78	<u>93.24</u> \pm 0.59	<u>0.76</u> \pm 0.59	0.77	<u>93.99</u> \pm 0.02	<u>0.01</u> \pm 0.02	0.91
	GRE	87.47 \pm 0.41	1.53 \pm 0.41	1.00	83.38 \pm 1.20	4.62 \pm 1.20	0.87	88.01 \pm 1.20	5.99 \pm 1.20	0.86	93.92 \pm 0.07	0.08 \pm 0.07	0.94
	GRE+	88.99 \pm 0.21	0.05 \pm 0.21	1.00	88.10 \pm 1.21	0.51 \pm 1.21	1.00	94.22 \pm 0.98	-0.21 \pm 0.98	1.00	94.32 \pm 0.06	-0.32 \pm 0.06	1.00
	GD	<u>85.05</u> \pm 0.11	<u>0.95</u> \pm 0.11	1.00	<u>85.93</u> \pm 0.08	<u>0.07</u> \pm 0.08	0.90	<u>93.87</u> \pm 0.20	<u>0.13</u> \pm 0.20	0.81	<u>95.04</u> \pm 0.01	<u>0.00</u> \pm 0.01	0.99
EGNN-SAGE	GRE	84.79 \pm 0.19	1.21 \pm 0.19	1.00	81.94 \pm 1.71	4.06 \pm 1.71	0.96	88.55 \pm 1.19	5.45 \pm 1.19	0.95	94.85 \pm 0.05	0.15 \pm 0.05	1.00
	GRE+	86.24 \pm 1.43	-0.24 \pm 1.43	1.00	85.97 \pm 0.83	-0.16 \pm 0.83	1.00	94.07 \pm 0.03	-0.07 \pm 0.03	0.98	95.07 \pm 0.03	-0.07 \pm 0.03	1.00

GRE+ In GRE, the training loss after model editing is required not to be larger than that before model editing. However, it is still possible that the training loss on specific sub-training sets performs worse after model editing. At the same time, the training loss for the whole training dataset, after model editing, is on par with or even lower than that of before editing. To tackle this issue, we proposed an advanced gradient rewiring approach, named GRE+, via applying loss

Table 2: The results on four large-scale datasets after applying one single edit. “OOM” is the out-of-memory error. The best/second-best results are highlighted in **boldface/underlined**, respectively. The results for more backbones (e.g., MLP, EGNN-GCN, EGNN-SAGE) are in Appendix D.1.

	Editor	Flickr			Reddit			ogbn-arxiv			ogbn-products		
		Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow
GCN	GD	13.95 \pm 11.00	37.25 \pm 10.20	1.00	75.20 \pm 12.30	20.32 \pm 11.30	1.00	23.71 \pm 16.90	46.50 \pm 14.90	1.00	53.29 \pm 0.94	20.71 \pm 0.94	1.00
	ENN	25.82 \pm 14.90	25.38 \pm 16.90	1.00	11.16 \pm 5.10	84.36 \pm 3.10	1.00	16.59 \pm 7.70	53.62 \pm 6.70	1.00	OOM	OOM	OOM
	GRE	17.36 \pm 1.50	33.64 \pm 1.50	0.98	24.74 \pm 1.92	45.26 \pm 1.92	1.00	77.84 \pm 1.16	18.16 \pm 1.16	1.00	53.99 \pm 0.60	20.01 \pm 0.60	1.00
	GRE+	22.94 \pm 0.67	28.14 \pm 0.67	0.97	34.15 \pm 1.33	35.85 \pm 1.33	1.00	80.61 \pm 1.10	15.39 \pm 1.10	1.00	57.43 \pm 1.30	16.89 \pm 1.30	1.00
Graph-SAGE	GD	17.16 \pm 12.20	31.88 \pm 12.20	1.00	55.85 \pm 22.50	40.71 \pm 20.30	1.00	19.07 \pm 14.10	36.68 \pm 10.10	1.00	62.16 \pm 2.10	4.38 \pm 2.10	1.00
	ENN	28.73 \pm 5.60	20.31 \pm 5.60	1.00	5.88 \pm 3.90	90.68 \pm 4.30	1.00	8.14 \pm 8.60	47.61 \pm 7.60	1.00	OOM	OOM	OOM
	GRE	20.69 \pm 1.62	28.31 \pm 1.62	0.99	21.93 \pm 0.94	47.07 \pm 0.94	1.00	47.16 \pm 1.22	48.84 \pm 1.22	1.00	61.96 \pm 1.02	4.58 \pm 1.02	1.00
	GRE+	38.41 \pm 1.17	10.59 \pm 1.17	0.82	29.26 \pm 2.10	39.74 \pm 2.10	1.00	58.29 \pm 2.35	37.71 \pm 2.35	1.00	63.25 \pm 2.25	3.29 \pm 2.25	1.00

constraint on multiple disjoint sub-training sets. Specifically, we split training dataset \mathcal{V}_{train} into K sub-training sets $\{\mathcal{V}_{train}^1, \mathcal{V}_{train}^2, \dots, \mathcal{V}_{train}^K\}$. Similarly, we define $g_{train}^k = \frac{\partial \mathcal{L}_{train}^k}{\partial \theta} \in \mathbb{R}^L$, where $\mathcal{L}_{train}^k = \frac{1}{|\mathcal{V}_{train}^k|} \sum_{i \in \mathcal{V}_{train}^k} CE(f_{\theta}(\mathbf{x}_i), y_i)$. Following the derivative clue in GRE, we can replace the training loss constraint on the whole training dataset with multiple training loss constraints on training subsets, and obtain the advanced gradient rewiring approach as follows:

$$\begin{aligned} \min_g \quad & \frac{1}{2} \|g - g_{tg}\|^2 + \frac{\lambda}{2} \|g\|^2 = \min_g \quad \frac{1+\lambda}{2} g^\top g - g_{tg}^\top g + \frac{1}{2} g_{tg}^\top g_{tg} \\ \text{s.t.} \quad & (g_{train}^k)^\top g \geq 0, \text{ for any } 1 \leq k \leq K. \end{aligned} \quad (9)$$

Notice that Eq.(9) is a quadratic program (QP) in L -variables (the number of model parameters are usually high in neural networks), and we can effectively solve this problem in the dual space via transforming as a smaller QP problem with only K variables $\mathbf{v} \in \mathbb{R}^K$ [22]. Define gradient matrix as $\mathbf{G} = [g_{train}^1, g_{train}^2, \dots, g_{train}^K]^\top \in \mathbb{R}^{K \times L}$, then the relation between primal and dual variable is given by $\mathbf{G}\mathbf{v} - (1+\lambda)g = -g_{tg}$. The original optimization problem can be transformed into the following dual problem:

$$\begin{aligned} \min_{\mathbf{v}} \quad & \frac{(1+\lambda)^{-1}}{2} \mathbf{v}^\top \mathbf{G} \mathbf{G}^\top \mathbf{v} + (1+\lambda)^{-1} g_{tg}^\top \mathbf{G}^\top \mathbf{v} + (1+\lambda)^{-1} g_{tg}^\top g_{tg} \\ \text{s.t.} \quad & \mathbf{v}_k \geq 0, \text{ for any } 1 \leq k \leq K. \end{aligned} \quad (10)$$

The dual problem is a QP with $K \ll L$ variables, and we usually consider the value of K to be smaller than 5 in practice. Once we tackle dual QP problem (10) for \mathbf{v}^* , we can recover the rewired gradient as $g = (1+\lambda)^{-1}(\mathbf{G}\mathbf{v} + g_{tg})$. Similarly, the gradient for training loss g_{train}^k , where $1 \leq k \leq K$, is required to be stored before model editing. The corresponding memory cost is given by $O(KL)$.

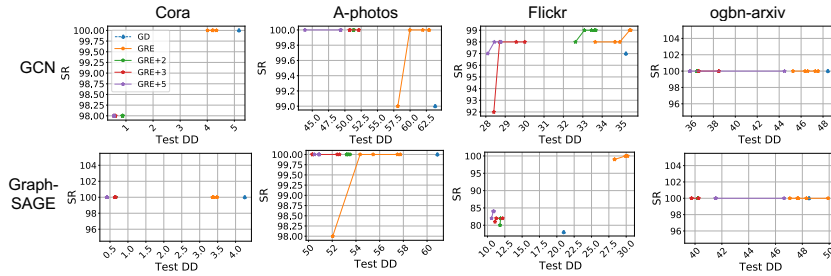


Figure 2: The success rate and test accuracy dropdown tradeoff in independent editing setting for GCN and GraphSAGE on various datasets. The trade-off curve close to the top left corner means better trade-off performance. The units for x- and y-axis are percentages (%).

4 Experiments

In this section, we conduct experiments to evaluate the effectiveness of our proposed GRE and GRE+, with the goal to answer the following three research questions. **RQ1:** Can the proposed solution correct the wrong model prediction with a lower accuracy drop after model editing in the independent and sequential editing setting? **RQ2:** What’s the tradeoff performance between accuracy drop and

200 success rate in the independent editing setting? **RQ3:** How sensitive are the proposed GRE and
201 GRE+ methods to the key hyperparameter λ ?

202 4.1 Experimental Setting

203 We follow the standard experimental setting for GNNs [17]. Specifically, we first randomly split the
204 train/validation/test dataset. Then, we ensure that each class has 20 samples in the training and 30
205 samples in the validation sets. The remaining samples are used for the test set. The target node is
206 randomly selected with 50 times from the validation set that the well-trained model makes the wrong
207 prediction. The average model editing performance (e.g., success rate, dropdown) is reported for
208 evaluation.

209 **Datasets and Models.** In our experiments, we utilize a selection of eight graph datasets from diverse
210 domains, split evenly between small-scale and large-scale datasets. The small-scale datasets include
211 Cora, A-computers [24], A-photo [24], and Coauthor-CS [24]. On the other hand, the large-scale
212 datasets encompass Reddit [20], Flickr [4], *ogbn-arxiv* [5], and *ogbn-products* [5]. Note that our
213 approach is based on gradient rewiring, which is orthogonal to model architectures. We adopt two
214 prevalent models GCN [19] and GraphSAGE [20], where both of them are trained with the entire
215 graph at each step. We evaluate our method under the **inductive setting**, which means the model is
216 trained on a subgraph containing only the training node, and evaluated on the whole graph.

217 **Baselines.** Our methods are evaluated against three notable baselines: the traditional gradient
218 descent editor (GD), the Editable Neural Network editor (ENN) [13], and editable training for
219 GNNs[17].³ The GD editor is a straightforward application using gradient descent on the target
220 loss with respect to the GNNs model parameters until the desired prediction outcome is achieved.
221 ENN adopts a different approach by initially training the GNN parameters for a few steps to prime
222 the model for subsequent edits. After this preparatory phase, ENN, like GD, applies the gradient
223 descent on the parameters of GNN until the correct prediction is attained. EGNN [17] stitches a peer
224 MLP and only trains MLP during model editing. Note that our method is compatible with EGNN,
225 and different GNN architectures integrated with EGNN (e.g., EGNN-GCN, EGNN-GraphSAGE) are
226 treated as distinct architectures..

227 **Independent, sequential, and batch editing.** All independent, sequential, and batch editing
228 processes involve well-trained GNN models using training datasets, with target samples randomly
229 selected multiple times from misclassified instances in the validation dataset. The key differences
230 lie in the base model that needs to be edited. For independent editing, the same well-trained model
231 using the training datasets is edited multiple times. In contrast, for sequential editing, the model is
232 edited iteratively, with each editing step using the previously edited model from the last target sample,
233 incorporating both the training datasets and partial samples from the validation dataset. For batch
234 editing, all batched samples are edited simultaneously in one editing process.⁴

235 **Evaluation Metrics.** Consistent with preceding studies [13, 15, 14], we assess the effectiveness of
236 the various methods using two primary metrics: (1) **Accuracy (Acc):** We use accuracy for the test
237 dataset to evaluate the effectiveness after model editing. (2) **DrawDown (DD):** This metric measures
238 the mean absolute difference in test accuracy before and after model editing. A lower drawdown
239 value signifies a superior editor locality. (3) **Success Rate (SR):** This metric evaluates the proportion
240 of edits in which the editor successfully amends the model’s prediction. Both metrics offer a different
241 perspective on the effectiveness of the editing process.

242 4.2 Experimental Results in the Independent and Sequential Editing Setting

243 In many real-world scenarios, well-trained models often produce inaccurate predictions on unseen
244 data. To evaluate the practical effectiveness of editors for independent editing (**RQ1**), we randomly

³MEND [14] and SERAC [15] are tailed for NLP application and are hard to extend to the graph area. MEND requires caching the input to each weight. Unfortunately, for graph data, the model edits cannot be done in a mini-batch way since the inference still runs in whole-batch, i.e., MEND requires caching the whole graph embedding at each layer.

⁴The experimental results on batch editing are in Appendix D.4.

choose nodes from the validation set that were misclassified during the training. The editor is then applied to rectify the model’s predictions for these misclassified nodes, and we evaluate the drawdown and edit success rate on the test set.

We edit one random single node 50 times and report the mean and standard deviation results in Tables 1 and 2 for small-scale and large-scale graph datasets, respectively. Our observations are made below:

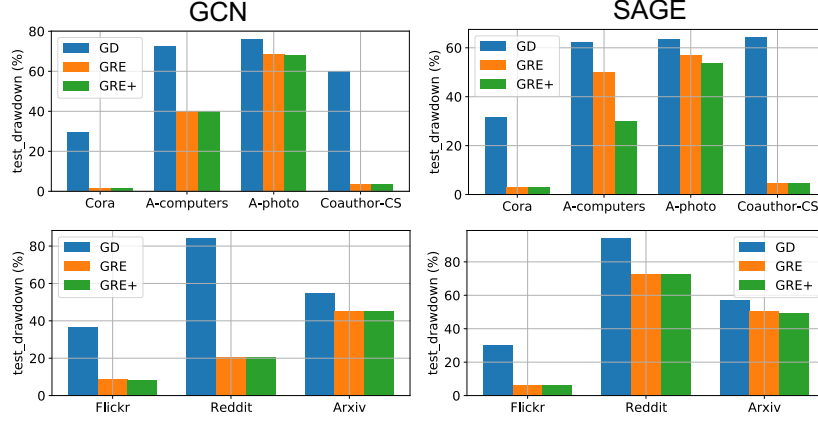


Figure 3: The test accuracy drawdown in sequential editing setting for GCN and GraphSAGE on various datasets. The units for y-axis are percentages (%).

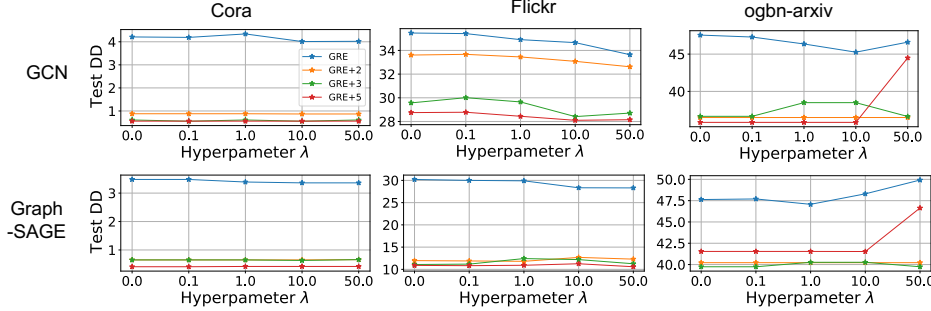


Figure 4: The hyperparameter study on test accuracy drawdown in independent editing setting w.r.t. λ .

❶ *Contrasting model editing on textual data* [14, 15, 25], all editors can effectively rectify model predictions in the graph domain. As shown in Table 1, all editors achieve a high success rate (typically from 96% ~ 100%) after editing GNNs, which is highly different from transformers with below 50% SR. This finding indicates that GNNs, unlike transformers, can be more easily adjusted to produce correct predictions. However, this improvement comes at the expense of substantial drawdown on other unrelated nodes, underscoring the key challenge of maintaining prediction locality for unrelated nodes before and after editing.

❷ *Our proposed GRE and GRE+ notably surpass both GD and ENN in terms of test drawdown.* This advantage stems mainly from the rewired gradient based on the pre-stored training loss gradient, which facilitates target sample correction while preserving the training loss. GD and ENN attempt to rectify model predictions by updating the parameters of GNNs without incorporating training loss information. In contrast, GRE and GRE+ maintain much better test accuracy after model editing. For example, for Amazon-photos, the accuracy drop dwindles from roughly 65.08% to around 43.87%, a 43.9% improvement over the baseline. This is due to the gradient rewiring approach that facilitates target sample correction while preserving the training loss. Interestingly, when applied to GNNs, ENN performs markedly worse than the basic editor GD. Moreover, GD performs well in MLP, which is consistent with the low gradient discrepancy of MLP.

❸ *Our proposed GRE and GRE+ are compatible with EGNN and further improve the performance.* We observe that while GRE occasionally underperforms, GRE+ consistently shows better performance than GD in reducing accuracy. For instance, when the A-computers dataset is evaluated with EGNN-GCN, GRE and GRE+ exhibit an average accuracy drop of 4.62% and 0.51%, respectively, whereas

GD shows a decrease of 0.73%. Notably, we find that for 7 out of 8 datasets, GRE+ with EGNN-SAGE shows a negative drop in accuracy, meaning that the test accuracy actually increases after model editing. This points towards the superior performance of the EGNN-SAGE model architecture.

In the **sequential editing setting**, we select a sequence of nodes from the validation set that were misclassified during the training phase. **the editor is then used to iteratively correct the model’s predictions for these sequentially misclassified nodes, and we** measure the resulting drawdown and success rate of edits on the test set.

In Figure 3, we report the test accuracy dropdown in the sequential setting, **a more challenging scenario that warrants** further investigation. In particular, we plot the test accuracy drawdown compared to GD across various GNN architectures and graph datasets. **Our observations are as follows:** ③ *The proposed GRE and GRE+ consistently outperform GD in the sequential setting.* However, the drawdown is **significantly higher** than in the single edit setting. For instance, GRE+ exhibits a 43.87% drawdown for GCN on the A-photo dataset in the single edit setting, which escalates up to a 65% drawdown in the sequential edit setting. These results also highlight the **challenge** of maintaining the locality of GNN prediction in sequential editing. ④ *The improvement of GRE+ over GRE is quite limited in the sequential setting.* For example, GRE+ exhibits a 24.52% drawdown over GRE for GCN on the A-photo dataset in the single edit setting while is on par with GRE in the sequential edit setting. These results further verify the difficulty of sequential editing and **indicate** more comprehensive training subset selection may be promising.

4.3 Trade-off Performance Comparison

We further compare **the trade-off between** accuracy dropdown and success rate of our method on various GNNs architectures and graph datasets. As shown in Figure 4, we plot Pareto **front** curves by assigning different hyperparameters **for** the proposed methods. The upper-left corner point represents the ideal performance, i.e., the highest SR and lowest accuracy dropdown. The results show that GRE+ achieves **a better trade-off results** compared to GRE, and all methods **consistently maintain a high** success rate on various GNNs architectures and graph datasets.

4.4 Hyperparameter Study

In this experiment, we **investigate** the sensitivity of our proposed method w.r.t. λ across a variety of GNN architectures and graph datasets. Specifically, we search **for** λ from the set of $\{0.0, 0.1, 1.0, 10.0, 50.0\}$. As **shown** in Figure 4, the test accuracy drop remains **relatively stable despite** variations in λ , suggesting that meticulous tuning of this parameter may not be crucial. For the ogbn-arxiv dataset, an uptick in accuracy drop corresponds with an increase in λ , reflecting the inherent difficulty of this dataset. Intriguingly, in the case of GRE+5 with 5 training subsets, the test accuracy drop exceeds that of GRE+2 and GRE+3, a pattern that diverges from the trend observed in other datasets.

5 Conclusion

In this paper, we **explore the** editing of graph neural networks from a new gradient perspective. Through empirical observations, we discover that conventional model editing techniques often **underperform** due to the gradient discrepancy between the training loss and target loss in GNNs. **To address this issue, we propose a gradient rewiring approach. Specifically, we formulate a constrained optimization problem to regulate the model performance during model editing and identify** a simple yet effective gradient rewiring approach to explicitly satisfy the constraints. In this way, the proposed approach can correct the target sample while preventing **an increase in training loss**. Experiments demonstrate the effectiveness of our approach, and our proposed method is also compatible with the existing baseline EGNN and can further improve performance. Future work includes more comprehensive training subset selection in GRE+ and a tailed approach for editable graph neural networks training in the sequential editing setting.

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A Experimental Setting

A.1 More details on EGNN

We provide more details on editable graph neural networks (EGNN), a method free of neighborhood propagation, designed specifically for correcting misclassified node predictions [17]. EGNN uniquely integrates a peer MLP (matching in the number of hidden units and layers) with GNNs (such as GCN and GraphSAGE), and trains solely the MLP model using the target loss during model editing. This strategy enables EGNN to leverage the propagation-free advantages of MLPs for model editing. However, it’s important to note that EGNN is incompatible with EGNN, as the model editing in EGNN refines a stitched MLP, which is not employed during model training. Our proposed methodologies, GRE and GRE+, are founded on gradient rewiring, which is orthogonal to the EGNN approach. In the appendix, we illustrate how our proposed methodologies can further augment the effectiveness of the EGNN approach and MLP models.

Table 3: Statistics information for datasets used for node classification.

Datasets	Cora	A-computers	A-photo	Coauthor-CS	Flickr	Reddit	<i>ogbn-arxiv</i>	<i>ogbn-products</i>
# Nodes	2,485	13,381	7,487	18,333	89,250	232,965	169,343	2,449,029
# GREes	5,069	245,778	119,	81,894	899,756	23,213,838	1,166,243	61,859,140
# Classes	7	10	8	15	7	41	40	47
# Feat	1433	767	745	6805	500	602	128	218

A.2 Datasets

The statistical information of all datasets is summarized in Table 3. The details of the datasets utilized for node classification are described as follows:

- **Cora** [26]: This citation network comprises 2,708 publications interconnected by 5,429 links. Each publication is characterized by a 1,433-dimensional binary vector that signifies the presence or absence of specific words from a predetermined vocabulary.
- **A-computers** [24]: This dataset is a segment of the Amazon co-purchase graph. In this network, nodes denote goods, and GREes represent frequent co-purchases of two goods. Node features are encoded as bag-of-words product reviews.
- **A-photo** [24]: Similar to A-computers, this is another segment of the Amazon co-purchase graph. Node features are also bag-of-words encoded product reviews.
- **Coauthor-CS** [24]: Derived from the Microsoft Academic Graph from the KDD Cup 2016 challenge 3, this co-authorship graph has nodes representing authors who are linked if they have co-authored a paper. Node features denote paper keywords for each author’s publications, while class labels indicate an author’s most active fields of study.
- **Reddit** [20]: This dataset is formulated from Reddit posts, with each node representing a post associated with different communities.
- **ogbn-arxiv** [5]: This dataset represents the citation network among all arXiv papers. Each node denotes a paper, and each GREe signifies a citation between two papers. Node features are generated from the average 128-dimensional word vector of each paper’s title and abstract.
- **ogbn-products** [5]: This is an Amazon product co-purchasing network, where nodes represent Amazon products and GREes denote co-purchases of two products. Node features are created from low-dimensional representations of product description text.

A.3 Implementation Details

The hyperparameters for model architecture, learning rate, dropout rate, and training epochs are shown in Table 4. For EGNN, we also adopt GNNs and MLPs with hyperparameters in Table 4. For GRE, we use the hyperparameters $\gamma = \{0.0, 0.1, 1.0, 10.0, 50.0\}$. For GRE+, we also select hyperparameters $\gamma = \{0.0, 0.1, 1.0, 10.0, 50.0\}$ and $K = \{1, 2, 3, 5\}$. As for QP problem Eq. (10), we use a standard package qpsolvers with version 3.4.0 to tackle this QP problem with ecos solver.

Table 4: Training hyperparameters configurations in the experiments

Model	Configuration	Cora	A-computers	A-photo	Coauthor-CS	Flickr	Reddit	ogbn-arxiv	ogbn-products
Graph-SAGE	#Layers	2	2	2	2	2	2	3	3
	#Hidden	32	32	32	32	256	256	128	256
	lr	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.002
	Dropout	0.1	0.1	0.1	0.1	0.3	0.5	0.5	0.5
	Epoch	200	400	400	400	400	400	500	500
GCN	#Layers	2	2	2	4	2	2	3	3
	#Hidden	32	32	32	32	256	256	128	256
	lr	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.002
	Dropout	0.1	0.1	0.1	0.1	0.3	0.5	0.5	0.5
	Epoch	200	400	400	400	400	400	500	500
MLP	#Layers	2	2	2	4	2	2	3	3
	#Hidden	32	32	32	32	256	256	128	256
	lr	0.01	0.01	0.01	0.01	0.01	0.01	0.01	0.002
	Dropout	0.1	0.1	0.1	0.1	0.3	0.5	0.5	0.5
	Epoch	200	400	400	400	400	400	500	500

A.4 Running Environment

For hardware configuration, all experiments are executed on a server with 251GB main memory, 24 AMD EPYC 7282 16-core processor CPUs, and a single NVIDIA GeForce-RTX 3090 (24GB). For software configuration, we use CUDA=11.3.1, python=3.8.0, pytorch=1.12.1, higher=0.2.1, torch-geometric=1.7.2, torch-sparse=0.6.16 in the software environment. Additionally, we use the package of higher in <https://github.com/eric-mitchell/mend> for ENN implementation.

B Limitations and Discussions

While our proposed GRE and GRE+ methods effectively mitigate the accuracy dropdown compared to conventional gradient descent algorithms, the success of our approaches is largely contingent on the precision of the pre-stored gradient for training loss. Despite the relatively few required model edit steps for single node editing, the accuracy of the pre-stored gradient may not sustain over long-term model editing, as the pre-stored gradient for training loss could exhibit significant discrepancy from the gradient of training loss for the edited model. To address such discrepancy, a straightforward strategy could involve leveraging critical training samples to estimate the true gradient of training loss for the edited model. Another possible direction is to identify critical samples instead of random samples for GRE+ with the aim of further constraining the model’s behavior before and after model editing.

Notice that the proposed gradient rewiring method is not inherently specific to graphs, the gradient rewiring method is particularly suitable in the graph domain due to the small model size. Specifically, graph models are typically a few layers and thus are smaller in model size compared to models (e.g., Transformers) used in NLP and CV tasks. This results in lower computational and storage costs for gradients, making our strategy particularly suitable for the graph domain. Additionally, it is more challenging to edit nodes in a graph due to the inherent propagation process within neighborhoods. Such propagation may lead to significant gradient discrepancies within the graph domain.

C Algorithms

We show the algorithms of GRE and GRE+ during model editing in Algorithm 1 and 2, respectively.

D More Experimental Results

In this section, we present experimental results to showcase the improved efficacy of our proposed methods, GRE and GRE+. These techniques enhance the performance of EGNN, a specifically designed editable graph neural network, across both independent and sequential editing settings.

Algorithm 1 Gradient Rewiring Editable (GRE) Graph Neural Networks Training

0: **Input:** Target samples $(\mathbf{x}_{tg}, \mathbf{y}_{tg})$, hyperparameters λ , well-trained GNNs model $f_{\theta}(\cdot)$, and its corresponding model gradient for training subgraph.
0: **Output:** Editable GNNs model $f_{\theta'}(\cdot)$.
0: **while** $f_{\theta}(\mathbf{x}_{tg}) \neq \mathbf{y}_{tg}$ **do**
0: Compute model gradient g_{tg} for target loss \mathcal{L}_{tg} .
0: Rewire target loss gradient g_{tg} via reducing the projection component on g_{train} and then scale with $(1 + \lambda)^{-1}$, i.e., $g^* = (1 + \lambda)^{-1}(g_{tg} - v^* g_{train})$.
0: Replace g_{tg} with g^* and then adopt optimizer to update model parameters as θ' .
0: **end while**

Algorithm 2 Gradient Rewiring Editable Plus (GRE+) Graph Neural Networks Training

0: **Input:** Target samples $(\mathbf{x}_{tg}, \mathbf{y}_{tg})$, hyperparameters λ , well-trained GNNs model $f_{\theta}(\cdot)$, and its corresponding model gradient for training subgraph.
0: **Output:** Editable GNNs model $f_{\theta'}(\cdot)$.
0: **while** $f_{\theta}(\mathbf{x}_{tg}) \neq \mathbf{y}_{tg}$ **do**
0: Compute model gradient g_{tg} for target loss \mathcal{L}_{tg} .
0: Solve QP problem Eq. (10) via standard QP solver package and obtain the optimal dual variable \mathbf{v}^* .
0: Calculate the rewired gradient using $g^* = (1 + \lambda)^{-1}(\mathbf{G}\mathbf{v}^* + g_{tg})$.
0: Replace g_{tg} with g^* and then adopt optimizer to update model parameters as θ' .
0: **end while**

D.1 More results on Model Architectures for Independent Editing

In this section, we conduct a sequence of 50 single-node edits and present the mean and standard deviation results in Tables 5 for large-scale graph datasets. Similarly, GRE occasionally underperforms, and GRE+ consistently shows better performance than GD with respect to the reduction in accuracy. For instance, when the Reddit dataset is evaluated with EGNN-GCN, GRE and GRE+ exhibit an average accuracy drop of 1.48% and -0.21% , respectively, whereas GD shows a decrease of 1.28%. Moreover, GRE+ with EGNN-SAGE shows a negative drop in accuracy among 6 out of 8 datasets, i.e., the test accuracy actually increases after model editing.

Table 5: The results on four large scale datasets after applying one single edit. “OOM” is the out-of-memory error.

Editor		Flickr			Reddit			ogbn-arxiv			ogbn-products		
		Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow
MLP	GD	35.84 \pm 1.23	11.16 \pm 1.23	0.83	45.27 \pm 0.97	7.73 \pm 0.97	0.99	70.31 \pm 0.40	2.69 \pm 0.40	1.00	74.19 \pm 3.40	0.20 \pm 3.40	1.00
	ENN	25.82 \pm 14.90	25.38 \pm 16.90	1.00	11.16 \pm 5.10	84.36 \pm 3.10	1.00	16.59 \pm 7.70	53.62 \pm 6.70	1.00	OOM	OOM	0
	GRE	36.47 \pm 0.57	10.53 \pm 0.57	0.81	35.85 \pm 2.60	17.15 \pm 2.60	1.00	62.20 \pm 0.94	10.80 \pm 0.94	1.00	53.99 \pm 0.60	20.01 \pm 0.60	1.00
	GRE+	43.23 \pm 0.17	3.77 \pm 0.17	0.84	41.33 \pm 0.87	11.67 \pm 0.87	0.99	64.11 \pm 0.95	8.40 \pm 0.95	1.00	57.43 \pm 1.30	16.89 \pm 1.30	1.00
EGNN-GCN	GD	46.10 \pm 0.91	4.90 \pm 0.91	0.93	68.72 \pm 0.55	1.28 \pm 0.55	1.00	86.08 \pm 0.83	-0.08 \pm 0.17	1.00	73.73 \pm 0.12	0.27 \pm 0.12	1.00
	GRE	45.70 \pm 0.97	5.30 \pm 0.97	0.94	68.52 \pm 0.51	1.48 \pm 0.51	1.00	89.22 \pm 0.34	-3.22 \pm 1.34	1.00	73.65 \pm 0.16	0.35 \pm 0.16	1.00
EGNN-GCN	GRE+	50.60 \pm 0.15	0.40 \pm 0.15	0.99	69.97 \pm 0.38	-0.21 \pm 0.38	1.00	88.51 \pm 0.57	-2.51 \pm 0.43	1.00	74.06 \pm 0.45	-0.80 \pm 0.45	1.00
EGNN-SAGE	GD	45.68 \pm 1.15	2.32 \pm 1.15	0.95	67.76 \pm 0.53	1.24 \pm 0.53	1.00	95.99 \pm 0.02	0.01 \pm 0.02	0.98	75.89 \pm 0.06	0.11 \pm 0.06	1.00
	GRE	42.25 \pm 1.64	5.75 \pm 1.64	1.00	67.34 \pm 0.35	1.66 \pm 0.35	0.99	94.09 \pm 1.29	1.91 \pm 1.29	1.00	75.90 \pm 0.05	0.10 \pm 0.05	1.00
EGNN-SAGE	GRE+	49.06 \pm 1.42	-1.05 \pm 1.42	1.00	68.48 \pm 0.78	0.11 \pm 0.78	1.00	96.06 \pm 0.10	-0.06 \pm 0.10	0.95	76.26 \pm 0.21	-0.17 \pm 0.21	1.00

D.2 Experimental Results on other Model Architectures for Sequential Editing Setting

In the sequential editing setting, we take a sequence of 50 misclassified nodes and use the editor to iteratively correct the model’s predictions for EGNN across different GNN architectures. The test accuracy drop associated with various model editing methods for different graph datasets is reported in Figure 7. Our observations indicate that the proposed GRE and GRE+ methods consistently outshine GD in this sequential setting. For instance, with the Coauthor-CS dataset and EGNN-GCN, our proposed methods achieve virtually no decrease in accuracy, while GD exhibits a drop of over 7%. Another compelling observation is that the improvement demonstrated by our methods over GD for EGNN is markedly larger than for GNNs. This suggests potential synergies between optimizer selection and model architecture design.

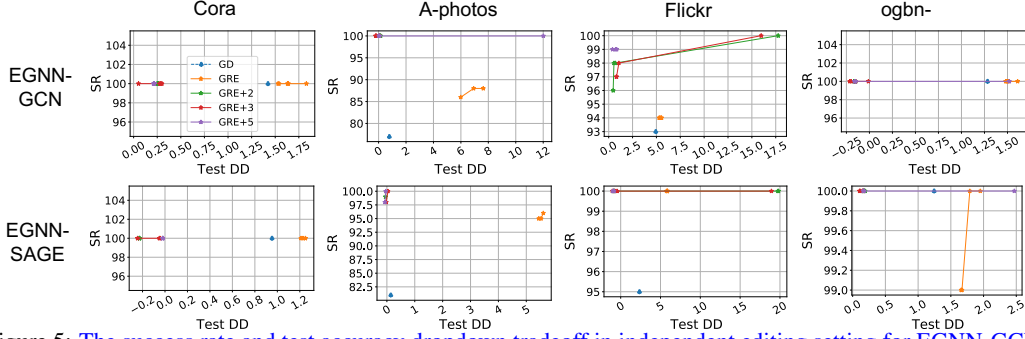


Figure 5: The success rate and test accuracy dropdown tradeoff in independent editing setting for EGNN-GCN and EGNN-SAGE on various datasets. The trade-off curve close to the top left corner means better trade-off performance. The units for x- and y-axis are percentages (%).

D.3 Trade-off Performance Comparison on other Model Architectures

We extend our evaluation by comparing the trade-off between accuracy drop and success rate of our method on EGNN across various graph datasets. By adjusting different hyperparameters for the proposed methods, we construct Pareto front curves as shown in Figure 5. The results underscore that both GRE+ and GRE outperform GD in achieving superior trade-off outcomes. Importantly, our proposed methods exhibit robust preservation of the success rate across various GNN architectures and graph datasets.

D.4 More Experimental results on Batch Editing

In this section, we present the experimental results of applying batch editing on four small-scale datasets (Table 6) and four large-scale datasets (Table 7).

For the small-scale datasets, our proposed methods, GRE and GRE+, consistently outperform the baseline methods. For example, on the Cora dataset, GRE+ achieves the highest accuracy with a minimal drawdown and a high success rate. Specifically, GRE+ can reduce 56.9% and 30.3% drawdown compared with 2nd best baseline in GCN and GraphSAGE architectures, respectively. For the large-scale datasets, GRE+ again demonstrates superior performance. On ogbn-products datasets GRE+ can reduce 2.5% and 0.5% drawdown compared with 2nd best baseline GRE in GCN and GraphSAGE architectures, respectively, while maintaining a high success rate.

Table 6: The results on four small-scale datasets after applying batch edit. **SR** is the edit success rate, **Acc** is the test accuracy after editing, and **DD** are the test drawdown, respectively. The best/second-best results are highlighted in **boldface/underlined**, respectively.

Editor	Cora			A-computers			A-photo			Coauthor-CS			
	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	
GCN	GD	81.72 \pm 5.24	7.28 \pm 4.04	0.77	60.98 \pm 22.41	27.02 \pm 3.89	0.53	44.32 \pm 11.26	49.64 \pm 11.54	0.52	67.64 \pm 6.23	26.36 \pm 7.05	1.00
	ENN	32.16 \pm 2.75	46.12 \pm 1.84	0.93	25.91 \pm 13.01	27.09 \pm 14.51	0.25	9.99 \pm 0.81	-0.99 \pm 0.99	0.06	45.59 \pm 13.21	-43.59 \pm 15.54	0.62
	GRE	82.96 \pm 2.47	6.04 \pm 3.29	0.96	64.67 \pm 3.47	23.33 \pm 13.85	0.63	54.66 \pm 26.26	39.34 \pm 28.82	0.34	76.24 \pm 5.29	17.76 \pm 5.87	1.00
	GRE+	86.40\pm0.76	2.60\pm0.55	0.97	65.25\pm0.35	22.70\pm0.65	0.62	57.83\pm1.36	36.13\pm9.25	0.50	76.80\pm9.56	17.20\pm9.93	1.00
Graph-SAGE	GD	78.48 \pm 4.33	8.52 \pm 1.70	1.00	29.95 \pm 18.28	53.08 \pm 9.55	0.53	46.98 \pm 15.24	47.02 \pm 17.52	0.50	67.64 \pm 7.58	23.27 \pm 7.97	1.00
	ENN	32.16 \pm 2.21	45.88 \pm 1.68	0.99	0.99 \pm 0.00	0.08 \pm 0.01	0.08	14.81 \pm 7.92	-4.81 \pm 18.23	0.17	77.55\pm2.12	-15.55 \pm 2.07	1.00
	GRE	80.68 \pm 1.17	6.32 \pm 1.17	0.99	46.58 \pm 2.25	36.42 \pm 10.43	0.54	56.95 \pm 18.27	37.05 \pm 20.18	0.46	75.68 \pm 8.44	19.32 \pm 8.99	1.00
	GRE+	82.60\pm0.87	4.40\pm1.07	1.00	51.24\pm12.87	32.51\pm15.77	0.62	62.60\pm11.82	31.40\pm12.93	0.52	76.51\pm6.21	18.49\pm6.80	1.00

Table 7: The results on four large-scale datasets after applying batch edit. “OOM” is the out-of-memory error. The best/second-best results are highlighted in **boldface/underlined**, respectively.

	Editor	Flickr			Reddit			ogbn-arxiv			ogbn-products		
		Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow	Acc \uparrow	DD \downarrow	SR \uparrow
GCN	GD	19.79 \pm 12.12	31.21 \pm 12.55	0.29	37.64 \pm 5.30	58.36 \pm 5.20	1.00	38.61 \pm 4.91	31.39 \pm 5.57	0.83	41.83 \pm 5.94	32.17 \pm 4.50	1.00
	ENN	42.82\pm1.92	0.00\pm1.90	0.00	65.70\pm3.11	-59.70\pm3.24	1.00	24.47 \pm 1.77	-18.41 \pm 1.81	0.77	OOM	OOM	0
	GRE	24.90 \pm 5.51	26.10 \pm 5.31	0.39	24.74 \pm 1.92	45.26 \pm 1.92	1.00	<u>41.96\pm7.26</u>	<u>29.04\pm7.51</u>	0.62	<u>42.52\pm4.60</u>	<u>31.48\pm4.86</u>	1.00
	GRE+	25.10 \pm 6.67	<u>25.90\pm6.47</u>	0.42	<u>52.61\pm4.23</u>	<u>43.59\pm5.81</u>	1.00	<u>41.13\pm4.10</u>	28.87\pm5.04	0.80	42.60\pm4.89	31.40\pm5.03	1.00
Graph-SAGE	GD	20.71 \pm 11.20	18.29 \pm 10.05	0.27	29.65 \pm 22.5	66.35 \pm 5.20	1.00	<u>41.05\pm6.81</u>	<u>27.95\pm7.87</u>	0.77	49.33 \pm 4.18	17.15 \pm 5.21	0.94
	ENN	41.89\pm0.60	-16.89\pm0.03	0.56	17.10 \pm 4.90	-15.10 \pm 5.56	0.24	13.82 \pm 2.68	8.18 \pm 6.52	0.26	OOM	OOM	0
	GRE	26.92 \pm 2.62	22.08 \pm 3.06	0.59	<u>31.40\pm8.94</u>	<u>64.60\pm9.76</u>	0.93	38.65 \pm 7.22	30.35 \pm 8.84	0.70	<u>50.21\pm3.82</u>	<u>16.33\pm4.92</u>	0.92
	GRE+	<u>27.97\pm1.17</u>	<u>21.03\pm7.97</u>	0.42	<u>38.01\pm7.32</u>	56.99\pm6.88	0.95	42.76\pm4.31	26.24\pm8.47	0.79	50.30\pm5.83	16.24\pm6.25	0.90

D.5 The Edit Time and Memory Comparison for Editing Methods

In this section, we present the experimental results of the edit time and memory required for editing across four large-scale datasets (Table 8).

We observe that GRE+ takes 1.5 $2.5\times$ wall-clock editing time than the GD/GRE editor in terms of the wall-clock edit time. This is because GRE+ requires QP solver to obtain the rewired gradient. In terms of memory consumption, the overall memory overhead is insignificant. For example, GRE+ (5) requires 17.9% GPU memory than GD editor in obgn-products dataset and GCN architecture. The reason is that the anchor gradient is required to store in memory and QP solver computation in memory.

Table 8: The edit time and memory required for editing. ET (ms) and PM (MB) represent the edit time in milliseconds and peak memory in megabytes, respectively.

Editor	Flickr		Reddit		ogbn-arxiv		ogbn-products	
	ET (ms)	PM (MB)	ET (ms)	PM (MB)	ET (ms)	PM (MB)	ET (ms)	PM (MB)
GCN	GD	67.46	707.0	345.23	3244.8	94.58	786.2	2374.15
	ENN	109.82	666.8	405.24	3244.8	242.85	786.2	OOM
	GRE	63.93	695.8	391.54	3491.3	84.74	956.9	2400.78
	GRE+ (2)	100.45	696.0	457.08	3493.2	121.11	957.8	2413.69
	GRE+ (3)	115.29	697.9	509.44	3493.9	131.06	957.9	2471.23
	GRE+ (5)	155.05	698.6	603.85	3495.6	162.24	958.3	2591.06
Graph-SAGE	GD	117.74	843.0	1024.12	4416.53	107.63	891.3	2125.07
	ENN	134.50	843.0	2597.21	4416.5	277.29	891.3	OOM
	GRE	116.03	952.4	1089.29	4955.4	100.09	1072.5	2132.02
	GRE+ (2)	167.17	954.5	1267.13	4959.0	136.28	1073.7	2135.88
	GRE+ (3)	176.66	955.5	1363.53	4960.7	154.29	1074.0	2211.63
	GRE+ (5)	219.81	957.5	1603.03	4964.2	180.73	1075.5	2275.72

D.6 More Test Accuracy Results on Sequential Editing

In this subsection, we present the after-editing test accuracy results of applying sequential editing on various datasets for both GCN and GraphSAGE models in Figure 6. The test accuracy is reported as a percentage for each dataset.

Overall, our proposed methods, GRE and GRE+, consistently outperform the baseline methods GD and ENN across all datasets in terms of test accuracy. For example, on the Reddit dataset, the proposed methods can achieve more than 100% improvement over GD and ENN in terms of accuracy. Besides, compared with GRE and GRE+, the improvement is marginal on most occasions except A-computer dataset in GraphSAGE, which indicates the limited effectiveness of the fine-grained gradient rewiring in GRE+.

E More Related Work

Gradient-based method for other tasks. The existing literature on gradient modification mainly incorporates continual learning and meta learning. In continual learning, work [27] proposes gradient projection methods to update the model with gradients in the orthogonal directions of old tasks, without access to old task data. GPM [28] identifies the bases of these subspaces by examining network representations after learning each task using Singular Value Decomposition (SVD) in a single-shot manner and stores them in memory as gradient projection memory. Class gradient projection is proposed in [29] to address the class deviation in gradient projection. In meta-learning, work [30] proposes a meta-learning algorithm to learn to modulate the gradient in the absence of abundant data. The implicit model-agnostic meta-learning (iMAML) algorithm is developed in [31] for optimization-based meta-learning with deep neural networks that remove the need for differentiating through the optimization path. [32] provides a theoretical framework for designing and understanding practical meta learning methods that integrate sophisticated formalizations of task-similarity.

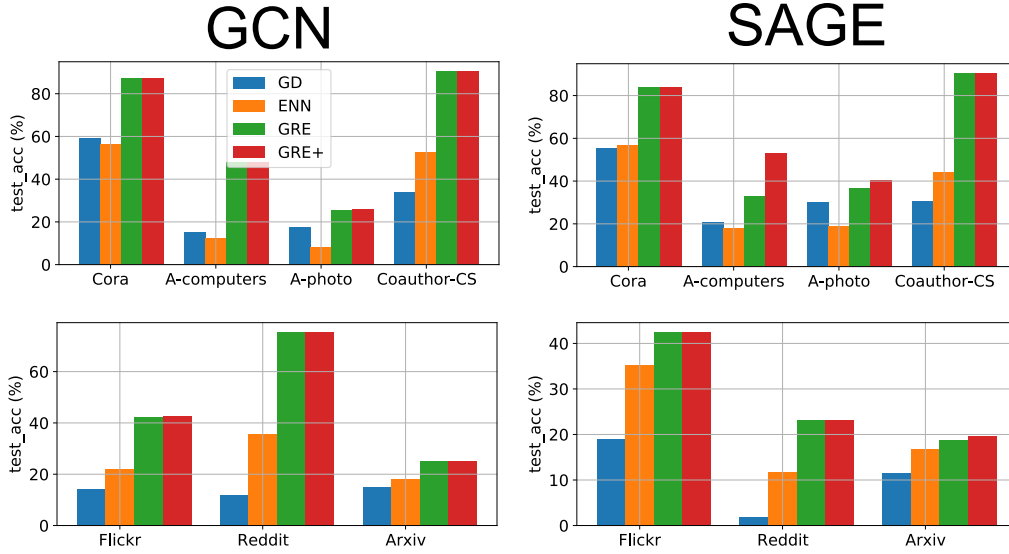


Figure 6: The test accuracy in sequential editing setting for GCN and GraphSAGE on various datasets. The units for y-axis are percentages (%).

F More discussion

Comparison with Curriculum Learning. Curriculum learning and model editing are two distinct approaches in the field of machine learning. Curriculum learning is an approach where the network is trained in a structured manner, starting with simpler tasks and gradually introducing more complex ones. This method aims to improve the learning process by mimicking how humans learn. Model editing is a fast and efficient approach to patch the well-trained model prediction for several failed test cases. Although both are multi-stage training stages, there are several key differences: (1) Goals: Curriculum Learning aims to improve the overall learning process by structuring the training data in a way that mimics human learning. In contrast, model editing aims to make targeted adjustments to a pre-trained model to correct undesirable behaviors. (2) Approach: curriculum learning mainly focuses on the sequence and complexity of the training data. Model editing typically modifies the model’s parameters or architecture to correct undesirable behavior goals. (3) Additional information in the multi-stage process. Model editing requires failure feedback for well-trained models as the target samples to patch, e.g., test failure cases after production is launched. In other words, such feedback can only be obtained after model pertaining. In curriculum learning, all information is given in multi-stage training. In summary, curriculum learning focuses on structuring the training process to improve overall learning, while model editing focuses on making targeted adjustments to a pre-trained model to correct specific behaviors. Both approaches can be complementary and used together to achieve better model performance.

Comparison with Domain Adaptation. To the best of our knowledge, many existing methods in domain adaptation (DA) [33, 34] integrate source and target gradients in the loss function. For example, [33] aims to minimize the gradient discrepancy for unsupervised DA, and [34] aligns gradient distribution for better adversarial DA. However, these methods can not be applied in graph model editing since (1) gradient discrepancy is required to successfully edit model prediction; (2) model editing collapses (i.e., no gradient discrepancy) at the initial stage; (3) regulating gradient behavior is insufficient for model editing task since the main problem is how to get an edited model instead of cross-domain generalization. To this end, we rewire the gradient before the model parameters update, and derive a closed-form, instead of a learning-based, gradient rewiring method to accelerate model editing.

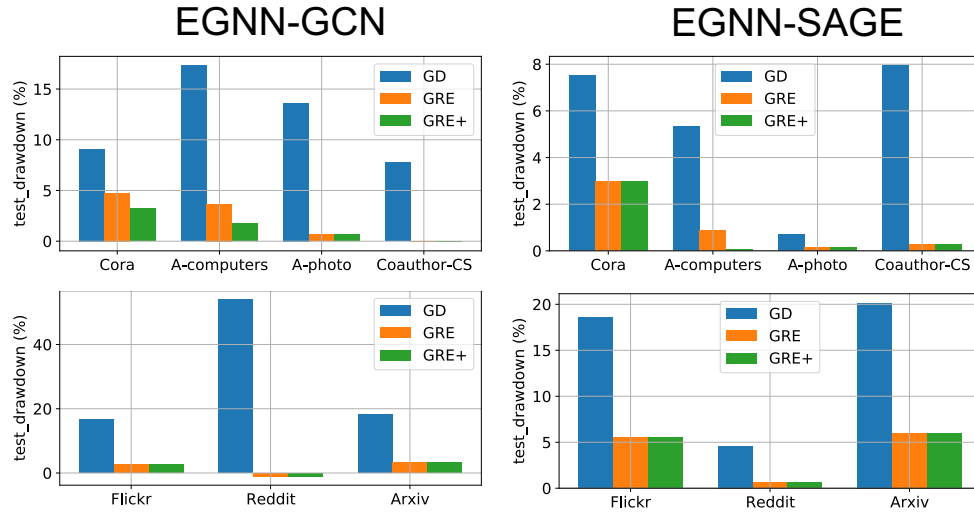


Figure 7: The test accuracy dropdown in sequential editing setting for EGNN-GCN and EGNN-SAGE on various datasets. The units for the y-axis are percentages (%).

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