# PROLOG

- PROLOG is a programming language
- PROLOG: PROgramming in LOGic
- Invented by Alain Colmerauer in1973 in Marseille (France)
- Use of <u>mathematical logic</u> to represent knowledge
- **Declarative** language



# **Syntax**

- Constants are character strings that begin with minuscule letters
  - e.g. alice, edward, james\_bond\_007
- Variables are character strings that begin with a capital or a
  e.g. X, G341, Stranger, The Older...
- Clauses begin by the positive literals, then the sign ':-' and the sequence of negative literals separated by comma (","); it always end with a dot (".")

#### Mode "consult"

```
femme(alice).
femme(victoria).
homme(albert).

homme(edward).
parents(edward, victoria, albert).
parents(alice, victoria, albert).
```

### Mode "query"

```
?- femme(alice).
Yes
?- homme(X).
X = albert
Yes
?- femme(X), parents(X, U, I).
X = alice
U = victoria
I = albert;
```

# Data Bases in PROLOG

**Atom Conjunction** 

#### Mode "consult"

```
femme (alice).
femme (victoria).
homme (albert).
homme (edward).
parents (edward, victoria, albert).
parents (alice, victoria, albert).
soeur( X, Y) :- femme( X), parents( X, Mere, Pere),
         parents (Y, Mere, Pere).

    Mode "query"

?- soeur(U, edward).
U = alice :
N \cap
?- soeur(U, V).
U = alice
V = edward;
U = alice
V = alice :
No
```

#### Set of Horn clauses

# Deduction in PROLOG

**Atom conjunction** 

Definition: a **positive Horn clause** is a clause (i.e. A disjunction of literals) that owns one and only one positive literal

## Examples:

### **Positive Horn Clauses**

```
femme (victoria).
```

homme (edward) .

```
parents (alice, victoria, albert).
```

```
soeur( X, Y) :- femme(X), parents(X, Mere, Pere),
parents( Y, Mere, Pere).
```

#### Are Horn clauses

- ¬barber(X) v shave(X, Y) v shave(Y, Y) which means: "the barbers shave those who don't shave by themselves" is not a Horn clause
- ¬barber(X) v ¬shave(X, Y) v ¬shave(Y, Y) which means "there is no barber who shaves someone who shaves himself" is not a positive Horn clause

# Declarative programming

• Description of predicate properties:

```
nombre(0).
nombre(s(X)) := nombre(X).
addition(0, X, X).
addition(s(X), Y, s(Z)) := addition(X, Y, Z).

• Call in query mode:
?= nombre(s(s(0))).

Yes

Cutput
?= addition(s(s(0)), s(s(s(0))))

Yes

Result
```



#### Mode "consult"

```
nombre(0). nombre(0) \rightarrow Set of Horn clauses = Rules nombre(s(X)):- nombre(X). nombre(s(X)) \rightarrow nombre(x) addition(0, X, X). addition(0, X, X) \rightarrow addition(s(X), Y, s(Z)):- addition(X, Y, Z). addition(s(X), Y, s(Z)) \rightarrow addition(X, Y, Z)
```

## Mode "query"

#### **Atom conjunction**

```
?- nombre(s(s(s(0))).
?- addition(s(s(0)), s(s(s(0))), X).
```

#### Work of the Interpreter

The query is rewritten using rules until it becomes empty.

PROLOG for "babies"

# PROLOG strategy

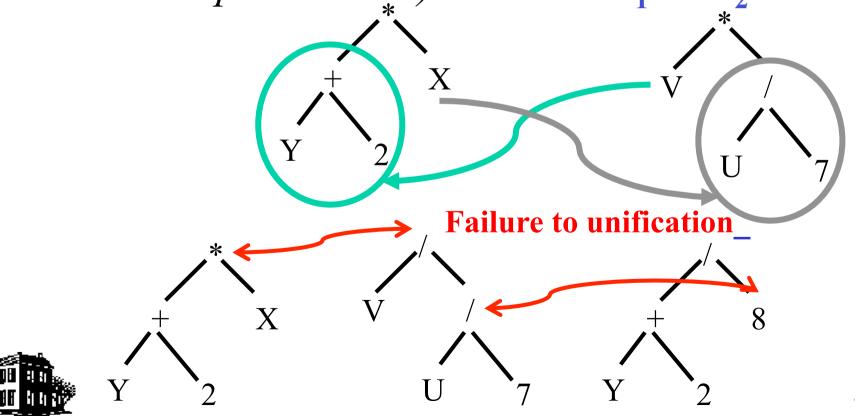
- PROLOG try to apply the "rules" (i.e. the clause) on the atoms of the "query"
- PROLOG makes use of the "unification" mechanism
- The atoms of the "query" are solved sequentially, from left to right.
- The clauses are considered one after one, from the first until the last.



## Unification

**Unify**: to make unique

**Unification**: two terms  $t_1$  and  $t_2$  unify if and only if there exists a substitution  $\sigma$  (*i.e.* a list of variable replacements) such that:  $t_1\sigma = t_2\sigma$ 



## Example: addition

```
:- addition(s(s(0)), s(s(s(0))), Z)
                                                      C2
                                                     C2
:- addition(s(0), s(s(s(0))), Z1)
:- addition(0, s(s(s(0))), Z2)
```



C1: addition(0, X, X). C2: addition(s(X), Y, s(Z)) :- addition(X, Y, Z).

## **Function Inversion**

• Description of predicate properties:

```
nombre (0).
nombre (s(X)) :- nombre(X).
addition(0, X, X).
addition(s(X), Y, s(Z)) :- addition(X, Y, Z).
• Call in query mode:
?- addition(s(s(0)), U, s(s(s(s(0)))))).
U = s(s(s(0)))
Yes
?- nombre (X).
X = 0;
X = s(0) ;
X = s(s(0)) ;
X = s(s(s(0))) ;
X = s(s(s(s(0))))
```

# Program

- A program is a set of clauses of which head literal has the same predicate name and the same arity
- Examples
- Program addition: [addition(X, Y, Z) means X+Y=Z] addition(0, X, X). addition(S(X), Y, S(Z)) :- addition(X, Y, Z).
- Program multiplication: [multiply(X, Y, Z) means Z=X.Y] multiply(0, X, 0). multiply(s(N), P, R) :- multiply(N, P, Q), addition(P, Q, R).
- Programme factorial: [ $fact_s(N, P)$  means P = N!]

  fact\_s(0, s(0)).

  fact\_s(s(0), s(0)).

  fact\_s(s(N), R) :- fact\_s(N, Q),

  multiply(s(N), Q, R).

## Procedure call

• A call to a procedure is an atom in the "query" mode:

```
Examples:

?- fact_s(s(s(s(s(0))), U)).

U = s(s(s(s(s(s(s(0))))))).

Yes

?- multiply(s(s(0)), s(s(s(0)))), R).

Input

Yes

?- multiply(s(s(0)), H) s(s(s(s(s(s(0)))))).

H = s(s(s(s(s(0))))

Yes
```



# 

# Example addition

and/or tree

:- addition(0, 
$$s(s(s(0)))$$
,  $Z2)$ 

C1  $\{Z2 = s(s(s(0)))\}$ 
 $I^{st}$  solution:
 $Z = s(s(Z2)) = s(s(s(s(s(0)))))$ 



C1: addition(0, X, X).

C2: addition(s(X), Y, s(Z)) :- addition(X, Y, Z).

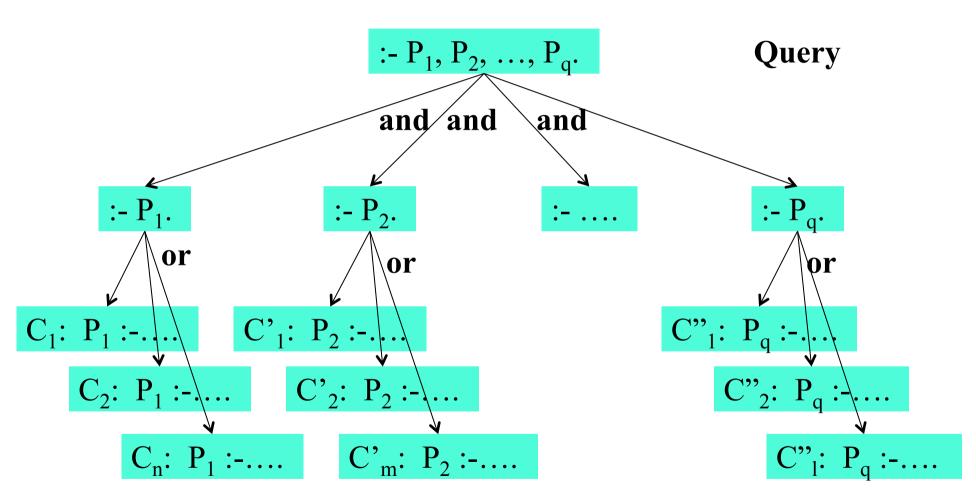
# Example addition: derivation tree

```
:- addition(s(s(0)), s(s(s(0))), Z)
                                                      C2
                                                     C2
:- addition(s(0), s(s(s(0))), Z1)
:- addition(0, s(s(s(0))), Z2)
        C1: addition(0, X, X).
```



C2: addition(s(X), Y, s(Z)) :- addition(X, Y, Z).

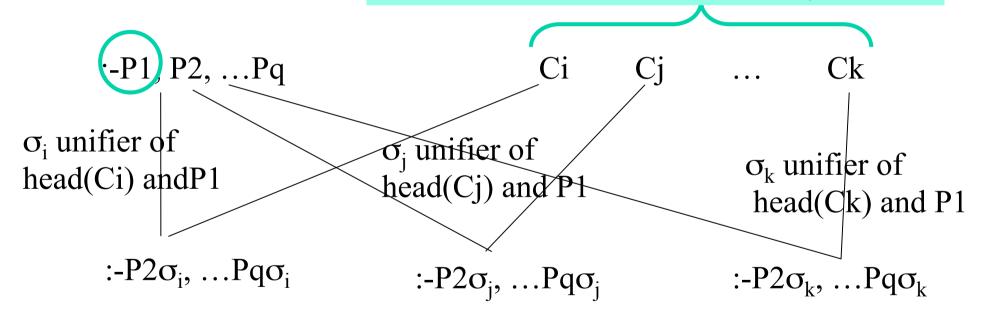
## Procedural interpretation: and/or tree





# Procedural interpretation: derivation tree

Clauses of which head literal unify with P1





## Data structures

- Terms:
  - Variables
  - Function with arguments: f(a, g(h, I), K)
- Atoms:
  - Character strings (beginning with a minuscule)
  - Numbers
- Lists:
  - Empty lists, list sequences
- Strings
- Numbers



### List structure

- Defined by the *constructor*, cons and by the *empty list*, nil
  - Form: cons(<head>, <queue>)
  - <head> is any literal
  - <queue> is a list

#### Examples:

```
The list (a b c) can be represented by:cons(a, cons(b, cons(c, nil)))
```

- The tree (+ (-b c) (\*d e)) can be represented by:



# List structure (2)

- Simplification:
  - The list (a b c) is written [a, b, c], which means cons(a, cons(b, cons(c, nil)))
  - In the same way, (+ ( b c) (\* d e)) is written
    [+, [-, b, c], [\*, d, e]]
- List constructor: "

Example: the list (a, b, c) is written:

```
- [a, b, c]
- [a | [b, c]]
- [a | [b | [c |[]]]]
- [a, b | [c]]
```



# Program example test if an element belong to a list

• Program « appartient » with terms:

• Program « appartient » with PROLOG representation :

```
appartient0(A, [A|B]).
appartient0(A, [B|C]) :- appartient0(A, C).
```



### **Execution**

```
C1: appartient(X, [X|L]).
 C2: appartient(X, [T|L]) :- appartient(X, L).
:- appartient(3, [1, 2, 3, 4])
                               \sigma_1 = \{x1/3, y1/1, L1/[2, 3, 4]\}
:- appartient(3, [2, 3, 4])
                               \sigma_2 = \{x2/3, y2/2, L2/[3, 4]\}
                                                     C2
:- appartient(3, [3, 4])
                               \sigma_3 = \{x3/3, L3/[4]\}
```

# Other examples with lists

#### **Concatenation of two lists:**

```
concat([], M, M).
concat([A|L], M, [A|N]) :- concat(L, M, N).
```

#### List inversion:



## Execution

```
C1: concat([], M, M).
 C2: concat([A|L], M, [A|N]) := concat(L, M, N).
:- concat([a, b], [c, d, e], R) ____C2
                               \sigma_1 = \{A1/a, L1/[b], M1/[c, d, e],
                                   R/[A1|N1]}
:- concat([b], [c, d, e], N1)
                                \sigma_2 = \{A2/b, L2/[], M2/[c, d, e],
                                N1/[A2|N2]
:- concat([], [c, d, e], N2)
                                     \sigma_3 = \{N2=M3=[c, d, e]\}
```

R = [A1|N1] = [a|[A2|N2]] = [a|[b|[c,d,e]]] = [a,b,c,d,e]