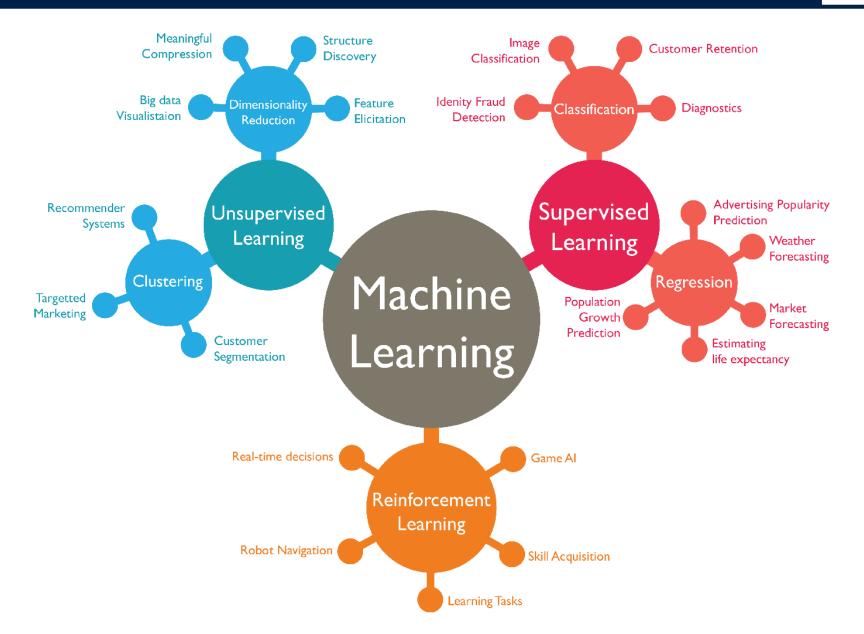
# Machine Learning +

# Programme Grant Update Science Talk

# **Machine Learning Overview**





# **Supervised Machine Learning**



### **General Idea:**

- Given a dataset with known labels ...
- "Train" a machine learning model using the dataset ...
- Then used the trained model to make predictions for new data which do not have labels

# **Supervised Machine Learning**



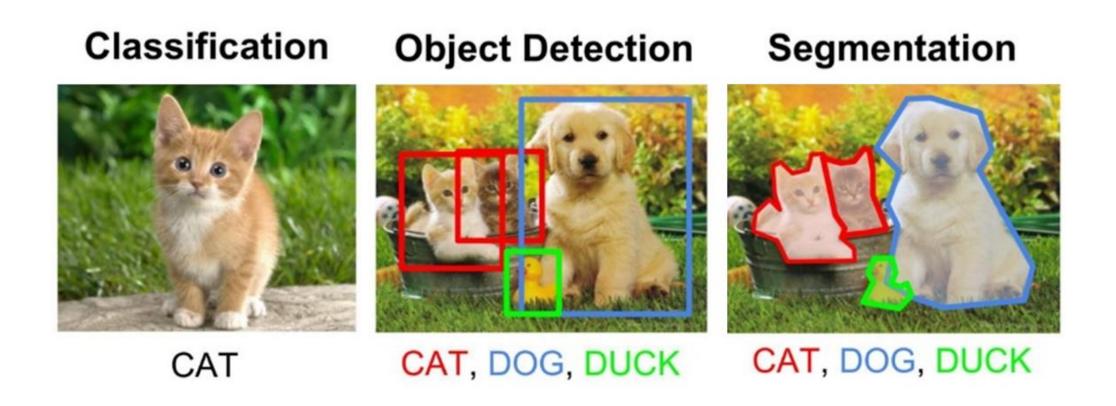
### **Methods:**

- Regression
- Random Forests, Support Vector Machines, K-Nearest Neighbor
- Deep Learning (Neural Networks)

# Types of Supervised Learning Tasks



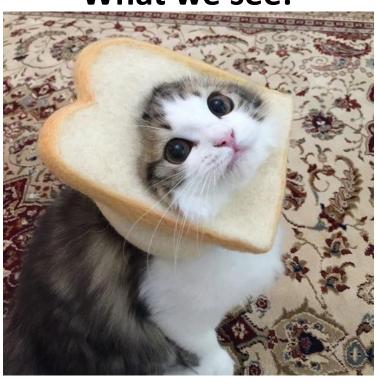
Image related tasks are the most common problems for machine learning



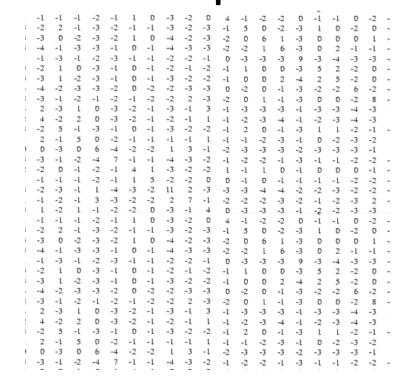
# Why These Tasks are Difficult?



### What we see:



# What the computer "sees":

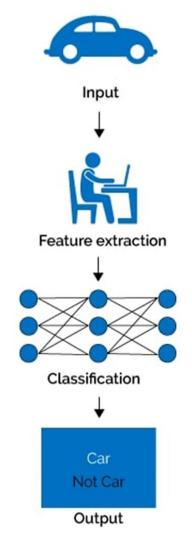


- It is difficult to come up with a set of "strict rules" to define image content
- Such tasks require the use of more sophisticated learning algorithms

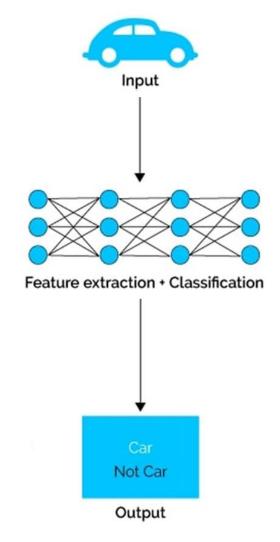
# Machine Learning vs Deep Learning



# **Machine Learning**



# **Deep Learning**



# **Neural Network Types**



# **Simple Neural Networks:**

Used on 1-Dimensional Data

### **Convolutional Neural Networks:**

Used on 2D or 3D Data (Images, Volumes, Videos)

### **Recurrent Neural Networks:**

Used on Sequential Data (Text, Time-Series)

# **Neural Network Types**



# **Simple Neural Networks:**

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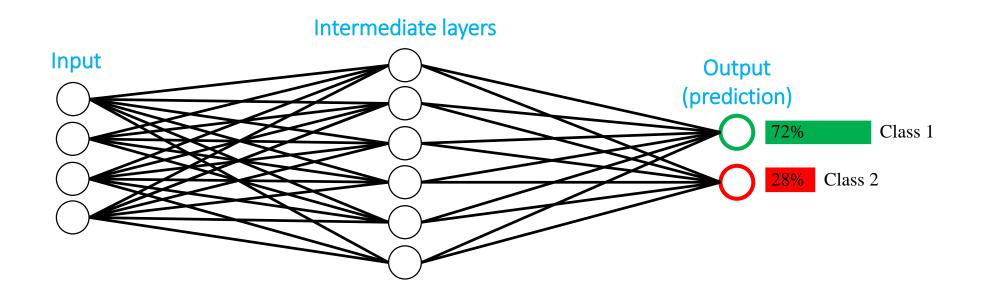
Used on 2D or 3D Data (Images, Volumes, Videos)

### **Recurrent Neural Networks:**

Used on Sequential Data (Text, Time-Series)

# **Introducing Neural Networks**

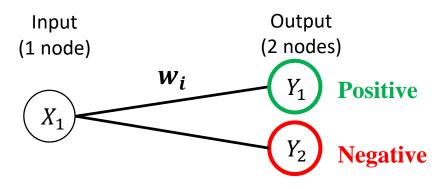




- Given some input data,
- **Transform** the data through **intermediate** layers (number can be  $N \ge 0$  layers) (we can also have as many nodes as we want for the intermediate layers),
- So the **output** becomes the probability of being in each class

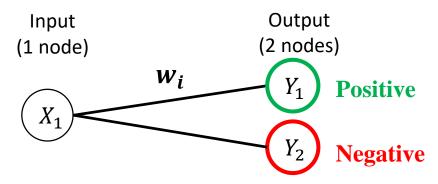


### Starting with a (very) simple neural network:





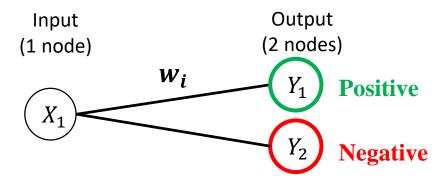
Starting with a (very) simple neural network:



**TASK:** given a single number at the input  $(X_1)$ , predict if its **positive** or **negative** (at the output, Y).



Starting with a (very) simple neural network:



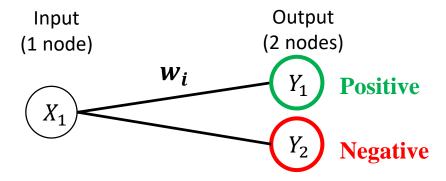
**TASK:** given a single number at the input  $(X_1)$ , predict if its **positive** or **negative** (at the output, Y).

### *Ideally:*

If 
$$x \ge 0$$
, we would want  $[Y_1 Y_2] = [1 0]$  (or any  $Y_1 > Y_2$ )
If  $x < 0$ , we would want  $[Y_1 Y_2] = [0 1]$  (or any  $Y_1 < Y_2$ )



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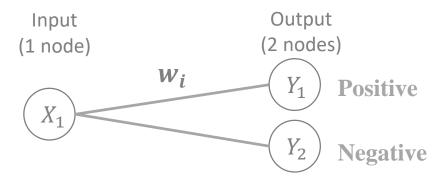
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To transform the input (1 node) to the output (2 nodes), we can perform a matrix multiplication:

$$[X_1][w_1 \quad w_2] = [Y_1 \quad Y_2]$$



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How do we choose which w's get our desired Y's?



Equation from last slide:

$$[X_1][W_1 \quad W_2] = [Y_1 \quad Y_2]$$

- Set up an optimization problem to solve the values of  $\mathbf{w}$ 's.



### Equation from last slide:

$$[X_1][w_1 \quad w_2] = [Y_1 \quad Y_2]$$

- Set up an optimization problem to solve the values of  $\mathbf{w}$ 's.
- Train the neural network with lots of **X**'s and **Y**'s so it can incrementally update **w**'s with gradient descent each iteration.



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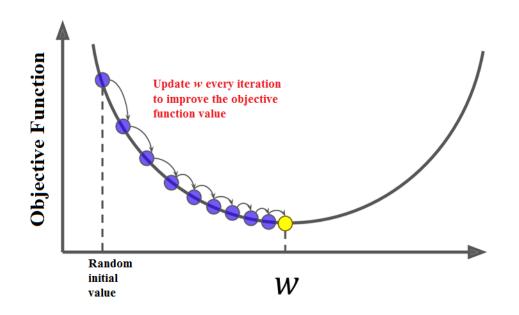
### Sample Training Set:



### Equation from last slide:

$$[X_1][w_1 \quad w_2] = [Y_1 \quad Y_2]$$

- Set up an optimization problem to solve the values of w's.
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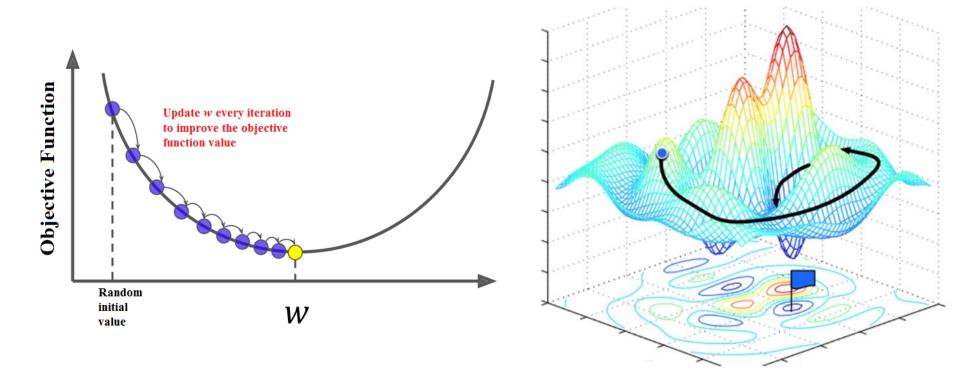




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This simple problem has many solutions for w, e.g.  $[w_1 \ w_2] = [0.6 \ 0.4]$  (or any  $w_1 > w_2$ ).



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```
If we input X = 1 and X = -1:

[1][0.6 	 0.4] = [0.6 	 0.4] 	 (Y_1 > Y_2, higher value for positive)

[-1][0.6 	 0.4] = [-0.6 	 -0.4] 	 (Y_1 < Y_2, higher value for negative)
```



Equation from last slide:

$$[X_1][w_1 \quad w_2] = [Y_1 \quad Y_2]$$

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If we input 
$$X = 1$$
 and  $X = -1$ :
$$[1][0.6 \quad 0.4] = [0.6 \quad 0.4]$$
normalize: 
$$\left[\frac{e^{0.6}}{e^{0.6} + e^{0.4}} \quad \frac{e^{0.4}}{e^{0.6} + e^{0.4}}\right] = [0.550 \quad 0.450]$$

$$[-1][0.6 \quad 0.4] = [-0.6 \quad -0.4]$$
normalize: 
$$\left[\frac{e^{-0.6}}{e^{-0.6} + e^{-0.4}} \quad \frac{e^{-0.4}}{e^{-0.6} + e^{-0.4}}\right] = [0.450 \quad 0.550]$$

# **Question?**



For our neural network:

$$[X_1][w_1 \quad w_2] = [Y_1 \quad Y_2]$$

We have weights of:

$$[W_1 \quad W_2] = [0.6 \quad 0.4]$$

- What is our output if the input is  $X_1 = 0$ ?

# **Question?**



For our neural network:

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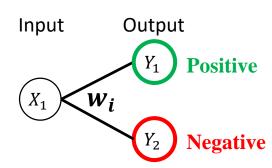
- What is our output if the input is  $X_1 = 0$ ?

$$[X_1][w_1 \quad w_2] = [0][0 \quad 0]$$

$$[\mathbf{Y_1} \quad \mathbf{Y_2}] = \begin{bmatrix} e^0 & e^0 \\ e^0 + e^0 & e^0 + e^0 \end{bmatrix} = [0.5 \quad 0.5]$$



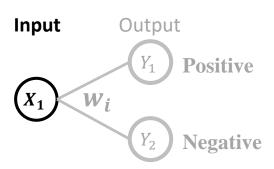
# import the packages we will be needing import tflearn





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# define the input layer (1 node)
X\_i = tflearn.input\_data(shape=[None, 1])

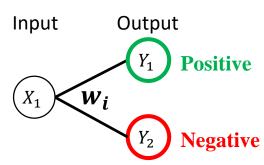




```
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# define the input layer (1 node)
X_i = tflearn.input_data(shape=[None, 1])
```

# define the output layer (2 nodes), softmax normalizes values between 0/1 Y\_j = tflearn.fully\_connected(X\_i, n\_units=2, activation='softmax')



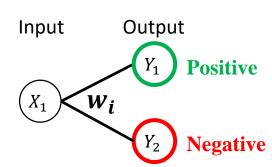


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We don't need to define  $w_i$ 





```
# import the packages we will be needing import tflearn

# define the input layer (1 node)

X_i = tflearn.input_data(shape=[None, 1])

Input Output

Y_1 Positive

X_1 Output

Y_2 Negative
```

# define the output layer (2 nodes), softmax normalizes values between 0/1 Y\_j = tflearn.fully\_connected(X\_i, n\_units=2, activation='softmax')

# set up optimization problem (sgd = stochastic gradient descent)
optimization\_problem = tflearn.regression(Y\_j, optimizer="sgd")

# initialize variables w\_i with random values to provide a starting point for optimization model = tflearn.DNN(optimization problem)



Input

Output

**Positive** 

Negative

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# train the model (assuming we have some data) for 100 iterations, update w every iteration model.fit(data, label, n epoch=100)



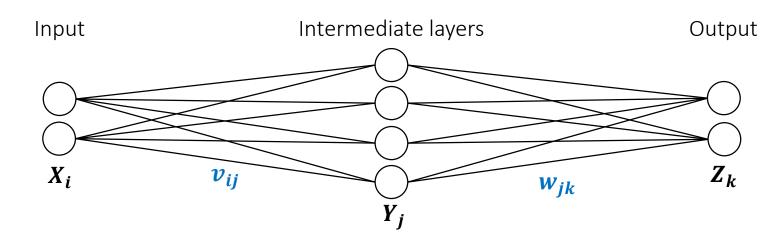
**Positive** 

Negative

```
Input
                                                                                      Output
# import the packages we will be needing
import tflearn
# define the input layer (1 node)
X i = tflearn.input data(shape=[None, 1])
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Y j = tflearn.fully connected(X i, n units=2, activation='softmax')
# set up optimization problem (sgd = stochastic gradient descent)
optimization problem = tflearn.regression(Y j, optimizer="sgd")
# initialize variables w i with random values to provide a starting point for optimization
model = tflearn.DNN(optimization problem)
# train the model (assuming we have some data) for 100 iterations, update w every iteration
model.fit(data, label, n epoch=100)
# make a prediction
print( model.predict([[1]]) )
                                 \# should get Y1 > Y2 (output = [Y1, Y2])
print( model.predict([[-1]]) )
                                 \# should get Y1 < Y2 (output = [Y1, Y2])
```

# **More Complicated Neural Network**





To map 
$$X_i \rightarrow Y_j$$
:

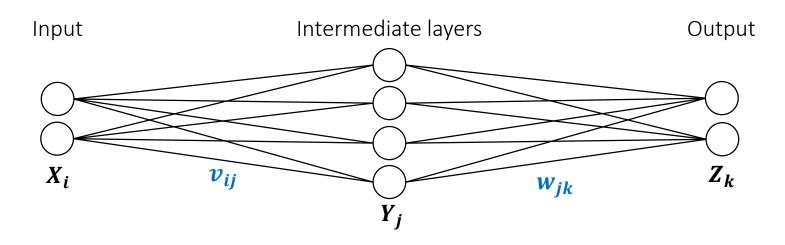
To map 
$$X_i \to Y_j$$
:
$$[X_1 \quad X_2] \begin{bmatrix} v_{11} & v_{12} & v_{13} & v_{14} \\ v_{21} & v_{22} & v_{23} & v_{24} \end{bmatrix} = [Y_1 \quad Y_2 \quad Y_3 \quad Y_4]$$

To map  $Y_j \to Z_k$ :

$$\begin{bmatrix} Y_1 & Y_2 & Y_3 & Y_4 \end{bmatrix} \begin{bmatrix} w_{11} & w_{12} \\ w_{21} & w_{22} \\ w_{31} & w_{32} \\ w_{41} & w_{42} \end{bmatrix} = \begin{bmatrix} Z_1 & Z_2 \end{bmatrix}$$

# **More Complicated Neural Network**





To map 
$$X_i \rightarrow Y_i$$
:

To map 
$$X_i \to Y_j$$
:  
 $[X_1 \quad X_2] \begin{bmatrix} v_{11} & v_{12} & v_{13} & v_{14} \\ v_{21} & v_{22} & v_{23} & v_{24} \end{bmatrix} = [Y_1 \quad Y_2 \quad Y_3 \quad Y_4]$ 

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Transformations are done with matrix multiplications

# Mid Session Break

# MRC – Hypertension Modelling



#### **Background:**

- Hypertension contributes to increased risk of stroke and heart attack
- Early detection of hypertension may aid the development of preventative measures
- We aim to identify trends and early indicators for hypertension to quantify progression in a population-wide dataset

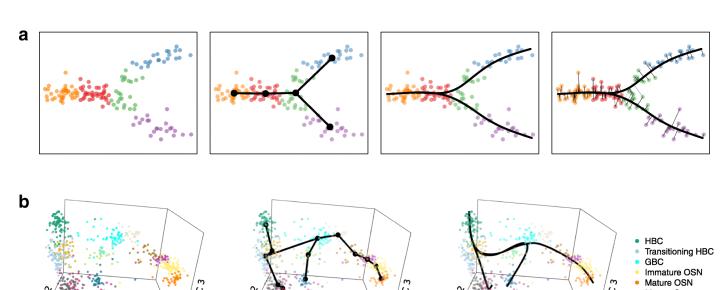
# **Method – Pseudo Temporal Modelling**



- In a population-level cohort (such as the UK Biobank), participants fit into different stages of disease progression and represent the entire healthy-to-disease scale
- Build a pseudo-temporal model using cross-sectional data to study the changes/progression of various biomarkers in patients from healthy to diseased
- Assign a score (0 to 1) to reflect the degree of disease, in our case the severity of hypertension
- "Trajectory inference" is the main method used

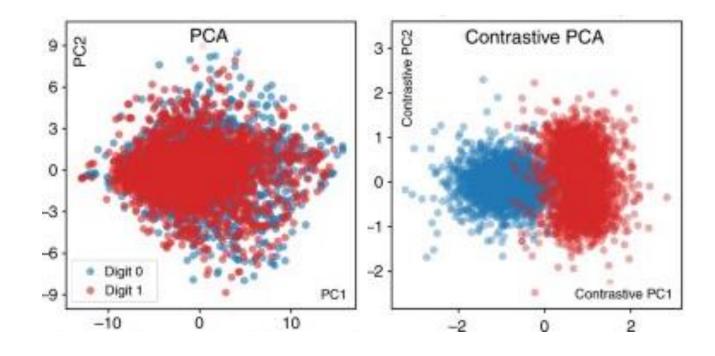
## **Trajectory Inference**

- Pseudo-temporal modelling to score patients based on their disease progression
- Fits patients on "trajectories" of disease progression
- Each trajectory may relate to changes in different combinations of biomarkers
- Trajectory inference 2 main steps:
  - Dimensionality reduction of features
  - Connect each patient in the reduced dimensional space to form a minimum spanning tree



## Contrastive Trajectory Inference (cTI)

- "Contrastive" trajectory inference method to improve separation of predefined groups
- Incorporate prior information (background/between/diseased) during the dimensionality reduction step of trajectory inference



#### Contrastive Trajectory Inference (cTI) – Dimensionality Reduction

Contrastive PCA (cPCA) for dimensionality reduction:

#### PCA:

- Standard PCA is done by first computing the covariance matrix (cov)
- Then perform eigen decomposition on the covariance matrix to transform features into a reduced representation

#### cPCA:

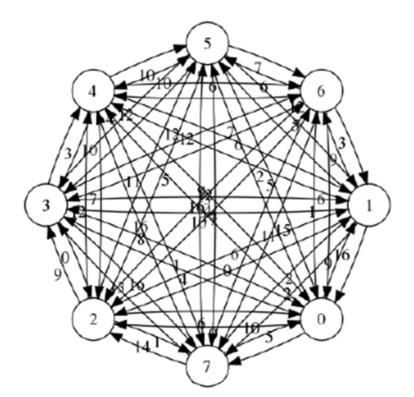
• cPCA is performed by computing a weighted sum between the covariance of the background  $(cov_b)$  and diseased  $(cov_d)$  group over a range of  $\alpha$ 's (~100 values from 10<sup>-2</sup> to 10<sup>2</sup>):

$$cov = cov_d - \alpha \times cov_b$$

- Perform eigen decomposition for each of these resulting covariance matrices
- Determine the optimal  $\alpha$  using K-means clustering to find the value which produces the best clustering tendency of the background and disease groups in the reduced space

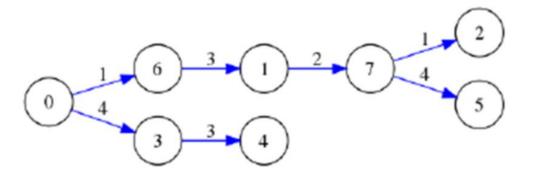
## Contrastive Trajectory Inference (cTI) – Trajectory Construction

- Consider each individual as a "node" in a complete graph in the contrastive principle component space (cPC)
- Edge of the graph are defined by the Euclidean distance between nodes in the cPC space
- Define "root node" as the node with the smallest overall distance in the cPC space from all nodes in in the population



## Contrastive Trajectory Inference (cTI) – Pseudo Time Score Calculation

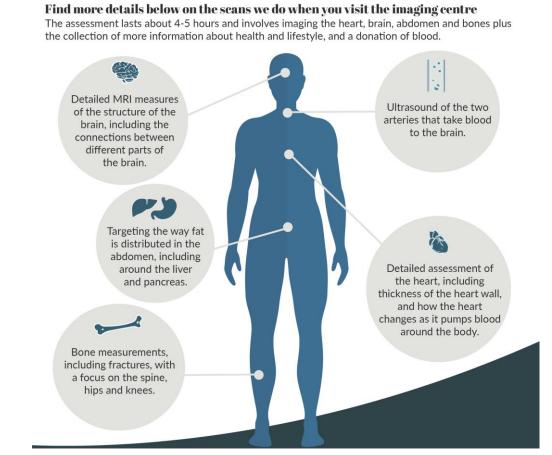
- Construct a minimum spanning tree which minimizes the overall distance between all nodes
- Find the shortest path between each node and the root node
- The disease (pseudo time) score is the normalized distance along the shortest path



## **Study Population – UK Biobank**



- UK Biobank has around 500,000 participants from the general population
- 100,000 of these participants are planned to undergo medical imaging (cardiac MRI + brain MRI + carotid ultrasound)
- UK Biobank contains ~15,000 features for each patient
- Imaging patient dataset contains ~30,000 participants with ~2,000 imaging features
- Aim:
  - Investigate the progression/change in features from the normotensive population to the hypertensive population



## **Data Pre-Processing**

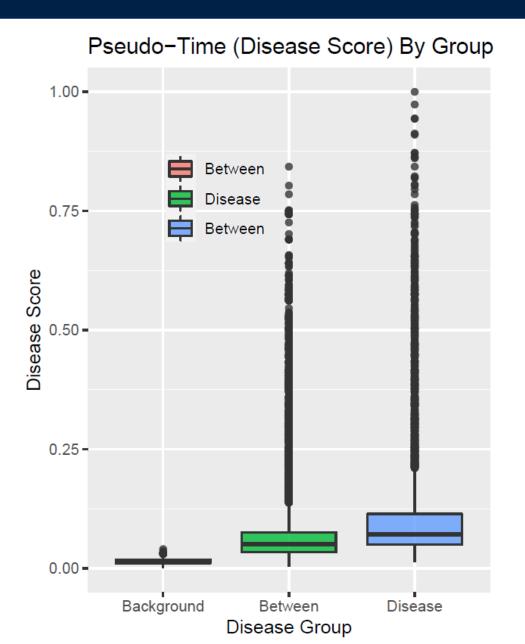
- Filter out patients without blood pressure readings
- Filter out variables which are not related to imaging/baseline measures
- Remove participants who have already experienced a heart attack, angina or stroke before the time of imaging
- Filter columns/rows with too many missing values
- Remove outliers
- Perform z-score normalization
- Adjust for age/sex

#### **Data Label Definition**

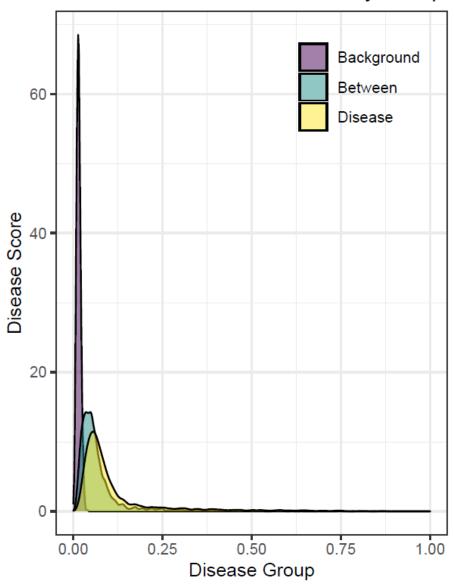
- Define blood pressure groups
  - Background: < 120/80 (both)
  - Disease: > 160/100 (either)
  - Between: Any patient otherwise
- Tightening "background" group definition
  - Remove patients already diagnosed with high blood pressure
  - Remove patients on blood pressure medication
  - Remove patients that had a high blood pressure reading at any stage (3 visits)
- The final data frame has 27,338 (participants) with 1,086 (features)
- Distribution of samples: background = 1,380, Between = 21,759, Disease = 4,199

## **Main Results – Pseudotime Score**



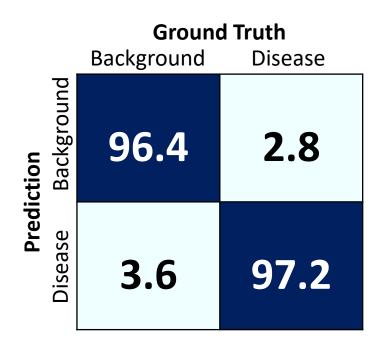


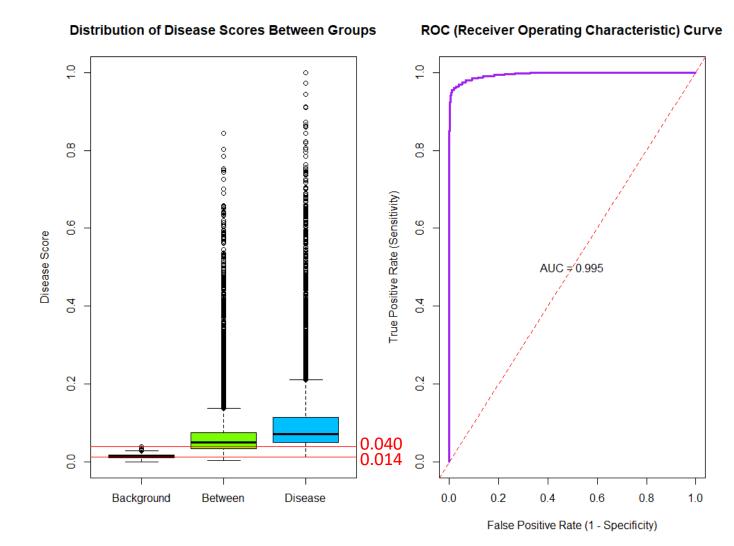
#### Distribution of Disease Score By Group



#### Evaluating the Accuracy of the cTI Model

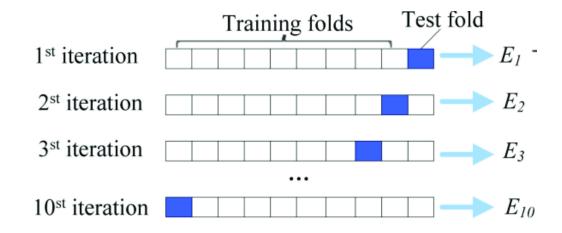
- AUC of 99.5% for distinguishing between "background" and "diseased"
- Sensitivity = 96.4%
- Specificity = 97.2%
- Optimal threshold = 0.027





#### Evaluating the Stability of the cTI Model

- Run the cTI model on 100% of the data to produce the set of baseline disease scores
- Split dataset into 90:10 splits
- Run cTI on 90% of the data to generate disease, ignore the 10% left out
- Compare the scores generated from the subset dataset with those obtained from the full dataset



- Repeat this for every 90:10 split (10-fold cross validation)
- Overall 10-fold validation resulted in an RMSE of 0.04 (sd = 0.004)

## **Predicting Scores for New Patients**



- Place new patient in the current trajectory map from the existing cTI model
  - cTI generates a reduced representation (cPC) for the existing data
  - Transform new patient into the existing cPC space of the current cTI model
  - "Infer" the disease score as the score of the patient in the existing model with the smallest distance from a new patient in the cPC space

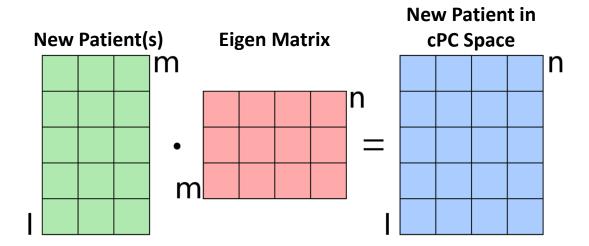
#### Advantages:

- Don't need to re-run cTI model
- Nearest neighbor is easy to quantify when there are only ~15 cPCs

#### Implementation of cPC Transformation

- Equation of transformation in/out of the cPC space:
  - $X_{cPC} = X * Eig(cov_d \alpha \times cov_b)$  (matrix multiplication with the most optimal  $\alpha$ )
  - The eigen matrix above is generated when building the cTI model, and can be stored as an intermediary value
  - New patients can be mapped into the cPC space with:

$$X_{cPC\ New} = X_{New} * Eig(cov_d - \alpha \times cov_b)$$

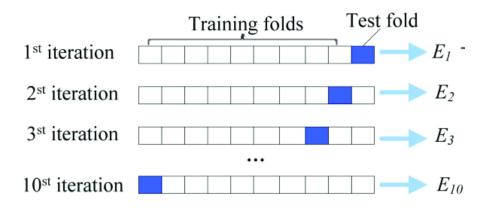


#### Implementation of cPC Transformation

- The transformed data for the new patient can then be compared with  $X_{cPC}$  to find the sample in the existing model with the closest Euclidean distance
- Disease score can then be inferred directly from the nearest existing sample

#### Experimental Setup for Evaluating the "Prediction" Method

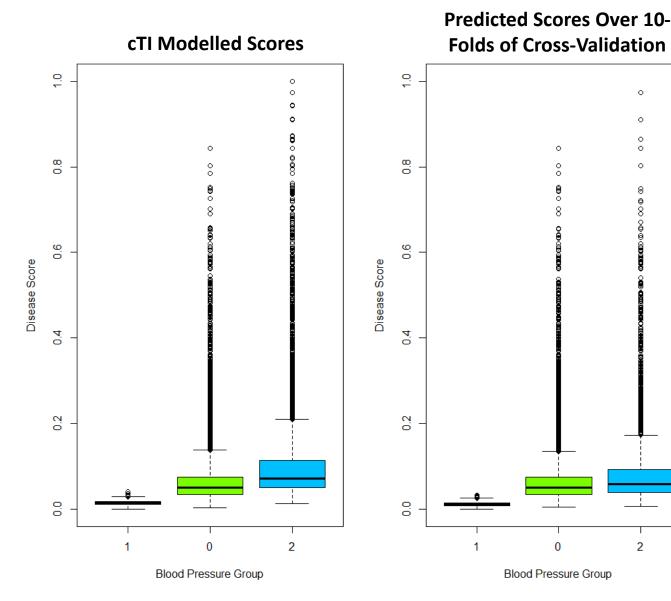
- Run the cTI model on 100% of the data to produce the set of baseline disease scores
- Split the data into 90% (training) and 10% (testing)
- Use the 90% to train the cTI model
- Use the proposed prediction approach to predict the 10% left out



- Compare the predicted scores of the 10% with scores of the same patient in the 100% run
- Repeat this for every 90:10 split (10-fold cross validation)

#### Experimental Results for "Prediction" Method

- 10-fold cross validation resulted in an RMSE of 0.043
- Errors for each group were:
  - Background = 0.018 RMSE
  - Between = **0.085 RMSE**
  - Disease = **0.094 RMSE**

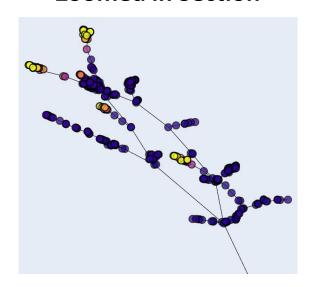


# **Trajectories – Preliminary Results**



- Compute the Laplacian of the matrix representation of the minimum spanning tree
- Perform eigen decomposition on the Laplacian, the coordinates are thus the first two eigen vectors

#### **Zoomed in Section**

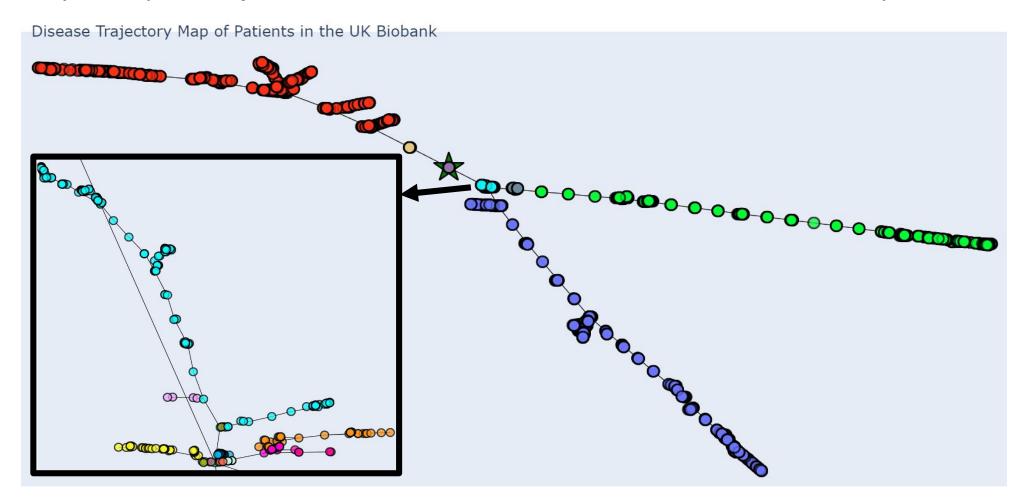




# **Trajectories – Preliminary Results**



- Color each unique trajectory
- Many "unique" trajectories close to the root node due to low overlap



## **Future Work**



### **Contrastive Trajectory Inference Model:**

Improve score distribution in the model output

#### **Understanding cTI Model:**

- Explore which variables contribute to elevated scores
- Explore the change in these variables from healthy to disease

#### **Trajectory Investigation:**

- Develop method to assign patients to a small number of "main" trajectories
- Explore which variables are more significant in different trajectories