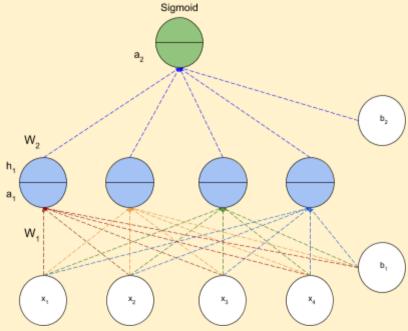
# One Fourth Labs

### **Loss function**

### **Loss function for Binary Classification**

What is the loss function that you can use for a binary classification problem

- 1. In normal cases, the number of neurons in the output layer would be equal to the number of classes
- 2. However a shortcut in the case of binary classification would be to use only one output neuron that uses a sigmoid function. Here is a diagrammatic representation of that configuration



- 3. Here,  $\hat{y} = P(y = 1)$
- 4. Therefore, we can obtain P(y = 0) = 1 P(y = 1)
- 5. Consider the following values for the variables

a. 
$$b = [0.5 \ 0.3]$$

b. 
$$y = 1$$

$$W_1 = \begin{bmatrix} 0.9 & 0.2 & 0.4 & 0.3 \\ -0.5 & 0.4 & 0.3 & 0.3 \\ 0.1 & 0.1 & -0.1 & 0.2 \\ -0.2 & 0.5 & 0.5 & / \end{bmatrix}$$

- c.  $W_2 = [0.5 \ 0.8 \ -0.6 \ 0.3]$
- d.  $x = [0.3 \ 0.5 \ -0.4 \ 0.3]$

# PadhAl: Deep Neural Networks

# One Fourth Labs

- 6. The output values are as follows
  - a.  $a_1 = W_1 * x + b_1 = [0.8 \ 0.52 \ 0.68 \ 0.67]$
  - b.  $h_1 = sigmoid(a_1) = [0.69 \ 0.63 \ 0.66 \ 0.67]$
  - c.  $a_2 = W_2 * h_1 + b_2 = 0.948$
  - d.  $\hat{y} = sigmoid(a_2) = 0.7207$
  - e. In this case y = 1 *True distribution* [0 1]
  - f. Predicted distribution  $\hat{y}$  [0.2793 0.7207]
  - g. Cross Entropy Loss:
  - i.  $L(\Theta) = (y)(-\log(\hat{y})) + (1-y)(-\log(\hat{y}))$
  - ii. In this case, since y = 1
  - iii.  $L(\Theta) = -1 * log(0.7207)$
  - iv.  $L(\Theta) = 0.327$
- 7. Consider another case where  $x = [-0.6 -0.6 \ 0.2 \ 0.3]$  and true class y = 1
- 8. The output values are as follows
  - a.  $a_1 = W_1 * x + b_1 = [0.01 \ 0.71 \ 0.42 \ 0.63]$
  - b.  $h_1 = sigmoid(a_1) = [0.50 \ 0.67 \ 0.60 \ 0.65]$
  - c.  $a_2 = W_2 * h_1 + b_2 = 0.921$
  - d.  $\hat{y} = sigmoid(a_2) = 0.7152$
  - e. In this case y = 0 *True distribution* [1 0]
  - f. Predicted distribution  $\hat{y}$  [0.2848 0.7152]
  - g. Cross Entropy Loss:
    - i.  $L(\Theta) = (y)(-\log(\hat{y})) + (1-y)(-\log(\hat{y}))$
  - ii. In this case, since y = 0
  - iii.  $L(\Theta) = -1 * log(1 0.7152)$
  - iv.  $L(\Theta) = 1.2560$
  - v. Here, even though the true value was 0, our neuron was outputting a very large value(0.7152) which was already indicative of a large loss value.