

McCulloch-Pitts Neuron

M medium.com/@manveetdn/notes-on-mp-neuron-padhai-onefourthlabs-course-a-first-course-on-deep-learning-8d2333170d1a

Disclaimer: This is notes on “MP Neuron” Lesson (PadhAI onefourthlabs course “A First Course on Deep Learning”)



Six Jars of the Machine Learning:

All the 6-jars put together what is the role of each jar and what we need to do in each stage to built a great Model.

Data: Find out a public source where tons and tons and tones of data sets available like Google, amazon.

Task: In the course we will learn and focus on Supervised learning Classification and Regression.

Learning Algorithm: We are going to focus on stochastic gradient descent, back propagation, Nesterov, RMS prop, momentum based gradient descent.

Evaluation: We are gonna focus on percision, accuracy, recall, top-k, f-score.

We also require:

Linear Algebra ,Probability, Calculus

These are 3 fundamentals areas of mathematics on which you built models.

1. Learning Algorithm that you do is are based on principles and theorems of Calculus
[Maxima, Taylor, gradient, Chain-rule]
2. We also require Probability we use are **likelyhood, cross-Entropy, KL-Divergence, didtributions.**

Model:

Some of the models we cover in the couse are $f(Wx+b)$

here W is matrix $R^{(m \times n)}$, x is vector of $R^{(1 \times n)}$.

1. We **use Linear Algebra** like **Vectors, matrix, dot-product, orthogonal vectors and orthogonal matrices ,etc.**

| We all require above all at one place to solve and built areal time Deep Learning model.

Why ML is very successful?
 Data, democratised, devices and
 Applying 6-jars for capstone project

(Available
 on various
 platforms online)
 Abundance

This is only thing
 we need to do
 different tasks
 to solve this data
 ← Left All Right →
 side all side all
 as available online

Models have been
 democratised

LSTM-f
 GRU
 Democratised

$$\min L(a, b, c)$$

The standard ~~frame~~
 works used in
 last decade are
 Pytorch and tensorflow
 we will be using pytorch
 mostly here. there
 are ready made.
 lots functions and learn
 algo available ready
 made in the framework
 for any problem

TENSORFLOW PYTORCH

If a test was
 conducted on a
 topic the test
 will be evaluated
 all the students are
 evaluated on same
 test in the same
 way we have many
 standard test sets
 are available
 IMAGENET for image
 classification
 PASCAL2 for object
 detection
 object detection
 Image data classification
 PASCAL2 IMAGENET

Data

Image of board
 x = hindi y = English
 word word
 गजरा Mumbai

Task

Binary classification
 has text? True/false
 character recognition
 object detection (obj
 detection)
 generation (Hindi → English)

Model

Sigmoid
 Deep NN
 CNN
 RNN
 Combination
 of above

Improving
 Loss Learning

Square Error Loss

$$\sum_{i=1}^n (y_i - \hat{f}(x_i))^2$$

 Cross Entropy Loss

$$-\sum_{i=1}^n \log \hat{f}(x_i)$$

Gradient descent,
 stochastic grad,
 and many
 more.....

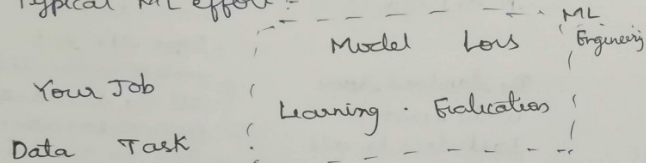
standard test
 sets
 are present
 Evaluation

Accuracy,
 Precision/Recall
 Top-K accuracy

All the 6-jars.

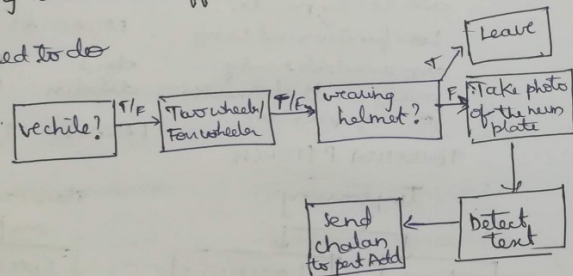
Distributing your work through 6 years

Typical ML effort:



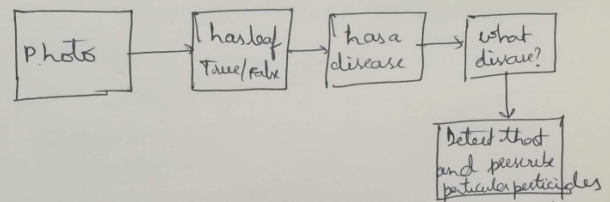
Detecting helmets in traffic

We need to do



Like this we start detecting the helmets not wearing two wheel driving persons by various steps with an android by putting the phone camera on recording the video

Detecting ~~po~~ infections and diseases of leaves in a farm:



Like this a photo can be take the photo of leaf then we will find wheather leaf is present or not again by binary classification we will find machine perticular infection and we will detect that a prescribe perticular pesticide also detecting the disease

There are two main tasks that can be done and models can be build

Real-time Examples.

McCulloch-Pitts Neuron:

Fundamental block of Deep Learning network is a Artificial Neuron.

Artificial Neuron

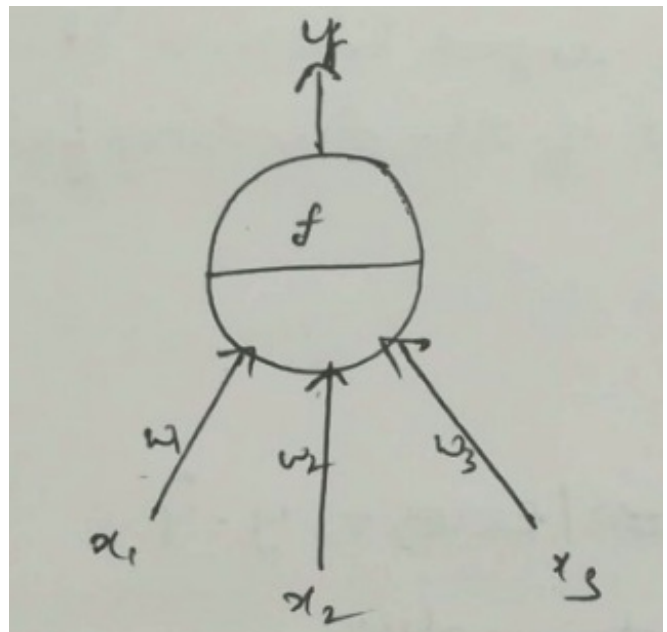
It takes input factors x_1, x_2, x_3 and it has added up weights w_1, w_2, w_3 in the above example it applies function and gives a output like **yes/no, true/false**.

Ex: Going to a Movie.

The various factors which acts as **inputs** for going the movie are

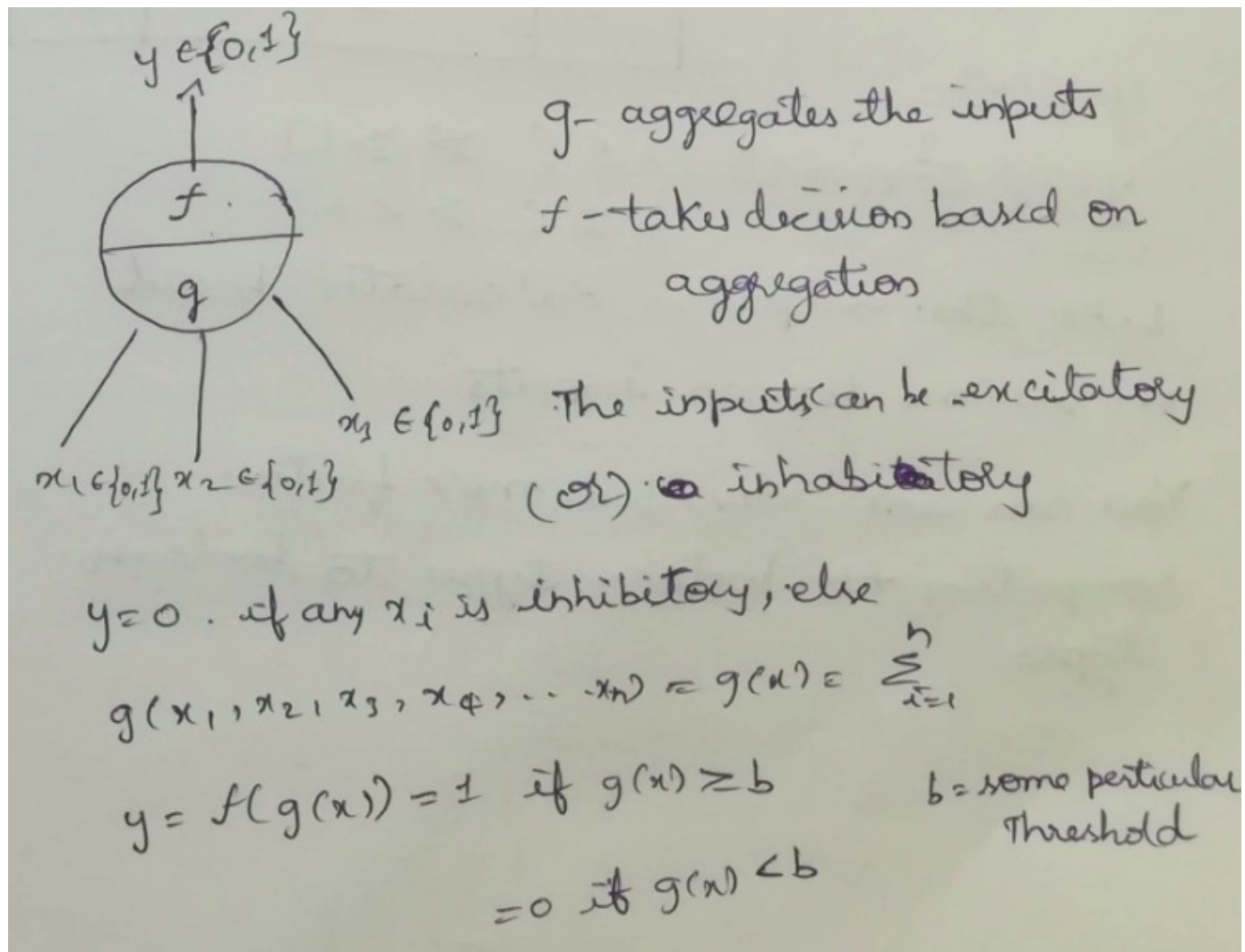
Genre ,Songs,Directors,Actor,Trailer.

The Inspiration of this Artificial Neuron is from Biological Neurons.



Artificial MP Neuron we proposed by **Watter-Pitts** (A Logician) and **Warren McCulloch** (A Neuro-Scientist).

MP Neuron Model:



MP Neuron Model

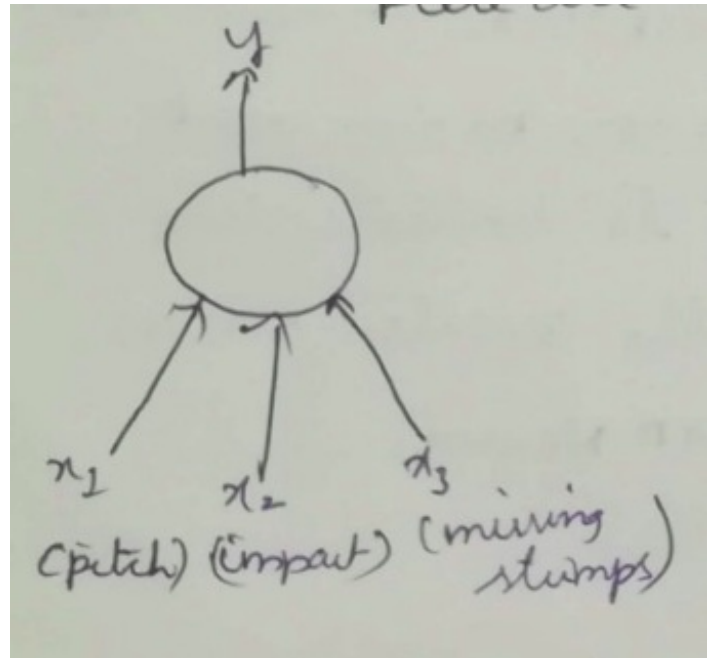
Data and Task:

Here, all inputs are boolean values

Data and Task

Here this is basic model MP-Neuron Model taking inputs and giving a output Y which is boolean in nature which is outputs **1 if True** and **0 if False**.

Lets Take the Example of the LBW out in a cricket match.



Factors for LBW out:-

Pitch	Impact	Missing stumps	Is it LBW?
1	0	0	0
0	1	1	0
1	1	1	1
0	1	0	0

Factors for an LBW out

We will use the function $y = f(x)$ and if the $y = 1$ its **true or LBW out** and if the final value $y = 0$ its **False and not Out**. Like that the outputs is calculated based on the inputs.

$$y = \left(\sum_{i=1}^3 x_i \geq b \right) \quad = 1 \quad (\sum \geq b)$$

$$= 0 \quad (\sum < b)$$

Calculating y for the about LBW-out.

The above is the image how we calculate the y based on the inputs given in the above table of the LBW-out.

You can even described more factors computing non boolean types to boolean types.

Loss Function:

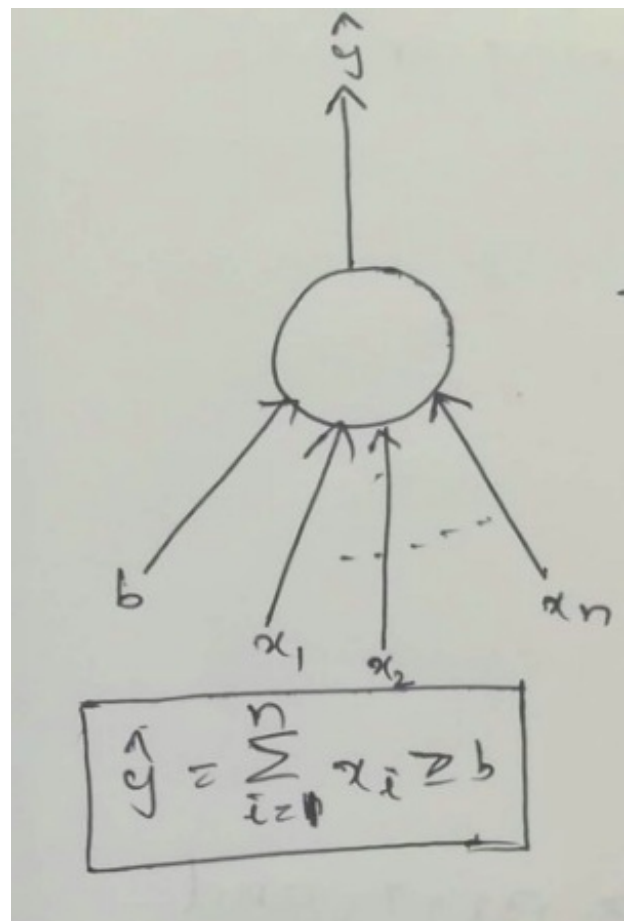
We will also pass threshold as the input because it is also one of the deciding factors.

$$\text{Loss/Error} = [y - (\hat{y})]$$

y = true value

(yhat) = predicted value

loss is calculated based on a particular formula, involving the true and the predicted values, its actually the summation of the all the difference for each and every prediction. Like that we will calculate the loss value.



$$\text{loss} = \sum_{i=1}^n y_i - \hat{y}_i \quad \text{all loss for all predictions}$$

(Firstly proposed) Loss formula.

let us assume for example if . for $i = 3$ loss = -1
 $i = 4$ loss = +1
 $i = 7$ loss = -1
 $i = 8$ loss = +1

Now summation of all losses = $-1 + 1 - 1 + 1$
 $= 0$

Taking an example applying the loss function.

We will get the zero as the final output which is a main drawback. There we need a modification in the formulae to predict the accurate loss and overcome the this main drawback.

Modified Loss Function:

And hence loss = $\sum_{i=1}^n (y_i - \hat{y}_i)^2$ To avoid the drawback

Modified Loss Function.

We will modify the loss function, based by squaring the difference and summing up all the square of differences.

This the formula which overcomes the drawback and suffices the need.

Learning Algorithm:

Learning Algorithm

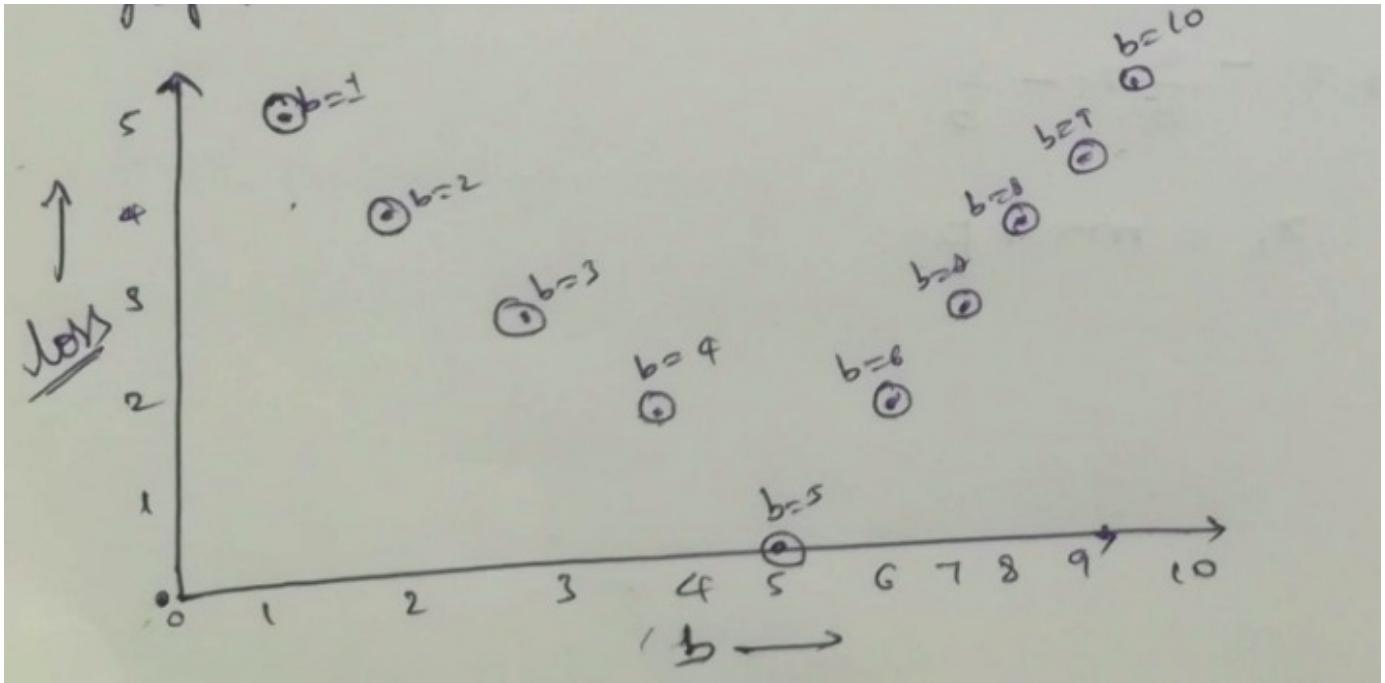
Now we have the output calculating function to predict the output, loss function and we need the b value that's the bias how will we calculate that.

According to a method we take b weight from 1 to 10 and taking each value at a time. we will plot a graph between b and loss and let the graph be as below.

$$\hat{y} = \sum_{i=1}^n x_i \geq b$$

$$\text{loss} = \sum_i (y_i - \hat{y}_i)^2$$

$$b = ?$$



Graph between loss and b (bias).

The output graph is graph as plotted above then **5 is the value of 'b' because the loss is zero** at that case like this we will find the b value in the learning algorithm part.

Evaluation:

Accuracy is calculated by the particular formula called the **Accuracy-Formulae**. The ratio of the Number of correction predictions to the total Number of predictions.

$$\text{Accuracy} = \frac{\text{Number of correct predictions}}{\text{Total Number of predictions}}$$

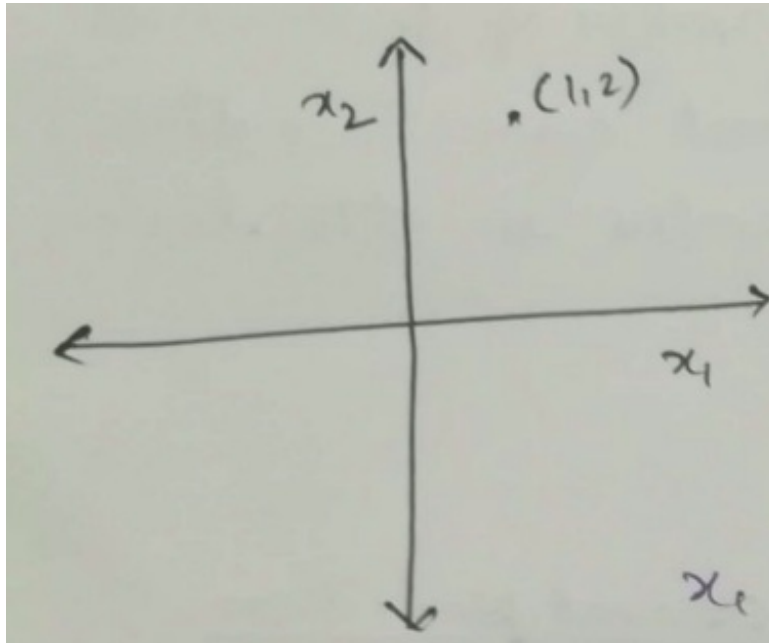
if they are total 4 predictions and only 3 are correct predictions in that

$$\text{Accuracy} = \frac{3}{4} \times 100 = 75\%$$

Evaluation Phase.

| Like that we will evaluate the model based on the accuracy value.

Geometric Interpretation:



Here, **y is the output** that's why we will not plot between y and x we will plot the graph always between **x_1 and x_2 which is input data.**

for example take the equation

$$x_2 = mx_1 + c$$

$$mx_1 - x_2 + c = 0$$

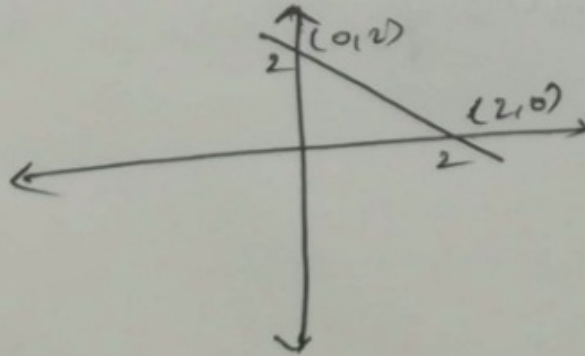
let assign some values for m & c

$$x_1 + x_2 - 2 = 0$$

$$m = -1 \quad c = 2$$

be of the form

This line on the graph will



Plotting $m = -1$ and $c = 2$

$$x_2 = m \cdot x_1 + c$$

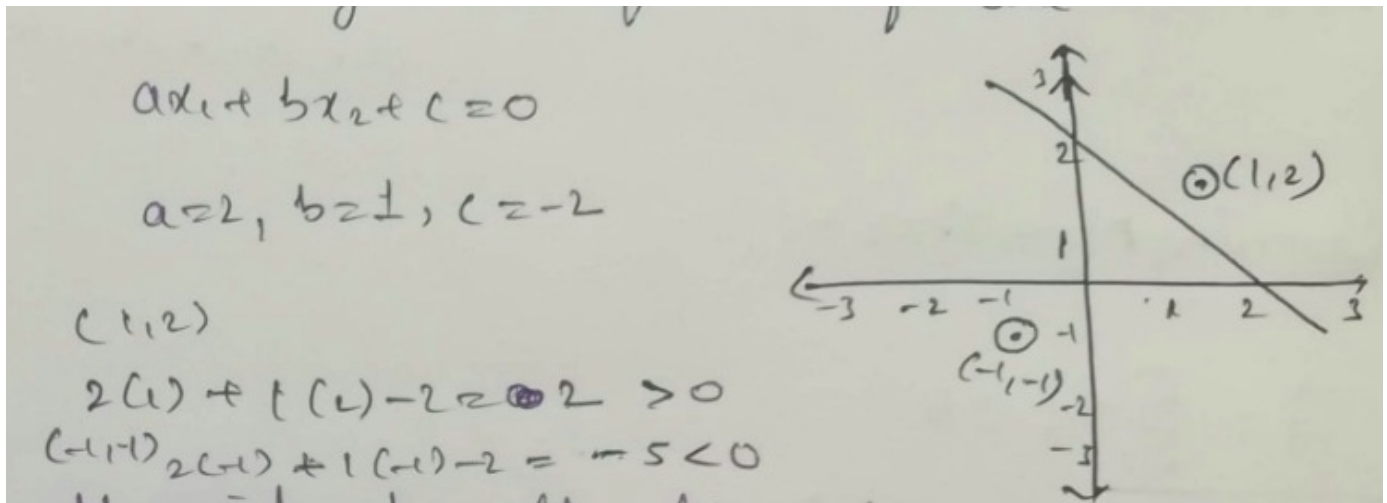
$$m \cdot x_1 - x_2 + c = 0$$

Let assign some values for m and c

$$x_1 + x_2 - 2 = 0, \quad m = -1 \quad \text{and} \quad c = 2$$

This on the graph will of the form as beside one.

Lets take the general equation of line



$a = 2, b = 1, c = -2$ graph.

all points above the line ~~is~~ satisfy the
 equation $ax_1 + bx_2 + c > 0$

all points below the line satisfy the
 equation $ax_1 + bx_2 + c < 0$

If point is lying on the line $ax_1 + bx_2 + c = 0$

$$x_2 = -\frac{a}{b}x_1 - \frac{c}{b}$$

$$x_2 = mx + p$$

$$a \cdot x_1 + b \cdot x_2 + c = 0$$

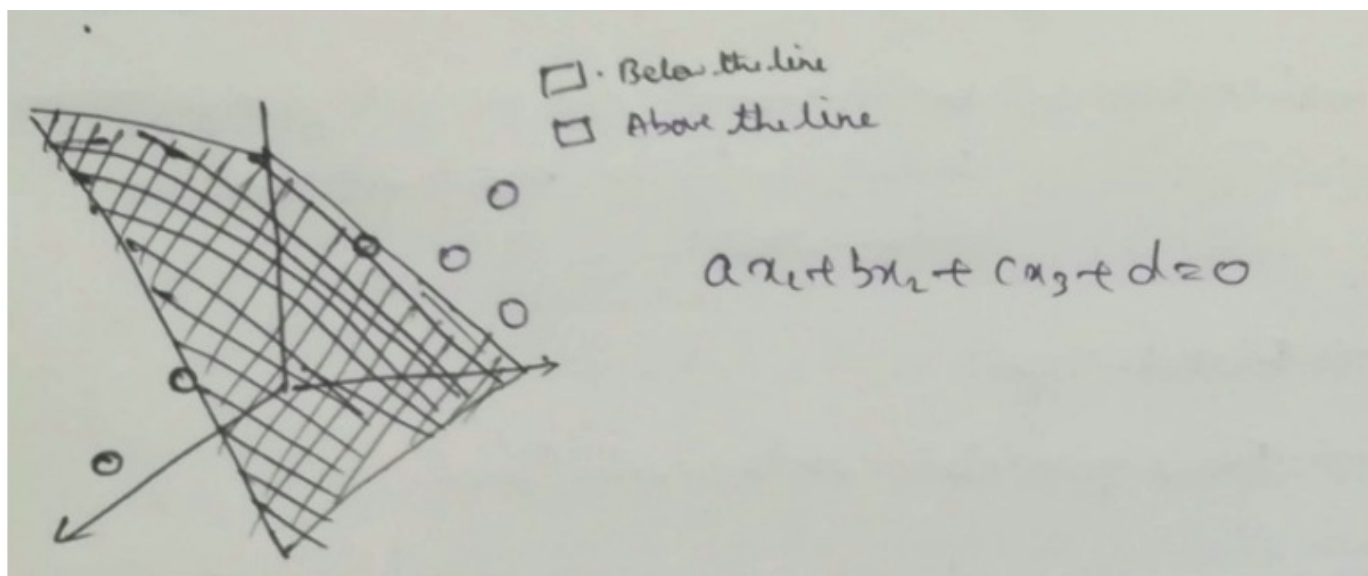
$$a = 2, b = 1, c = -2$$

All the points below the line satisfy the equation $a \cdot x_1 + b \cdot x_2 + c < 0$

If point is lying on the line $a \cdot x_1 + b \cdot x_2 + c = 0$

Like that the points are classification is done.

In 3-Dimension:



In 3-D its classified like that.

Geometrical Interpretation:

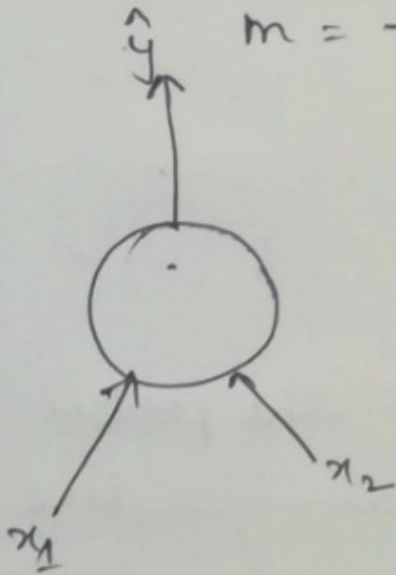
Line equation $a \cdot x_1 + b \cdot x_2 + d = 0$ (In 2-D)

line equation $\cdot ax_1 + bx_2 + d = 0$ (in 2D)

$$x_2 = -\frac{a}{b}x_1 - \frac{d}{b}$$

$$x_2 = mx_1 + c$$

$$m = -\frac{a}{b} \quad c = -\frac{d}{b}$$



$$\hat{y} = \left(\sum_{i=1}^n x_i \geq b \right)$$

In 2D we have x_1 & x_2 so
 $x_1 + x_2 - b \geq 0$

MP Neuron does the same thing it divides the whole points into two sets:

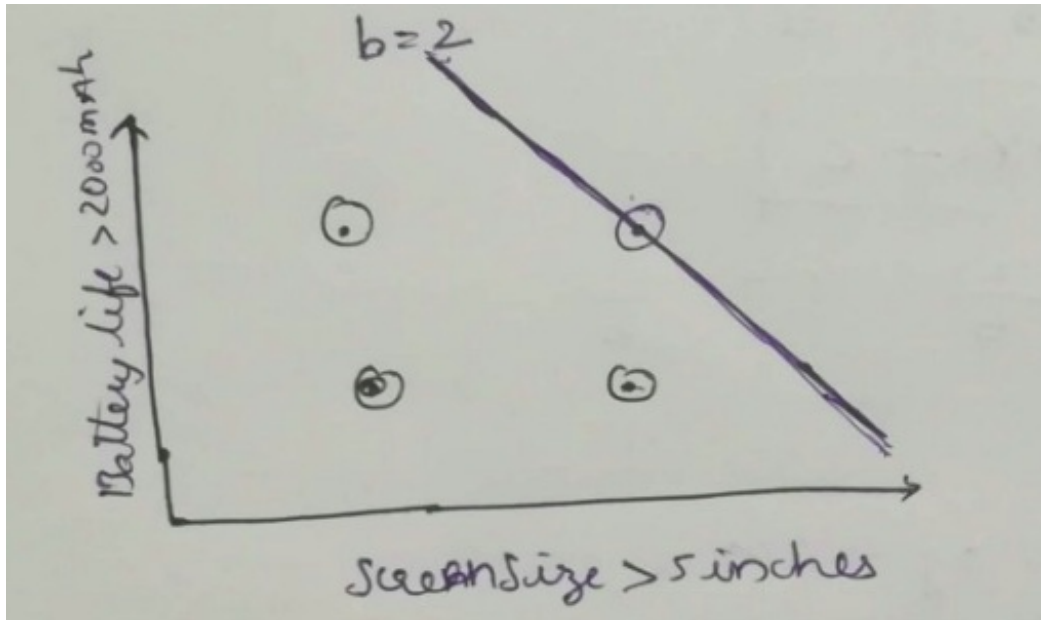
1. Set of points above the line ($x_1 + x_2 - b \geq 0$)
2. Set of points below the line ($x_1 + x_2 - b < 0$)

Examples of Cellphones:

Screen Size (> 5 in)	1	0	1	0	1	0	1	0
Battery (> 2000 mAh)	0	0	0	1	0	1	0	1
Like	1	0	1	0	1	1	0	1

Data-set of Cellphones Like/DisLike.

If we take the data set of the having mainly two columns of the **Screen-size** and **Battery life** and need to predict whether users may **Like [1]** or **DisLike[0]**.



Classification.

Here the MP-Neuron shows that all the positive likes will lie on the line on the above the line and another is all the points which are negative in likes will be negative and below the line.

Dis-advantages of the model:

1. **Linear**, we cannot fit any degree polynomial which be more efficient in other cases.
2. Fixed Slope
3. Few possible intercepts(b's)

This is all about the MP-Neuron Model including Advantages and the Dis -Advantages.

This is a small try ,uploading the notes . I believe in “**Sharing knowledge is that best way of developing skills**”.Comments will be appreciated. Even small edits can be suggested.

Each Applause will be a great encouragement.

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