PadhAl: The Convolution Operation

One Fourth Labs

Padding and Stride

What if we want the output to be the same size as the input?

1. Let us consider adding extra rows+columns of zeros so that we can access all the image pixels

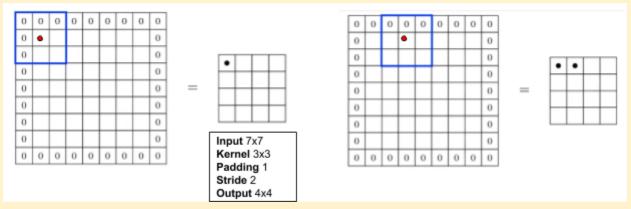
0	0	0	0	0	0	0	0	0								
0								0		•						
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0	0	0	0	0	0	0	0	0								
7x7 input, 3x3 kernel and padding of 1. The zeros denote the padding layer of 1.										Here, output remains 7x7 when a 3x3 kernel is used. Need extra padding for 5x5 kernel.						

- a. We can see that we must apply padding to preserve the output size
- b. The bigger the kernel size, the larger the padding required.
- 2. Thus, the formulae from the last section can be updates as follows

a.
$$W_O = W_I - F + 2P + 1$$

b.
$$H = H_I - F + 2P + 1$$

3. Another term that we use is called stride (S). It also affects the size of the output image.



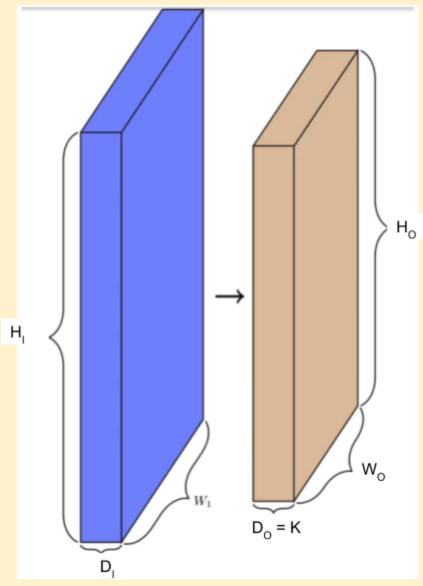
- a. Stride defines the interval at which the filter is applied
- b. Higher the stride, the smaller the size of the output

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- 4. We can see that the reduction in size can be given by the following equations

 - a. $W_O = \frac{W_I F + 2P}{S} + 1$ b. $H_O = \frac{H_I F + 2P}{S} + 1$
- 5. How do we compute the depth D of the output?
- 6. Consider the following image of a convolution operation



- 7. Each filter gives on 2D output
- 8. K filters will give K such 2D outputs
- 9. The depths of the output is the same as the number of filters
- 10. Thus, our final set of formulae are

a.
$$W_O = \frac{W_I - F + 2P}{S} + 1$$

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$$W_O = \frac{W_I - F + 2P}{S} + 1$$

b. $H_O = \frac{H_I - F + 2P}{S} + 1$

$$C. \quad D_O = K$$