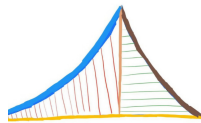


Digital Design Through Raspberry¹ pi Pico W



G. V. V. Sharma

ABOUT THIS BOOK

This book provides a simple introduction to digital design using the Raspberry pi Pico W framework, assembly and embedded C. It is suitable for students ranging from primary school to college. The content is sufficient for industry jobs. There is no copyright, so readers are free to print and share.

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1 INSTALLATION

1.1 Termux

1. On your android device, follow the instructions in

<https://github.com/gadepall/fwc-1>

to setup and install Debian on Termux.

1.2 Platformio

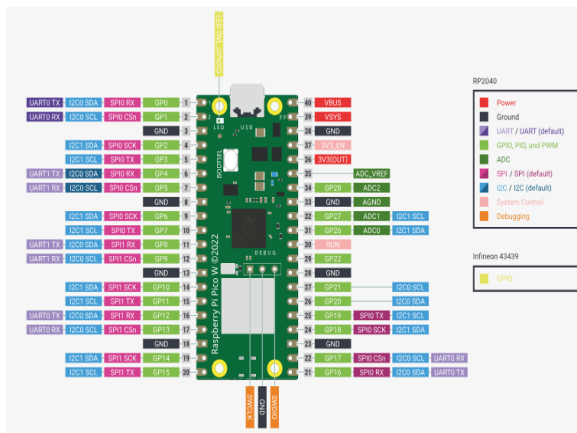
1. Follow the instructions in

<https://docs.platformio.org/en/stable/core/installation/methods/installer-script.html#super-quick-macos-linux>

to install platformio.

2. Execute the following on debian

```
cd ide/piosetup/codes
pio run
```



2 SEVEN SEGMENT DISPLAY

We show how to control a seven segment display.

2.1 Components

Component	Value	Quantity
Resistor	220 Ohm	1
pico W		1
Seven Segment Display		1
Decoder	7447	1
Flip Flop	7474	2
Jumper Wires		20

TABLE 2.1: Components

1. Breadboard:

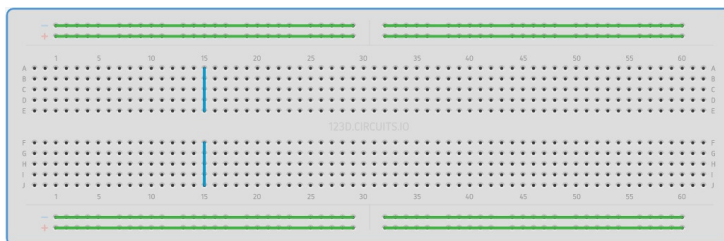


Fig. 2.1: Bread board connnctions

The breadboard can be divided into 5 segments. In each of the green segements, the pins are internally connected so as to have the same voltage. Similarly, in the central segments, the pins in each column are internally connected in the same fashion as the blue columns.

- Seven Segment Display: The seven segment display in Fig. 2.2 has eight pins, a, b, c, d, e, f, g and dot that take an active LOW input, i.e. the LED will glow only if the input is connected to ground. Each of these pins is connected to an LED segment. The dot pin is reserved for the \cdot LED.
- Raspberry pi pico W: The Raspberry pi pico W has some ground pins, all gpio pins can be used for both input as well as output. It also has 1 power pin that can generate 3.3V. In the following exercises, only the GND, 3.3V and gpio pins will be used.

2.2 Display Control through Hardware

2.2.1 Powering the Display:

- Plug the display to the breadboard in Fig. 2.1 and make the connections in Table 2.2. Henceforth, all 3.3V and GND connections will be made from the breadboard.

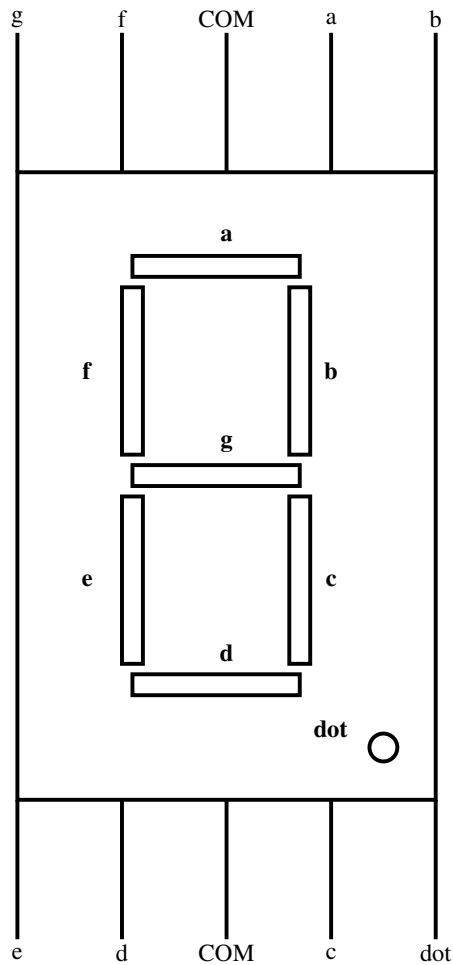


Fig. 2.2: Seven Segment pins

pico W	Breadboard
5V	Top Green
GND	Bottom Green

TABLE 2.2: Supply for Bread board

2. Make the connections in Table 2.3.

Breadboard		Display
5V	Resistor	COM
GND		DOT

TABLE 2.3: Connecting Seven segment display on Bread board

pico W	2	3	4	5	6	7	8
Display	a	b	c	d	e	f	g

TABLE 2.5

3. Connect the Raspberry pi pico W to the computer. The DOT led should glow.

2.2.2 *Controlling the Display*: Fig. 2.3 explains how to get decimal digits using the seven segment display. GND=0.

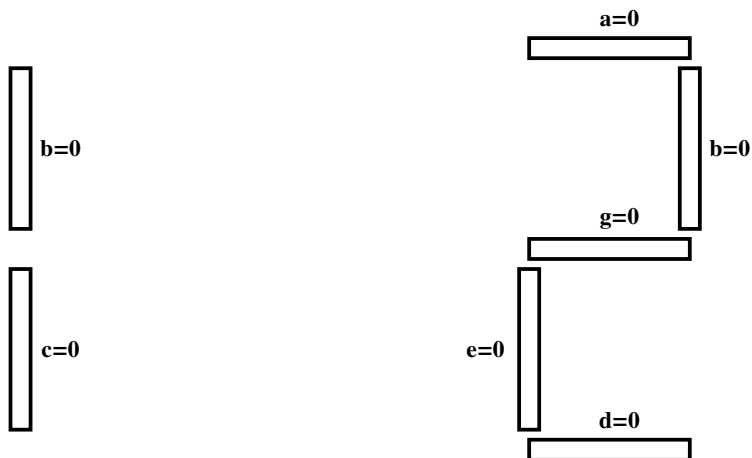


Fig. 2.3: Seven Segment connections

1. Generate the number 1 on the display by connecting only the pins *b* and *c* to GND (=0). This corresponds to the first row of 2.4. 1 means not connecting to GND.
2. Repeat the above exercise to generate the number 2 on the display.
3. Draw the numbers 0-9 as in Fig. 2.3 and complete Table 2.4

a	b	c	d	e	f	g	decimal
0	0	0	0	0	0	1	0

TABLE 2.4

2.3 Display Control through Software

1. Make connections according to Table 2.5
2. Download the following code using the platformio and execute

```
ide/sevenseg/codes/sevenseg/sevenseg.cpp
```

3. Now generate the numbers 0-9 by modifying the above program.

3 7447

Here we show how to use the 7447 BCD-Seven Segment Display decoder to learn Boolean logic.

3.1 Hardware

1. Make connections between the seven segment display in Fig. 2.2 and the 7447 IC in Fig. 3.1 as shown in Table 3.1

7447	\bar{a}	\bar{b}	\bar{c}	\bar{d}	\bar{e}	\bar{f}	\bar{g}
Display	a	b	c	d	e	f	g

TABLE 3.1

2. Make connections to the lower pins of the 7447 according to Table 3.2 and connect $V_{CC} = 3.3V$. You should see the number 0 displayed for 0000 and 1 for 0001.

D	C	B	A	Decimal
0	0	0	0	0
0	0	0	1	1

TABLE 3.2



Fig. 3.1: 7447 IC

3. Complete Table 3.2 by generating all numbers between 0-9.

3.2 Software

1. Now make the connections as per Table 3.3 and execute the following program

```
ide/7447/codes/gvv_ard_7447/gvv_ard_7447.cpp
```

7447	D	C	B	A
pico W	5	4	3	2

TABLE 3.3

Z	Y	X	W	D	C	B	A
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0

TABLE 3.4: Truth table for incrementing Decoder.

In the truth table in Table 3.4, W, X, Y, Z are the inputs and A, B, C, D are the outputs. This table represents the system that increments the numbers 0-8 by 1 and resets the number 9 to 0. Note that $D = 1$ for the inputs 0111 and 1000. Using *boolean* logic,

$$D = WXYZ' + W'X'Y'Z \quad (3.1)$$

Note that 0111 results in the expression $WXYZ'$ and 1000 yields $W'X'Y'Z$.

2. The code below realizes the Boolean logic for B, C and D in Table 3.4. Write the logic for A and verify.

```
ide/7447/codes/inc_dec/inc_dec.ino
```

3. Now make additional connections as shown in Table 3.5 and execute the following code. Comment.

```
ide/7447/codes/ip_inc_dec/ip_inc_dec.cpp
```

Solution: In this exercise, we are taking the number 5 as input to the pico W and displaying it on the seven segment display using the 7447 IC.

	Z	Y	X	W
Input	0	1	0	1
pico W	9	8	7	6

TABLE 3.5

4. Verify the above code for all inputs from 0-9.
 5. Now write a program where
- a) the binary inputs are given by connecting to 0 and 1 on the breadboard
 - b) incremented by 1 using Table 3.4 and
 - c) the incremented value is displayed on the seven segment display.

6. Write the truth table for the 7447 IC and obtain the corresponding boolean logic equations.
7. Implement the 7447 logic in the pico W. Verify that your pico W now behaves like the 7447 IC.

4 KARNAUGH MAP

4.1 Incrementing Decoder

We explain Karnaugh maps (K-map) by finding the logic functions for the incrementing decoder

1. The incrementing decoder takes the numbers $0, \dots, 9$ in binary as inputs and generates the consecutive number as output. The corresponding truth table is available in Table 3.4
2. Using Boolean logic, output A in Table 3.4 can be expressed in terms of the inputs W, X, Y, Z as

$$A = W'X'Y'Z' + W'XY'Z' + W'X'YZ' + W'XYZ' + W'X'Y'Z \quad (4.1)$$

3. K-Map for A : The expression in (4.1) can be minimized using the K-map in Fig. 4.1

		XW			
		00	01	11	10
ZY	00	1	0	0	1
	01	1	0	0	1
	11	0	0	0	0
	10	1	0	0	0

Fig. 4.1: K-map for A

In Fig. 4.1, the *implicants* in boxes 0,2,4,6 result in $W'Z'$. The implicants in boxes 0,8 result in $W'X'Y'$. Thus, after minimization using Fig. 4.1, (4.1) can be expressed as

$$A = W'Z' + W'X'Y' \quad (4.2)$$

Using the fact that

$$\begin{aligned} X + X' &= 1 \\ XX' &= 0, \end{aligned} \quad (4.3)$$

derive (4.2) from (4.1) algebraically

4. K-Map for B : From Table 3.4, using boolean logic,

$$B = WX'Y'Z' + W'XY'Z' + WX'YZ' + W'XYZ' \quad (4.4)$$

Show that (4.4) can be reduced to

$$B = WX'Z' + W'XZ' \quad (4.5)$$

using Fig 4.2

ZY \ XW	XW			
	00	01	11	10
00	0	1	0	1
01	0	1	0	1
11	0	0	0	0
10	0	0	0	0

Fig. 4.2: K-map for B

5. Derive (4.5) from (4.4) algebraically using (4.3)

6. K-Map for C : From Table 3.4, using boolean logic,

$$C = WXY'Z' + W'X'YZ' + WX'YZ' + W'XYZ' \quad (4.6)$$

Show that (4.6) can be reduced to

$$C = WXY'Z' + X'YZ' + W'YZ' \quad (4.7)$$

using Fig. 4.3.

ZY \ XW	XW			
	00	01	11	10
00	0	0	1	0
01	1	1	0	1
11	0	0	0	0
10	0	0	0	0

Fig. 4.3: K-map for C

7. Derive (4.7) from (4.6) algebraically using (4.3)

8. K-Map for D : From Table 3.4, using boolean logic,

$$D = WXYZ' + W'X'Y'Z \quad (4.8)$$

ZY \ XW				
	00	01	11	10
00	0	0	0	0
01	0	0	1	0
11	0	0	0	0
10	1	0	0	0

Fig. 4.4: K-map for D

9. Minimize (4.8) using Fig 4.4

10. Execute the code in

ide/7447/codes/inc_dec/inc_dec.cpp

and modify it using the K-Map equations for A, B, C and D . Execute and verify for each case.

11. Display Decoder: Table 4.1 is the truth table for the display decoder in Fig. 3.1. Use K-maps to obtain the minimized expressions for a, b, c, d, e, f, g in terms of A, B, C, D .

D	C	B	A	a	b	c	d	e	f	g	Decimal
0	0	0	0	0	0	0	0	0	0	1	0
0	0	0	1	1	0	0	1	1	1	1	1
0	0	1	0	0	0	1	0	0	1	0	2
0	0	1	1	0	0	0	0	1	1	0	3
0	1	0	0	1	0	0	1	1	0	0	4
0	1	0	1	0	1	0	0	1	0	0	5
0	1	1	0	0	1	0	0	0	0	0	6
0	1	1	1	0	0	0	1	1	1	1	7
1	0	0	0	0	0	0	0	0	0	0	8
1	0	0	1	0	0	0	1	1	0	0	9

TABLE 4.1: Truth table for display decoder.

4.2 Dont Care

We explain Karnaugh maps (K-map) using don't care conditions

1. Don't Care Conditions: 4 binary digits are used in the incrementing decoder in Table 4.1. However, only the numbers from 0-9 are used as input/output in the decoder and we *don't care* about the numbers from 10-15. This phenomenon can be addressed by revising the truth table in Table 4.1 to obtain Table 4.2.

Z	Y	X	W	D	C	B	A
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0
1	0	1	0	-	-	-	-
1	0	1	1	-	-	-	-
1	1	0	0	-	-	-	-
1	1	0	1	-	-	-	-
1	1	1	0	-	-	-	-
1	1	1	1	-	-	-	-

TABLE 4.2

2. The revised K-map for A is available in Fig 4.5. Show that

$$A = W' \quad (4.9)$$

		XW			
		00	01	11	10
ZY	00	1	0	0	1
	01	1	0	0	1
	11	-	-	-	-
	10	1	0	-	-

Fig. 4.5: K-map for A with don't cares

3. The revised K-map for B is available in Fig 4.6. Show that

$$B = WX'Z' + W'X \quad (4.10)$$

ZY \ XW				
	00	01	11	10
00	0	1	0	1
01	0	1	0	1
11	-	-	-	-
10	0	0	-	-

Fig. 4.6: K-map for B with don't cares

4. The revised K-map for C is available in Fig 4.7. Show that

$$C = X'Y + W'Y + WXY' \quad (4.11)$$

ZY \ XW				
	00	01	11	10
00	0	0	1	0
01	1	1	0	1
11	-	-	-	-
10	0	0	-	-

Fig. 4.7: K-map for C with don't cares

5. The revised K-map for D is available in Fig 4.8. Show that

$$D = W'Z + WXY \quad (4.12)$$

		XW			
		00	01	11	10
ZY	00	0	0	0	0
	01	0	0	1	0
	11	-	-	-	-
	10	1	0	-	-

Fig. 4.8: K-map for D with don't cares

6. Verify the incrementing decoder with don't care conditions using the pico W.
7. Display Decoder: In Table 4.1, use K-maps to obtain the minimized expressions for a, b, c, d, e, f, g in terms of A, B, C, D with don't care conditions. Verify using pico W.

5 7474

We show how to use the 7474 D-Flip Flop ICs in a sequential circuit to realize a decade counter.

1. Generate the **CLOCK** signal using the **blink** program in the pico W.
2. Connect the pico W, 7447 and the two 7474 ICs according to Table 5.1 and Fig. 5.2.
- The pin diagram for 7474 is available in Fig. 5.1

	INPUT				OUTPUT				CLOCK		3.3V			
	W	X	Y	Z	A	B	C	D						
pico W	D6	D7	D8	D9	D2	D3	D4	D5	D13					
7474	5	9			2	12			CLK1	CLK2	1	4	10	13
7474			5	9			2	12	CLK1	CLK2	1	4	10	13
7447					7	1	2	6			16			

TABLE 5.1

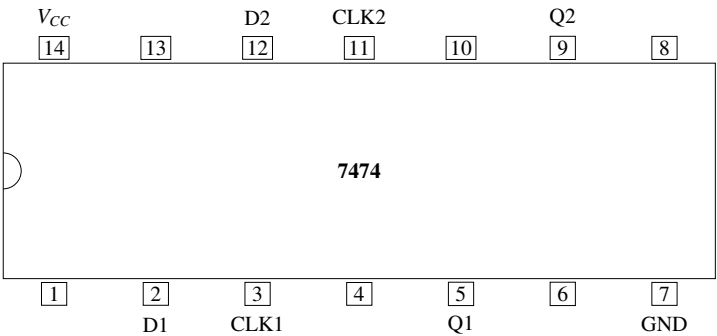


Fig. 5.1

3. Intelligently use the codes in

```
ide/7447/codes/inc_dec/inc_dec.ino
```

and

```
ide/7447/codes/inc_dec/ip_inc_dec.ino
```

to realize the decade counter in Fig. 5.2.

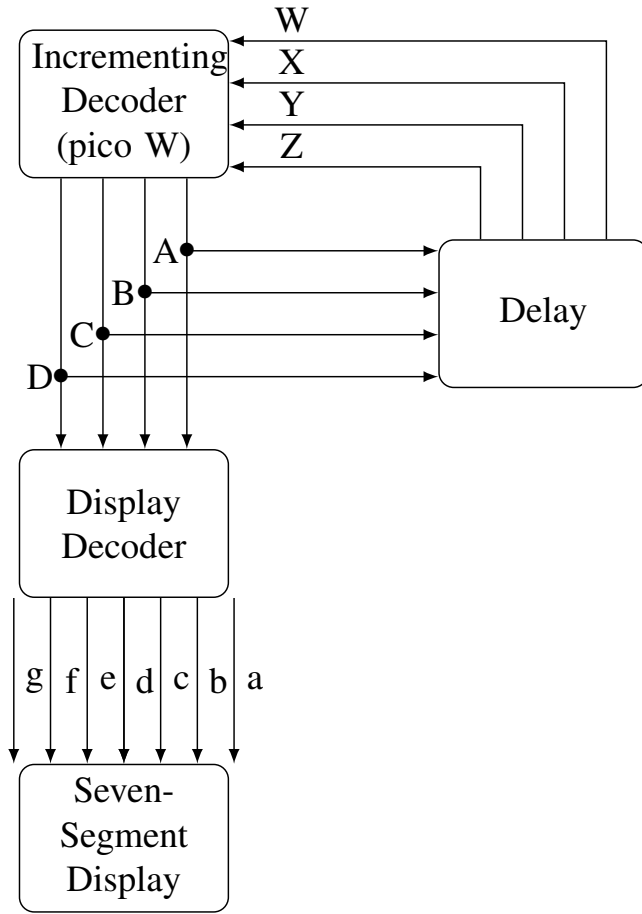


Fig. 5.2

6 FINITE STATE MACHINE

We explain a state machine by deconstructing the decade counter

The block diagram of a decade counter (repeatedly counts up from 0 to 9) is available in Fig. 5.2. The *incrementing* decoder and *display* decoder are part of *combinational* logic, while the *delay* is part of *sequential* logic.

1. Fig. 6.1 shows a *finite state machine* (FSM) diagram for the decade counter in Fig 5.2 s_0 is the state when the input to the incrementing decoder is 0. The *state transition table* for the FSM is Table 3.4, where the present state is denoted by the variables W, X, Y, Z and the next state by A, B, C, D .

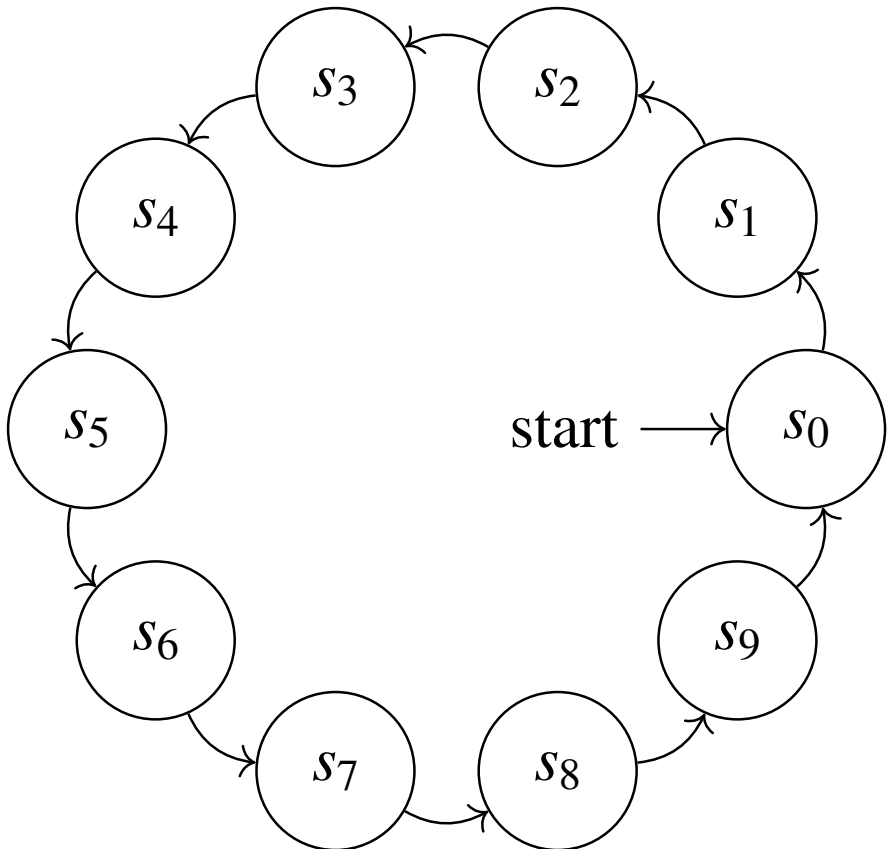


Fig. 6.1: FSM for the decade counter

2. The FSM implementation is available in Fig 6.2 The *flip-flops* hold the input for the time that is given by the *clock* This is nothing but the implementation of the *Delay* block in Fig 5.2

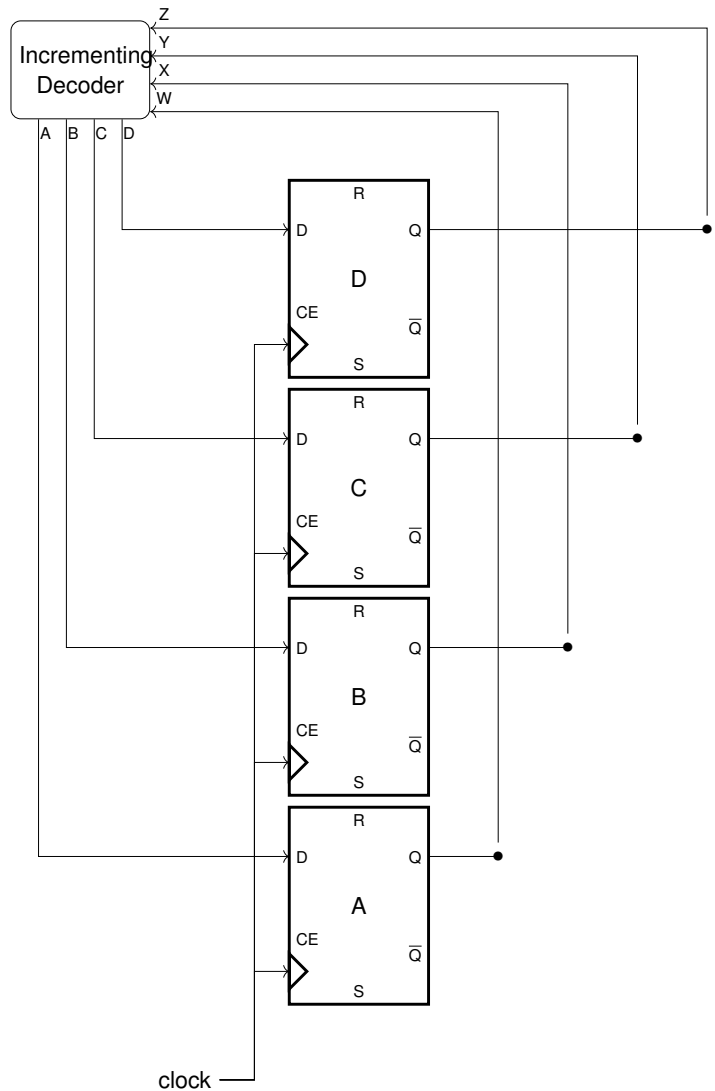


Fig. 6.2: Decade counter FSM implementation using D-Flip Flops

3. The hardware cost of the system is given by

$$\text{No of D Flip-Flops} = \lceil \log_2 (\text{No of States}) \rceil \quad (6.1)$$

For the FSM in Fig 6.1, the number of states is 9, hence the number of flip flops required = 4

4. Draw the state transition diagram for a decade down counter (counts from 9 to 0 repeatedly) using an FSM.
 5. Write the state transition table for the down counter.

6. Obtain the state transition equations with and without don't cares.
7. Verify your design using an pico W.