

DSC-VI : Practical-05

Method of Variation of Parameters

1 Solve $y'' - y = x$

Sol: The general solution comprises of two parts: $y = y_c + y_p$

We have:

```
--> de : 'diff( y , x , 2 ) - y = x ;    /* our d.e. */
      hp : lhs ( de ) = 0 $             /* homogeneous part */
      r : rhs ( de ) $                  /* `r` i.e. non-homogeneous part */
```

$$\frac{d^2}{dx^2}y - y = x$$

1.1 Calculating y_c

```
--> y_c : rhs ( ode2 ( hp , y , x ) ) ;
      y_1 : exp ( x ) $
      y_2 : exp ( - x ) $
```

$$\%k1\%e^x + \%k2\%e^{-x}$$

1.2 Calculating y_p

```
--> A : matrix (
      [ y_1 , y_2 ] ,
      [ diff ( y_1 , x ) , diff ( y_2 , x ) ]
      ) ;
```

$$\begin{pmatrix} \%e^x & \%e^{-x} \\ \%e^x & -\%e^{-x} \end{pmatrix}$$

```
--> W : determinant ( A ) ;
```

$$-2$$

We now find u_1 and u_2

```
--> u_1 : integrate ( - y_2 * r / W , x ) ;
      u_2 : integrate ( y_1 * r / W , x ) ;
```

$$\frac{(-x-1)\%e^{-x}}{2} - \frac{(x-1)\%e^x}{2}$$

Now, our y_p is:

```
--> y_p : ratsimp ( u_1 · y_1 + u_2 · y_2 ); /* this will return a simplified expression */
```

$$-x$$

1.3 General Solution

The general solution ($y=y_c+y_p$):

```
--> ' y = y_c + y_p ;
```

$$y = \%k1\%e^x + \%k2\%e^{-x} - x$$

Created with [wxMaxima](#).

The source of this Maxima session can be downloaded [here](#).