



In [4]:

```
In [5]: #Confirms main.py prints s1/s5 lines
MAIN = "/content/content/synth/main.py" #change only if your path is different

with open(MAIN, "r", errors="ignore") as f:
    txt = f.read()
assert "s1:" in txt and "s5:" in txt, "Please apply the s1/s5 patch to main.py"
print("Yes: main.py has s1/s5 in its progress print.")
```

Yes: main.py has s1/s5 in its progress print.

In [6]:

```
#paths
MAIN = "/content/content/synth/main.py" #keep consistent
LOGDIR = "/content/run_logs_full" #full-run logs here

import os, pathlib, shlex, subprocess
pathlib.Path(LOGDIR).mkdir(parents=True, exist_ok=True)

def run_and_log(tag, **kw):
    """
    Runs main.py with given kwargs and writes stdout to LOGDIR/{tag}.log
    """
    cmd = ["python", MAIN]
    for k, v in kw.items():
        cmd += [f"--{k}", str(v)]
    print("RUN:", " ".join(shlex.quote(c) for c in cmd))
    out = subprocess.run(cmd, text=True, capture_output=True)
    print(out.stdout)
    open(f"{LOGDIR}/{tag}.log", "w").write(out.stdout)
    if out.stderr.strip():
        print("STDERR:\n", out.stderr)
```

In [7]:

```
#Learning rates LR-finder and tests
LR_GD = "1e-3"
LR_ADAM = "1e-3"

#Long iteration counts
LONG_ITERS_GD = 800_000
LONG_ITERS_ADAM = 30_000

#Shared synthetic configuration
BASE_SYN = dict(
    method="DLNN",
    data="gaussian", #noiseless synthetic
    N=100, #problem size
    rank=5,
    reg_norm="ratio",
    init_scale="1e-3",
    sample_size=4000,
    log_interval=2000 #fewer log lines -> smaller files
)
```

```
In [8]: for depth in (2, 5):
        # GD (solid in plots)
        run_and_log(f"F1_gd_d{depth}_lam0",
                    **BASE_SYN, depth=depth, lam="0.0", optim="GD", lr=LR_GD, niters=L

        # Adam (dashed in plots)
        run_and_log(f"F1_adam_d{depth}_lam0",
                    **BASE_SYN, depth=depth, lam="0.0", optim="Adam", lr=LR_ADAM, niters=L
```

```
RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10
0 --rank 5 --reg_norm ratio --initscale 1e-3 --sample_size 4000 --log_interval
2000 --depth 2 --lam 0.0 --optim GD --lr 1e-3 --niters 800000
depth: 2, iteration: 0, test_RMSE: 1.1268175840377808, erank: 66.9690017700195
3, s1: 0.002483401680365205, s5: 0.0021783490665256977
depth: 2, iteration: 2000, test_RMSE: 1.1268175840377808, erank: 66.97414398193
36, s1: 0.0024833730421960354, s5: 0.0021786484867334366
depth: 2, iteration: 4000, test_RMSE: 1.1268175840377808, erank: 66.97360229492
188, s1: 0.002484648721292615, s5: 0.0021800678223371506
depth: 2, iteration: 6000, test_RMSE: 1.1268175840377808, erank: 66.96730804443
36, s1: 0.0024872703943401575, s5: 0.0021835591178387403
depth: 2, iteration: 8000, test_RMSE: 1.1268175840377808, erank: 66.95498657226
562, s1: 0.0024911893997341394, s5: 0.0021900746505707502
depth: 2, iteration: 10000, test_RMSE: 1.1268175840377808, erank: 66.9366607666
0156, s1: 0.002496513770893216, s5: 0.0021985953208059072
depth: 2, iteration: 12000, test_RMSE: 1.1268175840377808, erank: 66.9120254516
6016, s1: 0.00250330101698637, s5: 0.002207739744335413
depth: 2, iteration: 14000, test_RMSE: 1.1268175840377808, erank: 66.8808898925
7812, s1: 0.002511589555069804, s5: 0.002216300694271922
depth: 2, iteration: 16000, test_RMSE: 1.1268175840377808, erank: 66.8431777954
1016, s1: 0.002521514892578125, s5: 0.002224573167040944
depth: 2, iteration: 18000, test_RMSE: 1.1268175840377808, erank: 66.7985305786
1328, s1: 0.0025331659708172083, s5: 0.0022330337669700384
depth: 2, iteration: 20000, test_RMSE: 1.1268175840377808, erank: 66.7467651367
1875, s1: 0.002546718344092369, s5: 0.002241804962977767
depth: 2, iteration: 22000, test_RMSE: 1.1268175840377808, erank: 66.6876907348
6328, s1: 0.002562381327152252, s5: 0.0022509219124913216
depth: 2, iteration: 24000, test_RMSE: 1.1268175840377808, erank: 66.6210098266
6016, s1: 0.0025804811157286167, s5: 0.002260324778035283
depth: 2, iteration: 26000, test_RMSE: 1.1268175840377808, erank: 66.5465164184
5703, s1: 0.0026014847680926323, s5: 0.0022700026165694
depth: 2, iteration: 28000, test_RMSE: 1.1268175840377808, erank: 66.4640045166
0156, s1: 0.002626105211675167, s5: 0.0022799912840127945
depth: 2, iteration: 30000, test_RMSE: 1.1268174648284912, erank: 66.3732376098
6328, s1: 0.002655301010236144, s5: 0.002290369477123022
depth: 2, iteration: 32000, test_RMSE: 1.1268174648284912, erank: 66.2738647460
9375, s1: 0.002690454013645649, s5: 0.002301227068528533
depth: 2, iteration: 34000, test_RMSE: 1.1268174648284912, erank: 66.1657485961
914, s1: 0.002732722321525216, s5: 0.0023126970045268536
depth: 2, iteration: 36000, test_RMSE: 1.1268174648284912, erank: 66.0484848022
461, s1: 0.0027824800927191973, s5: 0.0023249881342053413
depth: 2, iteration: 38000, test_RMSE: 1.1268174648284912, erank: 65.9219360351
5625, s1: 0.0028392616659402847, s5: 0.002338516293093562
depth: 2, iteration: 40000, test_RMSE: 1.1268173456192017, erank: 65.7857513427
7344, s1: 0.002902455162256956, s5: 0.002353484509512782
depth: 2, iteration: 42000, test_RMSE: 1.1268173456192017, erank: 65.6395492553
711, s1: 0.002971600042656064, s5: 0.0023695286363363266
depth: 2, iteration: 44000, test_RMSE: 1.1268173456192017, erank: 65.4832992553
711, s1: 0.0030463754665106535, s5: 0.002385411411523819
depth: 2, iteration: 46000, test_RMSE: 1.1268173456192017, erank: 65.3167037963
8672, s1: 0.0031267658341675997, s5: 0.002400455065071583
depth: 2, iteration: 48000, test_RMSE: 1.126817226409912, erank: 65.13941955566
406, s1: 0.003212721087038517, s5: 0.0024148665834218264
depth: 2, iteration: 50000, test_RMSE: 1.126817226409912, erank: 64.95127105712
```

89, s1: 0.003304427256807685, s5: 0.002429282059893012  
depth: 2, iteration: 52000, test\_RMSE: 1.126817226409912, erank: 64.75187683105  
469, s1: 0.0034018773585557938, s5: 0.0024442151188850403  
depth: 2, iteration: 54000, test\_RMSE: 1.1268171072006226, erank: 64.5411605834  
961, s1: 0.0035052478779107332, s5: 0.0024599931202828884  
depth: 2, iteration: 56000, test\_RMSE: 1.126816987991333, erank: 64.3188476562  
5, s1: 0.003614695742726326, s5: 0.002476794645190239  
depth: 2, iteration: 58000, test\_RMSE: 1.126816987991333, erank: 64.08464813232  
422, s1: 0.0037304232828319073, s5: 0.002494827611371875  
depth: 2, iteration: 60000, test\_RMSE: 1.1268168687820435, erank: 63.8383369445  
8008, s1: 0.003852591384202242, s5: 0.002514178166165948  
depth: 2, iteration: 62000, test\_RMSE: 1.1268168687820435, erank: 63.5797576904  
2969, s1: 0.003981400281190872, s5: 0.002534953411668539  
depth: 2, iteration: 64000, test\_RMSE: 1.126816749572754, erank: 63.30899429321  
289, s1: 0.004117083270102739, s5: 0.002557359402999282  
depth: 2, iteration: 66000, test\_RMSE: 1.1268166303634644, erank: 63.0255012512  
207, s1: 0.004259930923581123, s5: 0.002581470413133502  
depth: 2, iteration: 68000, test\_RMSE: 1.1268165111541748, erank: 62.7290344238  
28125, s1: 0.004410162102431059, s5: 0.0026075365021824837  
depth: 2, iteration: 70000, test\_RMSE: 1.1268163919448853, erank: 62.4192924499  
5117, s1: 0.004568094853311777, s5: 0.002635799814015627  
depth: 2, iteration: 72000, test\_RMSE: 1.1268162727355957, erank: 62.0963287353  
5156, s1: 0.004733992274850607, s5: 0.0026665301993489265  
depth: 2, iteration: 74000, test\_RMSE: 1.1268162727355957, erank: 61.7598724365  
2344, s1: 0.004908200819045305, s5: 0.0026999348774552345  
depth: 2, iteration: 76000, test\_RMSE: 1.1268160343170166, erank: 61.4097709655  
7617, s1: 0.005091039929538965, s5: 0.0027363209519535303  
depth: 2, iteration: 78000, test\_RMSE: 1.126815915107727, erank: 61.04587936401  
367, s1: 0.005282912869006395, s5: 0.002775769215077162  
depth: 2, iteration: 80000, test\_RMSE: 1.1268157958984375, erank: 60.6681404113  
7695, s1: 0.005484155844897032, s5: 0.002818463137373328  
depth: 2, iteration: 82000, test\_RMSE: 1.126815676689148, erank: 60.27629470825  
195, s1: 0.005695205181837082, s5: 0.002864376176148653  
depth: 2, iteration: 84000, test\_RMSE: 1.1268154382705688, erank: 59.8705673217  
77344, s1: 0.00591647531837225, s5: 0.0029134887736290693  
depth: 2, iteration: 86000, test\_RMSE: 1.1268153190612793, erank: 59.4506683349  
6094, s1: 0.006148449145257473, s5: 0.0029658402781933546  
depth: 2, iteration: 88000, test\_RMSE: 1.1268150806427002, erank: 59.0164947509  
7656, s1: 0.006391571834683418, s5: 0.003021284006536007  
depth: 2, iteration: 90000, test\_RMSE: 1.1268149614334106, erank: 58.5681152343  
75, s1: 0.006646414287388325, s5: 0.003079788526520133  
depth: 2, iteration: 92000, test\_RMSE: 1.1268147230148315, erank: 58.1055755615  
2344, s1: 0.006913453806191683, s5: 0.0031413312535732985  
depth: 2, iteration: 94000, test\_RMSE: 1.1268144845962524, erank: 57.6288986206  
0547, s1: 0.00719320448115468, s5: 0.0032058674842119217  
depth: 2, iteration: 96000, test\_RMSE: 1.1268142461776733, erank: 57.1381835937  
5, s1: 0.007486290298402309, s5: 0.003273325739428401  
depth: 2, iteration: 98000, test\_RMSE: 1.1268140077590942, erank: 56.6333312988  
28125, s1: 0.007793441414833069, s5: 0.003343788906931877  
depth: 2, iteration: 100000, test\_RMSE: 1.1268136501312256, erank: 56.114585876  
464844, s1: 0.00811514537781477, s5: 0.003417138010263443  
depth: 2, iteration: 102000, test\_RMSE: 1.1268134117126465, erank: 55.582057952  
88086, s1: 0.008452177047729492, s5: 0.003493361407890916  
depth: 2, iteration: 104000, test\_RMSE: 1.1268131732940674, erank: 55.035869598

38867, s1: 0.008805247023701668, s5: 0.003572475863620639  
depth: 2, iteration: 106000, test\_RMSE: 1.1268128156661987, erank: 54.476287841  
796875, s1: 0.009175129234790802, s5: 0.003654350293800235  
depth: 2, iteration: 108000, test\_RMSE: 1.12681245803833, erank: 53.90345382690  
43, s1: 0.009562557563185692, s5: 0.003738728817552328  
depth: 2, iteration: 110000, test\_RMSE: 1.1268121004104614, erank: 53.317836761  
47461, s1: 0.009968362748622894, s5: 0.0038252195809036493  
depth: 2, iteration: 112000, test\_RMSE: 1.1268117427825928, erank: 52.719398498  
535156, s1: 0.010393479838967323, s5: 0.003913565538823605  
depth: 2, iteration: 114000, test\_RMSE: 1.1268112659454346, erank: 52.108871459  
96094, s1: 0.010838759131729603, s5: 0.004003607202321291  
depth: 2, iteration: 116000, test\_RMSE: 1.126810908317566, erank: 51.4863433837  
8906, s1: 0.011305205523967743, s5: 0.004095918498933315  
depth: 2, iteration: 118000, test\_RMSE: 1.1268104314804077, erank: 50.852317810  
058594, s1: 0.011793749406933784, s5: 0.004191141109913588  
depth: 2, iteration: 120000, test\_RMSE: 1.126810073852539, erank: 50.2072334289  
5508, s1: 0.01230555772781372, s5: 0.004289804492145777  
depth: 2, iteration: 122000, test\_RMSE: 1.1268094778060913, erank: 49.551273345  
947266, s1: 0.012841712683439255, s5: 0.0043924059718847275  
depth: 2, iteration: 124000, test\_RMSE: 1.126809000968933, erank: 48.8852539062  
5, s1: 0.01340328250080347, s5: 0.0044992719776928425  
depth: 2, iteration: 126000, test\_RMSE: 1.1268084049224854, erank: 48.209747314  
453125, s1: 0.013991564512252808, s5: 0.004610524978488684  
depth: 2, iteration: 128000, test\_RMSE: 1.1268079280853271, erank: 47.525146484  
375, s1: 0.014607813209295273, s5: 0.004726290702819824  
depth: 2, iteration: 130000, test\_RMSE: 1.1268073320388794, erank: 46.832019805  
9082, s1: 0.01525340136140585, s5: 0.004846774507313967  
depth: 2, iteration: 132000, test\_RMSE: 1.126806616783142, erank: 46.1310310363  
7695, s1: 0.01592974178493023, s5: 0.004971998743712902  
depth: 2, iteration: 134000, test\_RMSE: 1.1268060207366943, erank: 45.422870635  
98633, s1: 0.01663823612034321, s5: 0.0051021575927734375  
depth: 2, iteration: 136000, test\_RMSE: 1.126805305480957, erank: 44.7078742980  
957, s1: 0.017380397766828537, s5: 0.0052372002974152565  
depth: 2, iteration: 138000, test\_RMSE: 1.1268045902252197, erank: 43.987163543  
70117, s1: 0.018157852813601494, s5: 0.00537727028131485  
depth: 2, iteration: 140000, test\_RMSE: 1.1268037557601929, erank: 43.261184692  
38281, s1: 0.018972385674715042, s5: 0.005522469524294138  
depth: 2, iteration: 142000, test\_RMSE: 1.126802921295166, erank: 42.5306930541  
9922, s1: 0.019825682044029236, s5: 0.005672930274158716  
depth: 2, iteration: 144000, test\_RMSE: 1.1268022060394287, erank: 41.796463012  
69531, s1: 0.02071963995695114, s5: 0.005828638095408678  
depth: 2, iteration: 146000, test\_RMSE: 1.1268012523651123, erank: 41.059150695  
80078, s1: 0.021656246855854988, s5: 0.005989825818687677  
depth: 2, iteration: 148000, test\_RMSE: 1.126800298690796, erank: 40.3194732666  
0156, s1: 0.02263754978775978, s5: 0.006156534422188997  
depth: 2, iteration: 150000, test\_RMSE: 1.1267993450164795, erank: 39.578311920  
166016, s1: 0.023665448650717735, s5: 0.006328980438411236  
depth: 2, iteration: 152000, test\_RMSE: 1.1267982721328735, erank: 38.836364746  
09375, s1: 0.024742664769291878, s5: 0.006507200188934803  
depth: 2, iteration: 154000, test\_RMSE: 1.1267971992492676, erank: 38.094249725  
3418, s1: 0.025871073827147484, s5: 0.00669139763340354  
depth: 2, iteration: 156000, test\_RMSE: 1.126796007156372, erank: 37.3529396057  
1289, s1: 0.02705339714884758, s5: 0.006881778594106436  
depth: 2, iteration: 158000, test\_RMSE: 1.1267948150634766, erank: 36.612972259

521484, s1: 0.028292246162891388, s5: 0.007078399416059256  
depth: 2, iteration: 160000, test\_RMSE: 1.126793622970581, erank: 35.8751792907  
71484, s1: 0.029590236023068428, s5: 0.007281579542905092  
depth: 2, iteration: 162000, test\_RMSE: 1.126792311668396, erank: 35.1404647827  
14844, s1: 0.030949678272008896, s5: 0.007491336669772863  
depth: 2, iteration: 164000, test\_RMSE: 1.126791000366211, erank: 34.4090423583  
9844, s1: 0.03237448260188103, s5: 0.0077081178314983845  
depth: 2, iteration: 166000, test\_RMSE: 1.1267894506454468, erank: 33.681964874  
26758, s1: 0.03386765345931053, s5: 0.007931999862194061  
depth: 2, iteration: 168000, test\_RMSE: 1.1267880201339722, erank: 32.959815979  
003906, s1: 0.03543202579021454, s5: 0.00816313922405243  
depth: 2, iteration: 170000, test\_RMSE: 1.1267863512039185, erank: 32.243259429  
93164, s1: 0.03707119822502136, s5: 0.008401836268603802  
depth: 2, iteration: 172000, test\_RMSE: 1.1267848014831543, erank: 31.533073425  
29297, s1: 0.03878830373287201, s5: 0.008648455142974854  
depth: 2, iteration: 174000, test\_RMSE: 1.126783013343811, erank: 30.8296108245  
8496, s1: 0.040587857365608215, s5: 0.008903012610971928  
depth: 2, iteration: 176000, test\_RMSE: 1.1267812252044678, erank: 30.133592605  
59082, s1: 0.04247321933507919, s5: 0.009165904484689236  
depth: 2, iteration: 178000, test\_RMSE: 1.126779317855835, erank: 29.4455013275  
1465, s1: 0.044448915868997574, s5: 0.009437531232833862  
depth: 2, iteration: 180000, test\_RMSE: 1.1267772912979126, erank: 28.765838623  
046875, s1: 0.046518921852111816, s5: 0.009717931039631367  
depth: 2, iteration: 182000, test\_RMSE: 1.1267751455307007, erank: 28.095050811  
767578, s1: 0.04868829622864723, s5: 0.010007415898144245  
depth: 2, iteration: 184000, test\_RMSE: 1.1267729997634888, erank: 27.433828353  
881836, s1: 0.050961028784513474, s5: 0.010306315496563911  
depth: 2, iteration: 186000, test\_RMSE: 1.1267706155776978, erank: 26.782293319  
70215, s1: 0.05334286391735077, s5: 0.010615107603371143  
depth: 2, iteration: 188000, test\_RMSE: 1.1267682313919067, erank: 26.140924453  
73535, s1: 0.05583840236067772, s5: 0.010933943092823029  
depth: 2, iteration: 190000, test\_RMSE: 1.1267657279968262, erank: 25.510185241  
69922, s1: 0.0584535151720047, s5: 0.011263171210885048  
depth: 2, iteration: 192000, test\_RMSE: 1.126763105392456, erank: 24.8901176452  
63672, s1: 0.06119418889284134, s5: 0.011603149585425854  
depth: 2, iteration: 194000, test\_RMSE: 1.1267603635787964, erank: 24.281435012  
817383, s1: 0.06406527757644653, s5: 0.011954127810895443  
depth: 2, iteration: 196000, test\_RMSE: 1.1267575025558472, erank: 23.684045791  
625977, s1: 0.06707409024238586, s5: 0.012316657230257988  
depth: 2, iteration: 198000, test\_RMSE: 1.1267545223236084, erank: 23.098289489  
746094, s1: 0.07022697478532791, s5: 0.01269101444631815  
depth: 2, iteration: 200000, test\_RMSE: 1.1267513036727905, erank: 22.524267196  
655273, s1: 0.07353086769580841, s5: 0.013077585026621819  
depth: 2, iteration: 202000, test\_RMSE: 1.126747965812683, erank: 21.9622936248  
7793, s1: 0.07699260860681534, s5: 0.01347685419023037  
depth: 2, iteration: 204000, test\_RMSE: 1.1267445087432861, erank: 21.412357330  
322266, s1: 0.08062008023262024, s5: 0.013889024965465069  
depth: 2, iteration: 206000, test\_RMSE: 1.1267409324645996, erank: 20.874551773  
07129, s1: 0.08442170917987823, s5: 0.014314603991806507  
depth: 2, iteration: 208000, test\_RMSE: 1.126737117767334, erank: 20.3490943908  
6914, s1: 0.08840429037809372, s5: 0.014754201285541058  
depth: 2, iteration: 210000, test\_RMSE: 1.1267331838607788, erank: 19.835798263  
549805, s1: 0.09257835894823074, s5: 0.015208248980343342  
depth: 2, iteration: 212000, test\_RMSE: 1.1267290115356445, erank: 19.334901809

692383, s1: 0.0969519391655922, s5: 0.015676777809858322  
depth: 2, iteration: 214000, test\_RMSE: 1.1267247200012207, erank: 18.846252441  
40625, s1: 0.10153427720069885, s5: 0.016160815954208374  
depth: 2, iteration: 216000, test\_RMSE: 1.1267201900482178, erank: 18.369728088  
378906, s1: 0.10633710771799088, s5: 0.016660630702972412  
depth: 2, iteration: 218000, test\_RMSE: 1.1267154216766357, erank: 17.905488967  
895508, s1: 0.11136890202760696, s5: 0.017176862806081772  
depth: 2, iteration: 220000, test\_RMSE: 1.1267105340957642, erank: 17.453313827  
51465, s1: 0.11664194613695145, s5: 0.017709797248244286  
depth: 2, iteration: 222000, test\_RMSE: 1.126705288887024, erank: 17.0131416320  
80078, s1: 0.12216698378324509, s5: 0.018260229378938675  
depth: 2, iteration: 224000, test\_RMSE: 1.1266998052597046, erank: 16.584829330  
444336, s1: 0.12795713543891907, s5: 0.018828408792614937  
depth: 2, iteration: 226000, test\_RMSE: 1.1266942024230957, erank: 16.168321609  
49707, s1: 0.1340230107307434, s5: 0.01941538043320179  
depth: 2, iteration: 228000, test\_RMSE: 1.1266882419586182, erank: 15.763394355  
773926, s1: 0.14037886261940002, s5: 0.020021134987473488  
depth: 2, iteration: 230000, test\_RMSE: 1.126682162284851, erank: 15.3699417114  
25781, s1: 0.14703921973705292, s5: 0.020647287368774414  
depth: 2, iteration: 232000, test\_RMSE: 1.1266756057739258, erank: 14.987746238  
708496, s1: 0.15401816368103027, s5: 0.021293560042977333  
depth: 2, iteration: 234000, test\_RMSE: 1.126668930053711, erank: 14.6165714263  
91602, s1: 0.16133077442646027, s5: 0.02196088805794716  
depth: 2, iteration: 236000, test\_RMSE: 1.126661777496338, erank: 14.2562828063  
96484, s1: 0.16899244487285614, s5: 0.022649914026260376  
depth: 2, iteration: 238000, test\_RMSE: 1.1266543865203857, erank: 13.906742095  
947266, s1: 0.17701996862888336, s5: 0.023361505940556526  
depth: 2, iteration: 240000, test\_RMSE: 1.126646637916565, erank: 13.5676269531  
25, s1: 0.185431107878685, s5: 0.024096259847283363  
depth: 2, iteration: 242000, test\_RMSE: 1.126638650894165, erank: 13.2388181686  
40137, s1: 0.19424332678318024, s5: 0.02485533244907856  
depth: 2, iteration: 244000, test\_RMSE: 1.126630187034607, erank: 12.9199647903  
44238, s1: 0.20347756147384644, s5: 0.025638746097683907  
depth: 2, iteration: 246000, test\_RMSE: 1.1266213655471802, erank: 12.610950469  
970703, s1: 0.21315106749534607, s5: 0.026447780430316925  
depth: 2, iteration: 248000, test\_RMSE: 1.1266121864318848, erank: 12.311510086  
05957, s1: 0.22328640520572662, s5: 0.027283377945423126  
depth: 2, iteration: 250000, test\_RMSE: 1.1266025304794312, erank: 12.021406173  
706055, s1: 0.23390428721904755, s5: 0.02814604714512825  
depth: 2, iteration: 252000, test\_RMSE: 1.1265925168991089, erank: 11.740419387  
817383, s1: 0.24502919614315033, s5: 0.02903696522116661  
depth: 2, iteration: 254000, test\_RMSE: 1.126582145690918, erank: 11.4682941436  
76758, s1: 0.2566845417022705, s5: 0.029957063496112823  
depth: 2, iteration: 256000, test\_RMSE: 1.1265710592269897, erank: 11.204827308  
654785, s1: 0.2688937783241272, s5: 0.030907070264220238  
depth: 2, iteration: 258000, test\_RMSE: 1.1265596151351929, erank: 10.949774742  
126465, s1: 0.2816839814186096, s5: 0.03188781067728996  
depth: 2, iteration: 260000, test\_RMSE: 1.1265478134155273, erank: 10.702877998  
35205, s1: 0.2950836718082428, s5: 0.03290104120969772  
depth: 2, iteration: 262000, test\_RMSE: 1.1265352964401245, erank: 10.463941574  
09668, s1: 0.3091195225715637, s5: 0.0339469388127327  
depth: 2, iteration: 264000, test\_RMSE: 1.1265223026275635, erank: 10.232705116  
271973, s1: 0.32382267713546753, s5: 0.03502728044986725  
depth: 2, iteration: 266000, test\_RMSE: 1.1265087127685547, erank: 10.008959770

202637, s1: 0.33922502398490906, s5: 0.03614272177219391  
depth: 2, iteration: 268000, test\_RMSE: 1.1264945268630981, erank: 9.7924938201  
9043, s1: 0.3553570806980133, s5: 0.03729412704706192  
depth: 2, iteration: 270000, test\_RMSE: 1.1264797449111938, erank: 9.5830774307  
25098, s1: 0.37225407361984253, s5: 0.03848356381058693  
depth: 2, iteration: 272000, test\_RMSE: 1.1264642477035522, erank: 9.3804960250  
8545, s1: 0.3899522125720978, s5: 0.03971162810921669  
depth: 2, iteration: 274000, test\_RMSE: 1.1264482736587524, erank: 9.1845493316  
65039, s1: 0.4084862768650055, s5: 0.04097916558384895  
depth: 2, iteration: 276000, test\_RMSE: 1.1264313459396362, erank: 8.9949598312  
37793, s1: 0.42789992690086365, s5: 0.04228837043046951  
depth: 2, iteration: 278000, test\_RMSE: 1.1264138221740723, erank: 8.8116264343  
26172, s1: 0.4482291638851166, s5: 0.04364047944545746  
depth: 2, iteration: 280000, test\_RMSE: 1.126395583152771, erank: 8.63428974151  
6113, s1: 0.4695194363594055, s5: 0.0450364351272583  
depth: 2, iteration: 282000, test\_RMSE: 1.1263765096664429, erank: 8.4627666473  
38867, s1: 0.4918152093887329, s5: 0.04647781327366829  
depth: 2, iteration: 284000, test\_RMSE: 1.1263567209243774, erank: 8.2968606948  
85254, s1: 0.5151622295379639, s5: 0.047966260462999344  
depth: 2, iteration: 286000, test\_RMSE: 1.1263359785079956, erank: 8.1364135742  
1875, s1: 0.5396071076393127, s5: 0.049502767622470856  
depth: 2, iteration: 288000, test\_RMSE: 1.126314401626587, erank: 7.98120069503  
7842, s1: 0.5652033686637878, s5: 0.051089394837617874  
depth: 2, iteration: 290000, test\_RMSE: 1.1262918710708618, erank: 7.8310894966  
12549, s1: 0.5920032262802124, s5: 0.052727583795785904  
depth: 2, iteration: 292000, test\_RMSE: 1.1262683868408203, erank: 7.6859035491  
94336, s1: 0.6200568079948425, s5: 0.054419323801994324  
depth: 2, iteration: 294000, test\_RMSE: 1.126244068145752, erank: 7.54545497894  
2871, s1: 0.6494274735450745, s5: 0.056165795773267746  
depth: 2, iteration: 296000, test\_RMSE: 1.126218557357788, erank: 7.40962266921  
9971, s1: 0.6801697611808777, s5: 0.05796898156404495  
depth: 2, iteration: 298000, test\_RMSE: 1.1261920928955078, erank: 7.2781910896  
30127, s1: 0.7123532295227051, s5: 0.05983100086450577  
depth: 2, iteration: 300000, test\_RMSE: 1.1261645555496216, erank: 7.1510543823  
24219, s1: 0.7460382580757141, s5: 0.06175367534160614  
depth: 2, iteration: 302000, test\_RMSE: 1.1261358261108398, erank: 7.0280828475  
95215, s1: 0.7812865972518921, s5: 0.06373829394578934  
depth: 2, iteration: 304000, test\_RMSE: 1.1261059045791626, erank: 6.9090852737  
42676, s1: 0.8181771039962769, s5: 0.06578710675239563  
depth: 2, iteration: 306000, test\_RMSE: 1.1260749101638794, erank: 6.7939376831  
05469, s1: 0.8567851781845093, s5: 0.06790245324373245  
depth: 2, iteration: 308000, test\_RMSE: 1.1260426044464111, erank: 6.6825437545  
77637, s1: 0.8971773386001587, s5: 0.07008734345436096  
depth: 2, iteration: 310000, test\_RMSE: 1.1260089874267578, erank: 6.5747308731  
0791, s1: 0.9394433498382568, s5: 0.07234253734350204  
depth: 2, iteration: 312000, test\_RMSE: 1.1259740591049194, erank: 6.4704074859  
61914, s1: 0.9836559295654297, s5: 0.07467009872198105  
depth: 2, iteration: 314000, test\_RMSE: 1.1259377002716064, erank: 6.3694620132  
44629, s1: 1.029901385307312, s5: 0.0770740658044815  
depth: 2, iteration: 316000, test\_RMSE: 1.1258999109268188, erank: 6.2717218399  
04785, s1: 1.078285574913025, s5: 0.07955586165189743  
depth: 2, iteration: 318000, test\_RMSE: 1.1258608102798462, erank: 6.1771416664  
123535, s1: 1.1288793087005615, s5: 0.08211688697338104  
depth: 2, iteration: 320000, test\_RMSE: 1.1258200407028198, erank: 6.0855736732



48291, s1: 1.1817923784255981, s5: 0.08476101607084274  
depth: 2, iteration: 322000, test\_RMSE: 1.1257778406143188, erank: 5.9969582557  
67822, s1: 1.2371110916137695, s5: 0.0874917209148407  
depth: 2, iteration: 324000, test\_RMSE: 1.1257340908050537, erank: 5.9111385345  
45898, s1: 1.2949552536010742, s5: 0.09030918776988983  
depth: 2, iteration: 326000, test\_RMSE: 1.1256885528564453, erank: 5.8280644416  
80908, s1: 1.3554168939590454, s5: 0.09321818500757217  
depth: 2, iteration: 328000, test\_RMSE: 1.1256414651870728, erank: 5.7476210594  
17725, s1: 1.4186255931854248, s5: 0.09622201323509216  
depth: 2, iteration: 330000, test\_RMSE: 1.1255927085876465, erank: 5.6697392463  
68408, s1: 1.4846786260604858, s5: 0.09932206571102142  
depth: 2, iteration: 332000, test\_RMSE: 1.1255420446395874, erank: 5.5942912101  
745605, s1: 1.5537105798721313, s5: 0.10252127051353455  
depth: 2, iteration: 334000, test\_RMSE: 1.1254897117614746, erank: 5.5212397575  
37842, s1: 1.6258348226547241, s5: 0.10582444071769714  
depth: 2, iteration: 336000, test\_RMSE: 1.1254355907440186, erank: 5.4504923820  
495605, s1: 1.701175570487976, s5: 0.1092338040471077  
depth: 2, iteration: 338000, test\_RMSE: 1.1253796815872192, erank: 5.3820056915  
2832, s1: 1.7798479795455933, s5: 0.11275231093168259  
depth: 2, iteration: 340000, test\_RMSE: 1.1253217458724976, erank: 5.3156485557  
55615, s1: 1.86203134059906, s5: 0.1163855493068695  
depth: 2, iteration: 342000, test\_RMSE: 1.1252620220184326, erank: 5.2513608932  
49512, s1: 1.947845697402954, s5: 0.12013282626867294  
depth: 2, iteration: 344000, test\_RMSE: 1.1252002716064453, erank: 5.1890974044  
799805, s1: 2.037433624267578, s5: 0.1240023598074913  
depth: 2, iteration: 346000, test\_RMSE: 1.1251366138458252, erank: 5.1287984848  
02246, s1: 2.1309304237365723, s5: 0.12799495458602905  
depth: 2, iteration: 348000, test\_RMSE: 1.1250710487365723, erank: 5.0703883171  
08154, s1: 2.228503704071045, s5: 0.13211677968502045  
depth: 2, iteration: 350000, test\_RMSE: 1.1250033378601074, erank: 5.0138068199  
157715, s1: 2.3303096294403076, s5: 0.13636861741542816  
depth: 2, iteration: 352000, test\_RMSE: 1.1249338388442993, erank: 4.9590129852  
29492, s1: 2.4364941120147705, s5: 0.14075832068920135  
depth: 2, iteration: 354000, test\_RMSE: 1.1248624324798584, erank: 4.9059405326  
84326, s1: 2.5472309589385986, s5: 0.14528580009937286  
depth: 2, iteration: 356000, test\_RMSE: 1.1247889995574951, erank: 4.8545622825  
62256, s1: 2.662654161453247, s5: 0.14995978772640228  
depth: 2, iteration: 358000, test\_RMSE: 1.1247135400772095, erank: 4.8047456741  
33301, s1: 2.7830440998077393, s5: 0.15478289127349854  
depth: 2, iteration: 360000, test\_RMSE: 1.124636173248291, erank: 4.75654506683  
3496, s1: 2.908452033996582, s5: 0.15975888073444366  
depth: 2, iteration: 362000, test\_RMSE: 1.1245570182800293, erank: 4.7098617553  
71094, s1: 3.0391182899475098, s5: 0.1648922562599182  
depth: 2, iteration: 364000, test\_RMSE: 1.1244759559631348, erank: 4.6646604537  
96387, s1: 3.175213098526001, s5: 0.17018914222717285  
depth: 2, iteration: 366000, test\_RMSE: 1.1243932247161865, erank: 4.6209015846  
25244, s1: 3.3169236183166504, s5: 0.17565487325191498  
depth: 2, iteration: 368000, test\_RMSE: 1.1243088245391846, erank: 4.5785317420  
95947, s1: 3.464446544647217, s5: 0.18129360675811768  
depth: 2, iteration: 370000, test\_RMSE: 1.124222755432129, erank: 4.53753471374  
5117, s1: 3.617940902709961, s5: 0.18711017072200775  
depth: 2, iteration: 372000, test\_RMSE: 1.124135136604309, erank: 4.49785661697  
3877, s1: 3.777636766433716, s5: 0.1931094378232956  
depth: 2, iteration: 374000, test\_RMSE: 1.1240462064743042, erank: 4.4594655036

92627, s1: 3.9437179565429688, s5: 0.19930149614810944  
depth: 2, iteration: 376000, test\_RMSE: 1.1239560842514038, erank: 4.4223465919  
49463, s1: 4.116336345672607, s5: 0.20568548142910004  
depth: 2, iteration: 378000, test\_RMSE: 1.123864769935608, erank: 4.38643646240  
2344, s1: 4.29574728012085, s5: 0.21227020025253296  
depth: 2, iteration: 380000, test\_RMSE: 1.1237726211547852, erank: 4.3517217636  
1084, s1: 4.482119560241699, s5: 0.21906116604804993  
depth: 2, iteration: 382000, test\_RMSE: 1.123679757118225, erank: 4.31817483901  
9775, s1: 4.675647258758545, s5: 0.2260677069425583  
depth: 2, iteration: 384000, test\_RMSE: 1.1235862970352173, erank: 4.2857656478  
88184, s1: 4.876523494720459, s5: 0.23329292237758636  
depth: 2, iteration: 386000, test\_RMSE: 1.12349271774292, erank: 4.254464626312  
256, s1: 5.084959030151367, s5: 0.2407425343990326  
depth: 2, iteration: 388000, test\_RMSE: 1.123399019241333, erank: 4.22424411773  
6816, s1: 5.301104545593262, s5: 0.24842606484889984  
depth: 2, iteration: 390000, test\_RMSE: 1.1233057975769043, erank: 4.1950984001  
15967, s1: 5.52516508102417, s5: 0.25634434819221497  
depth: 2, iteration: 392000, test\_RMSE: 1.1232130527496338, erank: 4.1669831275  
93994, s1: 5.7573394775390625, s5: 0.2645135819911957  
depth: 2, iteration: 394000, test\_RMSE: 1.1231213808059692, erank: 4.1398787498  
47412, s1: 5.997807025909424, s5: 0.27293285727500916  
depth: 2, iteration: 396000, test\_RMSE: 1.1230310201644897, erank: 4.1137738227  
84424, s1: 6.246706962585449, s5: 0.2816140949726105  
depth: 2, iteration: 398000, test\_RMSE: 1.1229424476623535, erank: 4.0886406898  
498535, s1: 6.504222869873047, s5: 0.2905612587928772  
depth: 2, iteration: 400000, test\_RMSE: 1.1228561401367188, erank: 4.0644717216  
4917, s1: 6.770505428314209, s5: 0.2997850477695465  
depth: 2, iteration: 402000, test\_RMSE: 1.122772455215454, erank: 4.04123497009  
2773, s1: 7.045713424682617, s5: 0.30929023027420044  
depth: 2, iteration: 404000, test\_RMSE: 1.1226921081542969, erank: 4.0189208984  
375, s1: 7.329975605010986, s5: 0.31908920407295227  
depth: 2, iteration: 406000, test\_RMSE: 1.1226154565811157, erank: 3.9975197315  
216064, s1: 7.623386383056641, s5: 0.3291885256767273  
depth: 2, iteration: 408000, test\_RMSE: 1.1225430965423584, erank: 3.9770014286  
04126, s1: 7.926117420196533, s5: 0.3395951986312866  
depth: 2, iteration: 410000, test\_RMSE: 1.1224758625030518, erank: 3.9573659896  
850586, s1: 8.238195419311523, s5: 0.3503175675868988  
depth: 2, iteration: 412000, test\_RMSE: 1.1224141120910645, erank: 3.9385652542  
11426, s1: 8.559853553771973, s5: 0.3613601624965668  
depth: 2, iteration: 414000, test\_RMSE: 1.1223586797714233, erank: 3.9206264019  
01245, s1: 8.891002655029297, s5: 0.3727377951145172  
depth: 2, iteration: 416000, test\_RMSE: 1.1223102807998657, erank: 3.9035317897  
79663, s1: 9.23172378540039, s5: 0.38446423411369324  
depth: 2, iteration: 418000, test\_RMSE: 1.122269630432129, erank: 3.88724803924  
56055, s1: 9.582123756408691, s5: 0.39654111862182617  
depth: 2, iteration: 420000, test\_RMSE: 1.1222376823425293, erank: 3.8717784881  
591797, s1: 9.942152976989746, s5: 0.408977210521698  
depth: 2, iteration: 422000, test\_RMSE: 1.122214913368225, erank: 3.85710334777  
83203, s1: 10.31184196472168, s5: 0.4217848777770996  
depth: 2, iteration: 424000, test\_RMSE: 1.1222025156021118, erank: 3.8432188034  
057617, s1: 10.691123962402344, s5: 0.43497204780578613  
depth: 2, iteration: 426000, test\_RMSE: 1.1222010850906372, erank: 3.8301117420  
196533, s1: 11.079987525939941, s5: 0.44855183362960815  
depth: 2, iteration: 428000, test\_RMSE: 1.1222118139266968, erank: 3.8177685737

609863, s1: 11.478368759155273, s5: 0.4625345766544342  
depth: 2, iteration: 430000, test\_RMSE: 1.1222352981567383, erank: 3.8061730861  
66382, s1: 11.886181831359863, s5: 0.47692209482192993  
depth: 2, iteration: 432000, test\_RMSE: 1.1222727298736572, erank: 3.7953317165  
374756, s1: 12.3032808303833, s5: 0.4917483925819397  
depth: 2, iteration: 434000, test\_RMSE: 1.122324824333191, erank: 3.78522634506  
2256, s1: 12.729521751403809, s5: 0.5069928765296936  
depth: 2, iteration: 436000, test\_RMSE: 1.1223926544189453, erank: 3.7758457660  
67505, s1: 13.164750099182129, s5: 0.5226936936378479  
depth: 2, iteration: 438000, test\_RMSE: 1.1224772930145264, erank: 3.7671675682  
06787, s1: 13.608766555786133, s5: 0.5388351082801819  
depth: 2, iteration: 440000, test\_RMSE: 1.122579574584961, erank: 3.75921869277  
9541, s1: 14.061262130737305, s5: 0.5554531812667847  
depth: 2, iteration: 442000, test\_RMSE: 1.1227004528045654, erank: 3.7519528865  
81421, s1: 14.522160530090332, s5: 0.5725439190864563  
depth: 2, iteration: 444000, test\_RMSE: 1.1228408813476562, erank: 3.7453842163  
085938, s1: 14.99104118347168, s5: 0.5901304483413696  
depth: 2, iteration: 446000, test\_RMSE: 1.1230018138885498, erank: 3.7394866943  
359375, s1: 15.467660903930664, s5: 0.6082153916358948  
depth: 2, iteration: 448000, test\_RMSE: 1.1231842041015625, erank: 3.7342703342  
437744, s1: 15.951666831970215, s5: 0.6268126368522644  
depth: 2, iteration: 450000, test\_RMSE: 1.1233888864517212, erank: 3.7297132015  
22827, s1: 16.442737579345703, s5: 0.645941436290741  
depth: 2, iteration: 452000, test\_RMSE: 1.1236168146133423, erank: 3.7257919311  
523438, s1: 16.940568923950195, s5: 0.6656106114387512  
depth: 2, iteration: 454000, test\_RMSE: 1.123868703842163, erank: 3.72251558303  
833, s1: 17.44460105895996, s5: 0.6858221888542175  
depth: 2, iteration: 456000, test\_RMSE: 1.1241453886032104, erank: 3.7198891639  
709473, s1: 17.954442977905273, s5: 0.7066129446029663  
depth: 2, iteration: 458000, test\_RMSE: 1.1244477033615112, erank: 3.7178561687  
469482, s1: 18.469820022583008, s5: 0.7279718518257141  
depth: 2, iteration: 460000, test\_RMSE: 1.1247761249542236, erank: 3.7164468765  
25879, s1: 18.99004364013672, s5: 0.7499250769615173  
depth: 2, iteration: 462000, test\_RMSE: 1.1251314878463745, erank: 3.7156260013  
580322, s1: 19.51483917236328, s5: 0.772477388381958  
depth: 2, iteration: 464000, test\_RMSE: 1.125514268875122, erank: 3.71540760993  
9575, s1: 20.043529510498047, s5: 0.795655369758606  
depth: 2, iteration: 466000, test\_RMSE: 1.125925064086914, erank: 3.71574664115  
90576, s1: 20.57588768005371, s5: 0.819454550743103  
depth: 2, iteration: 468000, test\_RMSE: 1.1263643503189087, erank: 3.7166590690  
612793, s1: 21.111209869384766, s5: 0.8439114689826965  
depth: 2, iteration: 470000, test\_RMSE: 1.1268324851989746, erank: 3.7181241512  
298584, s1: 21.64887237548828, s5: 0.8690146207809448  
depth: 2, iteration: 472000, test\_RMSE: 1.1273298263549805, erank: 3.7201268672  
943115, s1: 22.1884765625, s5: 0.8948058485984802  
depth: 2, iteration: 474000, test\_RMSE: 1.1278564929962158, erank: 3.7226548194  
885254, s1: 22.729494094848633, s5: 0.9212673306465149  
depth: 2, iteration: 476000, test\_RMSE: 1.1284127235412598, erank: 3.7256913185  
11963, s1: 23.27143669128418, s5: 0.9484575986862183  
depth: 2, iteration: 478000, test\_RMSE: 1.1289986371994019, erank: 3.7292320728  
302, s1: 23.813657760620117, s5: 0.9763673543930054  
depth: 2, iteration: 480000, test\_RMSE: 1.1296144723892212, erank: 3.7332696914  
67285, s1: 24.355480194091797, s5: 1.0049967765808105  
depth: 2, iteration: 482000, test\_RMSE: 1.1302599906921387, erank: 3.7377753257

751465, s1: 24.896726608276367, s5: 1.0343984365463257  
depth: 2, iteration: 484000, test\_RMSE: 1.1309351921081543, erank: 3.7427384853  
363037, s1: 25.436752319335938, s5: 1.0645502805709839  
depth: 2, iteration: 486000, test\_RMSE: 1.131639838218689, erank: 3.74815511703  
4912, s1: 25.97484588623047, s5: 1.0954831838607788  
depth: 2, iteration: 488000, test\_RMSE: 1.1323736906051636, erank: 3.7540013790  
130615, s1: 26.510560989379883, s5: 1.1272082328796387  
depth: 2, iteration: 490000, test\_RMSE: 1.133136510848999, erank: 3.76026821136  
4746, s1: 27.043333053588867, s5: 1.1597528457641602  
depth: 2, iteration: 492000, test\_RMSE: 1.1339279413223267, erank: 3.7669317722  
320557, s1: 27.573223114013672, s5: 1.193143606185913  
depth: 2, iteration: 494000, test\_RMSE: 1.1347475051879883, erank: 3.7739920616  
149902, s1: 28.099008560180664, s5: 1.227354884147644  
depth: 2, iteration: 496000, test\_RMSE: 1.1355949640274048, erank: 3.7814145088  
1958, s1: 28.62078857421875, s5: 1.2624462842941284  
depth: 2, iteration: 498000, test\_RMSE: 1.1364694833755493, erank: 3.7892093658  
447266, s1: 29.13762664794922, s5: 1.2984027862548828  
depth: 2, iteration: 500000, test\_RMSE: 1.1373708248138428, erank: 3.7973468303  
68042, s1: 29.64961051940918, s5: 1.3352702856063843  
depth: 2, iteration: 502000, test\_RMSE: 1.1382982730865479, erank: 3.8058094978  
33252, s1: 30.156064987182617, s5: 1.3730344772338867  
depth: 2, iteration: 504000, test\_RMSE: 1.1392511129379272, erank: 3.8145847320  
55664, s1: 30.656763076782227, s5: 1.4117342233657837  
depth: 2, iteration: 506000, test\_RMSE: 1.1402288675308228, erank: 3.8236646652  
22168, s1: 31.151214599609375, s5: 1.4514076709747314  
depth: 2, iteration: 508000, test\_RMSE: 1.1412307024002075, erank: 3.8330266475  
67749, s1: 31.639184951782227, s5: 1.4920222759246826  
depth: 2, iteration: 510000, test\_RMSE: 1.1422559022903442, erank: 3.8426682949  
06616, s1: 32.1202507019043, s5: 1.5336095094680786  
depth: 2, iteration: 512000, test\_RMSE: 1.1433037519454956, erank: 3.8525624275  
20752, s1: 32.5944938659668, s5: 1.576223373413086  
depth: 2, iteration: 514000, test\_RMSE: 1.1443736553192139, erank: 3.8627045154  
571533, s1: 33.06134796142578, s5: 1.619848608970642  
depth: 2, iteration: 516000, test\_RMSE: 1.1454646587371826, erank: 3.8730943202  
97241, s1: 33.52036666870117, s5: 1.664507269859314  
depth: 2, iteration: 518000, test\_RMSE: 1.146576166152954, erank: 3.88369250297  
5464, s1: 33.971954345703125, s5: 1.710236668586731  
depth: 2, iteration: 520000, test\_RMSE: 1.147707223892212, erank: 3.89449095726  
0132, s1: 34.41550064086914, s5: 1.7570334672927856  
depth: 2, iteration: 522000, test\_RMSE: 1.1488572359085083, erank: 3.9054813385  
009766, s1: 34.851009368896484, s5: 1.8049123287200928  
depth: 2, iteration: 524000, test\_RMSE: 1.1500248908996582, erank: 3.9166598320  
007324, s1: 35.2780876159668, s5: 1.8539081811904907  
depth: 2, iteration: 526000, test\_RMSE: 1.151210069656372, erank: 3.92801785469  
05518, s1: 35.69672393798828, s5: 1.904045581817627  
depth: 2, iteration: 528000, test\_RMSE: 1.152411699295044, erank: 3.93950891494  
75098, s1: 36.107540130615234, s5: 1.9553160667419434  
depth: 2, iteration: 530000, test\_RMSE: 1.1536290645599365, erank: 3.9511511325  
83618, s1: 36.50974655151367, s5: 2.007784128189087  
depth: 2, iteration: 532000, test\_RMSE: 1.1548612117767334, erank: 3.9629416465  
759277, s1: 36.90311050415039, s5: 2.0614278316497803  
depth: 2, iteration: 534000, test\_RMSE: 1.1561074256896973, erank: 3.9748525619  
506836, s1: 37.28801727294922, s5: 2.1162614822387695  
depth: 2, iteration: 536000, test\_RMSE: 1.1573668718338013, erank: 3.9868831634

521484, s1: 37.664222717285156, s5: 2.172374963760376  
depth: 2, iteration: 538000, test\_RMSE: 1.1586387157440186, erank: 3.9990086555  
480957, s1: 38.03229522705078, s5: 2.2296857833862305  
depth: 2, iteration: 540000, test\_RMSE: 1.1599222421646118, erank: 4.0112624168  
396, s1: 38.39048767089844, s5: 2.2882869243621826  
depth: 2, iteration: 542000, test\_RMSE: 1.1612167358398438, erank: 4.0235691070  
55664, s1: 38.7415771484375, s5: 2.3481497764587402  
depth: 2, iteration: 544000, test\_RMSE: 1.162521481513977, erank: 4.03597354888  
916, s1: 39.08354568481445, s5: 2.409329891204834  
depth: 2, iteration: 546000, test\_RMSE: 1.1638356447219849, erank: 4.0484361648  
55957, s1: 39.417884826660156, s5: 2.4718680381774902  
depth: 2, iteration: 548000, test\_RMSE: 1.1651583909988403, erank: 4.0609827041  
62598, s1: 39.74277114868164, s5: 2.5357184410095215  
depth: 2, iteration: 550000, test\_RMSE: 1.166488858795166, erank: 4.0735793113  
7085, s1: 40.059974670410156, s5: 2.600955009460449  
depth: 2, iteration: 552000, test\_RMSE: 1.1678266525268555, erank: 4.0862216949  
46289, s1: 40.36909866333008, s5: 2.6675336360931396  
depth: 2, iteration: 554000, test\_RMSE: 1.1691707372665405, erank: 4.0989208221  
43555, s1: 40.669986724853516, s5: 2.7355892658233643  
depth: 2, iteration: 556000, test\_RMSE: 1.1705206632614136, erank: 4.1116442680  
35889, s1: 40.96356201171875, s5: 2.805008888244629  
depth: 2, iteration: 558000, test\_RMSE: 1.1718753576278687, erank: 4.1243977546  
691895, s1: 41.248695373535156, s5: 2.875884771347046  
depth: 2, iteration: 560000, test\_RMSE: 1.1732345819473267, erank: 4.1371841430  
66406, s1: 41.52610397338867, s5: 2.948223829269409  
depth: 2, iteration: 562000, test\_RMSE: 1.1745976209640503, erank: 4.1499919891  
35742, s1: 41.7962532043457, s5: 3.022061586380005  
depth: 2, iteration: 564000, test\_RMSE: 1.175963282585144, erank: 4.16280937194  
8242, s1: 42.05943298339844, s5: 3.097407341003418  
depth: 2, iteration: 566000, test\_RMSE: 1.1773312091827393, erank: 4.1756467819  
21387, s1: 42.31475830078125, s5: 3.174250841140747  
depth: 2, iteration: 568000, test\_RMSE: 1.1787010431289673, erank: 4.1884827613  
83057, s1: 42.563472747802734, s5: 3.252640724182129  
depth: 2, iteration: 570000, test\_RMSE: 1.1800718307495117, erank: 4.2013344764  
70947, s1: 42.80453872680664, s5: 3.3326210975646973  
depth: 2, iteration: 572000, test\_RMSE: 1.1814426183700562, erank: 4.2141733169  
55566, s1: 43.039344787597656, s5: 3.414123773574829  
depth: 2, iteration: 574000, test\_RMSE: 1.1828135251998901, erank: 4.2270154953  
00293, s1: 43.26714324951172, s5: 3.4972147941589355  
depth: 2, iteration: 576000, test\_RMSE: 1.1841834783554077, erank: 4.2398447990  
41748, s1: 43.488643646240234, s5: 3.5819599628448486  
depth: 2, iteration: 578000, test\_RMSE: 1.1855522394180298, erank: 4.2526640892  
02881, s1: 43.70383071899414, s5: 3.6683478355407715  
depth: 2, iteration: 580000, test\_RMSE: 1.1869187355041504, erank: 4.2654700279  
23584, s1: 43.912837982177734, s5: 3.756439447402954  
depth: 2, iteration: 582000, test\_RMSE: 1.1882829666137695, erank: 4.2782559394  
83643, s1: 44.11566925048828, s5: 3.8461227416992188  
depth: 2, iteration: 584000, test\_RMSE: 1.1896438598632812, erank: 4.2910056114  
19678, s1: 44.31340026855469, s5: 3.937513589859009  
depth: 2, iteration: 586000, test\_RMSE: 1.1910014152526855, erank: 4.3037381172  
18018, s1: 44.504817962646484, s5: 4.03057861328125  
depth: 2, iteration: 588000, test\_RMSE: 1.1923549175262451, erank: 4.3164505958  
55713, s1: 44.69038009643555, s5: 4.125367164611816  
depth: 2, iteration: 590000, test\_RMSE: 1.193703532218933, erank: 4.32912874221

8018, s1: 44.87070846557617, s5: 4.221885681152344  
depth: 2, iteration: 592000, test\_RMSE: 1.1950478553771973, erank: 4.3417706489  
56299, s1: 45.04558563232422, s5: 4.320121765136719  
depth: 2, iteration: 594000, test\_RMSE: 1.1963865756988525, erank: 4.3543767929  
07715, s1: 45.21567153930664, s5: 4.420170783996582  
depth: 2, iteration: 596000, test\_RMSE: 1.197719693183899, erank: 4.36695289611  
8164, s1: 45.3803596496582, s5: 4.522014617919922  
depth: 2, iteration: 598000, test\_RMSE: 1.1990467309951782, erank: 4.3794569969  
17725, s1: 45.54060363769531, s5: 4.62551212310791  
depth: 2, iteration: 600000, test\_RMSE: 1.2003669738769531, erank: 4.3919749259  
94873, s1: 45.69441604614258, s5: 4.731027603149414  
depth: 2, iteration: 602000, test\_RMSE: 1.2016804218292236, erank: 4.4044013023  
376465, s1: 45.845767974853516, s5: 4.838248252868652  
depth: 2, iteration: 604000, test\_RMSE: 1.2029868364334106, erank: 4.4167799949  
646, s1: 45.992584228515625, s5: 4.9472455978393555  
depth: 2, iteration: 606000, test\_RMSE: 1.204285740852356, erank: 4.42911529541  
0156, s1: 46.134521484375, s5: 5.058149337768555  
depth: 2, iteration: 608000, test\_RMSE: 1.20557701587677, erank: 4.441392421722  
412, s1: 46.27231979370117, s5: 5.170892238616943  
depth: 2, iteration: 610000, test\_RMSE: 1.2068603038787842, erank: 4.4536180496  
21582, s1: 46.40625762939453, s5: 5.285531520843506  
depth: 2, iteration: 612000, test\_RMSE: 1.2081354856491089, erank: 4.4657778739  
9292, s1: 46.53634262084961, s5: 5.401985168457031  
depth: 2, iteration: 614000, test\_RMSE: 1.2094013690948486, erank: 4.4778709411  
62109, s1: 46.663002014160156, s5: 5.520322322845459  
depth: 2, iteration: 616000, test\_RMSE: 1.2106592655181885, erank: 4.4899086952  
20947, s1: 46.785301208496094, s5: 5.640535354614258  
depth: 2, iteration: 618000, test\_RMSE: 1.2119089365005493, erank: 4.5018801689  
14795, s1: 46.90403366088867, s5: 5.762670516967773  
depth: 2, iteration: 620000, test\_RMSE: 1.213148832321167, erank: 4.51378250122  
0703, s1: 47.01984405517578, s5: 5.886621952056885  
depth: 2, iteration: 622000, test\_RMSE: 1.2143803834915161, erank: 4.5256061553  
95508, s1: 47.13235092163086, s5: 6.012543201446533  
depth: 2, iteration: 624000, test\_RMSE: 1.215602159500122, erank: 4.53737449645  
9961, s1: 47.240509033203125, s5: 6.1402764320373535  
depth: 2, iteration: 626000, test\_RMSE: 1.216814398765564, erank: 4.54904413223  
2666, s1: 47.34690475463867, s5: 6.270023822784424  
depth: 2, iteration: 628000, test\_RMSE: 1.218017816543579, erank: 4.56065893173  
2178, s1: 47.4495849609375, s5: 6.401581287384033  
depth: 2, iteration: 630000, test\_RMSE: 1.219211220741272, erank: 4.57219505310  
0586, s1: 47.54933547973633, s5: 6.535135269165039  
depth: 2, iteration: 632000, test\_RMSE: 1.2203949689865112, erank: 4.5836462974  
54834, s1: 47.646244049072266, s5: 6.670485019683838  
depth: 2, iteration: 634000, test\_RMSE: 1.2215704917907715, erank: 4.5950193405  
15137, s1: 47.740264892578125, s5: 6.807832717895508  
depth: 2, iteration: 636000, test\_RMSE: 1.2227356433868408, erank: 4.6062932014  
46533, s1: 47.832000732421875, s5: 6.946942329406738  
depth: 2, iteration: 638000, test\_RMSE: 1.223891258239746, erank: 4.61749696731  
5674, s1: 47.9207649230957, s5: 7.088150978088379  
depth: 2, iteration: 640000, test\_RMSE: 1.2250374555587769, erank: 4.6286134719  
84863, s1: 48.00733947753906, s5: 7.231203556060791  
depth: 2, iteration: 642000, test\_RMSE: 1.2261741161346436, erank: 4.6396298408  
5083, s1: 48.09149932861328, s5: 7.376042366027832  
depth: 2, iteration: 644000, test\_RMSE: 1.2273015975952148, erank: 4.6505618095

39795, s1: 48.17332458496094, s5: 7.522794246673584  
depth: 2, iteration: 646000, test\_RMSE: 1.2284188270568848, erank: 4.6613969802  
856445, s1: 48.252620697021484, s5: 7.671337127685547  
depth: 2, iteration: 648000, test\_RMSE: 1.229527473449707, erank: 4.67213296890  
2588, s1: 48.33016586303711, s5: 7.821728706359863  
depth: 2, iteration: 650000, test\_RMSE: 1.2306265830993652, erank: 4.6827855110  
16846, s1: 48.40483093261719, s5: 7.974019527435303  
depth: 2, iteration: 652000, test\_RMSE: 1.2317160367965698, erank: 4.6933336257  
93457, s1: 48.4781494140625, s5: 8.128202438354492  
depth: 2, iteration: 654000, test\_RMSE: 1.2327964305877686, erank: 4.7037930488  
58643, s1: 48.54877853393555, s5: 8.284062385559082  
depth: 2, iteration: 656000, test\_RMSE: 1.2338677644729614, erank: 4.7141466140  
74707, s1: 48.61811065673828, s5: 8.441883087158203  
depth: 2, iteration: 658000, test\_RMSE: 1.2349306344985962, erank: 4.7243847846  
98486, s1: 48.68589401245117, s5: 8.601304054260254  
depth: 2, iteration: 660000, test\_RMSE: 1.2359838485717773, erank: 4.7345399856  
56738, s1: 48.751346588134766, s5: 8.762516021728516  
depth: 2, iteration: 662000, test\_RMSE: 1.237027883529663, erank: 4.74458646774  
292, s1: 48.81500244140625, s5: 8.92546558380127  
depth: 2, iteration: 664000, test\_RMSE: 1.2380623817443848, erank: 4.7545266151  
42822, s1: 48.87744140625, s5: 9.090076446533203  
depth: 2, iteration: 666000, test\_RMSE: 1.239089012145996, erank: 4.76437187194  
8242, s1: 48.93765640258789, s5: 9.256406784057617  
depth: 2, iteration: 668000, test\_RMSE: 1.2401072978973389, erank: 4.7741036415  
1001, s1: 48.99663543701172, s5: 9.424407005310059  
depth: 2, iteration: 670000, test\_RMSE: 1.2411162853240967, erank: 4.7837371826  
171875, s1: 49.054073333740234, s5: 9.594146728515625  
depth: 2, iteration: 672000, test\_RMSE: 1.2421170473098755, erank: 4.7932505607  
60498, s1: 49.109771728515625, s5: 9.765318870544434  
depth: 2, iteration: 674000, test\_RMSE: 1.243109941482544, erank: 4.80267095565  
7959, s1: 49.1636848449707, s5: 9.93810749053955  
depth: 2, iteration: 676000, test\_RMSE: 1.2440946102142334, erank: 4.8119769096  
37451, s1: 49.216827392578125, s5: 10.112431526184082  
depth: 2, iteration: 678000, test\_RMSE: 1.2450709342956543, erank: 4.8211731910  
70557, s1: 49.26862716674805, s5: 10.28825855255127  
depth: 2, iteration: 680000, test\_RMSE: 1.246038794517517, erank: 4.83025932312  
0117, s1: 49.3187255859375, s5: 10.465548515319824  
depth: 2, iteration: 682000, test\_RMSE: 1.2469991445541382, erank: 4.8392386436  
4624, s1: 49.367454528808594, s5: 10.64431095123291  
depth: 2, iteration: 684000, test\_RMSE: 1.2479522228240967, erank: 4.8481125831  
604, s1: 49.415122985839844, s5: 10.82441234588623  
depth: 2, iteration: 686000, test\_RMSE: 1.2488970756530762, erank: 4.8568620681  
762695, s1: 49.46221160888672, s5: 11.005888938903809  
depth: 2, iteration: 688000, test\_RMSE: 1.2498339414596558, erank: 4.8655071258  
54492, s1: 49.507911682128906, s5: 11.1886625289917  
depth: 2, iteration: 690000, test\_RMSE: 1.2507643699645996, erank: 4.8740401268  
00537, s1: 49.55230712890625, s5: 11.372823715209961  
depth: 2, iteration: 692000, test\_RMSE: 1.2516872882843018, erank: 4.8824539184  
57031, s1: 49.59550094604492, s5: 11.55805778503418  
depth: 2, iteration: 694000, test\_RMSE: 1.252602219581604, erank: 4.89078044891  
3574, s1: 49.637577056884766, s5: 11.744680404663086  
depth: 2, iteration: 696000, test\_RMSE: 1.2535098791122437, erank: 4.8989748954  
77295, s1: 49.67918014526367, s5: 11.932263374328613  
depth: 2, iteration: 698000, test\_RMSE: 1.2544095516204834, erank: 4.9070816040

03906, s1: 49.7184944152832, s5: 12.12106990814209  
depth: 2, iteration: 700000, test\_RMSE: 1.2553033828735352, erank: 4.9150500297  
54639, s1: 49.7583122253418, s5: 12.310751914978027  
depth: 2, iteration: 702000, test\_RMSE: 1.2561899423599243, erank: 4.9229259490  
9668, s1: 49.796409606933594, s5: 12.501639366149902  
depth: 2, iteration: 704000, test\_RMSE: 1.2570703029632568, erank: 4.9306797981  
26221, s1: 49.834354400634766, s5: 12.693312644958496  
depth: 2, iteration: 706000, test\_RMSE: 1.2579433917999268, erank: 4.9383325576  
78223, s1: 49.87033462524414, s5: 12.885892868041992  
depth: 2, iteration: 708000, test\_RMSE: 1.2588104009628296, erank: 4.9458565711  
9751, s1: 49.90684127807617, s5: 13.079380989074707  
depth: 2, iteration: 710000, test\_RMSE: 1.259670615196228, erank: 4.95328903198  
2422, s1: 49.94176483154297, s5: 13.273691177368164  
depth: 2, iteration: 712000, test\_RMSE: 1.2605242729187012, erank: 4.9606099128  
723145, s1: 49.975914001464844, s5: 13.468838691711426  
depth: 2, iteration: 714000, test\_RMSE: 1.2613720893859863, erank: 4.9678287506  
10352, s1: 50.00863265991211, s5: 13.664477348327637  
depth: 2, iteration: 716000, test\_RMSE: 1.2622134685516357, erank: 4.9749231338  
50098, s1: 50.041629791259766, s5: 13.860967636108398  
depth: 2, iteration: 718000, test\_RMSE: 1.263048529624939, erank: 4.98191738128  
6621, s1: 50.073486328125, s5: 14.057855606079102  
depth: 2, iteration: 720000, test\_RMSE: 1.263878345489502, erank: 4.98880100250  
2441, s1: 50.104522705078125, s5: 14.255263328552246  
depth: 2, iteration: 722000, test\_RMSE: 1.2647018432617188, erank: 4.9955735206  
604, s1: 50.135005950927734, s5: 14.453232765197754  
depth: 2, iteration: 724000, test\_RMSE: 1.265519142150879, erank: 5.00220966339  
1113, s1: 50.16497039794922, s5: 14.650203704833984  
depth: 2, iteration: 726000, test\_RMSE: 1.266330361366272, erank: 5.00879383087  
1582, s1: 50.19515609741211, s5: 14.850200653076172  
depth: 2, iteration: 728000, test\_RMSE: 1.2671359777450562, erank: 5.0152583122  
25342, s1: 50.22356414794922, s5: 15.049517631530762  
depth: 2, iteration: 730000, test\_RMSE: 1.2679364681243896, erank: 5.0216135978  
69873, s1: 50.251522064208984, s5: 15.248839378356934  
depth: 2, iteration: 732000, test\_RMSE: 1.268731713294983, erank: 5.02785682678  
2227, s1: 50.27947235107422, s5: 15.448271751403809  
depth: 2, iteration: 734000, test\_RMSE: 1.2695205211639404, erank: 5.0340032577  
51465, s1: 50.3064079284668, s5: 15.647919654846191  
depth: 2, iteration: 736000, test\_RMSE: 1.2703039646148682, erank: 5.0400424003  
60107, s1: 50.332481384277344, s5: 15.84760856628418  
depth: 2, iteration: 738000, test\_RMSE: 1.271081805229187, erank: 5.04597616195  
6787, s1: 50.359100341796875, s5: 16.047685623168945  
depth: 2, iteration: 740000, test\_RMSE: 1.271854043006897, erank: 5.05180883407  
5928, s1: 50.3842658996582, s5: 16.24720573425293  
depth: 2, iteration: 742000, test\_RMSE: 1.2726209163665771, erank: 5.0575418472  
29004, s1: 50.40944290161133, s5: 16.446876525878906  
depth: 2, iteration: 744000, test\_RMSE: 1.2733820676803589, erank: 5.0631756782  
53174, s1: 50.434017181396484, s5: 16.646404266357422  
depth: 2, iteration: 746000, test\_RMSE: 1.2741384506225586, erank: 5.0687217712  
40234, s1: 50.45806121826172, s5: 16.84580421447754  
depth: 2, iteration: 748000, test\_RMSE: 1.2748894691467285, erank: 5.0741715431  
21338, s1: 50.48105239868164, s5: 17.044870376586914  
depth: 2, iteration: 750000, test\_RMSE: 1.275634765625, erank: 5.07951879501342  
8, s1: 50.50404739379883, s5: 17.24344253540039  
depth: 2, iteration: 752000, test\_RMSE: 1.2763744592666626, erank: 5.0847764015



19775, s1: 50.526649475097656, s5: 17.44194793701172  
depth: 2, iteration: 754000, test\_RMSE: 1.2771093845367432, erank: 5.0899338722  
229, s1: 50.54869079589844, s5: 17.639867782592773  
depth: 2, iteration: 756000, test\_RMSE: 1.2778401374816895, erank: 5.0949907302  
856445, s1: 50.570682525634766, s5: 17.83733558654785  
depth: 2, iteration: 758000, test\_RMSE: 1.2785654067993164, erank: 5.0999641418  
45703, s1: 50.59187316894531, s5: 18.0341739654541  
depth: 2, iteration: 760000, test\_RMSE: 1.2792857885360718, erank: 5.1048345565  
7959, s1: 50.613243103027344, s5: 18.23040771484375  
depth: 2, iteration: 762000, test\_RMSE: 1.2800008058547974, erank: 5.1096138954  
1626, s1: 50.63414764404297, s5: 18.425981521606445  
depth: 2, iteration: 764000, test\_RMSE: 1.2807115316390991, erank: 5.1143150329  
58984, s1: 50.65439987182617, s5: 18.62093734741211  
depth: 2, iteration: 766000, test\_RMSE: 1.2814182043075562, erank: 5.1189303398  
13232, s1: 50.674560546875, s5: 18.815629959106445  
depth: 2, iteration: 768000, test\_RMSE: 1.282119631767273, erank: 5.12345457077  
0264, s1: 50.693782806396484, s5: 19.00919532775879  
depth: 2, iteration: 770000, test\_RMSE: 1.2828162908554077, erank: 5.1278867721  
55762, s1: 50.7139778137207, s5: 19.202104568481445  
depth: 2, iteration: 772000, test\_RMSE: 1.28350830078125, erank: 5.132235527038  
574, s1: 50.73311233520508, s5: 19.393993377685547  
depth: 2, iteration: 774000, test\_RMSE: 1.2841956615447998, erank: 5.1365036964  
4165, s1: 50.75171661376953, s5: 19.584928512573242  
depth: 2, iteration: 776000, test\_RMSE: 1.2848776578903198, erank: 5.1406917572  
02148, s1: 50.77029037475586, s5: 19.775108337402344  
depth: 2, iteration: 778000, test\_RMSE: 1.285553216934204, erank: 5.14479541778  
56445, s1: 50.78831100463867, s5: 19.964000701904297  
depth: 2, iteration: 780000, test\_RMSE: 1.286224365234375, erank: 5.14881229400  
6348, s1: 50.806182861328125, s5: 20.15190315246582  
depth: 2, iteration: 782000, test\_RMSE: 1.2868911027908325, erank: 5.1527581214  
904785, s1: 50.82344436645508, s5: 20.338977813720703  
depth: 2, iteration: 784000, test\_RMSE: 1.287553071975708, erank: 5.15661764144  
8975, s1: 50.84089660644531, s5: 20.52471923828125  
depth: 2, iteration: 786000, test\_RMSE: 1.2882102727890015, erank: 5.1604018211  
36475, s1: 50.8579216003418, s5: 20.709362030029297  
depth: 2, iteration: 788000, test\_RMSE: 1.2888634204864502, erank: 5.1641025543  
21289, s1: 50.874759674072266, s5: 20.8927059173584  
depth: 2, iteration: 790000, test\_RMSE: 1.2895126342773438, erank: 5.1677331924  
43848, s1: 50.89174270629883, s5: 21.07496452331543  
depth: 2, iteration: 792000, test\_RMSE: 1.2901569604873657, erank: 5.1712999343  
87207, s1: 50.908172607421875, s5: 21.256332397460938  
depth: 2, iteration: 794000, test\_RMSE: 1.290796160697937, erank: 5.17479085922  
2412, s1: 50.924224853515625, s5: 21.43619155883789  
depth: 2, iteration: 796000, test\_RMSE: 1.2914307117462158, erank: 5.1782083511  
35254, s1: 50.94004821777344, s5: 21.61481285095215  
depth: 2, iteration: 798000, test\_RMSE: 1.2920613288879395, erank: 5.1815433502  
19727, s1: 50.95683288574219, s5: 21.79168701171875

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 2 --lam 0.0 --optim Adam --lr 1e-3 --niters 30000  
depth: 2, iteration: 0, test\_RMSE: 1.123241662979126, erank: 66.58731079101562,  
s1: 0.002587410621345043, s5: 0.002140388358384371  
depth: 2, iteration: 2000, test\_RMSE: 1.3218019008636475, erank: 12.18548965454

1016, s1: 56.586700439453125, s5: 31.40473747253418  
depth: 2, iteration: 4000, test\_RMSE: 1.3218036890029907, erank: 12.18581485748  
291, s1: 56.58657455444336, s5: 31.404823303222656  
depth: 2, iteration: 6000, test\_RMSE: 1.3218035697937012, erank: 12.18580532073  
9746, s1: 56.58660125732422, s5: 31.40477180480957  
depth: 2, iteration: 8000, test\_RMSE: 1.3218036890029907, erank: 12.18583202362  
0605, s1: 56.58653259277344, s5: 31.404489517211914  
depth: 2, iteration: 10000, test\_RMSE: 1.3217896223068237, erank: 12.1862878799  
43848, s1: 56.58448028564453, s5: 31.40440559387207  
depth: 2, iteration: 12000, test\_RMSE: 1.3217631578445435, erank: 12.1888713836  
66992, s1: 56.588375091552734, s5: 31.401304244995117  
depth: 2, iteration: 14000, test\_RMSE: 1.3216009140014648, erank: 12.1947174072  
26562, s1: 56.55916213989258, s5: 31.402374267578125  
depth: 2, iteration: 16000, test\_RMSE: 1.3215597867965698, erank: 12.1990499496  
45996, s1: 56.573646545410156, s5: 31.399080276489258  
depth: 2, iteration: 18000, test\_RMSE: 1.3213802576065063, erank: 12.2055196762  
08496, s1: 56.52980041503906, s5: 31.399749755859375  
depth: 2, iteration: 20000, test\_RMSE: 1.3213927745819092, erank: 12.2092971801  
75781, s1: 56.55703353881836, s5: 31.400169372558594  
depth: 2, iteration: 22000, test\_RMSE: 1.3211970329284668, erank: 12.2159099578  
85742, s1: 56.52116012573242, s5: 31.393829345703125  
depth: 2, iteration: 24000, test\_RMSE: 1.3210071325302124, erank: 12.2225084304  
80957, s1: 56.484275817871094, s5: 31.39174461364746  
depth: 2, iteration: 26000, test\_RMSE: 1.3209697008132935, erank: 12.2269277572  
63184, s1: 56.505126953125, s5: 31.3922061920166  
depth: 2, iteration: 28000, test\_RMSE: 1.3208431005477905, erank: 12.2327299118  
042, s1: 56.48236083984375, s5: 31.388839721679688

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 5 --lam 0.0 --optim GD --lr 1e-3 --niters 800000  
depth: 5, iteration: 0, test\_RMSE: 1.1190418004989624, erank: 44.3781814575195  
3, s1: 0.0033922006841748953, s5: 0.002414506860077381  
depth: 5, iteration: 2000, test\_RMSE: 1.1190418004989624, erank: 44.37757110595  
703, s1: 0.0033928570337593555, s5: 0.00241463421843946  
depth: 5, iteration: 4000, test\_RMSE: 1.1190418004989624, erank: 44.37694168090  
82, s1: 0.003393491031602025, s5: 0.0024147694930434227  
depth: 5, iteration: 6000, test\_RMSE: 1.1190418004989624, erank: 44.37633132934  
57, s1: 0.0033941222354769707, s5: 0.002414935501292348  
depth: 5, iteration: 8000, test\_RMSE: 1.1190418004989624, erank: 44.37559890747  
07, s1: 0.0033947934862226248, s5: 0.0024151168763637543  
depth: 5, iteration: 10000, test\_RMSE: 1.1190418004989624, erank: 44.3748817443  
84766, s1: 0.003395453095436096, s5: 0.002415270311757922  
depth: 5, iteration: 12000, test\_RMSE: 1.1190418004989624, erank: 44.3740959167  
4805, s1: 0.003396125975996256, s5: 0.0024154691491276026  
depth: 5, iteration: 14000, test\_RMSE: 1.1190418004989624, erank: 44.3733253479  
0039, s1: 0.0033967874478548765, s5: 0.0024156542494893074  
depth: 5, iteration: 16000, test\_RMSE: 1.1190418004989624, erank: 44.3725433349  
6094, s1: 0.0033974824473261833, s5: 0.002415885915979743  
depth: 5, iteration: 18000, test\_RMSE: 1.1190418004989624, erank: 44.3717079162  
59766, s1: 0.003398157889023423, s5: 0.0024161161854863167  
depth: 5, iteration: 20000, test\_RMSE: 1.1190418004989624, erank: 44.3707542419  
4336, s1: 0.0033988668583333492, s5: 0.002416362753137946  
depth: 5, iteration: 22000, test\_RMSE: 1.1190418004989624, erank: 44.3698539733

8867, s1: 0.0033995741978287697, s5: 0.00241659814491868  
depth: 5, iteration: 24000, test\_RMSE: 1.1190418004989624, erank: 44.3689575195  
3125, s1: 0.003400275483727455, s5: 0.002416873350739479  
depth: 5, iteration: 26000, test\_RMSE: 1.1190418004989624, erank: 44.3679847717  
28516, s1: 0.0034009560476988554, s5: 0.002417145064100623  
depth: 5, iteration: 28000, test\_RMSE: 1.1190418004989624, erank: 44.3670005798  
33984, s1: 0.0034016950521618128, s5: 0.002417417475953698  
depth: 5, iteration: 30000, test\_RMSE: 1.1190418004989624, erank: 44.3659629821  
77734, s1: 0.0034024266060441732, s5: 0.002417722251266241  
depth: 5, iteration: 32000, test\_RMSE: 1.1190418004989624, erank: 44.3648948669  
4336, s1: 0.0034031597897410393, s5: 0.0024180312175303698  
depth: 5, iteration: 34000, test\_RMSE: 1.1190418004989624, erank: 44.3638343811  
03516, s1: 0.003403879003599286, s5: 0.0024183709174394608  
depth: 5, iteration: 36000, test\_RMSE: 1.1190418004989624, erank: 44.3627166748  
0469, s1: 0.003404623130336404, s5: 0.0024186954833567142  
depth: 5, iteration: 38000, test\_RMSE: 1.1190418004989624, erank: 44.3615722656  
25, s1: 0.003405394032597542, s5: 0.0024190470576286316  
depth: 5, iteration: 40000, test\_RMSE: 1.1190418004989624, erank: 44.3603897094  
72656, s1: 0.0034061481710523367, s5: 0.00241939933039248  
depth: 5, iteration: 42000, test\_RMSE: 1.1190418004989624, erank: 44.3591842651  
3672, s1: 0.003406909527257085, s5: 0.002419765805825591  
depth: 5, iteration: 44000, test\_RMSE: 1.1190418004989624, erank: 44.3579788208  
0078, s1: 0.0034076597075909376, s5: 0.002420164179056883  
depth: 5, iteration: 46000, test\_RMSE: 1.1190418004989624, erank: 44.3566780090  
332, s1: 0.0034084341023117304, s5: 0.0024205443914979696  
depth: 5, iteration: 48000, test\_RMSE: 1.1190418004989624, erank: 44.3553962707  
5195, s1: 0.0034092082642018795, s5: 0.0024209723342210054  
depth: 5, iteration: 50000, test\_RMSE: 1.1190418004989624, erank: 44.3540534973  
1445, s1: 0.003410006407648325, s5: 0.002421384211629629  
depth: 5, iteration: 52000, test\_RMSE: 1.1190418004989624, erank: 44.3526687622  
0703, s1: 0.0034107991959899664, s5: 0.0024218184407800436  
depth: 5, iteration: 54000, test\_RMSE: 1.1190418004989624, erank: 44.3513145446  
77734, s1: 0.0034115908201783895, s5: 0.002422272926196456  
depth: 5, iteration: 56000, test\_RMSE: 1.1190418004989624, erank: 44.3498802185  
0586, s1: 0.003412387100979686, s5: 0.002422739751636982  
depth: 5, iteration: 58000, test\_RMSE: 1.1190418004989624, erank: 44.3484268188  
47656, s1: 0.0034132145810872316, s5: 0.0024232068099081516  
depth: 5, iteration: 60000, test\_RMSE: 1.1190418004989624, erank: 44.3469581604  
0039, s1: 0.003414023434743285, s5: 0.002423695055767894  
depth: 5, iteration: 62000, test\_RMSE: 1.1190418004989624, erank: 44.3454589843  
75, s1: 0.0034148520790040493, s5: 0.0024241660721600056  
depth: 5, iteration: 64000, test\_RMSE: 1.1190418004989624, erank: 44.3439025878  
90625, s1: 0.003415695857256651, s5: 0.0024246980901807547  
depth: 5, iteration: 66000, test\_RMSE: 1.1190418004989624, erank: 44.3422660827  
6367, s1: 0.003416521707549691, s5: 0.0024252254515886307  
depth: 5, iteration: 68000, test\_RMSE: 1.1190418004989624, erank: 44.3407669067  
3828, s1: 0.003417385509237647, s5: 0.0024257362820208073  
depth: 5, iteration: 70000, test\_RMSE: 1.1190418004989624, erank: 44.3390502929  
6875, s1: 0.0034182334784418344, s5: 0.0024262883234769106  
depth: 5, iteration: 72000, test\_RMSE: 1.1190418004989624, erank: 44.3374023437  
5, s1: 0.0034191147424280643, s5: 0.002426826860755682  
depth: 5, iteration: 74000, test\_RMSE: 1.1190418004989624, erank: 44.3357772827  
14844, s1: 0.0034199676010757685, s5: 0.002427408704534173  
depth: 5, iteration: 76000, test\_RMSE: 1.1190418004989624, erank: 44.3340225219

72656, s1: 0.003420873312279582, s5: 0.002427983796223998  
depth: 5, iteration: 78000, test\_RMSE: 1.1190418004989624, erank: 44.3322219848  
6328, s1: 0.003421757137402892, s5: 0.002428583335131407  
depth: 5, iteration: 80000, test\_RMSE: 1.1190418004989624, erank: 44.3304901123  
0469, s1: 0.003422666108235717, s5: 0.0024291689042001963  
depth: 5, iteration: 82000, test\_RMSE: 1.1190418004989624, erank: 44.3286628723  
1445, s1: 0.0034235480707138777, s5: 0.0024298045318573713  
depth: 5, iteration: 84000, test\_RMSE: 1.1190418004989624, erank: 44.3268241882  
3242, s1: 0.0034244635608047247, s5: 0.0024304210674017668  
depth: 5, iteration: 86000, test\_RMSE: 1.1190418004989624, erank: 44.3249740600  
58594, s1: 0.0034253804478794336, s5: 0.0024310618173331022  
depth: 5, iteration: 88000, test\_RMSE: 1.1190418004989624, erank: 44.3230934143  
0664, s1: 0.0034263061825186014, s5: 0.002431709785014391  
depth: 5, iteration: 90000, test\_RMSE: 1.1190418004989624, erank: 44.3211708068  
84766, s1: 0.003427231451496482, s5: 0.002432384295389056  
depth: 5, iteration: 92000, test\_RMSE: 1.1190418004989624, erank: 44.3192024230  
957, s1: 0.0034281802363693714, s5: 0.002433063695207238  
depth: 5, iteration: 94000, test\_RMSE: 1.1190418004989624, erank: 44.3172073364  
2578, s1: 0.003429120173677802, s5: 0.0024337489157915115  
depth: 5, iteration: 96000, test\_RMSE: 1.1190418004989624, erank: 44.3152389526  
3672, s1: 0.003430065931752324, s5: 0.0024344611447304487  
depth: 5, iteration: 98000, test\_RMSE: 1.1190418004989624, erank: 44.3132209777  
832, s1: 0.0034310088958591223, s5: 0.0024351736065000296  
depth: 5, iteration: 100000, test\_RMSE: 1.1190418004989624, erank: 44.311130523  
68164, s1: 0.0034319853875786066, s5: 0.002435911213979125  
depth: 5, iteration: 102000, test\_RMSE: 1.1190418004989624, erank: 44.309040069  
58008, s1: 0.00343296374194324, s5: 0.0024366413708776236  
depth: 5, iteration: 104000, test\_RMSE: 1.1190418004989624, erank: 44.306930541  
99219, s1: 0.00343391764909029, s5: 0.002437400398775935  
depth: 5, iteration: 106000, test\_RMSE: 1.1190418004989624, erank: 44.304782867  
43164, s1: 0.00343490531668067, s5: 0.002438183641061187  
depth: 5, iteration: 108000, test\_RMSE: 1.1190418004989624, erank: 44.302616119  
384766, s1: 0.003435884602367878, s5: 0.0024389412719756365  
depth: 5, iteration: 110000, test\_RMSE: 1.1190418004989624, erank: 44.300411224  
365234, s1: 0.003436870640143752, s5: 0.0024397592060267925  
depth: 5, iteration: 112000, test\_RMSE: 1.1190418004989624, erank: 44.298171997  
07031, s1: 0.003437869716435671, s5: 0.002440547803416848  
depth: 5, iteration: 114000, test\_RMSE: 1.1190418004989624, erank: 44.295886993  
4082, s1: 0.003438887419179082, s5: 0.0024413897190243006  
depth: 5, iteration: 116000, test\_RMSE: 1.1190418004989624, erank: 44.293556213  
378906, s1: 0.0034399277064949274, s5: 0.002442223485559225  
depth: 5, iteration: 118000, test\_RMSE: 1.1190418004989624, erank: 44.291221618  
652344, s1: 0.0034409519284963608, s5: 0.0024430935736745596  
depth: 5, iteration: 120000, test\_RMSE: 1.1190418004989624, erank: 44.288837432  
86133, s1: 0.0034419840667396784, s5: 0.002443956909701228  
depth: 5, iteration: 122000, test\_RMSE: 1.1190418004989624, erank: 44.286460876  
464844, s1: 0.0034430345986038446, s5: 0.002444847021251917  
depth: 5, iteration: 124000, test\_RMSE: 1.1190418004989624, erank: 44.284019470  
214844, s1: 0.0034440727904438972, s5: 0.0024457299150526524  
depth: 5, iteration: 126000, test\_RMSE: 1.1190418004989624, erank: 44.281581878  
66211, s1: 0.00344513775780797, s5: 0.0024466149043291807  
depth: 5, iteration: 128000, test\_RMSE: 1.1190418004989624, erank: 44.279067993  
16406, s1: 0.003446197835728526, s5: 0.002447534818202257  
depth: 5, iteration: 130000, test\_RMSE: 1.1190418004989624, erank: 44.276565551

75781, s1: 0.003447265364229679, s5: 0.0024484735913574696  
depth: 5, iteration: 132000, test\_RMSE: 1.1190418004989624, erank: 44.273960113  
52539, s1: 0.003448343137279153, s5: 0.0024493986275047064  
depth: 5, iteration: 134000, test\_RMSE: 1.1190418004989624, erank: 44.271427154  
541016, s1: 0.0034494332503527403, s5: 0.002450318541377783  
depth: 5, iteration: 136000, test\_RMSE: 1.1190418004989624, erank: 44.268806457  
51953, s1: 0.003450539894402027, s5: 0.0024512920062988997  
depth: 5, iteration: 138000, test\_RMSE: 1.1190418004989624, erank: 44.266136169  
433594, s1: 0.0034516246523708105, s5: 0.002452271990478039  
depth: 5, iteration: 140000, test\_RMSE: 1.1190418004989624, erank: 44.263500213  
62305, s1: 0.0034527601674199104, s5: 0.0024532382376492023  
depth: 5, iteration: 142000, test\_RMSE: 1.1190418004989624, erank: 44.260807037  
353516, s1: 0.003453847486525774, s5: 0.0024542200844734907  
depth: 5, iteration: 144000, test\_RMSE: 1.1190418004989624, erank: 44.258129119  
87305, s1: 0.0034549913834780455, s5: 0.0024552394170314074  
depth: 5, iteration: 146000, test\_RMSE: 1.1190418004989624, erank: 44.255363464  
35547, s1: 0.0034561019856482744, s5: 0.0024562543258070946  
depth: 5, iteration: 148000, test\_RMSE: 1.1190418004989624, erank: 44.252548217  
77344, s1: 0.003457245882600546, s5: 0.002457310678437352  
depth: 5, iteration: 150000, test\_RMSE: 1.1190418004989624, erank: 44.249759674  
072266, s1: 0.0034583774395287037, s5: 0.0024583558551967144  
depth: 5, iteration: 152000, test\_RMSE: 1.1190418004989624, erank: 44.246925354  
003906, s1: 0.0034595313481986523, s5: 0.0024594159331172705  
depth: 5, iteration: 154000, test\_RMSE: 1.1190418004989624, erank: 44.244098663  
33008, s1: 0.003460667561739683, s5: 0.002460507908836007  
depth: 5, iteration: 156000, test\_RMSE: 1.1190418004989624, erank: 44.241230010  
98633, s1: 0.0034618168137967587, s5: 0.002461578929796815  
depth: 5, iteration: 158000, test\_RMSE: 1.1190418004989624, erank: 44.238296508  
78906, s1: 0.003463003085926175, s5: 0.0024626904632896185  
depth: 5, iteration: 160000, test\_RMSE: 1.1190418004989624, erank: 44.235332489  
01367, s1: 0.0034641579259186983, s5: 0.0024638064205646515  
depth: 5, iteration: 162000, test\_RMSE: 1.1190418004989624, erank: 44.232391357  
421875, s1: 0.003465348621830344, s5: 0.0024649070110172033  
depth: 5, iteration: 164000, test\_RMSE: 1.1190418004989624, erank: 44.229373931  
884766, s1: 0.0034665714483708143, s5: 0.002466043923050165  
depth: 5, iteration: 166000, test\_RMSE: 1.1190418004989624, erank: 44.226367950  
43945, s1: 0.003467713249847293, s5: 0.0024672127328813076  
depth: 5, iteration: 168000, test\_RMSE: 1.1190418004989624, erank: 44.223320007  
32422, s1: 0.003468916052952409, s5: 0.00246836943551898  
depth: 5, iteration: 170000, test\_RMSE: 1.1190418004989624, erank: 44.220306396  
484375, s1: 0.003470106516033411, s5: 0.0024695314932614565  
depth: 5, iteration: 172000, test\_RMSE: 1.1190418004989624, erank: 44.217144012  
45117, s1: 0.003471310483291745, s5: 0.0024707240518182516  
depth: 5, iteration: 174000, test\_RMSE: 1.1190418004989624, erank: 44.213958740  
234375, s1: 0.0034725351724773645, s5: 0.0024719315115362406  
depth: 5, iteration: 176000, test\_RMSE: 1.1190418004989624, erank: 44.210849761  
96289, s1: 0.003473712131381035, s5: 0.002473129890859127  
depth: 5, iteration: 178000, test\_RMSE: 1.1190418004989624, erank: 44.207679748  
535156, s1: 0.0034749626647681, s5: 0.0024743296671658754  
depth: 5, iteration: 180000, test\_RMSE: 1.1190418004989624, erank: 44.204433441  
16211, s1: 0.0034761896822601557, s5: 0.0024755988270044327  
depth: 5, iteration: 182000, test\_RMSE: 1.1190418004989624, erank: 44.201164245  
60547, s1: 0.0034774341620504856, s5: 0.002476834924891591  
depth: 5, iteration: 184000, test\_RMSE: 1.1190418004989624, erank: 44.197864532

4707, s1: 0.0034786947071552277, s5: 0.0024780724197626114  
depth: 5, iteration: 186000, test\_RMSE: 1.1190418004989624, erank: 44.194568634  
0332, s1: 0.003479942912235856, s5: 0.0024793606717139482  
depth: 5, iteration: 188000, test\_RMSE: 1.1190418004989624, erank: 44.191219329  
833984, s1: 0.003481220221146941, s5: 0.0024806540459394455  
depth: 5, iteration: 190000, test\_RMSE: 1.1190418004989624, erank: 44.187824249  
26758, s1: 0.003482513828203082, s5: 0.002481941832229495  
depth: 5, iteration: 192000, test\_RMSE: 1.1190418004989624, erank: 44.184440612  
79297, s1: 0.003483812091872096, s5: 0.0024832328781485558  
depth: 5, iteration: 194000, test\_RMSE: 1.1190418004989624, erank: 44.181011199  
95117, s1: 0.0034850917290896177, s5: 0.0024845264852046967  
depth: 5, iteration: 196000, test\_RMSE: 1.1190418004989624, erank: 44.177532196  
04492, s1: 0.0034864041954278946, s5: 0.002485863398760557  
depth: 5, iteration: 198000, test\_RMSE: 1.1190418004989624, erank: 44.174110412  
597656, s1: 0.003487688722088933, s5: 0.002487179823219776  
depth: 5, iteration: 200000, test\_RMSE: 1.1190418004989624, erank: 44.170539855  
95703, s1: 0.003489036811515689, s5: 0.002488546771928668  
depth: 5, iteration: 202000, test\_RMSE: 1.1190418004989624, erank: 44.167053222  
65625, s1: 0.0034903164487332106, s5: 0.002489908365532756  
depth: 5, iteration: 204000, test\_RMSE: 1.1190418004989624, erank: 44.163494110  
10742, s1: 0.003491673618555069, s5: 0.0024912634398788214  
depth: 5, iteration: 206000, test\_RMSE: 1.1190418004989624, erank: 44.159820556  
640625, s1: 0.003492997959256172, s5: 0.002492687664926052  
depth: 5, iteration: 208000, test\_RMSE: 1.1190418004989624, erank: 44.15625, s  
1: 0.0034943323116749525, s5: 0.0024940697476267815  
depth: 5, iteration: 210000, test\_RMSE: 1.1190418004989624, erank: 44.152587890  
625, s1: 0.0034956804011017084, s5: 0.0024954902473837137  
depth: 5, iteration: 212000, test\_RMSE: 1.1190418004989624, erank: 44.148818969  
72656, s1: 0.0034970855340361595, s5: 0.0024969312362372875  
depth: 5, iteration: 214000, test\_RMSE: 1.1190418004989624, erank: 44.145206451  
416016, s1: 0.00349843199364841, s5: 0.0024983221665024757  
depth: 5, iteration: 216000, test\_RMSE: 1.1190418004989624, erank: 44.141483306  
884766, s1: 0.003499793354421854, s5: 0.002499761525541544  
depth: 5, iteration: 218000, test\_RMSE: 1.1190418004989624, erank: 44.137653350  
83008, s1: 0.003501185914501548, s5: 0.002501235343515873  
depth: 5, iteration: 220000, test\_RMSE: 1.1190418004989624, erank: 44.133895874  
02344, s1: 0.0035025642719119787, s5: 0.0025026812218129635  
depth: 5, iteration: 222000, test\_RMSE: 1.1190418004989624, erank: 44.130065917  
96875, s1: 0.0035039654467254877, s5: 0.002504186239093542  
depth: 5, iteration: 224000, test\_RMSE: 1.1190418004989624, erank: 44.126224517  
822266, s1: 0.0035053803585469723, s5: 0.002505689160898328  
depth: 5, iteration: 226000, test\_RMSE: 1.1190418004989624, erank: 44.122333526  
61133, s1: 0.0035067794378846884, s5: 0.0025071981362998486  
depth: 5, iteration: 228000, test\_RMSE: 1.1190418004989624, erank: 44.118396759  
0332, s1: 0.003508207621052861, s5: 0.0025087029207497835  
depth: 5, iteration: 230000, test\_RMSE: 1.1190418004989624, erank: 44.114444732  
666016, s1: 0.003509634407237172, s5: 0.002510222140699625  
depth: 5, iteration: 232000, test\_RMSE: 1.1190418004989624, erank: 44.110481262  
20703, s1: 0.0035110691096633673, s5: 0.002511761849746108  
depth: 5, iteration: 234000, test\_RMSE: 1.1190418004989624, erank: 44.106430053  
71094, s1: 0.00351254316046834, s5: 0.0025132931768894196  
depth: 5, iteration: 236000, test\_RMSE: 1.1190418004989624, erank: 44.102394104  
003906, s1: 0.0035139978863298893, s5: 0.0025148470886051655  
depth: 5, iteration: 238000, test\_RMSE: 1.1190418004989624, erank: 44.098335266

11328, s1: 0.0035154595971107483, s5: 0.0025164138060063124  
depth: 5, iteration: 240000, test\_RMSE: 1.1190418004989624, erank: 44.094223022  
46094, s1: 0.0035169224720448256, s5: 0.002517998917028308  
depth: 5, iteration: 242000, test\_RMSE: 1.1190418004989624, erank: 44.090061187  
74414, s1: 0.003518415614962578, s5: 0.0025195784401148558  
depth: 5, iteration: 244000, test\_RMSE: 1.1190418004989624, erank: 44.085876464  
84375, s1: 0.0035199071280658245, s5: 0.002521181246265769  
depth: 5, iteration: 246000, test\_RMSE: 1.1190418004989624, erank: 44.081691741  
94336, s1: 0.0035214268136769533, s5: 0.002522802446037531  
depth: 5, iteration: 248000, test\_RMSE: 1.1190418004989624, erank: 44.077449798  
583984, s1: 0.0035229509230703115, s5: 0.002524410840123892  
depth: 5, iteration: 250000, test\_RMSE: 1.1190418004989624, erank: 44.073192596  
43555, s1: 0.0035244475584477186, s5: 0.0025260495021939278  
depth: 5, iteration: 252000, test\_RMSE: 1.1190418004989624, erank: 44.068927764  
89258, s1: 0.003525984939187765, s5: 0.0025276849046349525  
depth: 5, iteration: 254000, test\_RMSE: 1.1190418004989624, erank: 44.064563751  
2207, s1: 0.003527543507516384, s5: 0.002529331250116229  
depth: 5, iteration: 256000, test\_RMSE: 1.1190418004989624, erank: 44.060218811  
035156, s1: 0.0035290780942887068, s5: 0.0025309764314442873  
depth: 5, iteration: 258000, test\_RMSE: 1.1190418004989624, erank: 44.055866241  
45508, s1: 0.003530639922246337, s5: 0.0025326665490865707  
depth: 5, iteration: 260000, test\_RMSE: 1.1190418004989624, erank: 44.051433563  
23242, s1: 0.003532205708324909, s5: 0.0025343364104628563  
depth: 5, iteration: 262000, test\_RMSE: 1.1190418004989624, erank: 44.046951293  
94531, s1: 0.00353377778083086, s5: 0.0025360395666211843  
depth: 5, iteration: 264000, test\_RMSE: 1.1190418004989624, erank: 44.042510986  
328125, s1: 0.0035353766288608313, s5: 0.0025377434212714434  
depth: 5, iteration: 266000, test\_RMSE: 1.1190418004989624, erank: 44.038024902  
34375, s1: 0.0035369605757296085, s5: 0.002539438894018531  
depth: 5, iteration: 268000, test\_RMSE: 1.1190418004989624, erank: 44.033458709  
7168, s1: 0.0035385596565902233, s5: 0.0025411697570234537  
depth: 5, iteration: 270000, test\_RMSE: 1.1190418004989624, erank: 44.028911590  
57617, s1: 0.0035401994828134775, s5: 0.002542884089052677  
depth: 5, iteration: 272000, test\_RMSE: 1.1190418004989624, erank: 44.024307250  
97656, s1: 0.0035418274346739054, s5: 0.002544647315517068  
depth: 5, iteration: 274000, test\_RMSE: 1.1190418004989624, erank: 44.019687652  
58789, s1: 0.0035434651654213667, s5: 0.0025463697966188192  
depth: 5, iteration: 276000, test\_RMSE: 1.1190418004989624, erank: 44.015026092  
5293, s1: 0.003545094281435013, s5: 0.00254812091588974  
depth: 5, iteration: 278000, test\_RMSE: 1.1190418004989624, erank: 44.010391235  
35156, s1: 0.003546785796061158, s5: 0.0025498729664832354  
depth: 5, iteration: 280000, test\_RMSE: 1.1190418004989624, erank: 44.005664825  
43945, s1: 0.0035484363324940205, s5: 0.002551644342020154  
depth: 5, iteration: 282000, test\_RMSE: 1.1190418004989624, erank: 44.000968933  
10547, s1: 0.0035501669626682997, s5: 0.002553400117903948  
depth: 5, iteration: 284000, test\_RMSE: 1.1190418004989624, erank: 43.996162414  
55078, s1: 0.0035518240183591843, s5: 0.0025551929138600826  
depth: 5, iteration: 286000, test\_RMSE: 1.1190418004989624, erank: 43.991359710  
69336, s1: 0.0035535546485334635, s5: 0.0025569910649210215  
depth: 5, iteration: 288000, test\_RMSE: 1.1190418004989624, erank: 43.986522674  
56055, s1: 0.003555262228474021, s5: 0.0025587768759578466  
depth: 5, iteration: 290000, test\_RMSE: 1.1190418004989624, erank: 43.981658935  
546875, s1: 0.00355696864426136, s5: 0.002560570603236556  
depth: 5, iteration: 292000, test\_RMSE: 1.1190418004989624, erank: 43.976760864

25781, s1: 0.003558723721653223, s5: 0.0025623792316764593  
depth: 5, iteration: 294000, test\_RMSE: 1.1190418004989624, erank: 43.971855163  
57422, s1: 0.0035604415461421013, s5: 0.0025641920510679483  
depth: 5, iteration: 296000, test\_RMSE: 1.1190418004989624, erank: 43.966918945  
3125, s1: 0.003562162397429347, s5: 0.002566027222201228  
depth: 5, iteration: 298000, test\_RMSE: 1.1190418004989624, erank: 43.961948394  
77539, s1: 0.003563930047675967, s5: 0.00256783957593143  
depth: 5, iteration: 300000, test\_RMSE: 1.1190418004989624, erank: 43.956951141  
35742, s1: 0.0035657130647450686, s5: 0.0025696423836052418  
depth: 5, iteration: 302000, test\_RMSE: 1.1190418004989624, erank: 43.951908111  
572266, s1: 0.0035674991086125374, s5: 0.0025714689400047064  
depth: 5, iteration: 304000, test\_RMSE: 1.1190418004989624, erank: 43.946857452  
39258, s1: 0.003569272579625249, s5: 0.002573317149654031  
depth: 5, iteration: 306000, test\_RMSE: 1.1190418004989624, erank: 43.941722869  
87305, s1: 0.0035710802767425776, s5: 0.0025751322973519564  
depth: 5, iteration: 308000, test\_RMSE: 1.1190418004989624, erank: 43.936573028  
56445, s1: 0.003572897519916296, s5: 0.0025769781786948442  
depth: 5, iteration: 310000, test\_RMSE: 1.1190418004989624, erank: 43.931404113  
76953, s1: 0.003574739210307598, s5: 0.0025787954218685627  
depth: 5, iteration: 312000, test\_RMSE: 1.1190418004989624, erank: 43.926242828  
36914, s1: 0.003576558083295822, s5: 0.002580622909590602  
depth: 5, iteration: 314000, test\_RMSE: 1.1190418004989624, erank: 43.920997619  
628906, s1: 0.0035784454084932804, s5: 0.002582462504506111  
depth: 5, iteration: 316000, test\_RMSE: 1.1190418004989624, erank: 43.915740966  
796875, s1: 0.003580262651666999, s5: 0.00258431164547801  
depth: 5, iteration: 318000, test\_RMSE: 1.1190418004989624, erank: 43.910442352  
29492, s1: 0.0035821632482111454, s5: 0.002586134010925889  
depth: 5, iteration: 320000, test\_RMSE: 1.1190418004989624, erank: 43.905136108  
39844, s1: 0.003584041027352214, s5: 0.0025879652239382267  
depth: 5, iteration: 322000, test\_RMSE: 1.1190418004989624, erank: 43.899765014  
64844, s1: 0.0035859481431543827, s5: 0.002589787822216749  
depth: 5, iteration: 324000, test\_RMSE: 1.1190418004989624, erank: 43.894382476  
80664, s1: 0.003587809856981039, s5: 0.0025916218291968107  
depth: 5, iteration: 326000, test\_RMSE: 1.119041919708252, erank: 43.8890380859  
375, s1: 0.0035896324552595615, s5: 0.0025934174191206694  
depth: 5, iteration: 328000, test\_RMSE: 1.119041919708252, erank: 43.8835678100  
58594, s1: 0.003591691143810749, s5: 0.0025952409487217665  
depth: 5, iteration: 330000, test\_RMSE: 1.119041919708252, erank: 43.8780403137  
207, s1: 0.003593625733628869, s5: 0.002597056794911623  
depth: 5, iteration: 332000, test\_RMSE: 1.1190418004989624, erank: 43.872581481  
933594, s1: 0.003595562418922782, s5: 0.0025988505221903324  
depth: 5, iteration: 334000, test\_RMSE: 1.119041919708252, erank: 43.8670997619  
6289, s1: 0.0035975356586277485, s5: 0.0026006451807916164  
depth: 5, iteration: 336000, test\_RMSE: 1.1190418004989624, erank: 43.861545562  
74414, s1: 0.003599518910050392, s5: 0.002602405147626996  
depth: 5, iteration: 338000, test\_RMSE: 1.1190418004989624, erank: 43.855911254  
88281, s1: 0.0036015163641422987, s5: 0.0026041732635349035  
depth: 5, iteration: 340000, test\_RMSE: 1.1190418004989624, erank: 43.850265502  
92969, s1: 0.0036035445518791676, s5: 0.0026059402152895927  
depth: 5, iteration: 342000, test\_RMSE: 1.1190418004989624, erank: 43.844684600  
83008, s1: 0.00360554619692266, s5: 0.002607691567391157  
depth: 5, iteration: 344000, test\_RMSE: 1.1190418004989624, erank: 43.838966369  
628906, s1: 0.003607600461691618, s5: 0.0026094233617186546  
depth: 5, iteration: 346000, test\_RMSE: 1.1190418004989624, erank: 43.833301544



18945, s1: 0.0036096128169447184, s5: 0.0026111507322639227  
depth: 5, iteration: 348000, test\_RMSE: 1.1190418004989624, erank: 43.827522277  
83203, s1: 0.0036117159761488438, s5: 0.002612868556752801  
depth: 5, iteration: 350000, test\_RMSE: 1.1190418004989624, erank: 43.821735382  
08008, s1: 0.0036138310097157955, s5: 0.002614542143419385  
depth: 5, iteration: 352000, test\_RMSE: 1.119041919708252, erank: 43.8159675598  
1445, s1: 0.003615883644670248, s5: 0.002616202225908637  
depth: 5, iteration: 354000, test\_RMSE: 1.1190418004989624, erank: 43.810104370  
11719, s1: 0.003617999143898487, s5: 0.00261786300688982  
depth: 5, iteration: 356000, test\_RMSE: 1.1190418004989624, erank: 43.804218292  
23633, s1: 0.003620090428739786, s5: 0.002619503764435649  
depth: 5, iteration: 358000, test\_RMSE: 1.1190418004989624, erank: 43.798316955  
566406, s1: 0.0036222264170646667, s5: 0.002621108666062355  
depth: 5, iteration: 360000, test\_RMSE: 1.1190418004989624, erank: 43.792366027  
83203, s1: 0.0036243388894945383, s5: 0.0026227158959954977  
depth: 5, iteration: 362000, test\_RMSE: 1.1190418004989624, erank: 43.786445617  
67578, s1: 0.00362645392306149, s5: 0.002624283079057932  
depth: 5, iteration: 364000, test\_RMSE: 1.1190418004989624, erank: 43.780445098  
87695, s1: 0.0036286169197410345, s5: 0.002625834196805954  
depth: 5, iteration: 366000, test\_RMSE: 1.1190418004989624, erank: 43.774433135  
98633, s1: 0.003630795981734991, s5: 0.0026273548137396574  
depth: 5, iteration: 368000, test\_RMSE: 1.1190418004989624, erank: 43.768337249  
75586, s1: 0.003632958512753248, s5: 0.0026288407389074564  
depth: 5, iteration: 370000, test\_RMSE: 1.1190418004989624, erank: 43.762245178  
222656, s1: 0.0036351631861180067, s5: 0.002630321541801095  
depth: 5, iteration: 372000, test\_RMSE: 1.1190418004989624, erank: 43.756160736  
083984, s1: 0.0036373548209667206, s5: 0.0026317760348320007  
depth: 5, iteration: 374000, test\_RMSE: 1.1190418004989624, erank: 43.749992370  
60547, s1: 0.0036395585630089045, s5: 0.002633207244798541  
depth: 5, iteration: 376000, test\_RMSE: 1.1190418004989624, erank: 43.743831634  
521484, s1: 0.003641788847744465, s5: 0.0026345811784267426  
depth: 5, iteration: 378000, test\_RMSE: 1.1190418004989624, erank: 43.737541198  
73047, s1: 0.003644044976681471, s5: 0.0026359285693615675  
depth: 5, iteration: 380000, test\_RMSE: 1.119041919708252, erank: 43.7312965393  
0664, s1: 0.0036462931893765926, s5: 0.0026372638531029224  
depth: 5, iteration: 382000, test\_RMSE: 1.119041919708252, erank: 43.7249679565  
4297, s1: 0.003648550482466817, s5: 0.0026385746896266937  
depth: 5, iteration: 384000, test\_RMSE: 1.119041919708252, erank: 43.7186088562  
0117, s1: 0.00365085550583899, s5: 0.0026398550253361464  
depth: 5, iteration: 386000, test\_RMSE: 1.119041919708252, erank: 43.7123336791  
9922, s1: 0.003653148887678981, s5: 0.002641082275658846  
depth: 5, iteration: 388000, test\_RMSE: 1.119041919708252, erank: 43.7058563232  
4219, s1: 0.003655466716736555, s5: 0.0026422906666994095  
depth: 5, iteration: 390000, test\_RMSE: 1.119041919708252, erank: 43.6994781494  
1406, s1: 0.0036577603314071894, s5: 0.0026434538885951042  
depth: 5, iteration: 392000, test\_RMSE: 1.119041919708252, erank: 43.6930465698  
2422, s1: 0.0036601065658032894, s5: 0.0026446054689586163  
depth: 5, iteration: 394000, test\_RMSE: 1.119041919708252, erank: 43.6865501403  
8086, s1: 0.003662438364699483, s5: 0.0026457204949110746  
depth: 5, iteration: 396000, test\_RMSE: 1.119041919708252, erank: 43.6800575256  
34766, s1: 0.0036648043897002935, s5: 0.0026467943098396063  
depth: 5, iteration: 398000, test\_RMSE: 1.119041919708252, erank: 43.6735534667  
96875, s1: 0.003667151555418968, s5: 0.00264785741455853  
depth: 5, iteration: 400000, test\_RMSE: 1.119041919708252, erank: 43.6669578552

2461, s1: 0.00366957182995975, s5: 0.0026488699950277805  
depth: 5, iteration: 402000, test\_RMSE: 1.119041919708252, erank: 43.6603622436  
52344, s1: 0.0036719748750329018, s5: 0.002649850444868207  
depth: 5, iteration: 404000, test\_RMSE: 1.119041919708252, erank: 43.6537628173  
8281, s1: 0.003674384206533432, s5: 0.0026508206501603127  
depth: 5, iteration: 406000, test\_RMSE: 1.119041919708252, erank: 43.6470489501  
9531, s1: 0.0036768238060176373, s5: 0.0026517563965171576  
depth: 5, iteration: 408000, test\_RMSE: 1.119041919708252, erank: 43.6403579711  
91406, s1: 0.00367923965677619, s5: 0.0026526853907853365  
depth: 5, iteration: 410000, test\_RMSE: 1.119041919708252, erank: 43.6336174011  
2305, s1: 0.003681708825752139, s5: 0.0026535720098763704  
depth: 5, iteration: 412000, test\_RMSE: 1.1190418004989624, erank: 43.626834869  
384766, s1: 0.003684175666421652, s5: 0.0026544590946286917  
depth: 5, iteration: 414000, test\_RMSE: 1.1190418004989624, erank: 43.620075225  
83008, s1: 0.003686648327857256, s5: 0.0026552921626716852  
depth: 5, iteration: 416000, test\_RMSE: 1.1190418004989624, erank: 43.613124847  
41211, s1: 0.003689168719574809, s5: 0.002656123833730817  
depth: 5, iteration: 418000, test\_RMSE: 1.119041919708252, erank: 43.6062660217  
28516, s1: 0.003691658843308687, s5: 0.0026569305919110775  
depth: 5, iteration: 420000, test\_RMSE: 1.1190418004989624, erank: 43.599300384  
521484, s1: 0.0036942108999937773, s5: 0.002657728036865592  
depth: 5, iteration: 422000, test\_RMSE: 1.1190418004989624, erank: 43.592376708  
984375, s1: 0.0036967401392757893, s5: 0.002658490091562271  
depth: 5, iteration: 424000, test\_RMSE: 1.1190418004989624, erank: 43.585380554  
19922, s1: 0.003699292428791523, s5: 0.0026592365466058254  
depth: 5, iteration: 426000, test\_RMSE: 1.1190418004989624, erank: 43.578361511  
23047, s1: 0.0037018710281699896, s5: 0.002659975551068783  
depth: 5, iteration: 428000, test\_RMSE: 1.119041919708252, erank: 43.5713043212  
8906, s1: 0.0037044694181531668, s5: 0.0026607185136526823  
depth: 5, iteration: 430000, test\_RMSE: 1.1190418004989624, erank: 43.564243316  
65039, s1: 0.0037070405669510365, s5: 0.002661404898390174  
depth: 5, iteration: 432000, test\_RMSE: 1.119041919708252, erank: 43.5571479797  
3633, s1: 0.0037096571177244186, s5: 0.002662093611434102  
depth: 5, iteration: 434000, test\_RMSE: 1.1190418004989624, erank: 43.550003051  
75781, s1: 0.003712311154231429, s5: 0.0026627976913005114  
depth: 5, iteration: 436000, test\_RMSE: 1.1190418004989624, erank: 43.542808532  
714844, s1: 0.003714978229254484, s5: 0.002663444960489869  
depth: 5, iteration: 438000, test\_RMSE: 1.1190418004989624, erank: 43.535572052  
00195, s1: 0.003717648098245263, s5: 0.002664108294993639  
depth: 5, iteration: 440000, test\_RMSE: 1.1190418004989624, erank: 43.528339385  
98633, s1: 0.00372034078463912, s5: 0.0026647341437637806  
depth: 5, iteration: 442000, test\_RMSE: 1.1190418004989624, erank: 43.521015167  
23633, s1: 0.00372305978089571, s5: 0.0026653532404452562  
depth: 5, iteration: 444000, test\_RMSE: 1.1190418004989624, erank: 43.513740539  
55078, s1: 0.003725743852555752, s5: 0.0026659714058041573  
depth: 5, iteration: 446000, test\_RMSE: 1.1190418004989624, erank: 43.506355285  
64453, s1: 0.003728515235707164, s5: 0.002666591899469495  
depth: 5, iteration: 448000, test\_RMSE: 1.1190418004989624, erank: 43.498939514  
160156, s1: 0.003731281030923128, s5: 0.002667180262506008  
depth: 5, iteration: 450000, test\_RMSE: 1.1190418004989624, erank: 43.491523742  
67578, s1: 0.0037340475246310234, s5: 0.0026677758432924747  
depth: 5, iteration: 452000, test\_RMSE: 1.1190418004989624, erank: 43.484046936  
035156, s1: 0.003736840793862939, s5: 0.0026683672331273556  
depth: 5, iteration: 454000, test\_RMSE: 1.1190418004989624, erank: 43.476573944

0918, s1: 0.0037396426778286695, s5: 0.002668951405212283  
depth: 5, iteration: 456000, test\_RMSE: 1.1190418004989624, erank: 43.469047546  
38672, s1: 0.0037424350157380104, s5: 0.0026695169508457184  
depth: 5, iteration: 458000, test\_RMSE: 1.1190418004989624, erank: 43.461452484  
13086, s1: 0.0037452985998243093, s5: 0.002670089714229107  
depth: 5, iteration: 460000, test\_RMSE: 1.1190418004989624, erank: 43.453891754  
15039, s1: 0.0037481465842574835, s5: 0.002670660149306059  
depth: 5, iteration: 462000, test\_RMSE: 1.1190418004989624, erank: 43.446315765  
38086, s1: 0.0037510155234485865, s5: 0.0026712052058428526  
depth: 5, iteration: 464000, test\_RMSE: 1.119041919708252, erank: 43.4386215209  
96094, s1: 0.0037539233453571796, s5: 0.002671782858669758  
depth: 5, iteration: 466000, test\_RMSE: 1.1190418004989624, erank: 43.430976867  
67578, s1: 0.0037568286061286926, s5: 0.0026723321061581373  
depth: 5, iteration: 468000, test\_RMSE: 1.119041919708252, erank: 43.4232330322  
2656, s1: 0.0037597541231662035, s5: 0.0026728555094450712  
depth: 5, iteration: 470000, test\_RMSE: 1.119041919708252, erank: 43.4154930114  
7461, s1: 0.0037627071142196655, s5: 0.0026734117418527603  
depth: 5, iteration: 472000, test\_RMSE: 1.1190418004989624, erank: 43.407695770  
26367, s1: 0.0037656703498214483, s5: 0.002673965645954013  
depth: 5, iteration: 474000, test\_RMSE: 1.1190418004989624, erank: 43.399864196  
777344, s1: 0.0037686596624553204, s5: 0.002674505580216646  
depth: 5, iteration: 476000, test\_RMSE: 1.1190418004989624, erank: 43.392021179  
19922, s1: 0.0037716457154601812, s5: 0.0026750352699309587  
depth: 5, iteration: 478000, test\_RMSE: 1.1190418004989624, erank: 43.384136199  
95117, s1: 0.00377468578517437, s5: 0.002675592200830579  
depth: 5, iteration: 480000, test\_RMSE: 1.1190418004989624, erank: 43.376235961  
91406, s1: 0.003777709323912859, s5: 0.0026761286426335573  
depth: 5, iteration: 482000, test\_RMSE: 1.1190418004989624, erank: 43.368251800  
53711, s1: 0.0037807768676429987, s5: 0.0026766699738800526  
depth: 5, iteration: 484000, test\_RMSE: 1.119041919708252, erank: 43.3602714538  
5742, s1: 0.0037838579155504704, s5: 0.002677195006981492  
depth: 5, iteration: 486000, test\_RMSE: 1.1190418004989624, erank: 43.352210998  
535156, s1: 0.003786975285038352, s5: 0.002677739132195711  
depth: 5, iteration: 488000, test\_RMSE: 1.1190418004989624, erank: 43.344177246  
09375, s1: 0.0037900744937360287, s5: 0.0026782469358295202  
depth: 5, iteration: 490000, test\_RMSE: 1.1190418004989624, erank: 43.336116790  
771484, s1: 0.0037931972183287144, s5: 0.002678787801414728  
depth: 5, iteration: 492000, test\_RMSE: 1.1190418004989624, erank: 43.327926635  
74219, s1: 0.0037963814102113247, s5: 0.002679324708878994  
depth: 5, iteration: 494000, test\_RMSE: 1.1190418004989624, erank: 43.319744110  
10742, s1: 0.0037995304446667433, s5: 0.002679861383512616  
depth: 5, iteration: 496000, test\_RMSE: 1.1190418004989624, erank: 43.311569213  
86719, s1: 0.003802731167525053, s5: 0.0026803722139447927  
depth: 5, iteration: 498000, test\_RMSE: 1.1190418004989624, erank: 43.303264617  
91992, s1: 0.003805930260568857, s5: 0.0026809279806911945  
depth: 5, iteration: 500000, test\_RMSE: 1.1190418004989624, erank: 43.295024871  
82617, s1: 0.0038091596215963364, s5: 0.002681442303583026  
depth: 5, iteration: 502000, test\_RMSE: 1.1190418004989624, erank: 43.286647796  
63086, s1: 0.003812416223809123, s5: 0.0026819887571036816  
depth: 5, iteration: 504000, test\_RMSE: 1.1190418004989624, erank: 43.278270721  
43555, s1: 0.00381567794829607, s5: 0.0026825270615518093  
depth: 5, iteration: 506000, test\_RMSE: 1.1190418004989624, erank: 43.269870758  
05664, s1: 0.0038189725019037724, s5: 0.002683050464838743  
depth: 5, iteration: 508000, test\_RMSE: 1.1190418004989624, erank: 43.261451721

191406, s1: 0.0038222589064389467, s5: 0.002683585276827216  
depth: 5, iteration: 510000, test\_RMSE: 1.1190418004989624, erank: 43.252956390  
38086, s1: 0.003825579537078738, s5: 0.0026841480284929276  
depth: 5, iteration: 512000, test\_RMSE: 1.119041919708252, erank: 43.2444572448  
7305, s1: 0.003828930202871561, s5: 0.002684670267626643  
depth: 5, iteration: 514000, test\_RMSE: 1.1190418004989624, erank: 43.235881805  
41992, s1: 0.0038322906475514174, s5: 0.002685200423002243  
depth: 5, iteration: 516000, test\_RMSE: 1.1190418004989624, erank: 43.227348327  
63672, s1: 0.003835675772279501, s5: 0.0026857294142246246  
depth: 5, iteration: 518000, test\_RMSE: 1.1190418004989624, erank: 43.21875, s  
1: 0.00383905996568501, s5: 0.00268629752099514  
depth: 5, iteration: 520000, test\_RMSE: 1.1190418004989624, erank: 43.210067749  
02344, s1: 0.003842522157356143, s5: 0.0026868211571127176  
depth: 5, iteration: 522000, test\_RMSE: 1.1190418004989624, erank: 43.201381683  
34961, s1: 0.0038459626957774162, s5: 0.002687381114810705  
depth: 5, iteration: 524000, test\_RMSE: 1.1190418004989624, erank: 43.192680358  
88672, s1: 0.003849416272714734, s5: 0.0026879103388637304  
depth: 5, iteration: 526000, test\_RMSE: 1.1190418004989624, erank: 43.183937072  
753906, s1: 0.003852908033877611, s5: 0.002688470995053649  
depth: 5, iteration: 528000, test\_RMSE: 1.1190418004989624, erank: 43.175155639  
64844, s1: 0.0038564109709113836, s5: 0.002689018612727523  
depth: 5, iteration: 530000, test\_RMSE: 1.1190418004989624, erank: 43.166336059  
57031, s1: 0.003859944175928831, s5: 0.002689577639102936  
depth: 5, iteration: 532000, test\_RMSE: 1.1190418004989624, erank: 43.157463073  
73047, s1: 0.0038634981028735638, s5: 0.0026901173405349255  
depth: 5, iteration: 534000, test\_RMSE: 1.1190418004989624, erank: 43.148616790  
771484, s1: 0.003867077175527811, s5: 0.0026906763669103384  
depth: 5, iteration: 536000, test\_RMSE: 1.1190418004989624, erank: 43.139671325  
683594, s1: 0.0038706506602466106, s5: 0.0026912465691566467  
depth: 5, iteration: 538000, test\_RMSE: 1.1190418004989624, erank: 43.130718231  
20117, s1: 0.0038742809556424618, s5: 0.0026917909272015095  
depth: 5, iteration: 540000, test\_RMSE: 1.1190418004989624, erank: 43.121734619  
140625, s1: 0.003877925453707576, s5: 0.0026923660188913345  
depth: 5, iteration: 542000, test\_RMSE: 1.1190418004989624, erank: 43.112667083  
740234, s1: 0.0038815555162727833, s5: 0.002692937385290861  
depth: 5, iteration: 544000, test\_RMSE: 1.1190418004989624, erank: 43.103603363  
03711, s1: 0.0038852673023939133, s5: 0.002693493850529194  
depth: 5, iteration: 546000, test\_RMSE: 1.1190418004989624, erank: 43.094539642  
333984, s1: 0.0038889495190232992, s5: 0.0026940449606627226  
depth: 5, iteration: 548000, test\_RMSE: 1.1190418004989624, erank: 43.085384368  
896484, s1: 0.0038927101995795965, s5: 0.0026946207508444786  
depth: 5, iteration: 550000, test\_RMSE: 1.1190418004989624, erank: 43.076267242  
43164, s1: 0.003896415000781417, s5: 0.0026951890904456377  
depth: 5, iteration: 552000, test\_RMSE: 1.1190418004989624, erank: 43.067073822  
021484, s1: 0.0039001943077892065, s5: 0.002695744624361396  
depth: 5, iteration: 554000, test\_RMSE: 1.1190418004989624, erank: 43.057865142  
822266, s1: 0.003903968259692192, s5: 0.002696316223591566  
depth: 5, iteration: 556000, test\_RMSE: 1.1190418004989624, erank: 43.048595428  
4668, s1: 0.003907815087586641, s5: 0.0026968899182975292  
depth: 5, iteration: 558000, test\_RMSE: 1.1190418004989624, erank: 43.039295196  
5332, s1: 0.003911642357707024, s5: 0.002697443589568138  
depth: 5, iteration: 560000, test\_RMSE: 1.1190418004989624, erank: 43.029918670  
6543, s1: 0.003915523178875446, s5: 0.002698049647733569  
depth: 5, iteration: 562000, test\_RMSE: 1.1190418004989624, erank: 43.020565032

958984, s1: 0.003919424023479223, s5: 0.0026986361481249332  
depth: 5, iteration: 564000, test\_RMSE: 1.1190418004989624, erank: 43.011199951  
171875, s1: 0.003923327196389437, s5: 0.0026992312632501125  
depth: 5, iteration: 566000, test\_RMSE: 1.1190418004989624, erank: 43.001796722  
41211, s1: 0.003927262965589762, s5: 0.0026997956447303295  
depth: 5, iteration: 568000, test\_RMSE: 1.1190418004989624, erank: 42.992324829  
10156, s1: 0.003931225277483463, s5: 0.002700385870411992  
depth: 5, iteration: 570000, test\_RMSE: 1.1190418004989624, erank: 42.982833862  
30469, s1: 0.003935176879167557, s5: 0.002701009390875697  
depth: 5, iteration: 572000, test\_RMSE: 1.1190418004989624, erank: 42.973304748  
535156, s1: 0.003939180634915829, s5: 0.0027015930972993374  
depth: 5, iteration: 574000, test\_RMSE: 1.1190418004989624, erank: 42.963706970  
214844, s1: 0.003943231422454119, s5: 0.002702202880755067  
depth: 5, iteration: 576000, test\_RMSE: 1.1190418004989624, erank: 42.954109191  
89453, s1: 0.003947282675653696, s5: 0.002702806144952774  
depth: 5, iteration: 578000, test\_RMSE: 1.1190418004989624, erank: 42.944477081  
29883, s1: 0.003951345104724169, s5: 0.0027034287340939045  
depth: 5, iteration: 580000, test\_RMSE: 1.1190418004989624, erank: 42.934799194  
33594, s1: 0.003955444321036339, s5: 0.0027040254790335894  
depth: 5, iteration: 582000, test\_RMSE: 1.1190418004989624, erank: 42.925075531  
00586, s1: 0.003959598019719124, s5: 0.0027046457398682833  
depth: 5, iteration: 584000, test\_RMSE: 1.1190418004989624, erank: 42.915275573  
73047, s1: 0.003963742405176163, s5: 0.0027052615769207478  
depth: 5, iteration: 586000, test\_RMSE: 1.1190418004989624, erank: 42.905460357  
666016, s1: 0.003967939410358667, s5: 0.0027058934792876244  
depth: 5, iteration: 588000, test\_RMSE: 1.1190418004989624, erank: 42.895622253  
41797, s1: 0.003972124774008989, s5: 0.002706507220864296  
depth: 5, iteration: 590000, test\_RMSE: 1.1190418004989624, erank: 42.885734558  
10547, s1: 0.003976336680352688, s5: 0.0027071319054812193  
depth: 5, iteration: 592000, test\_RMSE: 1.1190418004989624, erank: 42.875816345  
214844, s1: 0.003980599343776703, s5: 0.0027077691629529  
depth: 5, iteration: 594000, test\_RMSE: 1.1190418004989624, erank: 42.865848541  
259766, s1: 0.003984890412539244, s5: 0.0027084029279649258  
depth: 5, iteration: 596000, test\_RMSE: 1.1190418004989624, erank: 42.855857849  
121094, s1: 0.00398918054997921, s5: 0.0027090413495898247  
depth: 5, iteration: 598000, test\_RMSE: 1.1190418004989624, erank: 42.845752716  
06445, s1: 0.003993530757725239, s5: 0.002709704451262951  
depth: 5, iteration: 600000, test\_RMSE: 1.1190418004989624, erank: 42.835659027  
09961, s1: 0.00399788236245513, s5: 0.0027103370521217585  
depth: 5, iteration: 602000, test\_RMSE: 1.1190418004989624, erank: 42.825500488  
28125, s1: 0.0040023187175393105, s5: 0.0027110015507787466  
depth: 5, iteration: 604000, test\_RMSE: 1.1190418004989624, erank: 42.815280914  
30664, s1: 0.004006745759397745, s5: 0.002711653243750334  
depth: 5, iteration: 606000, test\_RMSE: 1.1190418004989624, erank: 42.805011749  
26758, s1: 0.004011193756014109, s5: 0.0027123072650283575  
depth: 5, iteration: 608000, test\_RMSE: 1.1190418004989624, erank: 42.794788360  
5957, s1: 0.0040156967006623745, s5: 0.002712988294661045  
depth: 5, iteration: 610000, test\_RMSE: 1.1190418004989624, erank: 42.784431457  
51953, s1: 0.004020173102617264, s5: 0.0027136546559631824  
depth: 5, iteration: 612000, test\_RMSE: 1.1190418004989624, erank: 42.774082183  
83789, s1: 0.004024723544716835, s5: 0.002714366652071476  
depth: 5, iteration: 614000, test\_RMSE: 1.1190418004989624, erank: 42.76367187  
5, s1: 0.004029286094009876, s5: 0.002715052105486393  
depth: 5, iteration: 616000, test\_RMSE: 1.1190418004989624, erank: 42.753219604

49219, s1: 0.004033870995044708, s5: 0.0027157459408044815  
depth: 5, iteration: 618000, test\_RMSE: 1.1190418004989624, erank: 42.742733001  
708984, s1: 0.004038463346660137, s5: 0.002716456539928913  
depth: 5, iteration: 620000, test\_RMSE: 1.1190418004989624, erank: 42.732204437  
25586, s1: 0.004043103661388159, s5: 0.0027171762194484472  
depth: 5, iteration: 622000, test\_RMSE: 1.1190418004989624, erank: 42.721641540  
527344, s1: 0.004047747701406479, s5: 0.0027179191820323467  
depth: 5, iteration: 624000, test\_RMSE: 1.1190418004989624, erank: 42.711002349  
853516, s1: 0.004052469972521067, s5: 0.0027186423540115356  
depth: 5, iteration: 626000, test\_RMSE: 1.1190418004989624, erank: 42.700408935  
546875, s1: 0.0040571847930550575, s5: 0.0027193783316761255  
depth: 5, iteration: 628000, test\_RMSE: 1.1190418004989624, erank: 42.689682006  
83594, s1: 0.004061951767653227, s5: 0.002720114542171359  
depth: 5, iteration: 630000, test\_RMSE: 1.1190418004989624, erank: 42.678947448  
73047, s1: 0.004066715948283672, s5: 0.0027208870742470026  
depth: 5, iteration: 632000, test\_RMSE: 1.1190418004989624, erank: 42.668212890  
625, s1: 0.004071503411978483, s5: 0.002721628872677684  
depth: 5, iteration: 634000, test\_RMSE: 1.1190418004989624, erank: 42.657379150  
390625, s1: 0.0040763490833342075, s5: 0.002722384873777628  
depth: 5, iteration: 636000, test\_RMSE: 1.1190418004989624, erank: 42.646499633  
78906, s1: 0.004081217106431723, s5: 0.0027231599669903517  
depth: 5, iteration: 638000, test\_RMSE: 1.1190418004989624, erank: 42.635581970  
214844, s1: 0.004086104221642017, s5: 0.002723940648138523  
depth: 5, iteration: 640000, test\_RMSE: 1.1190418004989624, erank: 42.624622344  
9707, s1: 0.004090987611562014, s5: 0.0027247178368270397  
depth: 5, iteration: 642000, test\_RMSE: 1.1190418004989624, erank: 42.613689422  
60742, s1: 0.004095888696610928, s5: 0.0027254882734268904  
depth: 5, iteration: 644000, test\_RMSE: 1.1190418004989624, erank: 42.602634429  
93164, s1: 0.004100858233869076, s5: 0.0027262752410024405  
depth: 5, iteration: 646000, test\_RMSE: 1.1190418004989624, erank: 42.591567993  
16406, s1: 0.004105811007320881, s5: 0.002727069891989231  
depth: 5, iteration: 648000, test\_RMSE: 1.1190418004989624, erank: 42.580410003  
66211, s1: 0.004110821522772312, s5: 0.0027278943452984095  
depth: 5, iteration: 650000, test\_RMSE: 1.1190418004989624, erank: 42.569313049  
316406, s1: 0.0041158683598041534, s5: 0.002728701801970601  
depth: 5, iteration: 652000, test\_RMSE: 1.1190418004989624, erank: 42.558120727  
53906, s1: 0.004120916128158569, s5: 0.0027295241598039865  
depth: 5, iteration: 654000, test\_RMSE: 1.1190418004989624, erank: 42.546901702  
88086, s1: 0.004125983454287052, s5: 0.0027303530368953943  
depth: 5, iteration: 656000, test\_RMSE: 1.1190418004989624, erank: 42.535682678  
222656, s1: 0.004131114576011896, s5: 0.0027310519944876432  
depth: 5, iteration: 658000, test\_RMSE: 1.1190418004989624, erank: 42.524337768  
55469, s1: 0.004136222414672375, s5: 0.002731981687247753  
depth: 5, iteration: 660000, test\_RMSE: 1.1190418004989624, erank: 42.513011932  
37305, s1: 0.004141408018767834, s5: 0.0027327907737344503  
depth: 5, iteration: 662000, test\_RMSE: 1.1190418004989624, erank: 42.501613616  
94336, s1: 0.004146575927734375, s5: 0.0027336999773979187  
depth: 5, iteration: 664000, test\_RMSE: 1.1190416812896729, erank: 42.490192413  
33008, s1: 0.004151780623942614, s5: 0.002734545385465026  
depth: 5, iteration: 666000, test\_RMSE: 1.1190418004989624, erank: 42.478836059  
57031, s1: 0.0041569811291992664, s5: 0.002735431306064129  
depth: 5, iteration: 668000, test\_RMSE: 1.1190418004989624, erank: 42.467285156  
25, s1: 0.004162302706390619, s5: 0.002736310474574566  
depth: 5, iteration: 670000, test\_RMSE: 1.1190418004989624, erank: 42.455802917

48047, s1: 0.004167534876614809, s5: 0.0027371689211577177  
depth: 5, iteration: 672000, test\_RMSE: 1.1190418004989624, erank: 42.444164276  
12305, s1: 0.0041728876531124115, s5: 0.002738070907071233  
depth: 5, iteration: 674000, test\_RMSE: 1.1190418004989624, erank: 42.432556152  
34375, s1: 0.0041781943291425705, s5: 0.0027389575261622667  
depth: 5, iteration: 676000, test\_RMSE: 1.1190418004989624, erank: 42.420936584  
472656, s1: 0.004183600656688213, s5: 0.002739852759987116  
depth: 5, iteration: 678000, test\_RMSE: 1.1190418004989624, erank: 42.409183502  
197266, s1: 0.004189022816717625, s5: 0.0027407826855778694  
depth: 5, iteration: 680000, test\_RMSE: 1.1190418004989624, erank: 42.397468566  
89453, s1: 0.004194463137537241, s5: 0.0027416942175477743  
depth: 5, iteration: 682000, test\_RMSE: 1.1190418004989624, erank: 42.385654449  
46289, s1: 0.004199912305921316, s5: 0.0027426162268966436  
depth: 5, iteration: 684000, test\_RMSE: 1.1190418004989624, erank: 42.373844146  
728516, s1: 0.004205412697046995, s5: 0.0027435636147856712  
depth: 5, iteration: 686000, test\_RMSE: 1.1190418004989624, erank: 42.361976623  
535156, s1: 0.004210928920656443, s5: 0.00274445116519928  
depth: 5, iteration: 688000, test\_RMSE: 1.1190418004989624, erank: 42.350078582  
76367, s1: 0.004216459114104509, s5: 0.002745432546362281  
depth: 5, iteration: 690000, test\_RMSE: 1.1190418004989624, erank: 42.338146209  
7168, s1: 0.004222018178552389, s5: 0.002746359445154667  
depth: 5, iteration: 692000, test\_RMSE: 1.1190418004989624, erank: 42.326164245  
60547, s1: 0.004227598663419485, s5: 0.0027473249938338995  
depth: 5, iteration: 694000, test\_RMSE: 1.1190418004989624, erank: 42.314117431  
640625, s1: 0.0042332434095442295, s5: 0.0027482849545776844  
depth: 5, iteration: 696000, test\_RMSE: 1.1190418004989624, erank: 42.302021026  
61133, s1: 0.0042389314621686935, s5: 0.0027492796070873737  
depth: 5, iteration: 698000, test\_RMSE: 1.1190418004989624, erank: 42.289878845  
214844, s1: 0.004244635347276926, s5: 0.0027502556331455708  
depth: 5, iteration: 700000, test\_RMSE: 1.1190416812896729, erank: 42.277763366  
69922, s1: 0.004250326193869114, s5: 0.0027512265369296074  
depth: 5, iteration: 702000, test\_RMSE: 1.1190416812896729, erank: 42.265609741  
21094, s1: 0.004256059415638447, s5: 0.0027521944139152765  
depth: 5, iteration: 704000, test\_RMSE: 1.1190418004989624, erank: 42.253326416  
015625, s1: 0.004261826165020466, s5: 0.002753197681158781  
depth: 5, iteration: 706000, test\_RMSE: 1.1190418004989624, erank: 42.241039276  
12305, s1: 0.004267618525773287, s5: 0.002754208631813526  
depth: 5, iteration: 708000, test\_RMSE: 1.1190418004989624, erank: 42.228702545  
166016, s1: 0.0042734588496387005, s5: 0.0027552058454602957  
depth: 5, iteration: 710000, test\_RMSE: 1.1190416812896729, erank: 42.216312408  
447266, s1: 0.004279330838471651, s5: 0.0027562505565583706  
depth: 5, iteration: 712000, test\_RMSE: 1.1190416812896729, erank: 42.203895568  
847656, s1: 0.004285206086933613, s5: 0.0027572941035032272  
depth: 5, iteration: 714000, test\_RMSE: 1.1190416812896729, erank: 42.191429138  
183594, s1: 0.004291146527975798, s5: 0.002758342307060957  
depth: 5, iteration: 716000, test\_RMSE: 1.1190416812896729, erank: 42.178897857  
666016, s1: 0.004297087900340557, s5: 0.0027593858540058136  
depth: 5, iteration: 718000, test\_RMSE: 1.1190416812896729, erank: 42.166328430  
17578, s1: 0.0043030851520597935, s5: 0.0027604529168456793  
depth: 5, iteration: 720000, test\_RMSE: 1.1190416812896729, erank: 42.153671264  
64844, s1: 0.00430914293974638, s5: 0.0027615490835160017  
depth: 5, iteration: 722000, test\_RMSE: 1.1190416812896729, erank: 42.141109466  
552734, s1: 0.00431514997035265, s5: 0.0027626119554042816  
depth: 5, iteration: 724000, test\_RMSE: 1.1190416812896729, erank: 42.128402709

96094, s1: 0.004321232903748751, s5: 0.0027636743616312742  
depth: 5, iteration: 726000, test\_RMSE: 1.1190416812896729, erank: 42.115650177  
00195, s1: 0.004327366128563881, s5: 0.002764821285381913  
depth: 5, iteration: 728000, test\_RMSE: 1.1190416812896729, erank: 42.102817535  
40039, s1: 0.004333546385169029, s5: 0.0027659095358103514  
depth: 5, iteration: 730000, test\_RMSE: 1.1190416812896729, erank: 42.090003967  
285156, s1: 0.004339722916483879, s5: 0.0027670494746416807  
depth: 5, iteration: 732000, test\_RMSE: 1.1190416812896729, erank: 42.077129364  
01367, s1: 0.004345927853137255, s5: 0.0027681870851665735  
depth: 5, iteration: 734000, test\_RMSE: 1.1190416812896729, erank: 42.064159393  
31055, s1: 0.004352184943854809, s5: 0.0027693321462720633  
depth: 5, iteration: 736000, test\_RMSE: 1.1190416812896729, erank: 42.051174163  
81836, s1: 0.004358488135039806, s5: 0.0027705186512321234  
depth: 5, iteration: 738000, test\_RMSE: 1.1190416812896729, erank: 42.038192749  
02344, s1: 0.004364776890724897, s5: 0.0027716641779989004  
depth: 5, iteration: 740000, test\_RMSE: 1.1190416812896729, erank: 42.025085449  
21875, s1: 0.004371143411844969, s5: 0.0027728420682251453  
depth: 5, iteration: 742000, test\_RMSE: 1.1190416812896729, erank: 42.012001037  
597656, s1: 0.004377468954771757, s5: 0.002774051856249571  
depth: 5, iteration: 744000, test\_RMSE: 1.1190416812896729, erank: 41.998889923  
0957, s1: 0.004383874591439962, s5: 0.0027752495370805264  
depth: 5, iteration: 746000, test\_RMSE: 1.1190416812896729, erank: 41.985626220  
703125, s1: 0.004390296526253223, s5: 0.0027764674741774797  
depth: 5, iteration: 748000, test\_RMSE: 1.1190416812896729, erank: 41.972404479  
98047, s1: 0.004396743606775999, s5: 0.002777694957330823  
depth: 5, iteration: 750000, test\_RMSE: 1.1190416812896729, erank: 41.959106445  
3125, s1: 0.00440321397036314, s5: 0.0027789536397904158  
depth: 5, iteration: 752000, test\_RMSE: 1.1190416812896729, erank: 41.945755004  
88281, s1: 0.0044097681529819965, s5: 0.0027802216354757547  
depth: 5, iteration: 754000, test\_RMSE: 1.1190416812896729, erank: 41.932373046  
875, s1: 0.004416279029101133, s5: 0.0027815154753625393  
depth: 5, iteration: 756000, test\_RMSE: 1.1190416812896729, erank: 41.918930053  
71094, s1: 0.004422890488058329, s5: 0.0027827906887978315  
depth: 5, iteration: 758000, test\_RMSE: 1.1190416812896729, erank: 41.905483245  
84961, s1: 0.004429493099451065, s5: 0.0027840903494507074  
depth: 5, iteration: 760000, test\_RMSE: 1.1190416812896729, erank: 41.891925811  
76758, s1: 0.00443617207929492, s5: 0.0027854167856276035  
depth: 5, iteration: 762000, test\_RMSE: 1.1190416812896729, erank: 41.878322601  
31836, s1: 0.004442831501364708, s5: 0.0027867599856108427  
depth: 5, iteration: 764000, test\_RMSE: 1.1190416812896729, erank: 41.864727020  
26367, s1: 0.004449528641998768, s5: 0.0027881055139005184  
depth: 5, iteration: 766000, test\_RMSE: 1.1190416812896729, erank: 41.851036071  
777344, s1: 0.004456282593309879, s5: 0.002789455931633711  
depth: 5, iteration: 768000, test\_RMSE: 1.1190416812896729, erank: 41.837326049  
80469, s1: 0.0044630663469433784, s5: 0.002790839411318302  
depth: 5, iteration: 770000, test\_RMSE: 1.1190416812896729, erank: 41.823554992  
67578, s1: 0.004469892475754023, s5: 0.0027922054287046194  
depth: 5, iteration: 772000, test\_RMSE: 1.1190416812896729, erank: 41.809745788  
57422, s1: 0.004476731177419424, s5: 0.002793621737509966  
depth: 5, iteration: 774000, test\_RMSE: 1.1190416812896729, erank: 41.795886993  
4082, s1: 0.004483617842197418, s5: 0.0027950468938797712  
depth: 5, iteration: 776000, test\_RMSE: 1.1190416812896729, erank: 41.781967163  
08594, s1: 0.00449054641649127, s5: 0.0027964806649833918  
depth: 5, iteration: 778000, test\_RMSE: 1.1190416812896729, erank: 41.768001556



396484, s1: 0.0044975075870752335, s5: 0.0027979116421192884  
depth: 5, iteration: 780000, test\_RMSE: 1.1190416812896729, erank: 41.754005432  
128906, s1: 0.004504503682255745, s5: 0.0027993740513920784  
depth: 5, iteration: 782000, test\_RMSE: 1.1190416812896729, erank: 41.739948272  
70508, s1: 0.004511547274887562, s5: 0.0028009002562612295  
depth: 5, iteration: 784000, test\_RMSE: 1.1190416812896729, erank: 41.725898742  
67578, s1: 0.004518596455454826, s5: 0.0028023417107760906  
depth: 5, iteration: 786000, test\_RMSE: 1.1190416812896729, erank: 41.711734771  
728516, s1: 0.004525693599134684, s5: 0.002803869778290391  
depth: 5, iteration: 788000, test\_RMSE: 1.1190416812896729, erank: 41.697536468  
50586, s1: 0.004532805643975735, s5: 0.0028053796850144863  
depth: 5, iteration: 790000, test\_RMSE: 1.1190416812896729, erank: 41.683300018  
31055, s1: 0.004539979621767998, s5: 0.0028069287072867155  
depth: 5, iteration: 792000, test\_RMSE: 1.1190416812896729, erank: 41.669013977  
05078, s1: 0.004547156859189272, s5: 0.0028084898367524147  
depth: 5, iteration: 794000, test\_RMSE: 1.1190416812896729, erank: 41.654689788  
81836, s1: 0.004554404877126217, s5: 0.0028100814670324326  
depth: 5, iteration: 796000, test\_RMSE: 1.1190416812896729, erank: 41.640285491  
94336, s1: 0.0045617083087563515, s5: 0.0028116502799093723  
depth: 5, iteration: 798000, test\_RMSE: 1.1190416812896729, erank: 41.625850677  
490234, s1: 0.004569032229483128, s5: 0.0028132700826972723

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 5 --lam 0.0 --optim Adam --lr 1e-3 --niters 30000  
depth: 5, iteration: 0, test\_RMSE: 1.1277276277542114, erank: 43.0359306335449  
2, s1: 0.003391407895833254, s5: 0.002699912991374731  
depth: 5, iteration: 2000, test\_RMSE: 1.3615732192993164, erank: 4.957746982574  
463, s1: 54.980186462402344, s5: 33.250892639160156  
depth: 5, iteration: 4000, test\_RMSE: 1.3616067171096802, erank: 4.954370498657  
227, s1: 54.9815673828125, s5: 33.25388717651367  
depth: 5, iteration: 6000, test\_RMSE: 1.361436128616333, erank: 4.9512362480163  
57, s1: 54.91874694824219, s5: 33.254764556884766  
depth: 5, iteration: 8000, test\_RMSE: 1.3632899522781372, erank: 4.946258068084  
717, s1: 55.43133544921875, s5: 33.26249694824219  
depth: 5, iteration: 10000, test\_RMSE: 1.3617908954620361, erank: 4.94684505462  
6465, s1: 55.0001220703125, s5: 33.26166534423828  
depth: 5, iteration: 12000, test\_RMSE: 1.3616728782653809, erank: 4.94585514068  
6035, s1: 55.03804016113281, s5: 33.25127029418945  
depth: 5, iteration: 14000, test\_RMSE: 1.3610843420028687, erank: 4.94569730758  
667, s1: 54.8225212097168, s5: 33.25967025756836  
depth: 5, iteration: 16000, test\_RMSE: 1.3615187406539917, erank: 4.94417953491  
2109, s1: 54.93376922607422, s5: 33.258731842041016  
depth: 5, iteration: 18000, test\_RMSE: 1.36151123046875, erank: 4.9434418678283  
69, s1: 54.94428253173828, s5: 33.26239776611328  
depth: 5, iteration: 20000, test\_RMSE: 1.3619416952133179, erank: 4.94231271743  
7744, s1: 55.15922927856445, s5: 33.254180908203125  
depth: 5, iteration: 22000, test\_RMSE: 1.3626022338867188, erank: 4.94067573547  
3633, s1: 55.4019775390625, s5: 33.25346374511719  
depth: 5, iteration: 24000, test\_RMSE: 1.3623000383377075, erank: 4.94069862365  
7227, s1: 55.190162658691406, s5: 33.264129638671875  
depth: 5, iteration: 26000, test\_RMSE: 1.3617221117019653, erank: 4.94111537933  
3496, s1: 54.98933410644531, s5: 33.26459884643555  
depth: 5, iteration: 28000, test\_RMSE: 1.3621761798858643, erank: 4.94002819061

2793, s1: 55.21480178833008, s5: 33.26804733276367

```
In [9]: for opt, lr, steps in (("Adam", LR_ADAM, LONG_ITERS_ADAM), ("GD", LR_GD, LONG_
run_and_log(f"F2_{opt.lower()}_d3_lam1e-4",
            **BASE_SYN, depth=3, lam="1e-4", optim=opt, lr=lr, niters=steps)
```

```
RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10
0 --rank 5 --reg_norm ratio --initscale 1e-3 --sample_size 4000 --log_interval
2000 --depth 3 --lam 1e-4 --optim Adam --lr 1e-3 --niters 30000
depth: 3, iteration: 0, test_RMSE: 1.130967140197754, erank: 57.43481063842773
4, s1: 0.002728724619373679, s5: 0.002215920016169548
depth: 3, iteration: 2000, test_RMSE: 1.3698301315307617, erank: 5.165743827819
824, s1: 52.67234802246094, s5: 35.7275390625
depth: 3, iteration: 4000, test_RMSE: 1.3699700832366943, erank: 5.087910652160
6445, s1: 52.66286087036133, s5: 35.75092315673828
depth: 3, iteration: 6000, test_RMSE: 1.3700666427612305, erank: 5.024189472198
486, s1: 52.658409118652344, s5: 35.766456604003906
depth: 3, iteration: 8000, test_RMSE: 1.3698979616165161, erank: 4.975847244262
695, s1: 52.60279083251953, s5: 35.78527069091797
depth: 3, iteration: 10000, test_RMSE: 1.3700504302978516, erank: 4.96147823333
7402, s1: 52.660823822021484, s5: 35.787109375
depth: 3, iteration: 12000, test_RMSE: 1.3699673414230347, erank: 4.95750141143
7988, s1: 52.59660720825195, s5: 35.77778244018555
depth: 3, iteration: 14000, test_RMSE: 1.3702518939971924, erank: 4.95539522171
0205, s1: 52.680049896240234, s5: 35.776161193847656
depth: 3, iteration: 16000, test_RMSE: 1.3700445890426636, erank: 4.95470952987
6709, s1: 52.62519454956055, s5: 35.780242919921875
depth: 3, iteration: 18000, test_RMSE: 1.3706032037734985, erank: 4.95371818542
4805, s1: 52.74528503417969, s5: 35.779197692871094
depth: 3, iteration: 20000, test_RMSE: 1.3703399896621704, erank: 4.95370817184
4482, s1: 52.661720275878906, s5: 35.781646728515625
depth: 3, iteration: 22000, test_RMSE: 1.3699939250946045, erank: 4.95366907119
751, s1: 52.628265380859375, s5: 35.776771545410156
depth: 3, iteration: 24000, test_RMSE: 1.3705860376358032, erank: 4.95293760299
6826, s1: 52.81112289428711, s5: 35.78339385986328
depth: 3, iteration: 26000, test_RMSE: 1.370229721069336, erank: 4.953372955322
266, s1: 52.652042388916016, s5: 35.77803421020508
depth: 3, iteration: 28000, test_RMSE: 1.3702884912490845, erank: 4.95299100875
8545, s1: 52.75730895996094, s5: 35.78458786010742
```

```
RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10
0 --rank 5 --reg_norm ratio --initscale 1e-3 --sample_size 4000 --log_interval
2000 --depth 3 --lam 1e-4 --optim GD --lr 1e-3 --niters 80000
depth: 3, iteration: 0, test_RMSE: 1.123811960220337, erank: 57.06502151489258,
s1: 0.0028843253385275602, s5: 0.0023306577932089567
depth: 3, iteration: 2000, test_RMSE: 1.123811960220337, erank: 56.867626190185
55, s1: 0.0029159048572182655, s5: 0.002346235094591975
depth: 3, iteration: 4000, test_RMSE: 1.123811960220337, erank: 56.669017791748
05, s1: 0.0029481269884854555, s5: 0.0023619537241756916
depth: 3, iteration: 6000, test_RMSE: 1.123811960220337, erank: 56.469058990478
516, s1: 0.002981087425723672, s5: 0.0023778739850968122
depth: 3, iteration: 8000, test_RMSE: 1.123811960220337, erank: 56.267951965332
03, s1: 0.0030147088691592216, s5: 0.002393896458670497
depth: 3, iteration: 10000, test_RMSE: 1.123811960220337, erank: 56.06547927856
445, s1: 0.003049146384000778, s5: 0.0024100840091705322
depth: 3, iteration: 12000, test_RMSE: 1.123811960220337, erank: 55.86176300048
828, s1: 0.003084275173023343, s5: 0.002426423830911517
depth: 3, iteration: 14000, test_RMSE: 1.123811960220337, erank: 55.65679550170
8984, s1: 0.003120200941339135, s5: 0.0024428858887404203
depth: 3, iteration: 16000, test_RMSE: 1.1238120794296265, erank: 55.4505691528
```

3203, s1: 0.0031568703707307577, s5: 0.002459508366882801  
depth: 3, iteration: 18000, test\_RMSE: 1.1238120794296265, erank: 55.2431068420  
41016, s1: 0.0031943523790687323, s5: 0.0024762540124356747  
depth: 3, iteration: 20000, test\_RMSE: 1.1238120794296265, erank: 55.0343437194  
8242, s1: 0.003232634160667658, s5: 0.002493133768439293  
depth: 3, iteration: 22000, test\_RMSE: 1.1238120794296265, erank: 54.8242797851  
5625, s1: 0.003271787893027067, s5: 0.002510164165869355  
depth: 3, iteration: 24000, test\_RMSE: 1.1238120794296265, erank: 54.6130142211  
91406, s1: 0.0033117630518972874, s5: 0.002527299802750349  
depth: 3, iteration: 26000, test\_RMSE: 1.123812198638916, erank: 54.40042495727  
539, s1: 0.0033526059705764055, s5: 0.0025445849169045687  
depth: 3, iteration: 28000, test\_RMSE: 1.123812198638916, erank: 54.18661880493  
164, s1: 0.0033944081515073776, s5: 0.0025619668886065483  
depth: 3, iteration: 30000, test\_RMSE: 1.123812198638916, erank: 53.97153091430  
664, s1: 0.0034370904322713614, s5: 0.002579447580501437  
depth: 3, iteration: 32000, test\_RMSE: 1.123812198638916, erank: 53.75527191162  
1094, s1: 0.0034807161428034306, s5: 0.0025970640126615763  
depth: 3, iteration: 34000, test\_RMSE: 1.123812198638916, erank: 53.53792572021  
4844, s1: 0.003525317879393697, s5: 0.0026147833559662104  
depth: 3, iteration: 36000, test\_RMSE: 1.123812198638916, erank: 53.31944656372  
07, s1: 0.0035708495415747166, s5: 0.002632569056004286  
depth: 3, iteration: 38000, test\_RMSE: 1.123812198638916, erank: 53.09966278076  
172, s1: 0.0036174363922327757, s5: 0.0026504364795982838  
depth: 3, iteration: 40000, test\_RMSE: 1.123812198638916, erank: 52.87861251831  
055, s1: 0.003665116848424077, s5: 0.0026683525647968054  
depth: 3, iteration: 42000, test\_RMSE: 1.1238123178482056, erank: 52.6563873291  
0156, s1: 0.0037138049956411123, s5: 0.0026864269748330116  
depth: 3, iteration: 44000, test\_RMSE: 1.1238123178482056, erank: 52.4330101013  
1836, s1: 0.0037635439075529575, s5: 0.0027044930029660463  
depth: 3, iteration: 46000, test\_RMSE: 1.1238123178482056, erank: 52.2084617614  
7461, s1: 0.0038144465070217848, s5: 0.0027226766105741262  
depth: 3, iteration: 48000, test\_RMSE: 1.1238123178482056, erank: 51.9827308654  
78516, s1: 0.0038664499297738075, s5: 0.0027408874593675137  
depth: 3, iteration: 50000, test\_RMSE: 1.1238123178482056, erank: 51.7558174133  
3008, s1: 0.003919675946235657, s5: 0.0027592016849666834  
depth: 3, iteration: 52000, test\_RMSE: 1.1238123178482056, erank: 51.5278129577  
6367, s1: 0.003974033985286951, s5: 0.002777501940727234  
depth: 3, iteration: 54000, test\_RMSE: 1.1238123178482056, erank: 51.2985076904  
2969, s1: 0.004029696341603994, s5: 0.0027958338614553213  
depth: 3, iteration: 56000, test\_RMSE: 1.1238124370574951, erank: 51.0680885314  
9414, s1: 0.004086596425622702, s5: 0.002814202569425106  
depth: 3, iteration: 58000, test\_RMSE: 1.1238124370574951, erank: 50.8364181518  
5547, s1: 0.004144811537116766, s5: 0.002832630882039666  
depth: 3, iteration: 60000, test\_RMSE: 1.1238124370574951, erank: 50.6035728454  
58984, s1: 0.004204422701150179, s5: 0.0028510636184364557  
depth: 3, iteration: 62000, test\_RMSE: 1.1238124370574951, erank: 50.3695678710  
9375, s1: 0.004265457391738892, s5: 0.0028694893699139357  
depth: 3, iteration: 64000, test\_RMSE: 1.1238124370574951, erank: 50.1346015930  
1758, s1: 0.004327851813286543, s5: 0.0028879025485366583  
depth: 3, iteration: 66000, test\_RMSE: 1.1238125562667847, erank: 49.8983955383  
3008, s1: 0.004391704685986042, s5: 0.0029063280671834946  
depth: 3, iteration: 68000, test\_RMSE: 1.1238125562667847, erank: 49.6611251831  
0547, s1: 0.004457039292901754, s5: 0.0029247284401208162  
depth: 3, iteration: 70000, test\_RMSE: 1.1238125562667847, erank: 49.4228363037

1094, s1: 0.004523859824985266, s5: 0.0029431628063321114  
depth: 3, iteration: 72000, test\_RMSE: 1.1238125562667847, erank: 49.1835060119  
6289, s1: 0.004592241253703833, s5: 0.002961535705253482  
depth: 3, iteration: 74000, test\_RMSE: 1.1238125562667847, erank: 48.9430999755  
8594, s1: 0.004662251565605402, s5: 0.0029799046460539103  
depth: 3, iteration: 76000, test\_RMSE: 1.1238125562667847, erank: 48.7016601562  
5, s1: 0.004733890760689974, s5: 0.0029981706757098436  
depth: 3, iteration: 78000, test\_RMSE: 1.1238125562667847, erank: 48.4590301513  
6719, s1: 0.0048072198405861855, s5: 0.003016409929841757  
depth: 3, iteration: 80000, test\_RMSE: 1.1238126754760742, erank: 48.2155647277  
832, s1: 0.004882258828729391, s5: 0.0030345406848937273  
depth: 3, iteration: 82000, test\_RMSE: 1.1238126754760742, erank: 47.9709777832  
03125, s1: 0.004959098529070616, s5: 0.003052610671147704  
depth: 3, iteration: 84000, test\_RMSE: 1.1238126754760742, erank: 47.7254676818  
84766, s1: 0.005037727300077677, s5: 0.003070579841732979  
depth: 3, iteration: 86000, test\_RMSE: 1.1238127946853638, erank: 47.4789276123  
0469, s1: 0.005118315573781729, s5: 0.003088423516601324  
depth: 3, iteration: 88000, test\_RMSE: 1.1238127946853638, erank: 47.2315216064  
4531, s1: 0.00520081352442503, s5: 0.003106111427769065  
depth: 3, iteration: 90000, test\_RMSE: 1.1238127946853638, erank: 46.9830207824  
707, s1: 0.005285287741571665, s5: 0.0031237376388162374  
depth: 3, iteration: 92000, test\_RMSE: 1.1238127946853638, erank: 46.7335739135  
7422, s1: 0.0053717694245278835, s5: 0.0031411652453243732  
depth: 3, iteration: 94000, test\_RMSE: 1.1238127946853638, erank: 46.4830245971  
6797, s1: 0.005460455548018217, s5: 0.0031584822572767735  
depth: 3, iteration: 96000, test\_RMSE: 1.1238127946853638, erank: 46.2313652038  
5742, s1: 0.005551300942897797, s5: 0.0031755922827869654  
depth: 3, iteration: 98000, test\_RMSE: 1.1238127946853638, erank: 45.9786758422  
85156, s1: 0.0056442925706505775, s5: 0.0031925803050398827  
depth: 3, iteration: 100000, test\_RMSE: 1.1238129138946533, erank: 45.724815368  
652344, s1: 0.0057396236807107925, s5: 0.0032094335183501244  
depth: 3, iteration: 102000, test\_RMSE: 1.1238129138946533, erank: 45.470130920  
410156, s1: 0.005837240722030401, s5: 0.003226066241040826  
depth: 3, iteration: 104000, test\_RMSE: 1.1238129138946533, erank: 45.214324951  
171875, s1: 0.005937193054705858, s5: 0.0032425459939986467  
depth: 3, iteration: 106000, test\_RMSE: 1.1238129138946533, erank: 44.957527160  
64453, s1: 0.006039561703801155, s5: 0.0032588294707238674  
depth: 3, iteration: 108000, test\_RMSE: 1.1238129138946533, erank: 44.699829101  
5625, s1: 0.006144389044493437, s5: 0.0032748922239989042  
depth: 3, iteration: 110000, test\_RMSE: 1.1238130331039429, erank: 44.441062927  
246094, s1: 0.006251859944313765, s5: 0.0032907016575336456  
depth: 3, iteration: 112000, test\_RMSE: 1.1238130331039429, erank: 44.181190490  
722656, s1: 0.006362014915794134, s5: 0.003306283615529537  
depth: 3, iteration: 114000, test\_RMSE: 1.1238130331039429, erank: 43.920379638  
671875, s1: 0.006474899593740702, s5: 0.003321629948914051  
depth: 3, iteration: 116000, test\_RMSE: 1.1238130331039429, erank: 43.658363342  
285156, s1: 0.006590600591152906, s5: 0.0033367439173161983  
depth: 3, iteration: 118000, test\_RMSE: 1.1238131523132324, erank: 43.395538330  
078125, s1: 0.006709060166031122, s5: 0.0033515579998493195  
depth: 3, iteration: 120000, test\_RMSE: 1.1238131523132324, erank: 43.131668090  
82031, s1: 0.006830420810729265, s5: 0.0033661234192550182  
depth: 3, iteration: 122000, test\_RMSE: 1.1238131523132324, erank: 42.866718292  
23633, s1: 0.0069547854363918304, s5: 0.0033804073464125395  
depth: 3, iteration: 124000, test\_RMSE: 1.1238131523132324, erank: 42.600818634

0332, s1: 0.007082115858793259, s5: 0.003394400468096137  
depth: 3, iteration: 126000, test\_RMSE: 1.1238131523132324, erank: 42.333824157  
714844, s1: 0.0072126928716897964, s5: 0.003408134216442704  
depth: 3, iteration: 128000, test\_RMSE: 1.123813271522522, erank: 42.0659370422  
3633, s1: 0.007346358150243759, s5: 0.003421478671953082  
depth: 3, iteration: 130000, test\_RMSE: 1.123813271522522, erank: 41.7970275878  
90625, s1: 0.00748326675966382, s5: 0.0034345209132879972  
depth: 3, iteration: 132000, test\_RMSE: 1.123813271522522, erank: 41.5270690917  
96875, s1: 0.007623615674674511, s5: 0.0034473200794309378  
depth: 3, iteration: 134000, test\_RMSE: 1.123813271522522, erank: 41.2561035156  
25, s1: 0.007767290808260441, s5: 0.0034597120247781277  
depth: 3, iteration: 136000, test\_RMSE: 1.123813271522522, erank: 40.9840888977  
0508, s1: 0.007914417423307896, s5: 0.003471874399110675  
depth: 3, iteration: 138000, test\_RMSE: 1.1238133907318115, erank: 40.711166381  
83594, s1: 0.008065057918429375, s5: 0.003483651438727975  
depth: 3, iteration: 140000, test\_RMSE: 1.1238133907318115, erank: 40.437114715  
57617, s1: 0.008219413459300995, s5: 0.0034951285924762487  
depth: 3, iteration: 142000, test\_RMSE: 1.1238133907318115, erank: 40.162261962  
890625, s1: 0.008377180434763432, s5: 0.003506219247356057  
depth: 3, iteration: 144000, test\_RMSE: 1.123813509941101, erank: 39.8863143920  
89844, s1: 0.008538726717233658, s5: 0.0035169795155525208  
depth: 3, iteration: 146000, test\_RMSE: 1.123813509941101, erank: 39.6093139648  
4375, s1: 0.008704137988388538, s5: 0.0035274310503154993  
depth: 3, iteration: 148000, test\_RMSE: 1.123813509941101, erank: 39.3313980102  
53906, s1: 0.008873272687196732, s5: 0.0035375352017581463  
depth: 3, iteration: 150000, test\_RMSE: 1.123813509941101, erank: 39.0525016784  
668, s1: 0.009046348743140697, s5: 0.003547277534380555  
depth: 3, iteration: 152000, test\_RMSE: 1.1238136291503906, erank: 38.772655487  
06055, s1: 0.009223364293575287, s5: 0.003556643845513463  
depth: 3, iteration: 154000, test\_RMSE: 1.1238136291503906, erank: 38.491909027  
09961, s1: 0.009404274635016918, s5: 0.003565690014511347  
depth: 3, iteration: 156000, test\_RMSE: 1.1238136291503906, erank: 38.210453033  
447266, s1: 0.009589128196239471, s5: 0.0035743608605116606  
depth: 3, iteration: 158000, test\_RMSE: 1.1238136291503906, erank: 37.927986145  
01953, s1: 0.009778117761015892, s5: 0.003582712495699525  
depth: 3, iteration: 160000, test\_RMSE: 1.1238137483596802, erank: 37.644889831  
54297, s1: 0.009971071034669876, s5: 0.0035906920675188303  
depth: 3, iteration: 162000, test\_RMSE: 1.1238137483596802, erank: 37.360839843  
75, s1: 0.010168233886361122, s5: 0.003598287235945463  
depth: 3, iteration: 164000, test\_RMSE: 1.1238137483596802, erank: 37.076080322  
265625, s1: 0.010369491763412952, s5: 0.0036055417731404305  
depth: 3, iteration: 166000, test\_RMSE: 1.1238137483596802, erank: 36.790561676  
02539, s1: 0.010574948973953724, s5: 0.003612420754507184  
depth: 3, iteration: 168000, test\_RMSE: 1.1238137483596802, erank: 36.504444122  
31445, s1: 0.010784506797790527, s5: 0.0036189425736665726  
depth: 3, iteration: 170000, test\_RMSE: 1.1238137483596802, erank: 36.217662811  
2793, s1: 0.010998271405696869, s5: 0.003625089768320322  
depth: 3, iteration: 172000, test\_RMSE: 1.1238137483596802, erank: 35.930255889  
89258, s1: 0.011216269806027412, s5: 0.003630983177572489  
depth: 3, iteration: 174000, test\_RMSE: 1.1238138675689697, erank: 35.642433166  
503906, s1: 0.011438342742621899, s5: 0.003636519657447934  
depth: 3, iteration: 176000, test\_RMSE: 1.1238138675689697, erank: 35.354164123  
535156, s1: 0.011664611287415028, s5: 0.003641655668616295  
depth: 3, iteration: 178000, test\_RMSE: 1.1238139867782593, erank: 35.065433502

197266, s1: 0.011895105242729187, s5: 0.0036465642042458057  
depth: 3, iteration: 180000, test\_RMSE: 1.1238139867782593, erank: 34.776466369  
628906, s1: 0.012129646725952625, s5: 0.0036510927602648735  
depth: 3, iteration: 182000, test\_RMSE: 1.1238139867782593, erank: 34.487136840  
82031, s1: 0.012368420138955116, s5: 0.0036553549580276012  
depth: 3, iteration: 184000, test\_RMSE: 1.1238141059875488, erank: 34.197853088  
378906, s1: 0.012611187994480133, s5: 0.0036592716351151466  
depth: 3, iteration: 186000, test\_RMSE: 1.1238141059875488, erank: 33.908359527  
58789, s1: 0.012858062982559204, s5: 0.003662888891994953  
depth: 3, iteration: 188000, test\_RMSE: 1.1238141059875488, erank: 33.619033813  
47656, s1: 0.013108806684613228, s5: 0.003666271222755313  
depth: 3, iteration: 190000, test\_RMSE: 1.1238141059875488, erank: 33.329727172  
85156, s1: 0.013363536447286606, s5: 0.0036693753208965063  
depth: 3, iteration: 192000, test\_RMSE: 1.1238142251968384, erank: 33.040580749  
51172, s1: 0.013622230850160122, s5: 0.003672224935144186  
depth: 3, iteration: 194000, test\_RMSE: 1.1238142251968384, erank: 32.751846313  
47656, s1: 0.01388460025191307, s5: 0.003674830310046673  
depth: 3, iteration: 196000, test\_RMSE: 1.1238142251968384, erank: 32.463516235  
35156, s1: 0.014150735922157764, s5: 0.0036771635059267282  
depth: 3, iteration: 198000, test\_RMSE: 1.1238142251968384, erank: 32.175651550  
29297, s1: 0.014420467428863049, s5: 0.0036793514154851437  
depth: 3, iteration: 200000, test\_RMSE: 1.1238142251968384, erank: 31.888357162  
475586, s1: 0.014693996869027615, s5: 0.0036812543403357267  
depth: 3, iteration: 202000, test\_RMSE: 1.123814344406128, erank: 31.6017951965  
33203, s1: 0.014970963820815086, s5: 0.003682955401018262  
depth: 3, iteration: 204000, test\_RMSE: 1.123814344406128, erank: 31.3159141540  
52734, s1: 0.01525152288377285, s5: 0.0036844501737505198  
depth: 3, iteration: 206000, test\_RMSE: 1.123814344406128, erank: 31.0310420989  
99023, s1: 0.015535388141870499, s5: 0.003685767063871026  
depth: 3, iteration: 208000, test\_RMSE: 1.123814344406128, erank: 30.7471332550  
04883, s1: 0.015822596848011017, s5: 0.00368693470954895  
depth: 3, iteration: 210000, test\_RMSE: 1.123814344406128, erank: 30.4643840789  
79492, s1: 0.01611296646296978, s5: 0.003687953809276223  
depth: 3, iteration: 212000, test\_RMSE: 1.1238144636154175, erank: 30.182601928  
710938, s1: 0.016406793147325516, s5: 0.0036888262256979942  
depth: 3, iteration: 214000, test\_RMSE: 1.1238144636154175, erank: 29.902170181  
274414, s1: 0.016703497618436813, s5: 0.003689568256959319  
depth: 3, iteration: 216000, test\_RMSE: 1.1238144636154175, erank: 29.622932434  
08203, s1: 0.017003417015075684, s5: 0.0036902003921568394  
depth: 3, iteration: 218000, test\_RMSE: 1.1238144636154175, erank: 29.345430374  
145508, s1: 0.01730583980679512, s5: 0.003690709825605154  
depth: 3, iteration: 220000, test\_RMSE: 1.1238144636154175, erank: 29.069034576  
416016, s1: 0.017611678689718246, s5: 0.00369109190069139  
depth: 3, iteration: 222000, test\_RMSE: 1.123814582824707, erank: 28.7942333221  
43555, s1: 0.017920317128300667, s5: 0.0036914111115038395  
depth: 3, iteration: 224000, test\_RMSE: 1.123814582824707, erank: 28.5213356018  
0664, s1: 0.018231254070997238, s5: 0.00369160040281713  
depth: 3, iteration: 226000, test\_RMSE: 1.123814582824707, erank: 28.2500686645  
5078, s1: 0.018544895574450493, s5: 0.0036917394027113914  
depth: 3, iteration: 228000, test\_RMSE: 1.123814582824707, erank: 27.9804172515  
86914, s1: 0.01886126399040222, s5: 0.0036918031983077526  
depth: 3, iteration: 230000, test\_RMSE: 1.123814582824707, erank: 27.7126235961  
91406, s1: 0.019180096685886383, s5: 0.0036918397527188063  
depth: 3, iteration: 232000, test\_RMSE: 1.123814582824707, erank: 27.4468021392

82227, s1: 0.019501205533742905, s5: 0.0036918295081704855  
depth: 3, iteration: 234000, test\_RMSE: 1.1238147020339966, erank: 27.182981491  
088867, s1: 0.019824577495455742, s5: 0.003691815072670579  
depth: 3, iteration: 236000, test\_RMSE: 1.1238147020339966, erank: 26.921003341  
674805, s1: 0.020150447264313698, s5: 0.003691761288791895  
depth: 3, iteration: 238000, test\_RMSE: 1.1238147020339966, erank: 26.660997390  
74707, s1: 0.0204786229878664, s5: 0.0036916963290423155  
depth: 3, iteration: 240000, test\_RMSE: 1.1238147020339966, erank: 26.403203964  
2334, s1: 0.020808793604373932, s5: 0.0036916586104780436  
depth: 3, iteration: 242000, test\_RMSE: 1.1238147020339966, erank: 26.147371292  
114258, s1: 0.02114131860435009, s5: 0.003691624151542783  
depth: 3, iteration: 244000, test\_RMSE: 1.1238147020339966, erank: 25.894115447  
998047, s1: 0.02147529274225235, s5: 0.003691597143188119  
depth: 3, iteration: 246000, test\_RMSE: 1.1238147020339966, erank: 25.642467498  
779297, s1: 0.021812260150909424, s5: 0.0036915780510753393  
depth: 3, iteration: 248000, test\_RMSE: 1.1238147020339966, erank: 25.393245697  
021484, s1: 0.022150881588459015, s5: 0.0036916318349540234  
depth: 3, iteration: 250000, test\_RMSE: 1.1238147020339966, erank: 25.146095275  
878906, s1: 0.022491756826639175, s5: 0.0036916974931955338  
depth: 3, iteration: 252000, test\_RMSE: 1.1238147020339966, erank: 24.901288986  
206055, s1: 0.022834546864032745, s5: 0.003691831137984991  
depth: 3, iteration: 254000, test\_RMSE: 1.1238147020339966, erank: 24.658884048  
461914, s1: 0.02317904122173786, s5: 0.0036919941194355488  
depth: 3, iteration: 256000, test\_RMSE: 1.1238147020339966, erank: 24.418745040  
893555, s1: 0.023525504395365715, s5: 0.003692226018756628  
depth: 3, iteration: 258000, test\_RMSE: 1.1238147020339966, erank: 24.180774688  
720703, s1: 0.02387411892414093, s5: 0.003692516591399908  
depth: 3, iteration: 260000, test\_RMSE: 1.1238147020339966, erank: 23.945262908  
935547, s1: 0.024224406108260155, s5: 0.0036928951740264893  
depth: 3, iteration: 262000, test\_RMSE: 1.1238147020339966, erank: 23.712232589  
72168, s1: 0.02457631379365921, s5: 0.0036933303344994783  
depth: 3, iteration: 264000, test\_RMSE: 1.1238147020339966, erank: 23.481325149  
536133, s1: 0.02493034489452839, s5: 0.003693805541843176  
depth: 3, iteration: 266000, test\_RMSE: 1.1238147020339966, erank: 23.252737045  
288086, s1: 0.02528633177280426, s5: 0.0036944763269275427  
depth: 3, iteration: 268000, test\_RMSE: 1.1238147020339966, erank: 23.026403427  
124023, s1: 0.02564435824751854, s5: 0.0036952344235032797  
depth: 3, iteration: 270000, test\_RMSE: 1.1238147020339966, erank: 22.802511215  
20996, s1: 0.026004033163189888, s5: 0.003695995546877384  
depth: 3, iteration: 272000, test\_RMSE: 1.1238147020339966, erank: 22.580945968  
62793, s1: 0.026365619152784348, s5: 0.003696898464113474  
depth: 3, iteration: 274000, test\_RMSE: 1.1238147020339966, erank: 22.361783981  
323242, s1: 0.026728812605142593, s5: 0.0036979259457439184  
depth: 3, iteration: 276000, test\_RMSE: 1.1238147020339966, erank: 22.144941329  
956055, s1: 0.027093829587101936, s5: 0.0036989960353821516  
depth: 3, iteration: 278000, test\_RMSE: 1.123814582824707, erank: 21.9301986694  
33594, s1: 0.027461126446723938, s5: 0.003700236091390252  
depth: 3, iteration: 280000, test\_RMSE: 1.123814582824707, erank: 21.7175655364  
99023, s1: 0.0278306994587183, s5: 0.003701582318171859  
depth: 3, iteration: 282000, test\_RMSE: 1.123814582824707, erank: 21.5075283050  
5371, s1: 0.028201546519994736, s5: 0.00370303587988019  
depth: 3, iteration: 284000, test\_RMSE: 1.123814582824707, erank: 21.2995853424  
07227, s1: 0.02857465110719204, s5: 0.0037046277429908514  
depth: 3, iteration: 286000, test\_RMSE: 1.123814582824707, erank: 21.0938587188



7207, s1: 0.02894974686205387, s5: 0.003706352086737752  
depth: 3, iteration: 288000, test\_RMSE: 1.1238144636154175, erank: 20.890344619  
750977, s1: 0.029326898977160454, s5: 0.003708217991515994  
depth: 3, iteration: 290000, test\_RMSE: 1.1238144636154175, erank: 20.688968658  
447266, s1: 0.029706330969929695, s5: 0.003710210556164384  
depth: 3, iteration: 292000, test\_RMSE: 1.1238144636154175, erank: 20.489919662  
475586, s1: 0.0300874263048172, s5: 0.003712297650054097  
depth: 3, iteration: 294000, test\_RMSE: 1.123814344406128, erank: 20.2929878234  
86328, s1: 0.030470959842205048, s5: 0.0037145756650716066  
depth: 3, iteration: 296000, test\_RMSE: 1.123814344406128, erank: 20.0981369018  
5547, s1: 0.030856769531965256, s5: 0.003716969396919012  
depth: 3, iteration: 298000, test\_RMSE: 1.1238142251968384, erank: 19.905534744  
262695, s1: 0.031244628131389618, s5: 0.0037195030599832535  
depth: 3, iteration: 300000, test\_RMSE: 1.1238142251968384, erank: 19.714759826  
660156, s1: 0.03163528069853783, s5: 0.0037221794482320547  
depth: 3, iteration: 302000, test\_RMSE: 1.1238142251968384, erank: 19.526107788  
085938, s1: 0.03202810883522034, s5: 0.0037250048480927944  
depth: 3, iteration: 304000, test\_RMSE: 1.1238142251968384, erank: 19.339540481  
567383, s1: 0.03242321312427521, s5: 0.0037279671523720026  
depth: 3, iteration: 306000, test\_RMSE: 1.1238141059875488, erank: 19.154853820  
80078, s1: 0.03282111883163452, s5: 0.0037310488987714052  
depth: 3, iteration: 308000, test\_RMSE: 1.1238141059875488, erank: 18.972249984  
74121, s1: 0.033221300691366196, s5: 0.0037343527656048536  
depth: 3, iteration: 310000, test\_RMSE: 1.1238139867782593, erank: 18.791509628  
2959, s1: 0.03362433239817619, s5: 0.003737739287316799  
depth: 3, iteration: 312000, test\_RMSE: 1.1238139867782593, erank: 18.612712860  
107422, s1: 0.03402993083000183, s5: 0.0037412839010357857  
depth: 3, iteration: 314000, test\_RMSE: 1.1238138675689697, erank: 18.435800552  
368164, s1: 0.03443834185600281, s5: 0.003744977992027998  
depth: 3, iteration: 316000, test\_RMSE: 1.1238137483596802, erank: 18.260553359  
98535, s1: 0.034850068390369415, s5: 0.003748801304027438  
depth: 3, iteration: 318000, test\_RMSE: 1.1238137483596802, erank: 18.087463378  
90625, s1: 0.03526391088962555, s5: 0.003752767574042082  
depth: 3, iteration: 320000, test\_RMSE: 1.1238137483596802, erank: 17.916055679  
32129, s1: 0.03568102419376373, s5: 0.0037568698171526194  
depth: 3, iteration: 322000, test\_RMSE: 1.1238136291503906, erank: 17.746143341  
064453, s1: 0.03610191494226456, s5: 0.0037611823063343763  
depth: 3, iteration: 324000, test\_RMSE: 1.123813509941101, erank: 17.5783481597  
9004, s1: 0.036524876952171326, s5: 0.0037655809428542852  
depth: 3, iteration: 326000, test\_RMSE: 1.123813509941101, erank: 17.4118461608  
88672, s1: 0.03695229813456535, s5: 0.003770200302824378  
depth: 3, iteration: 328000, test\_RMSE: 1.1238133907318115, erank: 17.247320175  
1709, s1: 0.037382178008556366, s5: 0.0037749088369309902  
depth: 3, iteration: 330000, test\_RMSE: 1.123813271522522, erank: 17.0843582153  
3203, s1: 0.03781570494174957, s5: 0.0037797661498188972  
depth: 3, iteration: 332000, test\_RMSE: 1.1238131523132324, erank: 16.922962188  
720703, s1: 0.03825295716524124, s5: 0.003784799249842763  
depth: 3, iteration: 334000, test\_RMSE: 1.1238131523132324, erank: 16.763235092  
163086, s1: 0.038693685084581375, s5: 0.00378994969651103  
depth: 3, iteration: 336000, test\_RMSE: 1.1238130331039429, erank: 16.605047225  
95215, s1: 0.03913819417357445, s5: 0.0037952368147671223  
depth: 3, iteration: 338000, test\_RMSE: 1.1238129138946533, erank: 16.448413848  
876953, s1: 0.03958667069673538, s5: 0.0038006906397640705  
depth: 3, iteration: 340000, test\_RMSE: 1.1238127946853638, erank: 16.293142318

725586, s1: 0.04003937914967537, s5: 0.0038062550593167543  
depth: 3, iteration: 342000, test\_RMSE: 1.1238126754760742, erank: 16.139505386  
35254, s1: 0.04049593210220337, s5: 0.0038119691889733076  
depth: 3, iteration: 344000, test\_RMSE: 1.1238125562667847, erank: 15.987321853  
637695, s1: 0.040956687182188034, s5: 0.003817829303443432  
depth: 3, iteration: 346000, test\_RMSE: 1.1238124370574951, erank: 15.836443901  
062012, s1: 0.04142220690846443, s5: 0.003823815379291773  
depth: 3, iteration: 348000, test\_RMSE: 1.1238123178482056, erank: 15.686971664  
428711, s1: 0.041892122477293015, s5: 0.0038299052976071835  
depth: 3, iteration: 350000, test\_RMSE: 1.123812198638916, erank: 15.5388727188  
11035, s1: 0.04236672446131706, s5: 0.0038361442275345325  
depth: 3, iteration: 352000, test\_RMSE: 1.1238120794296265, erank: 15.392175674  
438477, s1: 0.042845938354730606, s5: 0.00384249584749341  
depth: 3, iteration: 354000, test\_RMSE: 1.123811960220337, erank: 15.2467031478  
88184, s1: 0.04333028569817543, s5: 0.0038489552680402994  
depth: 3, iteration: 356000, test\_RMSE: 1.1238118410110474, erank: 15.102602958  
6792, s1: 0.043819379061460495, s5: 0.003855545539408922  
depth: 3, iteration: 358000, test\_RMSE: 1.1238116025924683, erank: 14.959714889  
526367, s1: 0.04431390389800072, s5: 0.0038622410502284765  
depth: 3, iteration: 360000, test\_RMSE: 1.1238114833831787, erank: 14.818076133  
728027, s1: 0.04481370747089386, s5: 0.0038690073415637016  
depth: 3, iteration: 362000, test\_RMSE: 1.1238113641738892, erank: 14.677508354  
187012, s1: 0.04531951621174812, s5: 0.0038758874870836735  
depth: 3, iteration: 364000, test\_RMSE: 1.1238112449645996, erank: 14.538201332  
092285, s1: 0.04583064839243889, s5: 0.0038828228134661913  
depth: 3, iteration: 366000, test\_RMSE: 1.1238110065460205, erank: 14.400044441  
223145, s1: 0.046347688883543015, s5: 0.003889833576977253  
depth: 3, iteration: 368000, test\_RMSE: 1.123810887336731, erank: 14.2630176544  
18945, s1: 0.046870846301317215, s5: 0.003896907204762101  
depth: 3, iteration: 370000, test\_RMSE: 1.1238107681274414, erank: 14.127121925  
354004, s1: 0.047399990260601044, s5: 0.0039039766415953636  
depth: 3, iteration: 372000, test\_RMSE: 1.1238105297088623, erank: 13.992209434  
509277, s1: 0.047935981303453445, s5: 0.003911161329597235  
depth: 3, iteration: 374000, test\_RMSE: 1.1238104104995728, erank: 13.858392715  
454102, s1: 0.04847843572497368, s5: 0.0039183394983410835  
depth: 3, iteration: 376000, test\_RMSE: 1.1238101720809937, erank: 13.725613594  
055176, s1: 0.04902767762541771, s5: 0.003925599157810211  
depth: 3, iteration: 378000, test\_RMSE: 1.1238099336624146, erank: 13.593879699  
707031, s1: 0.04958384484052658, s5: 0.00393284484744072  
depth: 3, iteration: 380000, test\_RMSE: 1.123809814453125, erank: 13.4632005691  
52832, s1: 0.05014694109559059, s5: 0.003940175287425518  
depth: 3, iteration: 382000, test\_RMSE: 1.123809576034546, erank: 13.3335084915  
16113, s1: 0.050717368721961975, s5: 0.00394746707752347  
depth: 3, iteration: 384000, test\_RMSE: 1.1238093376159668, erank: 13.204706192  
016602, s1: 0.051295675337314606, s5: 0.003954761661589146  
depth: 3, iteration: 386000, test\_RMSE: 1.1238090991973877, erank: 13.076921463  
012695, s1: 0.051881492137908936, s5: 0.003962063230574131  
depth: 3, iteration: 388000, test\_RMSE: 1.1238088607788086, erank: 12.950042724  
609375, s1: 0.05247535929083824, s5: 0.003969348035752773  
depth: 3, iteration: 390000, test\_RMSE: 1.1238086223602295, erank: 12.824025154  
11377, s1: 0.0530778132379055, s5: 0.003976575098931789  
depth: 3, iteration: 392000, test\_RMSE: 1.1238083839416504, erank: 12.698842048  
64502, s1: 0.05368896201252937, s5: 0.00398376677185297  
depth: 3, iteration: 394000, test\_RMSE: 1.1238082647323608, erank: 12.574584960

9375, s1: 0.054308682680130005, s5: 0.003990940749645233  
depth: 3, iteration: 396000, test\_RMSE: 1.1238079071044922, erank: 12.451019287  
109375, s1: 0.05493827536702156, s5: 0.0039980546571314335  
depth: 3, iteration: 398000, test\_RMSE: 1.1238077878952026, erank: 12.328410148  
620605, s1: 0.05557647719979286, s5: 0.004005113150924444  
depth: 3, iteration: 400000, test\_RMSE: 1.123807430267334, erank: 12.2065525054  
93164, s1: 0.05622449144721031, s5: 0.004012163728475571  
depth: 3, iteration: 402000, test\_RMSE: 1.1238071918487549, erank: 12.085599899  
291992, s1: 0.05688195303082466, s5: 0.0040191346779465675  
depth: 3, iteration: 404000, test\_RMSE: 1.1238069534301758, erank: 11.965274810  
791016, s1: 0.05755036324262619, s5: 0.004026064183562994  
depth: 3, iteration: 406000, test\_RMSE: 1.1238065958023071, erank: 11.845808982  
849121, s1: 0.05822882056236267, s5: 0.004032969940453768  
depth: 3, iteration: 408000, test\_RMSE: 1.123806357383728, erank: 11.7270412445  
06836, s1: 0.05891815572977066, s5: 0.004039811436086893  
depth: 3, iteration: 410000, test\_RMSE: 1.1238059997558594, erank: 11.608968734  
741211, s1: 0.05961909145116806, s5: 0.00404660589993  
depth: 3, iteration: 412000, test\_RMSE: 1.1238057613372803, erank: 11.491668701  
171875, s1: 0.06033123657107353, s5: 0.004053241107612848  
depth: 3, iteration: 414000, test\_RMSE: 1.1238054037094116, erank: 11.374988555  
908203, s1: 0.06105585768818855, s5: 0.004059885162860155  
depth: 3, iteration: 416000, test\_RMSE: 1.1238051652908325, erank: 11.259097099  
3042, s1: 0.06179193779826164, s5: 0.004066465888172388  
depth: 3, iteration: 418000, test\_RMSE: 1.1238048076629639, erank: 11.143758773  
803711, s1: 0.06254133582115173, s5: 0.004072980955243111  
depth: 3, iteration: 420000, test\_RMSE: 1.1238044500350952, erank: 11.029084205  
627441, s1: 0.06330367922782898, s5: 0.004079406149685383  
depth: 3, iteration: 422000, test\_RMSE: 1.1238040924072266, erank: 10.915085792  
541504, s1: 0.06407935172319412, s5: 0.0040857866406440735  
depth: 3, iteration: 424000, test\_RMSE: 1.123803734779358, erank: 10.8017082214  
35547, s1: 0.0648689866065979, s5: 0.004092180170118809  
depth: 3, iteration: 426000, test\_RMSE: 1.1238033771514893, erank: 10.688835144  
042969, s1: 0.06567355245351791, s5: 0.004098470788449049  
depth: 3, iteration: 428000, test\_RMSE: 1.1238030195236206, erank: 10.576537132  
263184, s1: 0.06649291515350342, s5: 0.004104766063392162  
depth: 3, iteration: 430000, test\_RMSE: 1.1238025426864624, erank: 10.464847564  
697266, s1: 0.06732717156410217, s5: 0.004111056216061115  
depth: 3, iteration: 432000, test\_RMSE: 1.1238021850585938, erank: 10.353759765  
625, s1: 0.06817710399627686, s5: 0.004117333330214024  
depth: 3, iteration: 434000, test\_RMSE: 1.1238017082214355, erank: 10.243257522  
583008, s1: 0.06904321908950806, s5: 0.004123648628592491  
depth: 3, iteration: 436000, test\_RMSE: 1.123801350593567, erank: 10.1332845687  
86621, s1: 0.06992624700069427, s5: 0.00413000863045454  
depth: 3, iteration: 438000, test\_RMSE: 1.1238008737564087, erank: 10.023797035  
217285, s1: 0.07082674652338028, s5: 0.004136344883590937  
depth: 3, iteration: 440000, test\_RMSE: 1.12380051612854, erank: 9.914855957031  
25, s1: 0.07174527645111084, s5: 0.004142673220485449  
depth: 3, iteration: 442000, test\_RMSE: 1.1238000392913818, erank: 9.8064260482  
78809, s1: 0.07268233597278595, s5: 0.004149090964347124  
depth: 3, iteration: 444000, test\_RMSE: 1.1237995624542236, erank: 9.6985502243  
042, s1: 0.0736382007598877, s5: 0.004155497997999191  
depth: 3, iteration: 446000, test\_RMSE: 1.1237990856170654, erank: 9.5911264419  
55566, s1: 0.07461398094892502, s5: 0.004161982797086239  
depth: 3, iteration: 448000, test\_RMSE: 1.1237984895706177, erank: 9.4841966629

02832, s1: 0.07561039179563522, s5: 0.0041685327887535095  
depth: 3, iteration: 450000, test\_RMSE: 1.1237980127334595, erank: 9.3777456283  
56934, s1: 0.07662788033485413, s5: 0.004175124689936638  
depth: 3, iteration: 452000, test\_RMSE: 1.1237975358963013, erank: 9.2717895507  
8125, s1: 0.0776672512292862, s5: 0.0041818018071353436  
depth: 3, iteration: 454000, test\_RMSE: 1.1237969398498535, erank: 9.1663026809  
69238, s1: 0.07872925698757172, s5: 0.00418859114870429  
depth: 3, iteration: 456000, test\_RMSE: 1.1237963438034058, erank: 9.0612869262  
69531, s1: 0.07981444895267487, s5: 0.004195455461740494  
depth: 3, iteration: 458000, test\_RMSE: 1.1237958669662476, erank: 8.9567642211  
91406, s1: 0.08092354238033295, s5: 0.004202377051115036  
depth: 3, iteration: 460000, test\_RMSE: 1.1237952709197998, erank: 8.8525924682  
61719, s1: 0.08205851912498474, s5: 0.004209365230053663  
depth: 3, iteration: 462000, test\_RMSE: 1.1237945556640625, erank: 8.7489681243  
89648, s1: 0.08321799337863922, s5: 0.00421641580760479  
depth: 3, iteration: 464000, test\_RMSE: 1.1237939596176147, erank: 8.6457471847  
53418, s1: 0.08440472185611725, s5: 0.0042236484587192535  
depth: 3, iteration: 466000, test\_RMSE: 1.123793363571167, erank: 8.54287624359  
1309, s1: 0.08561994880437851, s5: 0.004230896942317486  
depth: 3, iteration: 468000, test\_RMSE: 1.1237926483154297, erank: 8.4405488967  
8955, s1: 0.086862713098526, s5: 0.004238320980221033  
depth: 3, iteration: 470000, test\_RMSE: 1.123792052268982, erank: 8.33875179290  
7715, s1: 0.08813431113958359, s5: 0.004245849791914225  
depth: 3, iteration: 472000, test\_RMSE: 1.1237913370132446, erank: 8.2372646331  
78711, s1: 0.08943827450275421, s5: 0.004253552295267582  
depth: 3, iteration: 474000, test\_RMSE: 1.1237906217575073, erank: 8.1362361907  
95898, s1: 0.0907733142375946, s5: 0.004261366557329893  
depth: 3, iteration: 476000, test\_RMSE: 1.1237897872924805, erank: 8.0356359481  
81152, s1: 0.09214106947183609, s5: 0.00426931818947196  
depth: 3, iteration: 478000, test\_RMSE: 1.1237890720367432, erank: 7.9353747367  
85889, s1: 0.09354391694068909, s5: 0.004277367144823074  
depth: 3, iteration: 480000, test\_RMSE: 1.1237882375717163, erank: 7.8355698585  
51025, s1: 0.09498188644647598, s5: 0.004285591188818216  
depth: 3, iteration: 482000, test\_RMSE: 1.1237874031066895, erank: 7.7361536026  
00098, s1: 0.09645721316337585, s5: 0.004293940495699644  
depth: 3, iteration: 484000, test\_RMSE: 1.1237866878509521, erank: 7.6372838020  
32471, s1: 0.09796907007694244, s5: 0.004302455112338066  
depth: 3, iteration: 486000, test\_RMSE: 1.1237857341766357, erank: 7.5387568473  
81592, s1: 0.09952163696289062, s5: 0.004311151336878538  
depth: 3, iteration: 488000, test\_RMSE: 1.1237847805023193, erank: 7.4405937194  
82422, s1: 0.10111590474843979, s5: 0.0043199798092246056  
depth: 3, iteration: 490000, test\_RMSE: 1.1237839460372925, erank: 7.3428778648  
376465, s1: 0.1027529314160347, s5: 0.0043289936147630215  
depth: 3, iteration: 492000, test\_RMSE: 1.123782992362976, erank: 7.24571180343  
6279, s1: 0.10443275421857834, s5: 0.0043381997384130955  
depth: 3, iteration: 494000, test\_RMSE: 1.1237820386886597, erank: 7.1489143371  
58203, s1: 0.10615887492895126, s5: 0.00434758048504591  
depth: 3, iteration: 496000, test\_RMSE: 1.1237809658050537, erank: 7.0524802207  
94678, s1: 0.10793416947126389, s5: 0.0043571144342422485  
depth: 3, iteration: 498000, test\_RMSE: 1.1237800121307373, erank: 6.9564867019  
65332, s1: 0.10975930839776993, s5: 0.004366873297840357  
depth: 3, iteration: 500000, test\_RMSE: 1.1237789392471313, erank: 6.8609671592  
7124, s1: 0.11163526028394699, s5: 0.004376779776066542  
depth: 3, iteration: 502000, test\_RMSE: 1.1237778663635254, erank: 6.7659039497

37549, s1: 0.11356555670499802, s5: 0.004386914893984795  
depth: 3, iteration: 504000, test\_RMSE: 1.1237766742706299, erank: 6.6713442802  
4292, s1: 0.11555073410272598, s5: 0.0043971906416118145  
depth: 3, iteration: 506000, test\_RMSE: 1.1237754821777344, erank: 6.5772218704  
22363, s1: 0.1175943911075592, s5: 0.004407655447721481  
depth: 3, iteration: 508000, test\_RMSE: 1.1237742900848389, erank: 6.4834775924  
68262, s1: 0.11969985067844391, s5: 0.004418322816491127  
depth: 3, iteration: 510000, test\_RMSE: 1.1237729787826538, erank: 6.3902187347  
41211, s1: 0.12186802178621292, s5: 0.004429174121469259  
depth: 3, iteration: 512000, test\_RMSE: 1.1237717866897583, erank: 6.2974019050  
598145, s1: 0.12410292029380798, s5: 0.0044402386993169785  
depth: 3, iteration: 514000, test\_RMSE: 1.1237703561782837, erank: 6.2049984931  
9458, s1: 0.126407653093338, s5: 0.004451500717550516  
depth: 3, iteration: 516000, test\_RMSE: 1.123768925666809, erank: 6.11315631866  
4551, s1: 0.12878230214118958, s5: 0.004463000223040581  
depth: 3, iteration: 518000, test\_RMSE: 1.1237674951553345, erank: 6.0218725204  
46777, s1: 0.13122974336147308, s5: 0.0044746664352715015  
depth: 3, iteration: 520000, test\_RMSE: 1.1237660646438599, erank: 5.9310216903  
68652, s1: 0.13375696539878845, s5: 0.0044865477830171585  
depth: 3, iteration: 522000, test\_RMSE: 1.1237645149230957, erank: 5.8406801223  
75488, s1: 0.13636597990989685, s5: 0.004498666618019342  
depth: 3, iteration: 524000, test\_RMSE: 1.1237629652023315, erank: 5.7508192062  
37793, s1: 0.13906095921993256, s5: 0.0045110611245036125  
depth: 3, iteration: 526000, test\_RMSE: 1.1237612962722778, erank: 5.6615810394  
28711, s1: 0.1418420821428299, s5: 0.004523640964180231  
depth: 3, iteration: 528000, test\_RMSE: 1.1237596273422241, erank: 5.5727648735  
04639, s1: 0.14471887052059174, s5: 0.004536413587629795  
depth: 3, iteration: 530000, test\_RMSE: 1.1237578392028809, erank: 5.4845933914  
18457, s1: 0.14769010245800018, s5: 0.004549517761915922  
depth: 3, iteration: 532000, test\_RMSE: 1.123755931854248, erank: 5.39691066741  
9434, s1: 0.1507648378610611, s5: 0.004562752321362495  
depth: 3, iteration: 534000, test\_RMSE: 1.1237540245056152, erank: 5.3097801208  
49609, s1: 0.15394575893878937, s5: 0.004576348699629307  
depth: 3, iteration: 536000, test\_RMSE: 1.1237521171569824, erank: 5.2232751846  
31348, s1: 0.1572362631559372, s5: 0.004590137396007776  
depth: 3, iteration: 538000, test\_RMSE: 1.12375009059906, erank: 5.137362957000  
732, s1: 0.16064360737800598, s5: 0.0046042329631745815  
depth: 3, iteration: 540000, test\_RMSE: 1.1237479448318481, erank: 5.0520253181  
45752, s1: 0.16417410969734192, s5: 0.004618542268872261  
depth: 3, iteration: 542000, test\_RMSE: 1.1237457990646362, erank: 4.9672398567  
19971, s1: 0.1678348332643509, s5: 0.004633068107068539  
depth: 3, iteration: 544000, test\_RMSE: 1.1237434148788452, erank: 4.8831763267  
51709, s1: 0.17162635922431946, s5: 0.004647935274988413  
depth: 3, iteration: 546000, test\_RMSE: 1.1237410306930542, erank: 4.7997512817  
38281, s1: 0.17555853724479675, s5: 0.004663030616939068  
depth: 3, iteration: 548000, test\_RMSE: 1.1237386465072632, erank: 4.7169923782  
34863, s1: 0.1796378344297409, s5: 0.004678383003920317  
depth: 3, iteration: 550000, test\_RMSE: 1.123736023902893, erank: 4.63488340377  
8076, s1: 0.1838735193014145, s5: 0.00469398545101285  
depth: 3, iteration: 552000, test\_RMSE: 1.1237332820892334, erank: 4.5534310340  
88135, s1: 0.18827342987060547, s5: 0.004709891974925995  
depth: 3, iteration: 554000, test\_RMSE: 1.1237305402755737, erank: 4.4726514816  
28418, s1: 0.19284646213054657, s5: 0.00472603552043438  
depth: 3, iteration: 556000, test\_RMSE: 1.1237276792526245, erank: 4.3926324844

36035, s1: 0.19759780168533325, s5: 0.004742488730698824  
depth: 3, iteration: 558000, test\_RMSE: 1.1237245798110962, erank: 4.3132600784  
30176, s1: 0.20254310965538025, s5: 0.004759181756526232  
depth: 3, iteration: 560000, test\_RMSE: 1.1237214803695679, erank: 4.2347116470  
33691, s1: 0.2076837420463562, s5: 0.0047761923633515835  
depth: 3, iteration: 562000, test\_RMSE: 1.12371826171875, erank: 4.156874179840  
088, s1: 0.21303768455982208, s5: 0.004793452564626932  
depth: 3, iteration: 564000, test\_RMSE: 1.123714804649353, erank: 4.07980251312  
2559, s1: 0.2186153382062912, s5: 0.004811104387044907  
depth: 3, iteration: 566000, test\_RMSE: 1.1237112283706665, erank: 4.0035252571  
10596, s1: 0.22442688047885895, s5: 0.004828975535929203  
depth: 3, iteration: 568000, test\_RMSE: 1.1237075328826904, erank: 3.9279851913  
45215, s1: 0.23048840463161469, s5: 0.004847091622650623  
depth: 3, iteration: 570000, test\_RMSE: 1.1237035989761353, erank: 3.8532874584  
198, s1: 0.23681114614009857, s5: 0.004865514114499092  
depth: 3, iteration: 572000, test\_RMSE: 1.1236995458602905, erank: 3.7794430255  
889893, s1: 0.24340730905532837, s5: 0.004884213209152222  
depth: 3, iteration: 574000, test\_RMSE: 1.1236952543258667, erank: 3.7063810825  
3479, s1: 0.25030314922332764, s5: 0.004903238732367754  
depth: 3, iteration: 576000, test\_RMSE: 1.1236908435821533, erank: 3.6342139244  
07959, s1: 0.25750550627708435, s5: 0.004922558553516865  
depth: 3, iteration: 578000, test\_RMSE: 1.1236861944198608, erank: 3.5628643035  
88867, s1: 0.2650417387485504, s5: 0.004942199680954218  
depth: 3, iteration: 580000, test\_RMSE: 1.1236813068389893, erank: 3.4924497604  
370117, s1: 0.2729201912879944, s5: 0.004962111823260784  
depth: 3, iteration: 582000, test\_RMSE: 1.1236761808395386, erank: 3.4228563308  
71582, s1: 0.2811754047870636, s5: 0.00498230941593647  
depth: 3, iteration: 584000, test\_RMSE: 1.1236708164215088, erank: 3.3541765213  
012695, s1: 0.28982383012771606, s5: 0.005002822261303663  
depth: 3, iteration: 586000, test\_RMSE: 1.1236652135849, erank: 3.2864589691162  
11, s1: 0.29888424277305603, s5: 0.005023629404604435  
depth: 3, iteration: 588000, test\_RMSE: 1.123659372329712, erank: 3.21964764595  
03174, s1: 0.3083910644054413, s5: 0.005044717341661453  
depth: 3, iteration: 590000, test\_RMSE: 1.1236531734466553, erank: 3.1537599563  
598633, s1: 0.31837332248687744, s5: 0.0050661442801356316  
depth: 3, iteration: 592000, test\_RMSE: 1.12364661693573, erank: 3.088855028152  
466, s1: 0.3288547396659851, s5: 0.005087800789624453  
depth: 3, iteration: 594000, test\_RMSE: 1.1236398220062256, erank: 3.0248696804  
04663, s1: 0.3398791253566742, s5: 0.005109765101224184  
depth: 3, iteration: 596000, test\_RMSE: 1.123632550239563, erank: 2.96190094947  
81494, s1: 0.3514713943004608, s5: 0.005132105201482773  
depth: 3, iteration: 598000, test\_RMSE: 1.1236250400543213, erank: 2.8998951911  
92627, s1: 0.3636787235736847, s5: 0.005154753103852272  
depth: 3, iteration: 600000, test\_RMSE: 1.1236170530319214, erank: 2.8388996124  
26758, s1: 0.3765384554862976, s5: 0.005177663639187813  
depth: 3, iteration: 602000, test\_RMSE: 1.1236085891723633, erank: 2.7788963317  
871094, s1: 0.3901014029979706, s5: 0.005200920160859823  
depth: 3, iteration: 604000, test\_RMSE: 1.1235997676849365, erank: 2.7199506759  
643555, s1: 0.4044048488140106, s5: 0.005224450957030058  
depth: 3, iteration: 606000, test\_RMSE: 1.123590350151062, erank: 2.66197514533  
9966, s1: 0.41952165961265564, s5: 0.005248251836746931  
depth: 3, iteration: 608000, test\_RMSE: 1.1235804557800293, erank: 2.6050598621  
36841, s1: 0.4354970455169678, s5: 0.005272270180284977  
depth: 3, iteration: 610000, test\_RMSE: 1.1235699653625488, erank: 2.5491971969

60449, s1: 0.4523943364620209, s5: 0.005296590272337198  
depth: 3, iteration: 612000, test\_RMSE: 1.1235588788986206, erank: 2.4943692684  
173584, s1: 0.4702911972999573, s5: 0.005321191158145666  
depth: 3, iteration: 614000, test\_RMSE: 1.123547077178955, erank: 2.44058370590  
20996, s1: 0.48926326632499695, s5: 0.0053461166098713875  
depth: 3, iteration: 616000, test\_RMSE: 1.1235346794128418, erank: 2.3878772258  
758545, s1: 0.5093856453895569, s5: 0.005371255800127983  
depth: 3, iteration: 618000, test\_RMSE: 1.123521327972412, erank: 2.33622288703  
91846, s1: 0.5307577252388, s5: 0.005396637599915266  
depth: 3, iteration: 620000, test\_RMSE: 1.1235073804855347, erank: 2.2856602668  
762207, s1: 0.5534682869911194, s5: 0.005422358401119709  
depth: 3, iteration: 622000, test\_RMSE: 1.1234923601150513, erank: 2.2361586093  
90259, s1: 0.577637791633606, s5: 0.005448266863822937  
depth: 3, iteration: 624000, test\_RMSE: 1.123476505279541, erank: 2.18769717216  
4917, s1: 0.603404700756073, s5: 0.005474402103573084  
depth: 3, iteration: 626000, test\_RMSE: 1.1234595775604248, erank: 2.1403670310  
97412, s1: 0.6308541297912598, s5: 0.00550081068649888  
depth: 3, iteration: 628000, test\_RMSE: 1.1234415769577026, erank: 2.0941169261  
932373, s1: 0.6601632237434387, s5: 0.005527544766664505  
depth: 3, iteration: 630000, test\_RMSE: 1.123422384262085, erank: 2.04893922805  
78613, s1: 0.6914933919906616, s5: 0.005554419942200184  
depth: 3, iteration: 632000, test\_RMSE: 1.1234018802642822, erank: 2.0048375129  
699707, s1: 0.7250250577926636, s5: 0.005581546574831009  
depth: 3, iteration: 634000, test\_RMSE: 1.1233799457550049, erank: 1.9618123769  
760132, s1: 0.7609571814537048, s5: 0.005608915351331234  
depth: 3, iteration: 636000, test\_RMSE: 1.1233564615249634, erank: 1.9198975563  
049316, s1: 0.799480140209198, s5: 0.005636419169604778  
depth: 3, iteration: 638000, test\_RMSE: 1.1233313083648682, erank: 1.8790559768  
676758, s1: 0.8408645391464233, s5: 0.0056641846895217896  
depth: 3, iteration: 640000, test\_RMSE: 1.1233043670654297, erank: 1.8392531871  
795654, s1: 0.8854204416275024, s5: 0.005692189559340477  
depth: 3, iteration: 642000, test\_RMSE: 1.1232755184173584, erank: 1.8005573749  
542236, s1: 0.9333801865577698, s5: 0.005720234476029873  
depth: 3, iteration: 644000, test\_RMSE: 1.1232445240020752, erank: 1.7629323005  
67627, s1: 0.9851157665252686, s5: 0.005748556461185217  
depth: 3, iteration: 646000, test\_RMSE: 1.123211145401001, erank: 1.72640800476  
07422, s1: 1.040954828262329, s5: 0.005776953883469105  
depth: 3, iteration: 648000, test\_RMSE: 1.1231752634048462, erank: 1.6909081935  
882568, s1: 1.101427674293518, s5: 0.005805654916912317  
depth: 3, iteration: 650000, test\_RMSE: 1.1231365203857422, erank: 1.6564598083  
496094, s1: 1.1669659614562988, s5: 0.005834432318806648  
depth: 3, iteration: 652000, test\_RMSE: 1.123094916343689, erank: 1.62310564517  
97485, s1: 1.2380173206329346, s5: 0.0058632646687328815  
depth: 3, iteration: 654000, test\_RMSE: 1.1230498552322388, erank: 1.5907511711  
120605, s1: 1.3153605461120605, s5: 0.005892352666705847  
depth: 3, iteration: 656000, test\_RMSE: 1.1230013370513916, erank: 1.5594812631  
607056, s1: 1.3994804620742798, s5: 0.005921493284404278  
depth: 3, iteration: 658000, test\_RMSE: 1.1229488849639893, erank: 1.5292426347  
732544, s1: 1.4912450313568115, s5: 0.005950783379375935  
depth: 3, iteration: 660000, test\_RMSE: 1.1228920221328735, erank: 1.4999821186  
065674, s1: 1.5916798114776611, s5: 0.005980168003588915  
depth: 3, iteration: 662000, test\_RMSE: 1.1228305101394653, erank: 1.4717826843  
261719, s1: 1.7015001773834229, s5: 0.006009677890688181  
depth: 3, iteration: 664000, test\_RMSE: 1.122763991355896, erank: 1.44459390640

2588, s1: 1.8219544887542725, s5: 0.006039207801222801  
depth: 3, iteration: 666000, test\_RMSE: 1.1226918697357178, erank: 1.4184061288  
833618, s1: 1.9543423652648926, s5: 0.006068881135433912  
depth: 3, iteration: 668000, test\_RMSE: 1.122613787651062, erank: 1.39320981502  
53296, s1: 2.10013484954834, s5: 0.006098635960370302  
depth: 3, iteration: 670000, test\_RMSE: 1.122529149055481, erank: 1.36895561218  
26172, s1: 2.2612545490264893, s5: 0.006128417328000069  
depth: 3, iteration: 672000, test\_RMSE: 1.122437596321106, erank: 1.34571349620  
8191, s1: 2.439185380935669, s5: 0.006158377043902874  
depth: 3, iteration: 674000, test\_RMSE: 1.1223385334014893, erank: 1.3234349489  
212036, s1: 2.636347532272339, s5: 0.0061882780864834785  
depth: 3, iteration: 676000, test\_RMSE: 1.1222314834594727, erank: 1.3021090030  
670166, s1: 2.855264186859131, s5: 0.006218311842530966  
depth: 3, iteration: 678000, test\_RMSE: 1.122116208076477, erank: 1.28173136711  
1206, s1: 3.098832845687866, s5: 0.006248341873288155  
depth: 3, iteration: 680000, test\_RMSE: 1.1219922304153442, erank: 1.2622866630  
5542, s1: 3.3703994750976562, s5: 0.0062784780748188496  
depth: 3, iteration: 682000, test\_RMSE: 1.1218596696853638, erank: 1.2437674999  
23706, s1: 3.6737782955169678, s5: 0.006308681331574917  
depth: 3, iteration: 684000, test\_RMSE: 1.1217185258865356, erank: 1.2261627912  
521362, s1: 4.013369560241699, s5: 0.006338899489492178  
depth: 3, iteration: 686000, test\_RMSE: 1.1215695142745972, erank: 1.2094614505  
767822, s1: 4.394180774688721, s5: 0.006369215436279774  
depth: 3, iteration: 688000, test\_RMSE: 1.1214139461517334, erank: 1.1936526298  
52295, s1: 4.821934700012207, s5: 0.006399516481906176  
depth: 3, iteration: 690000, test\_RMSE: 1.1212538480758667, erank: 1.1787242889  
404297, s1: 5.3031487464904785, s5: 0.006429820321500301  
depth: 3, iteration: 692000, test\_RMSE: 1.121092438697815, erank: 1.16466581821  
44165, s1: 5.845150947570801, s5: 0.00646016513928771  
depth: 3, iteration: 694000, test\_RMSE: 1.1209347248077393, erank: 1.1514647006  
988525, s1: 6.456164836883545, s5: 0.00649058585986495  
depth: 3, iteration: 696000, test\_RMSE: 1.1207878589630127, erank: 1.1391091346  
740723, s1: 7.145200252532959, s5: 0.006520959082990885  
depth: 3, iteration: 698000, test\_RMSE: 1.1206618547439575, erank: 1.1275846958  
1604, s1: 7.922174453735352, s5: 0.006551375146955252  
depth: 3, iteration: 700000, test\_RMSE: 1.120570421218872, erank: 1.11687731742  
85889, s1: 8.797492980957031, s5: 0.0065818242728710175  
depth: 3, iteration: 702000, test\_RMSE: 1.120531678199768, erank: 1.10697197914  
12354, s1: 9.781913757324219, s5: 0.00661237258464098  
depth: 3, iteration: 704000, test\_RMSE: 1.1205697059631348, erank: 1.0978517532  
348633, s1: 10.886042594909668, s5: 0.0066428710706532  
depth: 3, iteration: 706000, test\_RMSE: 1.1207144260406494, erank: 1.0894970893  
859863, s1: 12.119468688964844, s5: 0.0066734845750033855  
depth: 3, iteration: 708000, test\_RMSE: 1.1210027933120728, erank: 1.0818893909  
454346, s1: 13.489730834960938, s5: 0.006703903432935476  
depth: 3, iteration: 710000, test\_RMSE: 1.121477723121643, erank: 1.07500386238  
09814, s1: 15.001480102539062, s5: 0.006734344642609358  
depth: 3, iteration: 712000, test\_RMSE: 1.1221872568130493, erank: 1.0688134431  
83899, s1: 16.654653549194336, s5: 0.006764844059944153  
depth: 3, iteration: 714000, test\_RMSE: 1.1231802701950073, erank: 1.0632898807  
525635, s1: 18.443012237548828, s5: 0.006795375142246485  
depth: 3, iteration: 716000, test\_RMSE: 1.1245028972625732, erank: 1.0584000349  
0448, s1: 20.353090286254883, s5: 0.006825856398791075  
depth: 3, iteration: 718000, test\_RMSE: 1.1261907815933228, erank: 1.0541079044



34204, s1: 22.363584518432617, s5: 0.006856315769255161  
depth: 3, iteration: 720000, test\_RMSE: 1.128262996673584, erank: 1.05037295818  
32886, s1: 24.44533920288086, s5: 0.006886673159897327  
depth: 3, iteration: 722000, test\_RMSE: 1.1307153701782227, erank: 1.0471541881  
56128, s1: 26.563051223754883, s5: 0.006917017046362162  
depth: 3, iteration: 724000, test\_RMSE: 1.1335177421569824, erank: 1.0444040298  
461914, s1: 28.67753791809082, s5: 0.006947333924472332  
depth: 3, iteration: 726000, test\_RMSE: 1.136614203453064, erank: 1.04207921028  
1372, s1: 30.749141693115234, s5: 0.006977622862905264  
depth: 3, iteration: 728000, test\_RMSE: 1.139929175376892, erank: 1.04013216495  
51392, s1: 32.741275787353516, s5: 0.00700791971758008  
depth: 3, iteration: 730000, test\_RMSE: 1.1433755159378052, erank: 1.0385179519  
65332, s1: 34.623207092285156, s5: 0.007038121111690998  
depth: 3, iteration: 732000, test\_RMSE: 1.1468641757965088, erank: 1.0371931791  
305542, s1: 36.37244415283203, s5: 0.007068397011607885  
depth: 3, iteration: 734000, test\_RMSE: 1.1503145694732666, erank: 1.0361185073  
85254, s1: 37.97538757324219, s5: 0.0070986058562994  
depth: 3, iteration: 736000, test\_RMSE: 1.1536593437194824, erank: 1.0352569818  
496704, s1: 39.42652130126953, s5: 0.007128859404474497  
depth: 3, iteration: 738000, test\_RMSE: 1.1568490266799927, erank: 1.0345767736  
434937, s1: 40.727691650390625, s5: 0.007159175351262093  
depth: 3, iteration: 740000, test\_RMSE: 1.1598511934280396, erank: 1.0340493917  
46521, s1: 41.885982513427734, s5: 0.0071893110871315  
depth: 3, iteration: 742000, test\_RMSE: 1.162649154663086, erank: 1.03365039825  
43945, s1: 42.912017822265625, s5: 0.0072196172550320625  
depth: 3, iteration: 744000, test\_RMSE: 1.1652384996414185, erank: 1.0333591699  
60022, s1: 43.81849670410156, s5: 0.00725007988512516  
depth: 3, iteration: 746000, test\_RMSE: 1.1676238775253296, erank: 1.0331585407  
25708, s1: 44.61892318725586, s5: 0.00728048849850893  
depth: 3, iteration: 748000, test\_RMSE: 1.1698161363601685, erank: 1.0330337285  
995483, s1: 45.32624816894531, s5: 0.0073109460063278675  
depth: 3, iteration: 750000, test\_RMSE: 1.1718294620513916, erank: 1.0329726934  
432983, s1: 45.95293045043945, s5: 0.0073416996747255325  
depth: 3, iteration: 752000, test\_RMSE: 1.1736798286437988, erank: 1.0329668521  
881104, s1: 46.51001739501953, s5: 0.007372466381639242  
depth: 3, iteration: 754000, test\_RMSE: 1.175383448600769, erank: 1.03300678730  
01099, s1: 47.00768280029297, s5: 0.00740313483402133  
depth: 3, iteration: 756000, test\_RMSE: 1.1769554615020752, erank: 1.0330870151  
519775, s1: 47.45429611206055, s5: 0.007434274535626173  
depth: 3, iteration: 758000, test\_RMSE: 1.1784101724624634, erank: 1.0332015752  
792358, s1: 47.857322692871094, s5: 0.007465296424925327  
depth: 3, iteration: 760000, test\_RMSE: 1.1797611713409424, erank: 1.0333476066  
589355, s1: 48.22345733642578, s5: 0.007496376056224108  
depth: 3, iteration: 762000, test\_RMSE: 1.181019902229309, erank: 1.03351974487  
30469, s1: 48.55752182006836, s5: 0.007527775131165981  
depth: 3, iteration: 764000, test\_RMSE: 1.1821961402893066, erank: 1.0337170362  
472534, s1: 48.864322662353516, s5: 0.007559339981526136  
depth: 3, iteration: 766000, test\_RMSE: 1.1832993030548096, erank: 1.0339365005  
493164, s1: 49.1475944519043, s5: 0.0075912741012871265  
depth: 3, iteration: 768000, test\_RMSE: 1.1843370199203491, erank: 1.0341764688  
491821, s1: 49.41032409667969, s5: 0.007622986566275358  
depth: 3, iteration: 770000, test\_RMSE: 1.1853158473968506, erank: 1.0344355106  
35376, s1: 49.655452728271484, s5: 0.007655376102775335  
depth: 3, iteration: 772000, test\_RMSE: 1.186241626739502, erank: 1.03471255302

```

4292, s1: 49.884971618652344, s5: 0.007687688805162907
depth: 3, iteration: 774000, test_RMSE: 1.1871191263198853, erank: 1.0350072383
880615, s1: 50.100914001464844, s5: 0.007720105350017548
depth: 3, iteration: 776000, test_RMSE: 1.1879527568817139, erank: 1.0353188514
709473, s1: 50.304649353027344, s5: 0.0077528017573058605
depth: 3, iteration: 778000, test_RMSE: 1.1887462139129639, erank: 1.0356469154
35791, s1: 50.497711181640625, s5: 0.0077855284325778484
depth: 3, iteration: 780000, test_RMSE: 1.1895034313201904, erank: 1.0359897613
52539, s1: 50.681121826171875, s5: 0.007818788290023804
depth: 3, iteration: 782000, test_RMSE: 1.1902258396148682, erank: 1.0363497734
069824, s1: 50.85594177246094, s5: 0.00785190612077713
depth: 3, iteration: 784000, test_RMSE: 1.1909170150756836, erank: 1.0367254018
78357, s1: 51.02287292480469, s5: 0.00788545235991478
depth: 3, iteration: 786000, test_RMSE: 1.19157874584198, erank: 1.037116765975
9521, s1: 51.18272399902344, s5: 0.007919298484921455
depth: 3, iteration: 788000, test_RMSE: 1.192212462425232, erank: 1.03752422332
76367, s1: 51.33589172363281, s5: 0.00795337650924921
depth: 3, iteration: 790000, test_RMSE: 1.1928209066390991, erank: 1.0379480123
519897, s1: 51.483253479003906, s5: 0.007987347431480885
depth: 3, iteration: 792000, test_RMSE: 1.1934043169021606, erank: 1.0383880138
397217, s1: 51.62477111816406, s5: 0.008021839894354343
depth: 3, iteration: 794000, test_RMSE: 1.1939644813537598, erank: 1.0388448238
372803, s1: 51.76114273071289, s5: 0.008056743070483208
depth: 3, iteration: 796000, test_RMSE: 1.1945019960403442, erank: 1.0393193960
18982, s1: 51.89247131347656, s5: 0.00809173658490181
depth: 3, iteration: 798000, test_RMSE: 1.1950194835662842, erank: 1.0398110151
290894, s1: 52.01951217651367, s5: 0.00812707468867302

```

```

In [10]: for lam in ("0.0", "1e-2"):
          run_and_log(f"F3_gd_d1_lam{lam}",
                      **BASE_SYN, depth=1, lam=lam, optim="GD", lr=LR_GD, niters=LONG_IT
          run_and_log(f"F3_adam_d1_lam{lam}",
                      **BASE_SYN, depth=1, lam=lam, optim="Adam", lr=LR_ADAM, niters=LONG_IT

```

```
RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10
0 --rank 5 --reg_norm ratio --initscale 1e-3 --sample_size 4000 --log_interval
2000 --depth 1 --lam 0.0 --optim GD --lr 1e-3 --niters 800000
depth: 1, iteration: 0, test_RMSE: 1.129388451576233, erank: 80.63429260253906,
s1: 0.0019347229972481728, s5: 0.0017415006877854466
depth: 1, iteration: 2000, test_RMSE: 1.129388451576233, erank: 66.095779418945
31, s1: 0.025106655433773994, s5: 0.016447316855192184
depth: 1, iteration: 4000, test_RMSE: 1.129388451576233, erank: 65.486106872558
6, s1: 0.05022093281149864, s5: 0.032651178538799286
depth: 1, iteration: 6000, test_RMSE: 1.129388451576233, erank: 65.386268615722
66, s1: 0.07532285898923874, s5: 0.04885831102728844
depth: 1, iteration: 8000, test_RMSE: 1.129388451576233, erank: 65.365318298339
84, s1: 0.1004033088684082, s5: 0.06505382806062698
depth: 1, iteration: 10000, test_RMSE: 1.129388451576233, erank: 65.36257171630
86, s1: 0.12545941770076752, s5: 0.08123534917831421
depth: 1, iteration: 12000, test_RMSE: 1.129388451576233, erank: 65.36247253417
969, s1: 0.15049166977405548, s5: 0.09740140289068222
depth: 1, iteration: 14000, test_RMSE: 1.129388451576233, erank: 65.36306762695
312, s1: 0.17549929022789001, s5: 0.11355193704366684
depth: 1, iteration: 16000, test_RMSE: 1.129388451576233, erank: 65.36391448974
61, s1: 0.20048213005065918, s5: 0.12968710064888
depth: 1, iteration: 18000, test_RMSE: 1.129388451576233, erank: 65.36481475830
078, s1: 0.22543974220752716, s5: 0.14580687880516052
depth: 1, iteration: 20000, test_RMSE: 1.129388451576233, erank: 65.36569213867
188, s1: 0.25037258863449097, s5: 0.1619095504283905
depth: 1, iteration: 22000, test_RMSE: 1.129388451576233, erank: 65.36650085449
219, s1: 0.2752813696861267, s5: 0.17799684405326843
depth: 1, iteration: 24000, test_RMSE: 1.129388451576233, erank: 65.36711883544
922, s1: 0.3001660108566284, s5: 0.19406813383102417
depth: 1, iteration: 26000, test_RMSE: 1.129388451576233, erank: 65.36780548095
703, s1: 0.3250233829021454, s5: 0.21012401580810547
depth: 1, iteration: 28000, test_RMSE: 1.129388451576233, erank: 65.36846160888
672, s1: 0.34985437989234924, s5: 0.22616316378116608
depth: 1, iteration: 30000, test_RMSE: 1.129388451576233, erank: 65.36896514892
578, s1: 0.37466710805892944, s5: 0.24218504130840302
depth: 1, iteration: 32000, test_RMSE: 1.129388451576233, erank: 65.36940002441
406, s1: 0.3994518220424652, s5: 0.2581931948661804
depth: 1, iteration: 34000, test_RMSE: 1.129388451576233, erank: 65.36986541748
047, s1: 0.42421022057533264, s5: 0.27418529987335205
depth: 1, iteration: 36000, test_RMSE: 1.129388451576233, erank: 65.37026977539
062, s1: 0.44894519448280334, s5: 0.2901591360569
depth: 1, iteration: 38000, test_RMSE: 1.129388451576233, erank: 65.37061309814
453, s1: 0.4736533761024475, s5: 0.3061160445213318
depth: 1, iteration: 40000, test_RMSE: 1.129388451576233, erank: 65.37095642089
844, s1: 0.4983418583869934, s5: 0.3220624327659607
depth: 1, iteration: 42000, test_RMSE: 1.129388451576233, erank: 65.37129974365
234, s1: 0.5230008959770203, s5: 0.3379882872104645
depth: 1, iteration: 44000, test_RMSE: 1.129388451576233, erank: 65.37148284912
11, s1: 0.5476401448249817, s5: 0.35389935970306396
depth: 1, iteration: 46000, test_RMSE: 1.129388451576233, erank: 65.37179565429
688, s1: 0.57225102186203, s5: 0.3697946071624756
depth: 1, iteration: 48000, test_RMSE: 1.129388451576233, erank: 65.37213897705
078, s1: 0.5968369841575623, s5: 0.38567596673965454
depth: 1, iteration: 50000, test_RMSE: 1.129388451576233, erank: 65.37239074707
```

031, s1: 0.6214010715484619, s5: 0.40154266357421875  
depth: 1, iteration: 52000, test\_RMSE: 1.129388451576233, erank: 65.37248229980  
469, s1: 0.6459424495697021, s5: 0.4173915684223175  
depth: 1, iteration: 54000, test\_RMSE: 1.129388451576233, erank: 65.37273406982  
422, s1: 0.6704553365707397, s5: 0.43321865797042847  
depth: 1, iteration: 56000, test\_RMSE: 1.129388451576233, erank: 65.37301635742  
188, s1: 0.6949409246444702, s5: 0.44903671741485596  
depth: 1, iteration: 58000, test\_RMSE: 1.129388451576233, erank: 65.37322998046  
875, s1: 0.719401478767395, s5: 0.4648396670818329  
depth: 1, iteration: 60000, test\_RMSE: 1.129388451576233, erank: 65.37351226806  
64, s1: 0.7438362240791321, s5: 0.4806210696697235  
depth: 1, iteration: 62000, test\_RMSE: 1.129388451576233, erank: 65.37357330322  
266, s1: 0.7682597637176514, s5: 0.4963916540145874  
depth: 1, iteration: 64000, test\_RMSE: 1.129388451576233, erank: 65.37369537353  
516, s1: 0.7926515340805054, s5: 0.5121440887451172  
depth: 1, iteration: 66000, test\_RMSE: 1.129388451576233, erank: 65.37385559082  
031, s1: 0.8170170187950134, s5: 0.5278818011283875  
depth: 1, iteration: 68000, test\_RMSE: 1.129388451576233, erank: 65.37403869628  
906, s1: 0.8413585424423218, s5: 0.543605625629425  
depth: 1, iteration: 70000, test\_RMSE: 1.129388451576233, erank: 65.37419891357  
422, s1: 0.8656699061393738, s5: 0.5593111515045166  
depth: 1, iteration: 72000, test\_RMSE: 1.129388451576233, erank: 65.37435150146  
484, s1: 0.8899617195129395, s5: 0.5750007629394531  
depth: 1, iteration: 74000, test\_RMSE: 1.129388451576233, erank: 65.37438201904  
297, s1: 0.9142379760742188, s5: 0.5906763672828674  
depth: 1, iteration: 76000, test\_RMSE: 1.129388451576233, erank: 65.37442016601  
562, s1: 0.9384819269180298, s5: 0.6063368916511536  
depth: 1, iteration: 78000, test\_RMSE: 1.129388451576233, erank: 65.37454223632  
812, s1: 0.9627012014389038, s5: 0.6219808459281921  
depth: 1, iteration: 80000, test\_RMSE: 1.129388451576233, erank: 65.37466430664  
062, s1: 0.9868934154510498, s5: 0.6376065015792847  
depth: 1, iteration: 82000, test\_RMSE: 1.129388451576233, erank: 65.37472534179  
688, s1: 1.011068344116211, s5: 0.6532166600227356  
depth: 1, iteration: 84000, test\_RMSE: 1.129388451576233, erank: 65.37497711181  
64, s1: 1.0352087020874023, s5: 0.6688105463981628  
depth: 1, iteration: 86000, test\_RMSE: 1.129388451576233, erank: 65.37506866455  
078, s1: 1.0593340396881104, s5: 0.6843931674957275  
depth: 1, iteration: 88000, test\_RMSE: 1.129388451576233, erank: 65.37506866455  
078, s1: 1.0834345817565918, s5: 0.699964165687561  
depth: 1, iteration: 90000, test\_RMSE: 1.129388451576233, erank: 65.37512969970  
703, s1: 1.1075078248977661, s5: 0.7155212163925171  
depth: 1, iteration: 92000, test\_RMSE: 1.129388451576233, erank: 65.37510681152  
344, s1: 1.1315730810165405, s5: 0.7310558557510376  
depth: 1, iteration: 94000, test\_RMSE: 1.129388451576233, erank: 65.37516021728  
516, s1: 1.1556082963943481, s5: 0.7465733885765076  
depth: 1, iteration: 96000, test\_RMSE: 1.129388451576233, erank: 65.37525177001  
953, s1: 1.1795982122421265, s5: 0.7620716094970703  
depth: 1, iteration: 98000, test\_RMSE: 1.129388451576233, erank: 65.37535095214  
844, s1: 1.2035819292068481, s5: 0.7775542736053467  
depth: 1, iteration: 100000, test\_RMSE: 1.129388451576233, erank: 65.3755111694  
336, s1: 1.2275280952453613, s5: 0.7930185794830322  
depth: 1, iteration: 102000, test\_RMSE: 1.129388451576233, erank: 65.3756027221  
6797, s1: 1.2514666318893433, s5: 0.8084782958030701  
depth: 1, iteration: 104000, test\_RMSE: 1.129388451576233, erank: 65.3756637573

2422, sl: 1.2753753662109375, s5: 0.8239226937294006  
depth: 1, iteration: 106000, test\_RMSE: 1.129388451576233, erank: 65.3756942749  
0234, sl: 1.2992507219314575, s5: 0.8393576741218567  
depth: 1, iteration: 108000, test\_RMSE: 1.129388451576233, erank: 65.3757858276  
3672, sl: 1.3231216669082642, s5: 0.854758083820343  
depth: 1, iteration: 110000, test\_RMSE: 1.129388451576233, erank: 65.3757858276  
3672, sl: 1.3469609022140503, s5: 0.8701513409614563  
depth: 1, iteration: 112000, test\_RMSE: 1.129388451576233, erank: 65.3758850097  
6562, sl: 1.3707664012908936, s5: 0.8855404257774353  
depth: 1, iteration: 114000, test\_RMSE: 1.129388451576233, erank: 65.3758468627  
9297, sl: 1.394549012184143, s5: 0.9009069204330444  
depth: 1, iteration: 116000, test\_RMSE: 1.129388451576233, erank: 65.3758163452  
1484, sl: 1.4183127880096436, s5: 0.9162452816963196  
depth: 1, iteration: 118000, test\_RMSE: 1.129388451576233, erank: 65.3758163452  
1484, sl: 1.442055583000183, s5: 0.9315831661224365  
depth: 1, iteration: 120000, test\_RMSE: 1.129388451576233, erank: 65.3758163452  
1484, sl: 1.4657635688781738, s5: 0.946902871131897  
depth: 1, iteration: 122000, test\_RMSE: 1.129388451576233, erank: 65.3759384155  
2734, sl: 1.4894509315490723, s5: 0.9622096419334412  
depth: 1, iteration: 124000, test\_RMSE: 1.129388451576233, erank: 65.3759155273  
4375, sl: 1.5131274461746216, s5: 0.9774978756904602  
depth: 1, iteration: 126000, test\_RMSE: 1.129388451576233, erank: 65.3759384155  
2734, sl: 1.5367769002914429, s5: 0.9927732944488525  
depth: 1, iteration: 128000, test\_RMSE: 1.129388451576233, erank: 65.3758468627  
9297, sl: 1.5604168176651, s5: 1.0080233812332153  
depth: 1, iteration: 130000, test\_RMSE: 1.129388451576233, erank: 65.3761291503  
9062, sl: 1.5840028524398804, s5: 1.0232731103897095  
depth: 1, iteration: 132000, test\_RMSE: 1.129388451576233, erank: 65.3762207031  
25, sl: 1.6075812578201294, s5: 1.038500428199768  
depth: 1, iteration: 134000, test\_RMSE: 1.129388451576233, erank: 65.3763809204  
1016, sl: 1.631130337715149, s5: 1.0537054538726807  
depth: 1, iteration: 136000, test\_RMSE: 1.129388451576233, erank: 65.3762893676  
7578, sl: 1.6546664237976074, s5: 1.0688951015472412  
depth: 1, iteration: 138000, test\_RMSE: 1.129388451576233, erank: 65.3763198852  
539, sl: 1.678164005279541, s5: 1.0840744972229004  
depth: 1, iteration: 140000, test\_RMSE: 1.129388451576233, erank: 65.3763427734  
375, sl: 1.7016464471817017, s5: 1.0992330312728882  
depth: 1, iteration: 142000, test\_RMSE: 1.129388451576233, erank: 65.3762512207  
0312, sl: 1.7251241207122803, s5: 1.1143876314163208  
depth: 1, iteration: 144000, test\_RMSE: 1.129388451576233, erank: 65.3761978149  
414, sl: 1.7485655546188354, s5: 1.129533290863037  
depth: 1, iteration: 146000, test\_RMSE: 1.129388451576233, erank: 65.3761291503  
9062, sl: 1.7719875574111938, s5: 1.144660472869873  
depth: 1, iteration: 148000, test\_RMSE: 1.129388451576233, erank: 65.3761596679  
6875, sl: 1.7953659296035767, s5: 1.1597665548324585  
depth: 1, iteration: 150000, test\_RMSE: 1.129388451576233, erank: 65.3761291503  
9062, sl: 1.8187307119369507, s5: 1.1748684644699097  
depth: 1, iteration: 152000, test\_RMSE: 1.129388451576233, erank: 65.3761291503  
9062, sl: 1.8420782089233398, s5: 1.1899428367614746  
depth: 1, iteration: 154000, test\_RMSE: 1.129388451576233, erank: 65.3761596679  
6875, sl: 1.8653942346572876, s5: 1.205004334449768  
depth: 1, iteration: 156000, test\_RMSE: 1.129388451576233, erank: 65.3761596679  
6875, sl: 1.8886795043945312, s5: 1.2200485467910767  
depth: 1, iteration: 158000, test\_RMSE: 1.129388451576233, erank: 65.3763427734

375, s1: 1.911941647529602, s5: 1.235077142715454  
depth: 1, iteration: 160000, test\_RMSE: 1.129388451576233, erank: 65.3764724731  
4453, s1: 1.9351850748062134, s5: 1.2500907182693481  
depth: 1, iteration: 162000, test\_RMSE: 1.129388451576233, erank: 65.3766555786  
1328, s1: 1.958398699760437, s5: 1.265090823173523  
depth: 1, iteration: 164000, test\_RMSE: 1.129388451576233, erank: 65.3766555786  
1328, s1: 1.9815999269485474, s5: 1.2800623178482056  
depth: 1, iteration: 166000, test\_RMSE: 1.129388451576233, erank: 65.3766937255  
8594, s1: 2.0047607421875, s5: 1.2950276136398315  
depth: 1, iteration: 168000, test\_RMSE: 1.129388451576233, erank: 65.3766021728  
5156, s1: 2.0279345512390137, s5: 1.3099802732467651  
depth: 1, iteration: 170000, test\_RMSE: 1.129388451576233, erank: 65.3766250610  
3516, s1: 2.051058292388916, s5: 1.324912428855896  
depth: 1, iteration: 172000, test\_RMSE: 1.129388451576233, erank: 65.3766937255  
8594, s1: 2.074176549911499, s5: 1.339835524559021  
depth: 1, iteration: 174000, test\_RMSE: 1.129388451576233, erank: 65.3766021728  
5156, s1: 2.0972654819488525, s5: 1.3547443151474  
depth: 1, iteration: 176000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.120338201522827, s5: 1.36965012550354  
depth: 1, iteration: 178000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.143388271331787, s5: 1.3845114707946777  
depth: 1, iteration: 180000, test\_RMSE: 1.129388451576233, erank: 65.3764724731  
4453, s1: 2.166395902633667, s5: 1.3993831872940063  
depth: 1, iteration: 182000, test\_RMSE: 1.129388451576233, erank: 65.3764114379  
8828, s1: 2.189399242401123, s5: 1.4142320156097412  
depth: 1, iteration: 184000, test\_RMSE: 1.129388451576233, erank: 65.3762893676  
7578, s1: 2.2123875617980957, s5: 1.4290826320648193  
depth: 1, iteration: 186000, test\_RMSE: 1.129388451576233, erank: 65.3762893676  
7578, s1: 2.2353079319000244, s5: 1.443907618522644  
depth: 1, iteration: 188000, test\_RMSE: 1.129388451576233, erank: 65.3763427734  
375, s1: 2.25821852684021, s5: 1.4587082862854004  
depth: 1, iteration: 190000, test\_RMSE: 1.129388451576233, erank: 65.3763427734  
375, s1: 2.2811226844787598, s5: 1.4734961986541748  
depth: 1, iteration: 192000, test\_RMSE: 1.129388451576233, erank: 65.3764114379  
8828, s1: 2.30399227142334, s5: 1.4882700443267822  
depth: 1, iteration: 194000, test\_RMSE: 1.129388451576233, erank: 65.3764114379  
8828, s1: 2.32686448097229, s5: 1.5030322074890137  
depth: 1, iteration: 196000, test\_RMSE: 1.129388451576233, erank: 65.3764724731  
4453, s1: 2.3496856689453125, s5: 1.5177772045135498  
depth: 1, iteration: 198000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.3724942207336426, s5: 1.532516360282898  
depth: 1, iteration: 200000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.3952689170837402, s5: 1.5472334623336792  
depth: 1, iteration: 202000, test\_RMSE: 1.129388451576233, erank: 65.3766555786  
1328, s1: 2.4180285930633545, s5: 1.5619362592697144  
depth: 1, iteration: 204000, test\_RMSE: 1.129388451576233, erank: 65.3767547607  
4219, s1: 2.4407730102539062, s5: 1.5766197443008423  
depth: 1, iteration: 206000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.463489294052124, s5: 1.5912978649139404  
depth: 1, iteration: 208000, test\_RMSE: 1.129388451576233, erank: 65.3768157958  
9844, s1: 2.4862101078033447, s5: 1.6059499979019165  
depth: 1, iteration: 210000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 2.508888006210327, s5: 1.6205809116363525  
depth: 1, iteration: 212000, test\_RMSE: 1.129388451576233, erank: 65.3768463134

7656, s1: 2.5315616130828857, s5: 1.6352219581604004  
depth: 1, iteration: 214000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.554198741912842, s5: 1.649837613105774  
depth: 1, iteration: 216000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 2.5767908096313477, s5: 1.6644320487976074  
depth: 1, iteration: 218000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.599403142929077, s5: 1.679028034210205  
depth: 1, iteration: 220000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.6219561100006104, s5: 1.6935861110687256  
depth: 1, iteration: 222000, test\_RMSE: 1.129388451576233, erank: 65.3768157958  
9844, s1: 2.64448881149292, s5: 1.7081431150436401  
depth: 1, iteration: 224000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 2.6669921875, s5: 1.7226622104644775  
depth: 1, iteration: 226000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.6894845962524414, s5: 1.7372009754180908  
depth: 1, iteration: 228000, test\_RMSE: 1.129388451576233, erank: 65.3767242431  
6406, s1: 2.711954116821289, s5: 1.7517274618148804  
depth: 1, iteration: 230000, test\_RMSE: 1.129388451576233, erank: 65.3766555786  
1328, s1: 2.734391927719116, s5: 1.766229271888733  
depth: 1, iteration: 232000, test\_RMSE: 1.129388451576233, erank: 65.3765640258  
789, s1: 2.756817102432251, s5: 1.780708909034729  
depth: 1, iteration: 234000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.7792165279388428, s5: 1.7951866388320923  
depth: 1, iteration: 236000, test\_RMSE: 1.129388451576233, erank: 65.3764419555  
664, s1: 2.801607608795166, s5: 1.809634804725647  
depth: 1, iteration: 238000, test\_RMSE: 1.129388451576233, erank: 65.3764724731  
4453, s1: 2.8239755630493164, s5: 1.8240728378295898  
depth: 1, iteration: 240000, test\_RMSE: 1.129388451576233, erank: 65.3764724731  
4453, s1: 2.8462915420532227, s5: 1.838494896888733  
depth: 1, iteration: 242000, test\_RMSE: 1.129388451576233, erank: 65.3765335083  
0078, s1: 2.868589162826538, s5: 1.8529013395309448  
depth: 1, iteration: 244000, test\_RMSE: 1.129388451576233, erank: 65.3766021728  
5156, s1: 2.890872001647949, s5: 1.8673148155212402  
depth: 1, iteration: 246000, test\_RMSE: 1.129388451576233, erank: 65.3767547607  
4219, s1: 2.913135051727295, s5: 1.8816847801208496  
depth: 1, iteration: 248000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 2.9353835582733154, s5: 1.8960740566253662  
depth: 1, iteration: 250000, test\_RMSE: 1.129388451576233, erank: 65.3769073486  
3281, s1: 2.957610607147217, s5: 1.9104286432266235  
depth: 1, iteration: 252000, test\_RMSE: 1.129388451576233, erank: 65.3770065307  
6172, s1: 2.9798223972320557, s5: 1.9247705936431885  
depth: 1, iteration: 254000, test\_RMSE: 1.129388451576233, erank: 65.3771286010  
7422, s1: 3.002009630203247, s5: 1.9390827417373657  
depth: 1, iteration: 256000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 3.0241520404815674, s5: 1.9533885717391968  
depth: 1, iteration: 258000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 3.046286106109619, s5: 1.9676920175552368  
depth: 1, iteration: 260000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 3.0683720111846924, s5: 1.9819495677947998  
depth: 1, iteration: 262000, test\_RMSE: 1.129388451576233, erank: 65.3777847290  
039, s1: 3.0904457569122314, s5: 1.9962199926376343  
depth: 1, iteration: 264000, test\_RMSE: 1.129388451576233, erank: 65.3778152465  
8203, s1: 3.1125261783599854, s5: 2.010474920272827  
depth: 1, iteration: 266000, test\_RMSE: 1.129388451576233, erank: 65.3777465820

3125, s1: 3.1345813274383545, s5: 2.024721384048462  
depth: 1, iteration: 268000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 3.156623601913452, s5: 2.0389552116394043  
depth: 1, iteration: 270000, test\_RMSE: 1.129388451576233, erank: 65.3776245117  
1875, s1: 3.1786153316497803, s5: 2.05317759513855  
depth: 1, iteration: 272000, test\_RMSE: 1.129388451576233, erank: 65.3775634765  
625, s1: 3.2005999088287354, s5: 2.0673651695251465  
depth: 1, iteration: 274000, test\_RMSE: 1.129388451576233, erank: 65.3775634765  
625, s1: 3.222550868988037, s5: 2.0815677642822266  
depth: 1, iteration: 276000, test\_RMSE: 1.129388451576233, erank: 65.3775329589  
8438, s1: 3.2444725036621094, s5: 2.0957350730895996  
depth: 1, iteration: 278000, test\_RMSE: 1.129388451576233, erank: 65.3774719238  
2812, s1: 3.266361713409424, s5: 2.1098849773406982  
depth: 1, iteration: 280000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 3.288240671157837, s5: 2.1240200996398926  
depth: 1, iteration: 282000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 3.310110330581665, s5: 2.138134002685547  
depth: 1, iteration: 284000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 3.3319644927978516, s5: 2.152244806289673  
depth: 1, iteration: 286000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 3.3537774085998535, s5: 2.166368007659912  
depth: 1, iteration: 288000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 3.3756015300750732, s5: 2.1804468631744385  
depth: 1, iteration: 290000, test\_RMSE: 1.129388451576233, erank: 65.3773117065  
4297, s1: 3.3973841667175293, s5: 2.194523572921753  
depth: 1, iteration: 292000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 3.419187068939209, s5: 2.2086124420166016  
depth: 1, iteration: 294000, test\_RMSE: 1.129388451576233, erank: 65.3772201538  
086, s1: 3.4409286975860596, s5: 2.222665309906006  
depth: 1, iteration: 296000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 3.4626386165618896, s5: 2.2366652488708496  
depth: 1, iteration: 298000, test\_RMSE: 1.129388451576233, erank: 65.3772506713  
8672, s1: 3.484337329864502, s5: 2.2506906986236572  
depth: 1, iteration: 300000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 3.5060055255889893, s5: 2.264662981033325  
depth: 1, iteration: 302000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 3.527676582336426, s5: 2.2786519527435303  
depth: 1, iteration: 304000, test\_RMSE: 1.129388451576233, erank: 65.3775329589  
8438, s1: 3.54929780960083, s5: 2.2925963401794434  
depth: 1, iteration: 306000, test\_RMSE: 1.129388451576233, erank: 65.3775939941  
4062, s1: 3.570939540863037, s5: 2.3065571784973145  
depth: 1, iteration: 308000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 3.5924782752990723, s5: 2.3204777240753174  
depth: 1, iteration: 310000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 3.6140713691711426, s5: 2.3343892097473145  
depth: 1, iteration: 312000, test\_RMSE: 1.129388451576233, erank: 65.3781204223  
6328, s1: 3.6356163024902344, s5: 2.3483009338378906  
depth: 1, iteration: 314000, test\_RMSE: 1.129388451576233, erank: 65.3781204223  
6328, s1: 3.657139778137207, s5: 2.3621933460235596  
depth: 1, iteration: 316000, test\_RMSE: 1.129388451576233, erank: 65.3782196044  
9219, s1: 3.678642511367798, s5: 2.37610125541687  
depth: 1, iteration: 318000, test\_RMSE: 1.129388451576233, erank: 65.3783416748  
0469, s1: 3.7001266479492188, s5: 2.3899762630462646  
depth: 1, iteration: 320000, test\_RMSE: 1.129388451576233, erank: 65.3783416748



0469, s1: 3.7215752601623535, s5: 2.4038243293762207  
depth: 1, iteration: 322000, test\_RMSE: 1.129388451576233, erank: 65.3782806396  
4844, s1: 3.743004083633423, s5: 2.41766619682312  
depth: 1, iteration: 324000, test\_RMSE: 1.129388451576233, erank: 65.3782196044  
9219, s1: 3.7644338607788086, s5: 2.4314992427825928  
depth: 1, iteration: 326000, test\_RMSE: 1.129388451576233, erank: 65.3782501220  
7031, s1: 3.7857937812805176, s5: 2.4453277587890625  
depth: 1, iteration: 328000, test\_RMSE: 1.129388451576233, erank: 65.3780670166  
0156, s1: 3.8071892261505127, s5: 2.45913028717041  
depth: 1, iteration: 330000, test\_RMSE: 1.129388451576233, erank: 65.3780670166  
0156, s1: 3.8285417556762695, s5: 2.4729111194610596  
depth: 1, iteration: 332000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 3.8498406410217285, s5: 2.4867143630981445  
depth: 1, iteration: 334000, test\_RMSE: 1.129388451576233, erank: 65.3778152465  
8203, s1: 3.8711869716644287, s5: 2.5004754066467285  
depth: 1, iteration: 336000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 3.892446517944336, s5: 2.5142407417297363  
depth: 1, iteration: 338000, test\_RMSE: 1.129388451576233, erank: 65.3777160644  
5312, s1: 3.9137253761291504, s5: 2.5279786586761475  
depth: 1, iteration: 340000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 3.93496036529541, s5: 2.541672945022583  
depth: 1, iteration: 342000, test\_RMSE: 1.129388451576233, erank: 65.3776245117  
1875, s1: 3.9561901092529297, s5: 2.555391788482666  
depth: 1, iteration: 344000, test\_RMSE: 1.129388451576233, erank: 65.3774337768  
5547, s1: 3.977405548095703, s5: 2.5690906047821045  
depth: 1, iteration: 346000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 3.9985756874084473, s5: 2.5827770233154297  
depth: 1, iteration: 348000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 4.019742965698242, s5: 2.5964250564575195  
depth: 1, iteration: 350000, test\_RMSE: 1.129388451576233, erank: 65.3770980834  
961, s1: 4.040886878967285, s5: 2.6101131439208984  
depth: 1, iteration: 352000, test\_RMSE: 1.129388451576233, erank: 65.3769760131  
836, s1: 4.062032699584961, s5: 2.623750686645508  
depth: 1, iteration: 354000, test\_RMSE: 1.129388451576233, erank: 65.3769073486  
3281, s1: 4.083125591278076, s5: 2.6373660564422607  
depth: 1, iteration: 356000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 4.1042160987854, s5: 2.6509759426116943  
depth: 1, iteration: 358000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 4.12529182434082, s5: 2.6645901203155518  
depth: 1, iteration: 360000, test\_RMSE: 1.129388451576233, erank: 65.3767242431  
6406, s1: 4.146359443664551, s5: 2.6782031059265137  
depth: 1, iteration: 362000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 4.167329788208008, s5: 2.691774845123291  
depth: 1, iteration: 364000, test\_RMSE: 1.129388451576233, erank: 65.3769073486  
3281, s1: 4.188360214233398, s5: 2.7053444385528564  
depth: 1, iteration: 366000, test\_RMSE: 1.129388451576233, erank: 65.3769378662  
1094, s1: 4.209342956542969, s5: 2.7188827991485596  
depth: 1, iteration: 368000, test\_RMSE: 1.129388451576233, erank: 65.3770294189  
4531, s1: 4.23028039932251, s5: 2.7323997020721436  
depth: 1, iteration: 370000, test\_RMSE: 1.129388451576233, erank: 65.3770980834  
961, s1: 4.251210689544678, s5: 2.745896339416504  
depth: 1, iteration: 372000, test\_RMSE: 1.129388451576233, erank: 65.3771896362  
3047, s1: 4.272160053253174, s5: 2.759363889694214  
depth: 1, iteration: 374000, test\_RMSE: 1.129388451576233, erank: 65.3773422241

211, s1: 4.29302453994751, s5: 2.772825002670288  
depth: 1, iteration: 376000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 4.313940525054932, s5: 2.7863173484802246  
depth: 1, iteration: 378000, test\_RMSE: 1.129388451576233, erank: 65.3774719238  
2812, s1: 4.334751605987549, s5: 2.799765110015869  
depth: 1, iteration: 380000, test\_RMSE: 1.129388451576233, erank: 65.3775329589  
8438, s1: 4.355574607849121, s5: 2.813187599182129  
depth: 1, iteration: 382000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 4.376357555389404, s5: 2.82661771774292  
depth: 1, iteration: 384000, test\_RMSE: 1.129388451576233, erank: 65.3777160644  
5312, s1: 4.3971052169799805, s5: 2.8400142192840576  
depth: 1, iteration: 386000, test\_RMSE: 1.129388451576233, erank: 65.3777847290  
039, s1: 4.417868137359619, s5: 2.8534116744995117  
depth: 1, iteration: 388000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 4.4385881423950195, s5: 2.8668107986450195  
depth: 1, iteration: 390000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 4.45928955078125, s5: 2.8801987171173096  
depth: 1, iteration: 392000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 4.479973793029785, s5: 2.8935704231262207  
depth: 1, iteration: 394000, test\_RMSE: 1.129388451576233, erank: 65.3780670166  
0156, s1: 4.500661849975586, s5: 2.90689754486084  
depth: 1, iteration: 396000, test\_RMSE: 1.129388451576233, erank: 65.3780288696  
289, s1: 4.521331787109375, s5: 2.9202475547790527  
depth: 1, iteration: 398000, test\_RMSE: 1.129388451576233, erank: 65.3780288696  
289, s1: 4.54196310043335, s5: 2.9335999488830566  
depth: 1, iteration: 400000, test\_RMSE: 1.129388451576233, erank: 65.3780975341  
7969, s1: 4.562586307525635, s5: 2.946904182434082  
depth: 1, iteration: 402000, test\_RMSE: 1.129388451576233, erank: 65.3780288696  
289, s1: 4.583175182342529, s5: 2.960197925567627  
depth: 1, iteration: 404000, test\_RMSE: 1.129388451576233, erank: 65.3780670166  
0156, s1: 4.603754997253418, s5: 2.973511219024658  
depth: 1, iteration: 406000, test\_RMSE: 1.129388451576233, erank: 65.3779983520  
5078, s1: 4.624309539794922, s5: 2.9867966175079346  
depth: 1, iteration: 408000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.644872188568115, s5: 3.000067949295044  
depth: 1, iteration: 410000, test\_RMSE: 1.129388451576233, erank: 65.3779373168  
9453, s1: 4.665374755859375, s5: 3.0133328437805176  
depth: 1, iteration: 412000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.685859203338623, s5: 3.0265603065490723  
depth: 1, iteration: 414000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.706357479095459, s5: 3.0397932529449463  
depth: 1, iteration: 416000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.726840972900391, s5: 3.0529816150665283  
depth: 1, iteration: 418000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.747215747833252, s5: 3.066190242767334  
depth: 1, iteration: 420000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 4.767637252807617, s5: 3.079388380050659  
depth: 1, iteration: 422000, test\_RMSE: 1.129388451576233, erank: 65.3779983520  
5078, s1: 4.787994384765625, s5: 3.0925259590148926  
depth: 1, iteration: 424000, test\_RMSE: 1.129388451576233, erank: 65.3779983520  
5078, s1: 4.808355331420898, s5: 3.105708122253418  
depth: 1, iteration: 426000, test\_RMSE: 1.129388451576233, erank: 65.3779373168  
9453, s1: 4.8286848068237305, s5: 3.1188766956329346  
depth: 1, iteration: 428000, test\_RMSE: 1.129388451576233, erank: 65.3779373168

9453, s1: 4.849020004272461, s5: 3.132019281387329  
depth: 1, iteration: 430000, test\_RMSE: 1.129388451576233, erank: 65.3779373168  
9453, s1: 4.869332790374756, s5: 3.145148277282715  
depth: 1, iteration: 432000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 4.889606475830078, s5: 3.158228635787964  
depth: 1, iteration: 434000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 4.9098992347717285, s5: 3.171355724334717  
depth: 1, iteration: 436000, test\_RMSE: 1.129388451576233, erank: 65.3777465820  
3125, s1: 4.930122375488281, s5: 3.184448480606079  
depth: 1, iteration: 438000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 4.95035982131958, s5: 3.1975295543670654  
depth: 1, iteration: 440000, test\_RMSE: 1.129388451576233, erank: 65.3775329589  
8438, s1: 4.970555782318115, s5: 3.2106003761291504  
depth: 1, iteration: 442000, test\_RMSE: 1.129388451576233, erank: 65.3775634765  
625, s1: 4.990731239318848, s5: 3.2236528396606445  
depth: 1, iteration: 444000, test\_RMSE: 1.129388451576233, erank: 65.3775939941  
4062, s1: 5.01088285446167, s5: 3.2366786003112793  
depth: 1, iteration: 446000, test\_RMSE: 1.129388451576233, erank: 65.3774719238  
2812, s1: 5.031062126159668, s5: 3.249674081802368  
depth: 1, iteration: 448000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 5.05120325088501, s5: 3.262688159942627  
depth: 1, iteration: 450000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 5.07130765914917, s5: 3.2756597995758057  
depth: 1, iteration: 452000, test\_RMSE: 1.129388451576233, erank: 65.3773117065  
4297, s1: 5.091337203979492, s5: 3.288609743118286  
depth: 1, iteration: 454000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 5.111443042755127, s5: 3.301546335220337  
depth: 1, iteration: 456000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 5.131542205810547, s5: 3.3145089149475098  
depth: 1, iteration: 458000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 5.151531219482422, s5: 3.327408790588379  
depth: 1, iteration: 460000, test\_RMSE: 1.129388451576233, erank: 65.3771286010  
7422, s1: 5.171554088592529, s5: 3.3403050899505615  
depth: 1, iteration: 462000, test\_RMSE: 1.129388451576233, erank: 65.3770675659  
1797, s1: 5.191554069519043, s5: 3.353181838989258  
depth: 1, iteration: 464000, test\_RMSE: 1.129388451576233, erank: 65.3770065307  
6172, s1: 5.211547374725342, s5: 3.3660452365875244  
depth: 1, iteration: 466000, test\_RMSE: 1.129388451576233, erank: 65.3770294189  
4531, s1: 5.231472015380859, s5: 3.378894805908203  
depth: 1, iteration: 468000, test\_RMSE: 1.129388451576233, erank: 65.3770294189  
4531, s1: 5.251397609710693, s5: 3.391737937927246  
depth: 1, iteration: 470000, test\_RMSE: 1.129388451576233, erank: 65.3770294189  
4531, s1: 5.271305561065674, s5: 3.4045732021331787  
depth: 1, iteration: 472000, test\_RMSE: 1.129388451576233, erank: 65.3769760131  
836, s1: 5.291223526000977, s5: 3.4174084663391113  
depth: 1, iteration: 474000, test\_RMSE: 1.129388451576233, erank: 65.3769760131  
836, s1: 5.311069488525391, s5: 3.4302103519439697  
depth: 1, iteration: 476000, test\_RMSE: 1.129388451576233, erank: 65.3770294189  
4531, s1: 5.330911159515381, s5: 3.4430243968963623  
depth: 1, iteration: 478000, test\_RMSE: 1.129388451576233, erank: 65.3769760131  
836, s1: 5.350759983062744, s5: 3.455850601196289  
depth: 1, iteration: 480000, test\_RMSE: 1.129388451576233, erank: 65.3769760131  
836, s1: 5.370598316192627, s5: 3.4686262607574463  
depth: 1, iteration: 482000, test\_RMSE: 1.129388451576233, erank: 65.3769073486

3281, s1: 5.390417575836182, s5: 3.481398820877075  
depth: 1, iteration: 484000, test\_RMSE: 1.129388451576233, erank: 65.3769073486  
3281, s1: 5.410178184509277, s5: 3.4941840171813965  
depth: 1, iteration: 486000, test\_RMSE: 1.129388451576233, erank: 65.3768157958  
9844, s1: 5.429947376251221, s5: 3.506927251815796  
depth: 1, iteration: 488000, test\_RMSE: 1.129388451576233, erank: 65.3767547607  
4219, s1: 5.449706554412842, s5: 3.5197064876556396  
depth: 1, iteration: 490000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 5.46938943862915, s5: 3.5324060916900635  
depth: 1, iteration: 492000, test\_RMSE: 1.129388451576233, erank: 65.3767547607  
4219, s1: 5.489124774932861, s5: 3.545126438140869  
depth: 1, iteration: 494000, test\_RMSE: 1.129388451576233, erank: 65.3767852783  
2031, s1: 5.508813858032227, s5: 3.5578229427337646  
depth: 1, iteration: 496000, test\_RMSE: 1.129388451576233, erank: 65.3768463134  
7656, s1: 5.528477191925049, s5: 3.570542335510254  
depth: 1, iteration: 498000, test\_RMSE: 1.129388451576233, erank: 65.3769073486  
3281, s1: 5.548087120056152, s5: 3.583219289779663  
depth: 1, iteration: 500000, test\_RMSE: 1.129388451576233, erank: 65.3770675659  
1797, s1: 5.567665100097656, s5: 3.595888614654541  
depth: 1, iteration: 502000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 5.587271213531494, s5: 3.6085498332977295  
depth: 1, iteration: 504000, test\_RMSE: 1.129388451576233, erank: 65.3771591186  
5234, s1: 5.606869220733643, s5: 3.6212337017059326  
depth: 1, iteration: 506000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 5.626433849334717, s5: 3.633871555328369  
depth: 1, iteration: 508000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 5.645961761474609, s5: 3.6465141773223877  
depth: 1, iteration: 510000, test\_RMSE: 1.129388451576233, erank: 65.3775939941  
4062, s1: 5.665441036224365, s5: 3.659132480621338  
depth: 1, iteration: 512000, test\_RMSE: 1.129388451576233, erank: 65.3777160644  
5312, s1: 5.684874534606934, s5: 3.6717541217803955  
depth: 1, iteration: 514000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 5.704365253448486, s5: 3.684335708618164  
depth: 1, iteration: 516000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 5.723827838897705, s5: 3.6969425678253174  
depth: 1, iteration: 518000, test\_RMSE: 1.129388451576233, erank: 65.3782196044  
9219, s1: 5.743242263793945, s5: 3.709505796432495  
depth: 1, iteration: 520000, test\_RMSE: 1.129388451576233, erank: 65.3784332275  
3906, s1: 5.762667179107666, s5: 3.7220406532287598  
depth: 1, iteration: 522000, test\_RMSE: 1.129388451576233, erank: 65.3786544799  
8047, s1: 5.782019138336182, s5: 3.734588861465454  
depth: 1, iteration: 524000, test\_RMSE: 1.129388451576233, erank: 65.3787155151  
3672, s1: 5.801420211791992, s5: 3.747098684310913  
depth: 1, iteration: 526000, test\_RMSE: 1.129388451576233, erank: 65.3788452148  
4375, s1: 5.8207831382751465, s5: 3.7596027851104736  
depth: 1, iteration: 528000, test\_RMSE: 1.129388451576233, erank: 65.3788757324  
2188, s1: 5.8401408195495605, s5: 3.772087812423706  
depth: 1, iteration: 530000, test\_RMSE: 1.129388451576233, erank: 65.3789367675  
7812, s1: 5.859407901763916, s5: 3.784571647644043  
depth: 1, iteration: 532000, test\_RMSE: 1.129388451576233, erank: 65.37890625,  
s1: 5.878689289093018, s5: 3.7970454692840576  
depth: 1, iteration: 534000, test\_RMSE: 1.129388451576233, erank: 65.3788452148  
4375, s1: 5.897915363311768, s5: 3.8094966411590576  
depth: 1, iteration: 536000, test\_RMSE: 1.129388451576233, erank: 65.3787460327

1484, s1: 5.917184829711914, s5: 3.8219025135040283  
depth: 1, iteration: 538000, test\_RMSE: 1.129388451576233, erank: 65.3785018920  
8984, s1: 5.936442852020264, s5: 3.8343746662139893  
depth: 1, iteration: 540000, test\_RMSE: 1.129388451576233, erank: 65.3784027099  
6094, s1: 5.955679893493652, s5: 3.846796989440918  
depth: 1, iteration: 542000, test\_RMSE: 1.129388451576233, erank: 65.3781585693  
3594, s1: 5.974881172180176, s5: 3.8592097759246826  
depth: 1, iteration: 544000, test\_RMSE: 1.129388451576233, erank: 65.3780288696  
289, s1: 5.994083404541016, s5: 3.8715853691101074  
depth: 1, iteration: 546000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 6.01322603225708, s5: 3.883955478668213  
depth: 1, iteration: 548000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.032364845275879, s5: 3.8963119983673096  
depth: 1, iteration: 550000, test\_RMSE: 1.129388451576233, erank: 65.3778152465  
8203, s1: 6.051433086395264, s5: 3.908647060394287  
depth: 1, iteration: 552000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.070526599884033, s5: 3.920978307723999  
depth: 1, iteration: 554000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.089583396911621, s5: 3.9332566261291504  
depth: 1, iteration: 556000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 6.108647346496582, s5: 3.9455406665802  
depth: 1, iteration: 558000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 6.127692699432373, s5: 3.957843780517578  
depth: 1, iteration: 560000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 6.146696090698242, s5: 3.9701030254364014  
depth: 1, iteration: 562000, test\_RMSE: 1.129388451576233, erank: 65.3779067993  
164, s1: 6.1657538414001465, s5: 3.9823358058929443  
depth: 1, iteration: 564000, test\_RMSE: 1.129388451576233, erank: 65.3779678344  
7266, s1: 6.18467903137207, s5: 3.99452543258667  
depth: 1, iteration: 566000, test\_RMSE: 1.129388451576233, erank: 65.3778762817  
3828, s1: 6.203657150268555, s5: 4.006747245788574  
depth: 1, iteration: 568000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.222601413726807, s5: 4.018961429595947  
depth: 1, iteration: 570000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.241529941558838, s5: 4.031159400939941  
depth: 1, iteration: 572000, test\_RMSE: 1.129388451576233, erank: 65.3776245117  
1875, s1: 6.260491847991943, s5: 4.043376445770264  
depth: 1, iteration: 574000, test\_RMSE: 1.129388451576233, erank: 65.3775024414  
0625, s1: 6.279430389404297, s5: 4.055549144744873  
depth: 1, iteration: 576000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 6.2983012199401855, s5: 4.067727088928223  
depth: 1, iteration: 578000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 6.317144870758057, s5: 4.079926013946533  
depth: 1, iteration: 580000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 6.336025238037109, s5: 4.092057704925537  
depth: 1, iteration: 582000, test\_RMSE: 1.129388451576233, erank: 65.3772201538  
086, s1: 6.354860782623291, s5: 4.104221820831299  
depth: 1, iteration: 584000, test\_RMSE: 1.129388451576233, erank: 65.3772201538  
086, s1: 6.373619556427002, s5: 4.116359233856201  
depth: 1, iteration: 586000, test\_RMSE: 1.129388451576233, erank: 65.3772201538  
086, s1: 6.392346382141113, s5: 4.128455638885498  
depth: 1, iteration: 588000, test\_RMSE: 1.129388451576233, erank: 65.3772888183  
5938, s1: 6.411064624786377, s5: 4.140562057495117  
depth: 1, iteration: 590000, test\_RMSE: 1.129388451576233, erank: 65.3773422241

211, s1: 6.429720401763916, s5: 4.1526336669921875  
depth: 1, iteration: 592000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 6.4483842849731445, s5: 4.164750099182129  
depth: 1, iteration: 594000, test\_RMSE: 1.129388451576233, erank: 65.3773117065  
4297, s1: 6.4671831130981445, s5: 4.176808834075928  
depth: 1, iteration: 596000, test\_RMSE: 1.129388451576233, erank: 65.3773422241  
211, s1: 6.485839366912842, s5: 4.18890380859375  
depth: 1, iteration: 598000, test\_RMSE: 1.129388451576233, erank: 65.3773803710  
9375, s1: 6.504518985748291, s5: 4.200963497161865  
depth: 1, iteration: 600000, test\_RMSE: 1.129388451576233, erank: 65.3774108886  
7188, s1: 6.523141384124756, s5: 4.213038444519043  
depth: 1, iteration: 602000, test\_RMSE: 1.129388451576233, erank: 65.3773803710  
9375, s1: 6.541783809661865, s5: 4.2250847816467285  
depth: 1, iteration: 604000, test\_RMSE: 1.129388451576233, erank: 65.3775634765  
625, s1: 6.56033992767334, s5: 4.237094879150391  
depth: 1, iteration: 606000, test\_RMSE: 1.129388451576233, erank: 65.3775329589  
8438, s1: 6.578910827636719, s5: 4.249118804931641  
depth: 1, iteration: 608000, test\_RMSE: 1.129388451576233, erank: 65.3776550292  
9688, s1: 6.597480773925781, s5: 4.261106491088867  
depth: 1, iteration: 610000, test\_RMSE: 1.129388451576233, erank: 65.3776931762  
6953, s1: 6.616052150726318, s5: 4.2730889320373535  
depth: 1, iteration: 612000, test\_RMSE: 1.129388451576233, erank: 65.3777160644  
5312, s1: 6.634603500366211, s5: 4.285036563873291  
depth: 1, iteration: 614000, test\_RMSE: 1.129388451576233, erank: 65.3778152465  
8203, s1: 6.653146266937256, s5: 4.297053813934326  
depth: 1, iteration: 616000, test\_RMSE: 1.129388451576233, erank: 65.3778457641  
6016, s1: 6.671614646911621, s5: 4.309004306793213  
depth: 1, iteration: 618000, test\_RMSE: 1.129388451576233, erank: 65.3779373168  
9453, s1: 6.690098762512207, s5: 4.320950508117676  
depth: 1, iteration: 620000, test\_RMSE: 1.129388451576233, erank: 65.3780975341  
7969, s1: 6.708571910858154, s5: 4.332903861999512  
depth: 1, iteration: 622000, test\_RMSE: 1.129388451576233, erank: 65.3781890869  
1406, s1: 6.727034568786621, s5: 4.344827175140381  
depth: 1, iteration: 624000, test\_RMSE: 1.129388451576233, erank: 65.3782501220  
7031, s1: 6.745476722717285, s5: 4.356788158416748  
depth: 1, iteration: 626000, test\_RMSE: 1.129388451576233, erank: 65.3783416748  
0469, s1: 6.763828277587891, s5: 4.368722915649414  
depth: 1, iteration: 628000, test\_RMSE: 1.129388451576233, erank: 65.3783111572  
2656, s1: 6.782301425933838, s5: 4.380608558654785  
depth: 1, iteration: 630000, test\_RMSE: 1.129388451576233, erank: 65.3783721923  
8281, s1: 6.800653457641602, s5: 4.392525672912598  
depth: 1, iteration: 632000, test\_RMSE: 1.129388451576233, erank: 65.3784027099  
6094, s1: 6.81893253326416, s5: 4.404419422149658  
depth: 1, iteration: 634000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, s1: 6.837334632873535, s5: 4.416271209716797  
depth: 1, iteration: 636000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, s1: 6.855575084686279, s5: 4.428129196166992  
depth: 1, iteration: 638000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, s1: 6.873847007751465, s5: 4.4399518966674805  
depth: 1, iteration: 640000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, s1: 6.8922247886657715, s5: 4.451780796051025  
depth: 1, iteration: 642000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, s1: 6.910440444946289, s5: 4.463613986968994  
depth: 1, iteration: 644000, test\_RMSE: 1.129388451576233, erank: 65.3785934448

2422, sl: 6.9286909103393555, s5: 4.475407600402832  
depth: 1, iteration: 646000, test\_RMSE: 1.129388451576233, erank: 65.3785629272  
461, sl: 6.946896553039551, s5: 4.4871907234191895  
depth: 1, iteration: 648000, test\_RMSE: 1.129388451576233, erank: 65.3786544799  
8047, sl: 6.965054035186768, s5: 4.498961925506592  
depth: 1, iteration: 650000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 6.983249664306641, s5: 4.510726451873779  
depth: 1, iteration: 652000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, sl: 7.00142765045166, s5: 4.522480487823486  
depth: 1, iteration: 654000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.019534111022949, s5: 4.5342183113098145  
depth: 1, iteration: 656000, test\_RMSE: 1.129388451576233, erank: 65.3786544799  
8047, sl: 7.03764533996582, s5: 4.54594087600708  
depth: 1, iteration: 658000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.055824279785156, s5: 4.557666301727295  
depth: 1, iteration: 660000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.073887825012207, s5: 4.569359302520752  
depth: 1, iteration: 662000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.091961860656738, s5: 4.581092834472656  
depth: 1, iteration: 664000, test\_RMSE: 1.129388451576233, erank: 65.3786239624  
0234, sl: 7.110030651092529, s5: 4.592761516571045  
depth: 1, iteration: 666000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, sl: 7.128096580505371, s5: 4.604455471038818  
depth: 1, iteration: 668000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, sl: 7.146108627319336, s5: 4.616094589233398  
depth: 1, iteration: 670000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, sl: 7.164141654968262, s5: 4.6276960372924805  
depth: 1, iteration: 672000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, sl: 7.18211030960083, s5: 4.639340400695801  
depth: 1, iteration: 674000, test\_RMSE: 1.129388451576233, erank: 65.3785018920  
8984, sl: 7.200122833251953, s5: 4.650977611541748  
depth: 1, iteration: 676000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, sl: 7.21812105178833, s5: 4.66259241104126  
depth: 1, iteration: 678000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.236023426055908, s5: 4.6741557121276855  
depth: 1, iteration: 680000, test\_RMSE: 1.129388451576233, erank: 65.3785629272  
461, sl: 7.253933429718018, s5: 4.685736179351807  
depth: 1, iteration: 682000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.271838665008545, s5: 4.697259426116943  
depth: 1, iteration: 684000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.289700508117676, s5: 4.708840370178223  
depth: 1, iteration: 686000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.307548999786377, s5: 4.720361709594727  
depth: 1, iteration: 688000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, sl: 7.32542610168457, s5: 4.731855392456055  
depth: 1, iteration: 690000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, sl: 7.343233585357666, s5: 4.7433576583862305  
depth: 1, iteration: 692000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, sl: 7.361069679260254, s5: 4.75486421585083  
depth: 1, iteration: 694000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, sl: 7.378819465637207, s5: 4.766332149505615  
depth: 1, iteration: 696000, test\_RMSE: 1.129388451576233, erank: 65.3784027099  
6094, sl: 7.396631240844727, s5: 4.777844429016113  
depth: 1, iteration: 698000, test\_RMSE: 1.129388451576233, erank: 65.3784027099

6094, s1: 7.414412021636963, s5: 4.789299011230469  
depth: 1, iteration: 700000, test\_RMSE: 1.129388451576233, erank: 65.3784332275  
3906, s1: 7.432157516479492, s5: 4.800716400146484  
depth: 1, iteration: 702000, test\_RMSE: 1.129388451576233, erank: 65.3784332275  
3906, s1: 7.449897766113281, s5: 4.812169551849365  
depth: 1, iteration: 704000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, s1: 7.467588901519775, s5: 4.823577404022217  
depth: 1, iteration: 706000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, s1: 7.485274314880371, s5: 4.83499002456665  
depth: 1, iteration: 708000, test\_RMSE: 1.129388451576233, erank: 65.3784332275  
3906, s1: 7.502978801727295, s5: 4.846413612365723  
depth: 1, iteration: 710000, test\_RMSE: 1.129388451576233, erank: 65.3783721923  
8281, s1: 7.520634651184082, s5: 4.857817649841309  
depth: 1, iteration: 712000, test\_RMSE: 1.129388451576233, erank: 65.3783721923  
8281, s1: 7.53831148147583, s5: 4.86919641494751  
depth: 1, iteration: 714000, test\_RMSE: 1.129388451576233, erank: 65.3783721923  
8281, s1: 7.555987358093262, s5: 4.880549430847168  
depth: 1, iteration: 716000, test\_RMSE: 1.129388451576233, erank: 65.3783416748  
0469, s1: 7.573647975921631, s5: 4.8918962478637695  
depth: 1, iteration: 718000, test\_RMSE: 1.129388451576233, erank: 65.3783416748  
0469, s1: 7.591256618499756, s5: 4.9032511711120605  
depth: 1, iteration: 720000, test\_RMSE: 1.129388451576233, erank: 65.3784027099  
6094, s1: 7.608865737915039, s5: 4.914647579193115  
depth: 1, iteration: 722000, test\_RMSE: 1.129388451576233, erank: 65.3784027099  
6094, s1: 7.626498699188232, s5: 4.925992488861084  
depth: 1, iteration: 724000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, s1: 7.644110679626465, s5: 4.937265396118164  
depth: 1, iteration: 726000, test\_RMSE: 1.129388451576233, erank: 65.3784713745  
1172, s1: 7.661661624908447, s5: 4.948627948760986  
depth: 1, iteration: 728000, test\_RMSE: 1.129388451576233, erank: 65.3784332275  
3906, s1: 7.67924690246582, s5: 4.9599609375  
depth: 1, iteration: 730000, test\_RMSE: 1.129388451576233, erank: 65.3785018920  
8984, s1: 7.6967597007751465, s5: 4.971234321594238  
depth: 1, iteration: 732000, test\_RMSE: 1.129388451576233, erank: 65.3785247802  
7344, s1: 7.714295864105225, s5: 4.982519626617432  
depth: 1, iteration: 734000, test\_RMSE: 1.129388451576233, erank: 65.3785018920  
8984, s1: 7.731789588928223, s5: 4.99376916885376  
depth: 1, iteration: 736000, test\_RMSE: 1.129388451576233, erank: 65.3785629272  
461, s1: 7.749192237854004, s5: 5.005049228668213  
depth: 1, iteration: 738000, test\_RMSE: 1.129388451576233, erank: 65.3785934448  
2422, s1: 7.766638278961182, s5: 5.016298770904541  
depth: 1, iteration: 740000, test\_RMSE: 1.129388451576233, erank: 65.3786849975  
586, s1: 7.784031867980957, s5: 5.027519702911377  
depth: 1, iteration: 742000, test\_RMSE: 1.129388451576233, erank: 65.3787155151  
3672, s1: 7.801393508911133, s5: 5.0387420654296875  
depth: 1, iteration: 744000, test\_RMSE: 1.129388451576233, erank: 65.3787460327  
1484, s1: 7.818779468536377, s5: 5.049977779388428  
depth: 1, iteration: 746000, test\_RMSE: 1.129388451576233, erank: 65.3788452148  
4375, s1: 7.836112976074219, s5: 5.061140537261963  
depth: 1, iteration: 748000, test\_RMSE: 1.129388451576233, erank: 65.3788452148  
4375, s1: 7.853438377380371, s5: 5.0723042488098145  
depth: 1, iteration: 750000, test\_RMSE: 1.129388451576233, erank: 65.37890625,  
s1: 7.870701789855957, s5: 5.083494186401367  
depth: 1, iteration: 752000, test\_RMSE: 1.129388451576233, erank: 65.3789672851



5625, s1: 7.887970447540283, s5: 5.094629764556885  
depth: 1, iteration: 754000, test\_RMSE: 1.129388451576233, erank: 65.3789672851  
5625, s1: 7.90527868270874, s5: 5.10579252243042  
depth: 1, iteration: 756000, test\_RMSE: 1.129388451576233, erank: 65.3790588378  
9062, s1: 7.922473907470703, s5: 5.116911888122559  
depth: 1, iteration: 758000, test\_RMSE: 1.129388451576233, erank: 65.3791198730  
4688, s1: 7.939672946929932, s5: 5.1280364990234375  
depth: 1, iteration: 760000, test\_RMSE: 1.129388451576233, erank: 65.3791885375  
9766, s1: 7.956871032714844, s5: 5.139138698577881  
depth: 1, iteration: 762000, test\_RMSE: 1.129388451576233, erank: 65.3792114257  
8125, s1: 7.97399377822876, s5: 5.150224685668945  
depth: 1, iteration: 764000, test\_RMSE: 1.129388451576233, erank: 65.3793411254  
8828, s1: 7.991099834442139, s5: 5.161290645599365  
depth: 1, iteration: 766000, test\_RMSE: 1.129388451576233, erank: 65.3794326782  
2266, s1: 8.008237838745117, s5: 5.172372341156006  
depth: 1, iteration: 768000, test\_RMSE: 1.129388451576233, erank: 65.3794937133  
789, s1: 8.025338172912598, s5: 5.183413028717041  
depth: 1, iteration: 770000, test\_RMSE: 1.129388451576233, erank: 65.3795928955  
0781, s1: 8.042387008666992, s5: 5.194485187530518  
depth: 1, iteration: 772000, test\_RMSE: 1.129388451576233, erank: 65.3796539306  
6406, s1: 8.059490203857422, s5: 5.2055230140686035  
depth: 1, iteration: 774000, test\_RMSE: 1.129388451576233, erank: 65.3797760009  
7656, s1: 8.076496124267578, s5: 5.2165727615356445  
depth: 1, iteration: 776000, test\_RMSE: 1.129388451576233, erank: 65.3798980712  
8906, s1: 8.09350299835205, s5: 5.2275776863098145  
depth: 1, iteration: 778000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.110552787780762, s5: 5.238574981689453  
depth: 1, iteration: 780000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.127632141113281, s5: 5.249549388885498  
depth: 1, iteration: 782000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.144617080688477, s5: 5.260532855987549  
depth: 1, iteration: 784000, test\_RMSE: 1.129388451576233, erank: 65.3799972534  
1797, s1: 8.161637306213379, s5: 5.271458625793457  
depth: 1, iteration: 786000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.178644180297852, s5: 5.2824249267578125  
depth: 1, iteration: 788000, test\_RMSE: 1.129388451576233, erank: 65.3800277709  
961, s1: 8.195670127868652, s5: 5.293374538421631  
depth: 1, iteration: 790000, test\_RMSE: 1.129388451576233, erank: 65.3800277709  
961, s1: 8.212568283081055, s5: 5.304340839385986  
depth: 1, iteration: 792000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.229517936706543, s5: 5.3152899742126465  
depth: 1, iteration: 794000, test\_RMSE: 1.129388451576233, erank: 65.3799667358  
3984, s1: 8.246498107910156, s5: 5.326203346252441  
depth: 1, iteration: 796000, test\_RMSE: 1.129388451576233, erank: 65.3798980712  
8906, s1: 8.263460159301758, s5: 5.337158679962158  
depth: 1, iteration: 798000, test\_RMSE: 1.129388451576233, erank: 65.3798980712  
8906, s1: 8.280402183532715, s5: 5.348091125488281

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 1 --lam 0.0 --optim Adam --lr 1e-3 --niters 30000  
depth: 1, iteration: 0, test\_RMSE: 1.1278135776519775, erank: 76.3040008544921  
9, s1: 0.018671663478016853, s5: 0.015004964545369148  
depth: 1, iteration: 2000, test\_RMSE: 1.1278135776519775, erank: 69.57570648193

36, s1: 17.799293518066406, s5: 13.286659240722656  
depth: 1, iteration: 4000, test\_RMSE: 1.1278135776519775, erank: 67.13298034667  
969, s1: 21.592870712280273, s5: 15.757697105407715  
depth: 1, iteration: 6000, test\_RMSE: 1.1278135776519775, erank: 66.56858062744  
14, s1: 22.308605194091797, s5: 16.094003677368164  
depth: 1, iteration: 8000, test\_RMSE: 1.1278135776519775, erank: 66.51020050048  
828, s1: 22.37144660949707, s5: 16.10695457458496  
depth: 1, iteration: 10000, test\_RMSE: 1.1278135776519775, erank: 66.5084533691  
4062, s1: 22.37373161315918, s5: 16.10698127746582  
depth: 1, iteration: 12000, test\_RMSE: 1.1278135776519775, erank: 66.5085144042  
9688, s1: 22.373680114746094, s5: 16.1069278717041  
depth: 1, iteration: 14000, test\_RMSE: 1.1278135776519775, erank: 66.5084228515  
625, s1: 22.373754501342773, s5: 16.10698699951172  
depth: 1, iteration: 16000, test\_RMSE: 1.1278135776519775, erank: 66.5084838867  
1875, s1: 22.373754501342773, s5: 16.1069278717041  
depth: 1, iteration: 18000, test\_RMSE: 1.1278135776519775, erank: 66.5084838867  
1875, s1: 22.37367057800293, s5: 16.107004165649414  
depth: 1, iteration: 20000, test\_RMSE: 1.1278135776519775, erank: 66.5085525512  
6953, s1: 22.37350082397461, s5: 16.106956481933594  
depth: 1, iteration: 22000, test\_RMSE: 1.1278135776519775, erank: 66.5084838867  
1875, s1: 22.37363052368164, s5: 16.106971740722656  
depth: 1, iteration: 24000, test\_RMSE: 1.1278135776519775, erank: 66.5085525512  
6953, s1: 22.37350082397461, s5: 16.106956481933594  
depth: 1, iteration: 26000, test\_RMSE: 1.1278135776519775, erank: 66.5084838867  
1875, s1: 22.37374496459961, s5: 16.10698699951172  
depth: 1, iteration: 28000, test\_RMSE: 1.1278135776519775, erank: 66.5085525512  
6953, s1: 22.37350082397461, s5: 16.106956481933594

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 1 --lam 1e-2 --optim GD --lr 1e-3 --niters 800000  
depth: 1, iteration: 0, test\_RMSE: 1.1314451694488525, erank: 76.3760757446289,  
s1: 0.0026101309340447187, s5: 0.002271020784974098  
depth: 1, iteration: 2000, test\_RMSE: 1.1314349174499512, erank: 1.742164373397  
8271, s1: 0.07887715846300125, s5: 0.0001268037303816527  
depth: 1, iteration: 4000, test\_RMSE: 1.1314337253570557, erank: 1.520890712738  
037, s1: 0.09427691251039505, s5: 0.00010611215839162469  
depth: 1, iteration: 6000, test\_RMSE: 1.1314326524734497, erank: 1.413182139396  
6675, s1: 0.10525203496217728, s5: 9.505931666353717e-05  
depth: 1, iteration: 8000, test\_RMSE: 1.1314316987991333, erank: 1.356327176094  
0552, s1: 0.11443479359149933, s5: 8.700563193997368e-05  
depth: 1, iteration: 10000, test\_RMSE: 1.1314306259155273, erank: 1.32409632205  
96313, s1: 0.12274536490440369, s5: 7.952041778480634e-05  
depth: 1, iteration: 12000, test\_RMSE: 1.1314295530319214, erank: 1.28537392616  
27197, s1: 0.13063113391399384, s5: 7.150768942665309e-05  
depth: 1, iteration: 14000, test\_RMSE: 1.1314277648925781, erank: 1.25715291500  
09155, s1: 0.13835203647613525, s5: 7.01474491506815e-05  
depth: 1, iteration: 16000, test\_RMSE: 1.1314259767532349, erank: 1.23962283134  
46045, s1: 0.1460801362991333, s5: 6.62084567011334e-05  
depth: 1, iteration: 18000, test\_RMSE: 1.1314235925674438, erank: 1.20969641208  
64868, s1: 0.15393859148025513, s5: 6.156103336252272e-05  
depth: 1, iteration: 20000, test\_RMSE: 1.1314207315444946, erank: 1.18891251087  
18872, s1: 0.16201922297477722, s5: 5.831431190017611e-05  
depth: 1, iteration: 22000, test\_RMSE: 1.1314172744750977, erank: 1.17412877082

8247, s1: 0.17039212584495544, s5: 5.701229747501202e-05  
depth: 1, iteration: 24000, test\_RMSE: 1.1314133405685425, erank: 1.15684401988  
98315, s1: 0.17911100387573242, s5: 5.377516936277971e-05  
depth: 1, iteration: 26000, test\_RMSE: 1.1314088106155396, erank: 1.14794456958  
77075, s1: 0.18821589648723602, s5: 5.480875552166253e-05  
depth: 1, iteration: 28000, test\_RMSE: 1.1314036846160889, erank: 1.12989413738  
25073, s1: 0.1977350413799286, s5: 4.747866478282958e-05  
depth: 1, iteration: 30000, test\_RMSE: 1.1313979625701904, erank: 1.11772108078  
00293, s1: 0.20768864452838898, s5: 4.716530747828074e-05  
depth: 1, iteration: 32000, test\_RMSE: 1.1313917636871338, erank: 1.10931789875  
03052, s1: 0.21808511018753052, s5: 4.519701178651303e-05  
depth: 1, iteration: 34000, test\_RMSE: 1.1313849687576294, erank: 1.10047161579  
13208, s1: 0.22892966866493225, s5: 4.172511398792267e-05  
depth: 1, iteration: 36000, test\_RMSE: 1.1313775777816772, erank: 1.09197688102  
72217, s1: 0.24021822214126587, s5: 4.079929203726351e-05  
depth: 1, iteration: 38000, test\_RMSE: 1.131369709968567, erank: 1.085700869560  
2417, s1: 0.25194332003593445, s5: 3.929105514544062e-05  
depth: 1, iteration: 40000, test\_RMSE: 1.131361484527588, erank: 1.074059247970  
581, s1: 0.26409289240837097, s5: 3.60980884579476e-05  
depth: 1, iteration: 42000, test\_RMSE: 1.1313527822494507, erank: 1.06944453716  
27808, s1: 0.2766552269458771, s5: 3.439066495047882e-05  
depth: 1, iteration: 44000, test\_RMSE: 1.1313436031341553, erank: 1.06521821022  
0337, s1: 0.2896078824996948, s5: 3.5140888940077275e-05  
depth: 1, iteration: 46000, test\_RMSE: 1.1313341856002808, erank: 1.05825114250  
1831, s1: 0.3029397130012512, s5: 3.2598731195321307e-05  
depth: 1, iteration: 48000, test\_RMSE: 1.1313241720199585, erank: 1.05654954910  
27832, s1: 0.31662940979003906, s5: 3.100370668107644e-05  
depth: 1, iteration: 50000, test\_RMSE: 1.1313140392303467, erank: 1.04921543598  
17505, s1: 0.33065930008888245, s5: 3.0213694117264822e-05  
depth: 1, iteration: 52000, test\_RMSE: 1.1313035488128662, erank: 1.04476749897  
00317, s1: 0.345012366771698, s5: 2.7567190045374446e-05  
depth: 1, iteration: 54000, test\_RMSE: 1.131292700767517, erank: 1.042999744415  
2832, s1: 0.3596690595149994, s5: 2.77571270999033e-05  
depth: 1, iteration: 56000, test\_RMSE: 1.1312816143035889, erank: 1.03936922550  
20142, s1: 0.3746105432510376, s5: 2.7344163754605688e-05  
depth: 1, iteration: 58000, test\_RMSE: 1.131270408630371, erank: 1.037289857864  
3799, s1: 0.3898230195045471, s5: 2.721527016547043e-05  
depth: 1, iteration: 60000, test\_RMSE: 1.1312588453292847, erank: 1.03425884246  
82617, s1: 0.4052872955799103, s5: 2.4661510906298645e-05  
depth: 1, iteration: 62000, test\_RMSE: 1.1312470436096191, erank: 1.03154551982  
87964, s1: 0.4209936261177063, s5: 2.319494160474278e-05  
depth: 1, iteration: 64000, test\_RMSE: 1.131235122680664, erank: 1.029598474502  
5635, s1: 0.4369222237586975, s5: 2.306915121152997e-05  
depth: 1, iteration: 66000, test\_RMSE: 1.1312229633331299, erank: 1.02814328670  
5017, s1: 0.4530662000179291, s5: 2.2923619326320477e-05  
depth: 1, iteration: 68000, test\_RMSE: 1.1312108039855957, erank: 1.02657353878  
02124, s1: 0.46940138936042786, s5: 2.2010361135471612e-05  
depth: 1, iteration: 70000, test\_RMSE: 1.1311984062194824, erank: 1.02485764026  
64185, s1: 0.48593419790267944, s5: 2.1424451915663667e-05  
depth: 1, iteration: 72000, test\_RMSE: 1.13118577003479, erank: 1.0234256982803  
345, s1: 0.502634584903717, s5: 2.078042962239124e-05  
depth: 1, iteration: 74000, test\_RMSE: 1.1311731338500977, erank: 1.02284348011  
01685, s1: 0.5195059776306152, s5: 2.035166289715562e-05  
depth: 1, iteration: 76000, test\_RMSE: 1.1311603784561157, erank: 1.02034914493

5608, s1: 0.5365304350852966, s5: 1.943835559359286e-05  
depth: 1, iteration: 78000, test\_RMSE: 1.1311473846435547, erank: 1.01934564113  
61694, s1: 0.5537043809890747, s5: 2.0567065803334117e-05  
depth: 1, iteration: 80000, test\_RMSE: 1.1311343908309937, erank: 1.01848423480  
98755, s1: 0.571021318435669, s5: 1.8800419638864696e-05  
depth: 1, iteration: 82000, test\_RMSE: 1.131121277809143, erank: 1.018239974975  
586, s1: 0.5884658098220825, s5: 1.8411363271297887e-05  
depth: 1, iteration: 84000, test\_RMSE: 1.1311081647872925, erank: 1.01645052433  
01392, s1: 0.6060341596603394, s5: 1.7337813915219158e-05  
depth: 1, iteration: 86000, test\_RMSE: 1.1310948133468628, erank: 1.01601016521  
45386, s1: 0.6237242817878723, s5: 1.6582107491558418e-05  
depth: 1, iteration: 88000, test\_RMSE: 1.131081461906433, erank: 1.014736890792  
8467, s1: 0.6415268778800964, s5: 1.65241308422992e-05  
depth: 1, iteration: 90000, test\_RMSE: 1.1310679912567139, erank: 1.01455473899  
8413, s1: 0.6594281792640686, s5: 1.588968007126823e-05  
depth: 1, iteration: 92000, test\_RMSE: 1.1310546398162842, erank: 1.01545095443  
72559, s1: 0.6774398684501648, s5: 1.8866971004172228e-05  
depth: 1, iteration: 94000, test\_RMSE: 1.1310409307479858, erank: 1.01328647136  
68823, s1: 0.6955479979515076, s5: 1.5258241546689533e-05  
depth: 1, iteration: 96000, test\_RMSE: 1.131027340888977, erank: 1.012340426445  
0073, s1: 0.7137336134910583, s5: 1.5186511518550105e-05  
depth: 1, iteration: 98000, test\_RMSE: 1.1310137510299683, erank: 1.01212203502  
65503, s1: 0.7320166230201721, s5: 1.619010254216846e-05  
depth: 1, iteration: 100000, test\_RMSE: 1.1309999227523804, erank: 1.0115675926  
208496, s1: 0.7503824830055237, s5: 1.3683826182386838e-05  
depth: 1, iteration: 102000, test\_RMSE: 1.130986213684082, erank: 1.01073622703  
55225, s1: 0.768822968006134, s5: 1.4727528650837485e-05  
depth: 1, iteration: 104000, test\_RMSE: 1.1309723854064941, erank: 1.0102436542  
510986, s1: 0.7873379588127136, s5: 1.3005495929974131e-05  
depth: 1, iteration: 106000, test\_RMSE: 1.1309585571289062, erank: 1.0099884271  
621704, s1: 0.8059223294258118, s5: 1.3835794561600778e-05  
depth: 1, iteration: 108000, test\_RMSE: 1.1309446096420288, erank: 1.0092437267  
303467, s1: 0.8245754241943359, s5: 1.3025905900576618e-05  
depth: 1, iteration: 110000, test\_RMSE: 1.130930781364441, erank: 1.00893938541  
41235, s1: 0.8432869911193848, s5: 1.3564776963903569e-05  
depth: 1, iteration: 112000, test\_RMSE: 1.130916714668274, erank: 1.00963795185  
08911, s1: 0.8620649576187134, s5: 1.4991996977187227e-05  
depth: 1, iteration: 114000, test\_RMSE: 1.130902886390686, erank: 1.00911736488  
34229, s1: 0.880914032459259, s5: 1.3309625501278788e-05  
depth: 1, iteration: 116000, test\_RMSE: 1.130888819694519, erank: 1.00843691825  
8667, s1: 0.8998008966445923, s5: 1.3087540537526365e-05  
depth: 1, iteration: 118000, test\_RMSE: 1.130874752998352, erank: 1.00827121734  
61914, s1: 0.9187561869621277, s5: 1.2694225006271154e-05  
depth: 1, iteration: 120000, test\_RMSE: 1.130860686302185, erank: 1.00843846797  
94312, s1: 0.9377554655075073, s5: 1.3828684132022317e-05  
depth: 1, iteration: 122000, test\_RMSE: 1.1308461427688599, erank: 1.0118680000  
305176, s1: 0.9568192958831787, s5: 1.238464938069228e-05  
depth: 1, iteration: 124000, test\_RMSE: 1.1308313608169556, erank: 1.0177471637  
72583, s1: 0.9759303331375122, s5: 1.2451905604393687e-05  
depth: 1, iteration: 126000, test\_RMSE: 1.130816102027893, erank: 1.02501726150  
5127, s1: 0.9951127171516418, s5: 1.260701992578106e-05  
depth: 1, iteration: 128000, test\_RMSE: 1.1308006048202515, erank: 1.0337961912  
155151, s1: 1.0143685340881348, s5: 1.1053606613131706e-05  
depth: 1, iteration: 130000, test\_RMSE: 1.1307843923568726, erank: 1.0461541414

260864, s1: 1.033699631690979, s5: 1.298989536735462e-05  
depth: 1, iteration: 132000, test\_RMSE: 1.130767822265625, erank: 1.06129527091  
97998, s1: 1.0531128644943237, s5: 1.4612935046898201e-05  
depth: 1, iteration: 134000, test\_RMSE: 1.1307505369186401, erank: 1.0792965888  
97705, s1: 1.0726203918457031, s5: 1.2056649211444892e-05  
depth: 1, iteration: 136000, test\_RMSE: 1.1307328939437866, erank: 1.0996744632  
720947, s1: 1.0922268629074097, s5: 1.216578675666824e-05  
depth: 1, iteration: 138000, test\_RMSE: 1.1307145357131958, erank: 1.1227016448  
97461, s1: 1.1119362115859985, s5: 1.3362652680370957e-05  
depth: 1, iteration: 140000, test\_RMSE: 1.1306954622268677, erank: 1.1493782997  
131348, s1: 1.1317288875579834, s5: 1.3153013242117595e-05  
depth: 1, iteration: 142000, test\_RMSE: 1.1306756734848022, erank: 1.1794685125  
350952, s1: 1.1517096757888794, s5: 1.2693365533777978e-05  
depth: 1, iteration: 144000, test\_RMSE: 1.1306551694869995, erank: 1.2112863063  
812256, s1: 1.1717519760131836, s5: 1.4455540622293483e-05  
depth: 1, iteration: 146000, test\_RMSE: 1.1306339502334595, erank: 1.2455472946  
166992, s1: 1.1919690370559692, s5: 1.2335425708442926e-05  
depth: 1, iteration: 148000, test\_RMSE: 1.1306120157241821, erank: 1.2820444107  
055664, s1: 1.212327480316162, s5: 1.0138644029211719e-05  
depth: 1, iteration: 150000, test\_RMSE: 1.130589485168457, erank: 1.31963717937  
46948, s1: 1.2328062057495117, s5: 1.2139755199314095e-05  
depth: 1, iteration: 152000, test\_RMSE: 1.130566120147705, erank: 1.35874295234  
68018, s1: 1.2534277439117432, s5: 1.232054091815371e-05  
depth: 1, iteration: 154000, test\_RMSE: 1.1305421590805054, erank: 1.3996983766  
555786, s1: 1.2741771936416626, s5: 4.4612123019760475e-05  
depth: 1, iteration: 156000, test\_RMSE: 1.1305173635482788, erank: 1.4426945447  
921753, s1: 1.2950981855392456, s5: 0.0003134452854283154  
depth: 1, iteration: 158000, test\_RMSE: 1.130492091178894, erank: 1.48846924304  
96216, s1: 1.3161402940750122, s5: 0.0008394326432608068  
depth: 1, iteration: 160000, test\_RMSE: 1.1304659843444824, erank: 1.5360740423  
202515, s1: 1.3373277187347412, s5: 0.001619765185751021  
depth: 1, iteration: 162000, test\_RMSE: 1.1304391622543335, erank: 1.5853857994  
07959, s1: 1.3586699962615967, s5: 0.0026514995843172073  
depth: 1, iteration: 164000, test\_RMSE: 1.1304117441177368, erank: 1.6364171504  
974365, s1: 1.380162239074707, s5: 0.003931752871721983  
depth: 1, iteration: 166000, test\_RMSE: 1.1303836107254028, erank: 1.6879429817  
199707, s1: 1.401788592338562, s5: 0.005457573104649782  
depth: 1, iteration: 168000, test\_RMSE: 1.130354881286621, erank: 1.74098575115  
20386, s1: 1.4235711097717285, s5: 0.007226076442748308  
depth: 1, iteration: 170000, test\_RMSE: 1.130325436592102, erank: 1.79471850395  
20264, s1: 1.4454985857009888, s5: 0.009234171360731125  
depth: 1, iteration: 172000, test\_RMSE: 1.1302953958511353, erank: 1.8486303091  
049194, s1: 1.4675512313842773, s5: 0.011478893458843231  
depth: 1, iteration: 174000, test\_RMSE: 1.1302647590637207, erank: 1.9021040201  
187134, s1: 1.4897401332855225, s5: 0.013957369141280651  
depth: 1, iteration: 176000, test\_RMSE: 1.1302335262298584, erank: 1.9572823047  
63794, s1: 1.5120668411254883, s5: 0.016666291281580925  
depth: 1, iteration: 178000, test\_RMSE: 1.1302016973495483, erank: 2.0123214721  
679688, s1: 1.5345178842544556, s5: 0.019602663815021515  
depth: 1, iteration: 180000, test\_RMSE: 1.1301692724227905, erank: 2.0661377906  
799316, s1: 1.5570859909057617, s5: 0.022764144465327263  
depth: 1, iteration: 182000, test\_RMSE: 1.1301363706588745, erank: 2.1197443008  
42285, s1: 1.5797810554504395, s5: 0.02614636905491352  
depth: 1, iteration: 184000, test\_RMSE: 1.1301028728485107, erank: 2.1738879680

633545, s1: 1.6025792360305786, s5: 0.02974679321050644  
depth: 1, iteration: 186000, test\_RMSE: 1.1300687789916992, erank: 2.2273588180  
54199, s1: 1.625502347946167, s5: 0.033562276512384415  
depth: 1, iteration: 188000, test\_RMSE: 1.1300342082977295, erank: 2.2806732654  
571533, s1: 1.6485300064086914, s5: 0.037589386105537415  
depth: 1, iteration: 190000, test\_RMSE: 1.1299991607666016, erank: 2.3330626487  
731934, s1: 1.6716431379318237, s5: 0.04182486608624458  
depth: 1, iteration: 192000, test\_RMSE: 1.1299636363983154, erank: 2.3850755691  
52832, s1: 1.6948606967926025, s5: 0.0462653785943985  
depth: 1, iteration: 194000, test\_RMSE: 1.129927635192871, erank: 2.43628025054  
93164, s1: 1.7181706428527832, s5: 0.05090872943401337  
depth: 1, iteration: 196000, test\_RMSE: 1.1298911571502686, erank: 2.4867093563  
079834, s1: 1.7415672540664673, s5: 0.05575078725814819  
depth: 1, iteration: 198000, test\_RMSE: 1.1298542022705078, erank: 2.5362477302  
55127, s1: 1.765039086341858, s5: 0.060787416994571686  
depth: 1, iteration: 200000, test\_RMSE: 1.1298167705535889, erank: 2.5852730274  
20044, s1: 1.788580060005188, s5: 0.06601633131504059  
depth: 1, iteration: 202000, test\_RMSE: 1.1297789812088013, erank: 2.6330645084  
381104, s1: 1.8122000694274902, s5: 0.07143330574035645  
depth: 1, iteration: 204000, test\_RMSE: 1.129740834236145, erank: 2.68053746223  
4497, s1: 1.8358863592147827, s5: 0.07703686505556107  
depth: 1, iteration: 206000, test\_RMSE: 1.1297022104263306, erank: 2.7270143032  
073975, s1: 1.8596277236938477, s5: 0.08282206207513809  
depth: 1, iteration: 208000, test\_RMSE: 1.1296632289886475, erank: 2.7742438316  
345215, s1: 1.883434772491455, s5: 0.08878455311059952  
depth: 1, iteration: 210000, test\_RMSE: 1.1296242475509644, erank: 2.8228781223  
29712, s1: 1.9072906970977783, s5: 0.09492339193820953  
depth: 1, iteration: 212000, test\_RMSE: 1.129584789276123, erank: 2.87298583984  
375, s1: 1.93120539188385, s5: 0.10123571753501892  
depth: 1, iteration: 214000, test\_RMSE: 1.1295453310012817, erank: 2.9248175621  
032715, s1: 1.955159068107605, s5: 0.10771485418081284  
depth: 1, iteration: 216000, test\_RMSE: 1.1295055150985718, erank: 2.9783563613  
8916, s1: 1.97916579246521, s5: 0.11436058580875397  
depth: 1, iteration: 218000, test\_RMSE: 1.1294655799865723, erank: 3.0339024066  
92505, s1: 2.0032100677490234, s5: 0.12116920202970505  
depth: 1, iteration: 220000, test\_RMSE: 1.1294256448745728, erank: 3.0916285514  
831543, s1: 2.02730393409729, s5: 0.12813697755336761  
depth: 1, iteration: 222000, test\_RMSE: 1.1293855905532837, erank: 3.1516182422  
63794, s1: 2.051431894302368, s5: 0.1352623552083969  
depth: 1, iteration: 224000, test\_RMSE: 1.129345417022705, erank: 3.21296858787  
5366, s1: 2.0756163597106934, s5: 0.14253994822502136  
depth: 1, iteration: 226000, test\_RMSE: 1.129305124282837, erank: 3.27562904357  
91016, s1: 2.0998165607452393, s5: 0.14996789395809174  
depth: 1, iteration: 228000, test\_RMSE: 1.1292648315429688, erank: 3.3398783206  
939697, s1: 2.1240594387054443, s5: 0.15754437446594238  
depth: 1, iteration: 230000, test\_RMSE: 1.1292245388031006, erank: 3.4055397510  
528564, s1: 2.148341417312622, s5: 0.16526418924331665  
depth: 1, iteration: 232000, test\_RMSE: 1.1291841268539429, erank: 3.4728722572  
32666, s1: 2.172652006149292, s5: 0.1731274127960205  
depth: 1, iteration: 234000, test\_RMSE: 1.1291437149047852, erank: 3.5418369770  
05005, s1: 2.1969916820526123, s5: 0.18112871050834656  
depth: 1, iteration: 236000, test\_RMSE: 1.1291035413742065, erank: 3.6125433444  
976807, s1: 2.2213587760925293, s5: 0.1892678588628769  
depth: 1, iteration: 238000, test\_RMSE: 1.1290631294250488, erank: 3.6844630241

394043, s1: 2.2457611560821533, s5: 0.19753918051719666  
depth: 1, iteration: 240000, test\_RMSE: 1.1290229558944702, erank: 3.7582368850  
70801, s1: 2.2701897621154785, s5: 0.20594146847724915  
depth: 1, iteration: 242000, test\_RMSE: 1.1289827823638916, erank: 3.8336985111  
236572, s1: 2.294642210006714, s5: 0.21447354555130005  
depth: 1, iteration: 244000, test\_RMSE: 1.1289427280426025, erank: 3.9104723930  
358887, s1: 2.3191092014312744, s5: 0.2231321930885315  
depth: 1, iteration: 246000, test\_RMSE: 1.128902792930603, erank: 3.98917841911  
3159, s1: 2.3436222076416016, s5: 0.23191244900226593  
depth: 1, iteration: 248000, test\_RMSE: 1.128862977027893, erank: 4.06926727294  
9219, s1: 2.3681278228759766, s5: 0.24081093072891235  
depth: 1, iteration: 250000, test\_RMSE: 1.1288232803344727, erank: 4.1505942344  
66553, s1: 2.392669439315796, s5: 0.24983231723308563  
depth: 1, iteration: 252000, test\_RMSE: 1.1287837028503418, erank: 4.2330164909  
36279, s1: 2.4172279834747314, s5: 0.2589688301086426  
depth: 1, iteration: 254000, test\_RMSE: 1.1287442445755005, erank: 4.3168735504  
15039, s1: 2.441815137863159, s5: 0.26821812987327576  
depth: 1, iteration: 256000, test\_RMSE: 1.1287047863006592, erank: 4.4019365310  
668945, s1: 2.4663946628570557, s5: 0.27757784724235535  
depth: 1, iteration: 258000, test\_RMSE: 1.128665566444397, erank: 4.48829126358  
0322, s1: 2.4910192489624023, s5: 0.2870490550994873  
depth: 1, iteration: 260000, test\_RMSE: 1.1286264657974243, erank: 4.5761179924  
01123, s1: 2.5156383514404297, s5: 0.2966219484806061  
depth: 1, iteration: 262000, test\_RMSE: 1.1285874843597412, erank: 4.6654634475  
70801, s1: 2.5402700901031494, s5: 0.30630573630332947  
depth: 1, iteration: 264000, test\_RMSE: 1.1285487413406372, erank: 4.7571020126  
34277, s1: 2.5649285316467285, s5: 0.3160894215106964  
depth: 1, iteration: 266000, test\_RMSE: 1.1285102367401123, erank: 4.8504042625  
42725, s1: 2.589587926864624, s5: 0.325971394777298  
depth: 1, iteration: 268000, test\_RMSE: 1.128471851348877, erank: 4.94531774520  
874, s1: 2.614255905151367, s5: 0.3359566330909729  
depth: 1, iteration: 270000, test\_RMSE: 1.1284335851669312, erank: 5.0414791107  
17773, s1: 2.6389200687408447, s5: 0.34603506326675415  
depth: 1, iteration: 272000, test\_RMSE: 1.128395676612854, erank: 5.13927364349  
3652, s1: 2.6636219024658203, s5: 0.35620540380477905  
depth: 1, iteration: 274000, test\_RMSE: 1.1283578872680664, erank: 5.2385029792  
785645, s1: 2.6883177757263184, s5: 0.3664681017398834  
depth: 1, iteration: 276000, test\_RMSE: 1.1283204555511475, erank: 5.3392744064  
331055, s1: 2.7130253314971924, s5: 0.37682586908340454  
depth: 1, iteration: 278000, test\_RMSE: 1.128283143043518, erank: 5.44145631790  
1611, s1: 2.7377254962921143, s5: 0.3872682750225067  
depth: 1, iteration: 280000, test\_RMSE: 1.1282460689544678, erank: 5.5447392463  
68408, s1: 2.7624356746673584, s5: 0.3977968692779541  
depth: 1, iteration: 282000, test\_RMSE: 1.1282092332839966, erank: 5.6494126319  
88525, s1: 2.7871553897857666, s5: 0.4084092080593109  
depth: 1, iteration: 284000, test\_RMSE: 1.1281726360321045, erank: 5.7554807662  
96387, s1: 2.8118863105773926, s5: 0.41910719871520996  
depth: 1, iteration: 286000, test\_RMSE: 1.1281362771987915, erank: 5.8632025718  
688965, s1: 2.8366081714630127, s5: 0.4298856854438782  
depth: 1, iteration: 288000, test\_RMSE: 1.1281001567840576, erank: 5.9729003906  
25, s1: 2.861344575881958, s5: 0.44074344635009766  
depth: 1, iteration: 290000, test\_RMSE: 1.1280642747879028, erank: 6.0841178894  
04297, s1: 2.8860628604888916, s5: 0.4516778290271759  
depth: 1, iteration: 292000, test\_RMSE: 1.1280286312103271, erank: 6.1970381736

75537, s1: 2.910790205001831, s5: 0.46268871426582336  
depth: 1, iteration: 294000, test\_RMSE: 1.1279932260513306, erank: 6.3112783432  
00684, s1: 2.9355342388153076, s5: 0.47377339005470276  
depth: 1, iteration: 296000, test\_RMSE: 1.127958059310913, erank: 6.42681312561  
0352, s1: 2.9602670669555664, s5: 0.48492947220802307  
depth: 1, iteration: 298000, test\_RMSE: 1.1279231309890747, erank: 6.5435366630  
5542, s1: 2.9850006103515625, s5: 0.49616190791130066  
depth: 1, iteration: 300000, test\_RMSE: 1.127888560295105, erank: 6.66163063049  
3164, s1: 3.0097098350524902, s5: 0.5074590444564819  
depth: 1, iteration: 302000, test\_RMSE: 1.1278541088104248, erank: 6.7810440063  
47656, s1: 3.0344338417053223, s5: 0.5188281536102295  
depth: 1, iteration: 304000, test\_RMSE: 1.1278200149536133, erank: 6.9017448425  
29297, s1: 3.0591604709625244, s5: 0.5302588939666748  
depth: 1, iteration: 306000, test\_RMSE: 1.1277860403060913, erank: 7.0239191055  
29785, s1: 3.0838470458984375, s5: 0.5417607426643372  
depth: 1, iteration: 308000, test\_RMSE: 1.127752423286438, erank: 7.14753532409  
668, s1: 3.108592987060547, s5: 0.553321123123169  
depth: 1, iteration: 310000, test\_RMSE: 1.1277190446853638, erank: 7.2727222442  
62695, s1: 3.133314847946167, s5: 0.5649475455284119  
depth: 1, iteration: 312000, test\_RMSE: 1.1276859045028687, erank: 7.3994522094  
72656, s1: 3.1580114364624023, s5: 0.5766323804855347  
depth: 1, iteration: 314000, test\_RMSE: 1.1276531219482422, erank: 7.5273628234  
86328, s1: 3.1827075481414795, s5: 0.5883809328079224  
depth: 1, iteration: 316000, test\_RMSE: 1.1276204586029053, erank: 7.6563353538  
51318, s1: 3.2074220180511475, s5: 0.6001859903335571  
depth: 1, iteration: 318000, test\_RMSE: 1.127588152885437, erank: 7.78621482849  
1211, s1: 3.232091188430786, s5: 0.6120470762252808  
depth: 1, iteration: 320000, test\_RMSE: 1.1275562047958374, erank: 7.9165930747  
98584, s1: 3.256774663925171, s5: 0.6239635944366455  
depth: 1, iteration: 322000, test\_RMSE: 1.127524495124817, erank: 8.04803371429  
4434, s1: 3.281463146209717, s5: 0.6359363794326782  
depth: 1, iteration: 324000, test\_RMSE: 1.127492904663086, erank: 8.18058776855  
4688, s1: 3.306128978729248, s5: 0.6479641795158386  
depth: 1, iteration: 326000, test\_RMSE: 1.1274616718292236, erank: 8.3139629364  
01367, s1: 3.3307862281799316, s5: 0.6600383520126343  
depth: 1, iteration: 328000, test\_RMSE: 1.1274306774139404, erank: 8.4482059478  
75977, s1: 3.355438232421875, s5: 0.6721723675727844  
depth: 1, iteration: 330000, test\_RMSE: 1.1274000406265259, erank: 8.5834245681  
7627, s1: 3.3800601959228516, s5: 0.6843468546867371  
depth: 1, iteration: 332000, test\_RMSE: 1.1273696422576904, erank: 8.7192611694  
33594, s1: 3.40468430519104, s5: 0.6965728402137756  
depth: 1, iteration: 334000, test\_RMSE: 1.1273393630981445, erank: 8.8556251525  
8789, s1: 3.4293100833892822, s5: 0.7088491320610046  
depth: 1, iteration: 336000, test\_RMSE: 1.1273095607757568, erank: 8.9926548004  
15039, s1: 3.4539191722869873, s5: 0.7211673855781555  
depth: 1, iteration: 338000, test\_RMSE: 1.1272799968719482, erank: 9.1302900314  
33105, s1: 3.478511333465576, s5: 0.7335387468338013  
depth: 1, iteration: 340000, test\_RMSE: 1.1272505521774292, erank: 9.2682933807  
37305, s1: 3.5031116008758545, s5: 0.7459346055984497  
depth: 1, iteration: 342000, test\_RMSE: 1.1272214651107788, erank: 9.4069528579  
71191, s1: 3.527662515640259, s5: 0.7584071755409241  
depth: 1, iteration: 344000, test\_RMSE: 1.1271926164627075, erank: 9.5460405349  
73145, s1: 3.5522234439849854, s5: 0.7709015607833862  
depth: 1, iteration: 346000, test\_RMSE: 1.1271641254425049, erank: 9.6852474212



64648, s1: 3.576770544052124, s5: 0.7834386825561523  
depth: 1, iteration: 348000, test\_RMSE: 1.1271356344223022, erank: 9.8247165679  
93164, s1: 3.6012825965881348, s5: 0.7960208654403687  
depth: 1, iteration: 350000, test\_RMSE: 1.1271076202392578, erank: 9.9643316268  
9209, s1: 3.6258106231689453, s5: 0.8086334466934204  
depth: 1, iteration: 352000, test\_RMSE: 1.1270798444747925, erank: 10.104218482  
971191, s1: 3.650305986404419, s5: 0.8212890028953552  
depth: 1, iteration: 354000, test\_RMSE: 1.1270521879196167, erank: 10.244197845  
458984, s1: 3.674806594848633, s5: 0.8339805006980896  
depth: 1, iteration: 356000, test\_RMSE: 1.12702476978302, erank: 10.38408470153  
8086, s1: 3.699270486831665, s5: 0.8467203974723816  
depth: 1, iteration: 358000, test\_RMSE: 1.126997709274292, erank: 10.5240592956  
54297, s1: 3.723750352859497, s5: 0.8594859838485718  
depth: 1, iteration: 360000, test\_RMSE: 1.1269707679748535, erank: 10.664166450  
500488, s1: 3.7481849193573, s5: 0.8722894191741943  
depth: 1, iteration: 362000, test\_RMSE: 1.1269441843032837, erank: 10.804463386  
535645, s1: 3.7726008892059326, s5: 0.8851134777069092  
depth: 1, iteration: 364000, test\_RMSE: 1.126917839050293, erank: 10.9449071884  
15527, s1: 3.7970082759857178, s5: 0.8979853391647339  
depth: 1, iteration: 366000, test\_RMSE: 1.1268916130065918, erank: 11.085493087  
768555, s1: 3.821403980255127, s5: 0.9108867645263672  
depth: 1, iteration: 368000, test\_RMSE: 1.1268657445907593, erank: 11.226219177  
246094, s1: 3.845794916152954, s5: 0.9238183498382568  
depth: 1, iteration: 370000, test\_RMSE: 1.1268401145935059, erank: 11.366929054  
260254, s1: 3.8701517581939697, s5: 0.9367741942405701  
depth: 1, iteration: 372000, test\_RMSE: 1.1268147230148315, erank: 11.507660865  
783691, s1: 3.89447283744812, s5: 0.9497638940811157  
depth: 1, iteration: 374000, test\_RMSE: 1.1267895698547363, erank: 11.648324012  
756348, s1: 3.9187939167022705, s5: 0.9627904891967773  
depth: 1, iteration: 376000, test\_RMSE: 1.1267646551132202, erank: 11.788918495  
178223, s1: 3.943108320236206, s5: 0.9758439064025879  
depth: 1, iteration: 378000, test\_RMSE: 1.1267399787902832, erank: 11.929463386  
535645, s1: 3.9673845767974854, s5: 0.9889151453971863  
depth: 1, iteration: 380000, test\_RMSE: 1.1267154216766357, erank: 12.069889068  
603516, s1: 3.9916558265686035, s5: 1.0020235776901245  
depth: 1, iteration: 382000, test\_RMSE: 1.126691222190857, erank: 12.2103452682  
49512, s1: 4.015883445739746, s5: 1.0151479244232178  
depth: 1, iteration: 384000, test\_RMSE: 1.1266671419143677, erank: 12.350633621  
21582, s1: 4.040085792541504, s5: 1.028303623199463  
depth: 1, iteration: 386000, test\_RMSE: 1.1266433000564575, erank: 12.490744590  
759277, s1: 4.064300537109375, s5: 1.041487693786621  
depth: 1, iteration: 388000, test\_RMSE: 1.126619815826416, erank: 12.6308336257  
93457, s1: 4.088492393493652, s5: 1.0546925067901611  
depth: 1, iteration: 390000, test\_RMSE: 1.126596450805664, erank: 12.7708559036  
25488, s1: 4.112645626068115, s5: 1.0679149627685547  
depth: 1, iteration: 392000, test\_RMSE: 1.1265732049942017, erank: 12.910850524  
902344, s1: 4.136783123016357, s5: 1.0811654329299927  
depth: 1, iteration: 394000, test\_RMSE: 1.126550316810608, erank: 13.0506019592  
28516, s1: 4.160913944244385, s5: 1.0944368839263916  
depth: 1, iteration: 396000, test\_RMSE: 1.1265275478363037, erank: 13.190050125  
12207, s1: 4.185041427612305, s5: 1.1077197790145874  
depth: 1, iteration: 398000, test\_RMSE: 1.1265050172805786, erank: 13.329220771  
78955, s1: 4.209107398986816, s5: 1.1210429668426514  
depth: 1, iteration: 400000, test\_RMSE: 1.1264827251434326, erank: 13.467913627

624512, s1: 4.233188152313232, s5: 1.1343761682510376  
depth: 1, iteration: 402000, test\_RMSE: 1.1264605522155762, erank: 13.606206893  
920898, s1: 4.257207870483398, s5: 1.1477326154708862  
depth: 1, iteration: 404000, test\_RMSE: 1.1264387369155884, erank: 13.744023323  
059082, s1: 4.281169891357422, s5: 1.161097526550293  
depth: 1, iteration: 406000, test\_RMSE: 1.1264170408248901, erank: 13.881154060  
36377, s1: 4.3052239418029785, s5: 1.1744940280914307  
depth: 1, iteration: 408000, test\_RMSE: 1.126395583152771, erank: 14.0179738998  
41309, s1: 4.32918119430542, s5: 1.1878917217254639  
depth: 1, iteration: 410000, test\_RMSE: 1.1263741254806519, erank: 14.154357910  
15625, s1: 4.353137493133545, s5: 1.2013282775878906  
depth: 1, iteration: 412000, test\_RMSE: 1.1263530254364014, erank: 14.290534973  
144531, s1: 4.377058029174805, s5: 1.214762806892395  
depth: 1, iteration: 414000, test\_RMSE: 1.12633216381073, erank: 14.42642974853  
5156, s1: 4.40093469619751, s5: 1.228232502937317  
depth: 1, iteration: 416000, test\_RMSE: 1.1263114213943481, erank: 14.562109947  
20459, s1: 4.424807071685791, s5: 1.241698145866394  
depth: 1, iteration: 418000, test\_RMSE: 1.1262907981872559, erank: 14.697335243  
225098, s1: 4.4486918449401855, s5: 1.2551915645599365  
depth: 1, iteration: 420000, test\_RMSE: 1.1262704133987427, erank: 14.832235336  
303711, s1: 4.472541332244873, s5: 1.268707513809204  
depth: 1, iteration: 422000, test\_RMSE: 1.126250147819519, erank: 14.9668960571  
28906, s1: 4.496339321136475, s5: 1.282221794128418  
depth: 1, iteration: 424000, test\_RMSE: 1.1262301206588745, erank: 15.101191520  
690918, s1: 4.520127773284912, s5: 1.2957550287246704  
depth: 1, iteration: 426000, test\_RMSE: 1.1262102127075195, erank: 15.235091209  
411621, s1: 4.543896198272705, s5: 1.309280276298523  
depth: 1, iteration: 428000, test\_RMSE: 1.1261905431747437, erank: 15.368740081  
78711, s1: 4.567622184753418, s5: 1.3228509426116943  
depth: 1, iteration: 430000, test\_RMSE: 1.1261709928512573, erank: 15.501973152  
160645, s1: 4.591360569000244, s5: 1.3364312648773193  
depth: 1, iteration: 432000, test\_RMSE: 1.12615168094635, erank: 15.63480949401  
8555, s1: 4.6150593757629395, s5: 1.3500126600265503  
depth: 1, iteration: 434000, test\_RMSE: 1.1261324882507324, erank: 15.767160415  
649414, s1: 4.638740062713623, s5: 1.3636342287063599  
depth: 1, iteration: 436000, test\_RMSE: 1.1261134147644043, erank: 15.899114608  
764648, s1: 4.662347793579102, s5: 1.3772051334381104  
depth: 1, iteration: 438000, test\_RMSE: 1.1260945796966553, erank: 16.030656814  
575195, s1: 4.6859869956970215, s5: 1.3908556699752808  
depth: 1, iteration: 440000, test\_RMSE: 1.1260758638381958, erank: 16.161781311  
035156, s1: 4.709585666656494, s5: 1.4044804573059082  
depth: 1, iteration: 442000, test\_RMSE: 1.1260572671890259, erank: 16.292381286  
621094, s1: 4.733159065246582, s5: 1.4181181192398071  
depth: 1, iteration: 444000, test\_RMSE: 1.126038908958435, erank: 16.4226417541  
5039, s1: 4.756692409515381, s5: 1.4317654371261597  
depth: 1, iteration: 446000, test\_RMSE: 1.1260206699371338, erank: 16.552507400  
512695, s1: 4.78018856048584, s5: 1.44542396068573  
depth: 1, iteration: 448000, test\_RMSE: 1.126002550125122, erank: 16.6818294525  
1465, s1: 4.803738117218018, s5: 1.459093689918518  
depth: 1, iteration: 450000, test\_RMSE: 1.1259846687316895, erank: 16.810695648  
19336, s1: 4.8271870613098145, s5: 1.472762942314148  
depth: 1, iteration: 452000, test\_RMSE: 1.1259669065475464, erank: 16.938976287  
841797, s1: 4.850641250610352, s5: 1.4864501953125  
depth: 1, iteration: 454000, test\_RMSE: 1.1259492635726929, erank: 17.066722869

873047, s1: 4.874059200286865, s5: 1.5001379251480103  
depth: 1, iteration: 456000, test\_RMSE: 1.1259318590164185, erank: 17.193822860  
717773, s1: 4.897474765777588, s5: 1.513847827911377  
depth: 1, iteration: 458000, test\_RMSE: 1.125914454460144, erank: 17.3204708099  
36523, s1: 4.920853137969971, s5: 1.527541160583496  
depth: 1, iteration: 460000, test\_RMSE: 1.1258972883224487, erank: 17.446567535  
40039, s1: 4.944221019744873, s5: 1.5412535667419434  
depth: 1, iteration: 462000, test\_RMSE: 1.125880241394043, erank: 17.5721015930  
17578, s1: 4.967533111572266, s5: 1.5549746751785278  
depth: 1, iteration: 464000, test\_RMSE: 1.1258634328842163, erank: 17.697208404  
541016, s1: 4.990802764892578, s5: 1.5686968564987183  
depth: 1, iteration: 466000, test\_RMSE: 1.1258466243743896, erank: 17.821735382  
080078, s1: 5.014117240905762, s5: 1.582427978515625  
depth: 1, iteration: 468000, test\_RMSE: 1.1258299350738525, erank: 17.945905685  
424805, s1: 5.037344455718994, s5: 1.5961593389511108  
depth: 1, iteration: 470000, test\_RMSE: 1.1258134841918945, erank: 18.069641113  
28125, s1: 5.060574531555176, s5: 1.6099164485931396  
depth: 1, iteration: 472000, test\_RMSE: 1.1257970333099365, erank: 18.192867279  
052734, s1: 5.083782196044922, s5: 1.6236523389816284  
depth: 1, iteration: 474000, test\_RMSE: 1.1257808208465576, erank: 18.315622329  
711914, s1: 5.106968879699707, s5: 1.6373995542526245  
depth: 1, iteration: 476000, test\_RMSE: 1.1257647275924683, erank: 18.437801361  
083984, s1: 5.1301045417785645, s5: 1.6511565446853638  
depth: 1, iteration: 478000, test\_RMSE: 1.125748634338379, erank: 18.5594482421  
875, s1: 5.15324592590332, s5: 1.664907693862915  
depth: 1, iteration: 480000, test\_RMSE: 1.1257327795028687, erank: 18.680490493  
774414, s1: 5.176344394683838, s5: 1.678672432899475  
depth: 1, iteration: 482000, test\_RMSE: 1.125717043876648, erank: 18.8009071350  
09766, s1: 5.199434757232666, s5: 1.6924349069595337  
depth: 1, iteration: 484000, test\_RMSE: 1.1257014274597168, erank: 18.920804977  
416992, s1: 5.2224531173706055, s5: 1.706198811531067  
depth: 1, iteration: 486000, test\_RMSE: 1.1256859302520752, erank: 19.040073394  
77539, s1: 5.245525360107422, s5: 1.7199792861938477  
depth: 1, iteration: 488000, test\_RMSE: 1.1256705522537231, erank: 19.158891677  
856445, s1: 5.268508434295654, s5: 1.733746886253357  
depth: 1, iteration: 490000, test\_RMSE: 1.125655174255371, erank: 19.2771492004  
39453, s1: 5.291469573974609, s5: 1.747503638267517  
depth: 1, iteration: 492000, test\_RMSE: 1.1256400346755981, erank: 19.395040512  
08496, s1: 5.31434965133667, s5: 1.7612969875335693  
depth: 1, iteration: 494000, test\_RMSE: 1.1256250143051147, erank: 19.512258529  
663086, s1: 5.33733606338501, s5: 1.7750794887542725  
depth: 1, iteration: 496000, test\_RMSE: 1.125610113143921, erank: 19.6290245056  
15234, s1: 5.360236644744873, s5: 1.7888623476028442  
depth: 1, iteration: 498000, test\_RMSE: 1.125595211982727, erank: 19.7451190948  
48633, s1: 5.38315486907959, s5: 1.8026338815689087  
depth: 1, iteration: 500000, test\_RMSE: 1.1255804300308228, erank: 19.860765457  
15332, s1: 5.405979633331299, s5: 1.8164324760437012  
depth: 1, iteration: 502000, test\_RMSE: 1.1255658864974976, erank: 19.975753784  
179688, s1: 5.428829669952393, s5: 1.8302083015441895  
depth: 1, iteration: 504000, test\_RMSE: 1.1255513429641724, erank: 20.090240478  
515625, s1: 5.4516167640686035, s5: 1.8439996242523193  
depth: 1, iteration: 506000, test\_RMSE: 1.1255369186401367, erank: 20.204231262  
20703, s1: 5.474364280700684, s5: 1.857789397239685  
depth: 1, iteration: 508000, test\_RMSE: 1.1255226135253906, erank: 20.317626953

125, s1: 5.497163772583008, s5: 1.8715726137161255  
depth: 1, iteration: 510000, test\_RMSE: 1.1255085468292236, erank: 20.430582046  
50879, s1: 5.519848823547363, s5: 1.8853458166122437  
depth: 1, iteration: 512000, test\_RMSE: 1.125494360923767, erank: 20.5430545806  
88477, s1: 5.54254150390625, s5: 1.8991279602050781  
depth: 1, iteration: 514000, test\_RMSE: 1.1254804134368896, erank: 20.655025482  
177734, s1: 5.565201282501221, s5: 1.9129003286361694  
depth: 1, iteration: 516000, test\_RMSE: 1.1254665851593018, erank: 20.766490936  
279297, s1: 5.587863922119141, s5: 1.9266984462738037  
depth: 1, iteration: 518000, test\_RMSE: 1.1254527568817139, erank: 20.877374649  
04785, s1: 5.6104841232299805, s5: 1.9404900074005127  
depth: 1, iteration: 520000, test\_RMSE: 1.1254390478134155, erank: 20.987688064  
575195, s1: 5.633089542388916, s5: 1.9542756080627441  
depth: 1, iteration: 522000, test\_RMSE: 1.1254254579544067, erank: 21.097425460  
81543, s1: 5.655673980712891, s5: 1.9680588245391846  
depth: 1, iteration: 524000, test\_RMSE: 1.1254119873046875, erank: 21.206624984  
74121, s1: 5.678220748901367, s5: 1.9818246364593506  
depth: 1, iteration: 526000, test\_RMSE: 1.1253985166549683, erank: 21.315284729  
003906, s1: 5.700732707977295, s5: 1.9956098794937134  
depth: 1, iteration: 528000, test\_RMSE: 1.1253852844238281, erank: 21.423376083  
374023, s1: 5.7232184410095215, s5: 2.0093908309936523  
depth: 1, iteration: 530000, test\_RMSE: 1.125372052192688, erank: 21.5309505462  
6465, s1: 5.745710372924805, s5: 2.023163080215454  
depth: 1, iteration: 532000, test\_RMSE: 1.1253589391708374, erank: 21.638134002  
685547, s1: 5.768167018890381, s5: 2.036926507949829  
depth: 1, iteration: 534000, test\_RMSE: 1.1253459453582764, erank: 21.744750976  
5625, s1: 5.790585041046143, s5: 2.050704002380371  
depth: 1, iteration: 536000, test\_RMSE: 1.1253329515457153, erank: 21.850936889  
648438, s1: 5.812992572784424, s5: 2.064473867416382  
depth: 1, iteration: 538000, test\_RMSE: 1.1253200769424438, erank: 21.956592559  
814453, s1: 5.835371971130371, s5: 2.078237533569336  
depth: 1, iteration: 540000, test\_RMSE: 1.125307321548462, erank: 22.0617866516  
11328, s1: 5.857701301574707, s5: 2.092022180557251  
depth: 1, iteration: 542000, test\_RMSE: 1.1252946853637695, erank: 22.166481018  
066406, s1: 5.880013465881348, s5: 2.1057724952697754  
depth: 1, iteration: 544000, test\_RMSE: 1.1252820491790771, erank: 22.270786285  
40039, s1: 5.902270793914795, s5: 2.119520902633667  
depth: 1, iteration: 546000, test\_RMSE: 1.1252695322036743, erank: 22.374502182  
006836, s1: 5.924544334411621, s5: 2.1332919597625732  
depth: 1, iteration: 548000, test\_RMSE: 1.1252572536468506, erank: 22.477706909  
179688, s1: 5.9468231201171875, s5: 2.147031784057617  
depth: 1, iteration: 550000, test\_RMSE: 1.1252448558807373, erank: 22.580499649  
04785, s1: 5.9690117835998535, s5: 2.1607863903045654  
depth: 1, iteration: 552000, test\_RMSE: 1.1252325773239136, erank: 22.682712554  
93164, s1: 5.991210460662842, s5: 2.1745214462280273  
depth: 1, iteration: 554000, test\_RMSE: 1.1252204179763794, erank: 22.784414291  
381836, s1: 6.013378143310547, s5: 2.188244581222534  
depth: 1, iteration: 556000, test\_RMSE: 1.1252083778381348, erank: 22.885503768  
9209, s1: 6.0355730056762695, s5: 2.202000617980957  
depth: 1, iteration: 558000, test\_RMSE: 1.1251963376998901, erank: 22.986192703  
24707, s1: 6.0576629638671875, s5: 2.2157235145568848  
depth: 1, iteration: 560000, test\_RMSE: 1.125184416770935, erank: 23.0862331390  
38086, s1: 6.079774379730225, s5: 2.2294375896453857  
depth: 1, iteration: 562000, test\_RMSE: 1.12517249584198, erank: 23.18577575683

5938, s1: 6.101870059967041, s5: 2.243189811706543  
depth: 1, iteration: 564000, test\_RMSE: 1.1251606941223145, erank: 23.284770965  
576172, s1: 6.123878002166748, s5: 2.256908655166626  
depth: 1, iteration: 566000, test\_RMSE: 1.125149130821228, erank: 23.3832283020  
01953, s1: 6.145890712738037, s5: 2.2706360816955566  
depth: 1, iteration: 568000, test\_RMSE: 1.125137448310852, erank: 23.4811859130  
85938, s1: 6.167875289916992, s5: 2.284316301345825  
depth: 1, iteration: 570000, test\_RMSE: 1.1251258850097656, erank: 23.578556060  
791016, s1: 6.1898698806762695, s5: 2.2980337142944336  
depth: 1, iteration: 572000, test\_RMSE: 1.1251144409179688, erank: 23.675457000  
732422, s1: 6.211832523345947, s5: 2.311727285385132  
depth: 1, iteration: 574000, test\_RMSE: 1.1251029968261719, erank: 23.771951675  
41504, s1: 6.233757019042969, s5: 2.3254151344299316  
depth: 1, iteration: 576000, test\_RMSE: 1.1250916719436646, erank: 23.868007659  
91211, s1: 6.255621433258057, s5: 2.339110851287842  
depth: 1, iteration: 578000, test\_RMSE: 1.1250804662704468, erank: 23.963487625  
12207, s1: 6.277537822723389, s5: 2.352813720703125  
depth: 1, iteration: 580000, test\_RMSE: 1.125069260597229, erank: 24.0585517883  
30078, s1: 6.29940938949585, s5: 2.3664839267730713  
depth: 1, iteration: 582000, test\_RMSE: 1.1250581741333008, erank: 24.153141021  
728516, s1: 6.3212127685546875, s5: 2.380176305770874  
depth: 1, iteration: 584000, test\_RMSE: 1.1250470876693726, erank: 24.247385025  
024414, s1: 6.343015193939209, s5: 2.3938422203063965  
depth: 1, iteration: 586000, test\_RMSE: 1.1250361204147339, erank: 24.341049194  
335938, s1: 6.364812850952148, s5: 2.407508373260498  
depth: 1, iteration: 588000, test\_RMSE: 1.1250252723693848, erank: 24.434341430  
664062, s1: 6.386579513549805, s5: 2.421163558959961  
depth: 1, iteration: 590000, test\_RMSE: 1.1250144243240356, erank: 24.527227401  
7334, s1: 6.408235549926758, s5: 2.434817314147949  
depth: 1, iteration: 592000, test\_RMSE: 1.1250035762786865, erank: 24.619525909  
423828, s1: 6.4300336837768555, s5: 2.4484736919403076  
depth: 1, iteration: 594000, test\_RMSE: 1.124992847442627, erank: 24.7114772796  
63086, s1: 6.451676845550537, s5: 2.4620602130889893  
depth: 1, iteration: 596000, test\_RMSE: 1.124982237815857, erank: 24.8028240203  
85742, s1: 6.473364353179932, s5: 2.4757254123687744  
depth: 1, iteration: 598000, test\_RMSE: 1.1249717473983765, erank: 24.893869400  
024414, s1: 6.49494743347168, s5: 2.4894328117370605  
depth: 1, iteration: 600000, test\_RMSE: 1.1249611377716064, erank: 24.984382629  
39453, s1: 6.5166168212890625, s5: 2.503020763397217  
depth: 1, iteration: 602000, test\_RMSE: 1.1249507665634155, erank: 25.074443817  
138672, s1: 6.538193225860596, s5: 2.5166738033294678  
depth: 1, iteration: 604000, test\_RMSE: 1.1249403953552246, erank: 25.164163589  
47754, s1: 6.559791564941406, s5: 2.530266046524048  
depth: 1, iteration: 606000, test\_RMSE: 1.1249300241470337, erank: 25.253435134  
887695, s1: 6.5812883377075195, s5: 2.543877601623535  
depth: 1, iteration: 608000, test\_RMSE: 1.1249197721481323, erank: 25.342151641  
845703, s1: 6.602846622467041, s5: 2.5574586391448975  
depth: 1, iteration: 610000, test\_RMSE: 1.124909520149231, erank: 25.4305686950  
6836, s1: 6.624356269836426, s5: 2.5710432529449463  
depth: 1, iteration: 612000, test\_RMSE: 1.1248993873596191, erank: 25.518508911  
132812, s1: 6.645777225494385, s5: 2.584649085998535  
depth: 1, iteration: 614000, test\_RMSE: 1.1248893737792969, erank: 25.606103897  
094727, s1: 6.667224884033203, s5: 2.5982017517089844  
depth: 1, iteration: 616000, test\_RMSE: 1.1248793601989746, erank: 25.693223953

24707, s1: 6.688706874847412, s5: 2.611794948577881  
depth: 1, iteration: 618000, test\_RMSE: 1.1248693466186523, erank: 25.780000686  
645508, s1: 6.710064888000488, s5: 2.6253576278686523  
depth: 1, iteration: 620000, test\_RMSE: 1.1248594522476196, erank: 25.866428375  
24414, s1: 6.731431007385254, s5: 2.6389076709747314  
depth: 1, iteration: 622000, test\_RMSE: 1.1248496770858765, erank: 25.952428817  
749023, s1: 6.752808570861816, s5: 2.6524603366851807  
depth: 1, iteration: 624000, test\_RMSE: 1.1248399019241333, erank: 26.038021087  
646484, s1: 6.77412223815918, s5: 2.6660099029541016  
depth: 1, iteration: 626000, test\_RMSE: 1.1248301267623901, erank: 26.123254776  
000977, s1: 6.795420169830322, s5: 2.679534435272217  
depth: 1, iteration: 628000, test\_RMSE: 1.1248204708099365, erank: 26.208059310  
913086, s1: 6.816690921783447, s5: 2.6930627822875977  
depth: 1, iteration: 630000, test\_RMSE: 1.1248109340667725, erank: 26.292514801  
02539, s1: 6.8379340171813965, s5: 2.7065908908843994  
depth: 1, iteration: 632000, test\_RMSE: 1.1248012781143188, erank: 26.376590728  
759766, s1: 6.8591837882995605, s5: 2.7200441360473633  
depth: 1, iteration: 634000, test\_RMSE: 1.1247917413711548, erank: 26.460336685  
180664, s1: 6.880344867706299, s5: 2.7335891723632812  
depth: 1, iteration: 636000, test\_RMSE: 1.1247823238372803, erank: 26.543521881  
103516, s1: 6.901592254638672, s5: 2.7470953464508057  
depth: 1, iteration: 638000, test\_RMSE: 1.1247729063034058, erank: 26.626489639  
282227, s1: 6.9227142333984375, s5: 2.7605764865875244  
depth: 1, iteration: 640000, test\_RMSE: 1.1247636079788208, erank: 26.708986282  
348633, s1: 6.943857669830322, s5: 2.774035930633545  
depth: 1, iteration: 642000, test\_RMSE: 1.1247544288635254, erank: 26.791254043  
5791, s1: 6.964919567108154, s5: 2.787485361099243  
depth: 1, iteration: 644000, test\_RMSE: 1.1247451305389404, erank: 26.872928619  
384766, s1: 6.986072540283203, s5: 2.8009872436523438  
depth: 1, iteration: 646000, test\_RMSE: 1.1247360706329346, erank: 26.954317092  
895508, s1: 7.007143497467041, s5: 2.8144290447235107  
depth: 1, iteration: 648000, test\_RMSE: 1.1247268915176392, erank: 27.035179138  
183594, s1: 7.028223514556885, s5: 2.827871084213257  
depth: 1, iteration: 650000, test\_RMSE: 1.1247178316116333, erank: 27.115774154  
663086, s1: 7.049198150634766, s5: 2.8413171768188477  
depth: 1, iteration: 652000, test\_RMSE: 1.1247087717056274, erank: 27.196075439  
453125, s1: 7.070096969604492, s5: 2.8547427654266357  
depth: 1, iteration: 654000, test\_RMSE: 1.1246998310089111, erank: 27.275770187  
37793, s1: 7.091127395629883, s5: 2.8681812286376953  
depth: 1, iteration: 656000, test\_RMSE: 1.1246910095214844, erank: 27.355131149  
291992, s1: 7.11205530166626, s5: 2.8815746307373047  
depth: 1, iteration: 658000, test\_RMSE: 1.1246821880340576, erank: 27.434103012  
08496, s1: 7.132980823516846, s5: 2.8949732780456543  
depth: 1, iteration: 660000, test\_RMSE: 1.1246733665466309, erank: 27.512680053  
710938, s1: 7.153851509094238, s5: 2.9084017276763916  
depth: 1, iteration: 662000, test\_RMSE: 1.124664545059204, erank: 27.5908222198  
48633, s1: 7.174755096435547, s5: 2.9217891693115234  
depth: 1, iteration: 664000, test\_RMSE: 1.124655842781067, erank: 27.6686077117  
91992, s1: 7.195571422576904, s5: 2.9351468086242676  
depth: 1, iteration: 666000, test\_RMSE: 1.1246472597122192, erank: 27.746023178  
100586, s1: 7.216407775878906, s5: 2.9485363960266113  
depth: 1, iteration: 668000, test\_RMSE: 1.1246386766433716, erank: 27.823049545  
288086, s1: 7.23723030090332, s5: 2.9619126319885254  
depth: 1, iteration: 670000, test\_RMSE: 1.124630093574524, erank: 27.8997268676

7578, s1: 7.257967948913574, s5: 2.9752535820007324  
depth: 1, iteration: 672000, test\_RMSE: 1.1246216297149658, erank: 27.975973129  
27246, s1: 7.278792858123779, s5: 2.9886269569396973  
depth: 1, iteration: 674000, test\_RMSE: 1.1246131658554077, erank: 28.051898956  
298828, s1: 7.299529552459717, s5: 3.0019609928131104  
depth: 1, iteration: 676000, test\_RMSE: 1.1246047019958496, erank: 28.127403259  
277344, s1: 7.320297718048096, s5: 3.015293836593628  
depth: 1, iteration: 678000, test\_RMSE: 1.1245964765548706, erank: 28.202564239  
501953, s1: 7.341007709503174, s5: 3.0286097526550293  
depth: 1, iteration: 680000, test\_RMSE: 1.124588131904602, erank: 28.2774028778  
07617, s1: 7.361669540405273, s5: 3.0419294834136963  
depth: 1, iteration: 682000, test\_RMSE: 1.1245797872543335, erank: 28.351867675  
78125, s1: 7.382347583770752, s5: 3.055239200592041  
depth: 1, iteration: 684000, test\_RMSE: 1.1245715618133545, erank: 28.426017761  
23047, s1: 7.402942180633545, s5: 3.068544864654541  
depth: 1, iteration: 686000, test\_RMSE: 1.124563455581665, erank: 28.4998760223  
38867, s1: 7.4235334396362305, s5: 3.0818052291870117  
depth: 1, iteration: 688000, test\_RMSE: 1.1245553493499756, erank: 28.573247909  
5459, s1: 7.444179534912109, s5: 3.095132350921631  
depth: 1, iteration: 690000, test\_RMSE: 1.1245472431182861, erank: 28.646324157  
714844, s1: 7.464696407318115, s5: 3.1083619594573975  
depth: 1, iteration: 692000, test\_RMSE: 1.1245392560958862, erank: 28.719062805  
17578, s1: 7.485263347625732, s5: 3.1216440200805664  
depth: 1, iteration: 694000, test\_RMSE: 1.1245312690734863, erank: 28.791425704  
956055, s1: 7.505812168121338, s5: 3.134882688522339  
depth: 1, iteration: 696000, test\_RMSE: 1.1245232820510864, erank: 28.863460540  
771484, s1: 7.52631139755249, s5: 3.1481621265411377  
depth: 1, iteration: 698000, test\_RMSE: 1.124515414237976, erank: 28.9350624084  
47266, s1: 7.546787738800049, s5: 3.161374092102051  
depth: 1, iteration: 700000, test\_RMSE: 1.1245075464248657, erank: 29.006332397  
460938, s1: 7.567276954650879, s5: 3.1746222972869873  
depth: 1, iteration: 702000, test\_RMSE: 1.124499797821045, erank: 29.0772819519  
04297, s1: 7.587682247161865, s5: 3.1878206729888916  
depth: 1, iteration: 704000, test\_RMSE: 1.1244920492172241, erank: 29.147893905  
63965, s1: 7.608094215393066, s5: 3.201042413711548  
depth: 1, iteration: 706000, test\_RMSE: 1.1244843006134033, erank: 29.218097686  
767578, s1: 7.628499507904053, s5: 3.2142550945281982  
depth: 1, iteration: 708000, test\_RMSE: 1.1244765520095825, erank: 29.287952423  
095703, s1: 7.648880481719971, s5: 3.2274274826049805  
depth: 1, iteration: 710000, test\_RMSE: 1.1244689226150513, erank: 29.357507705  
688477, s1: 7.669214248657227, s5: 3.240626335144043  
depth: 1, iteration: 712000, test\_RMSE: 1.1244614124298096, erank: 29.426635742  
1875, s1: 7.689565658569336, s5: 3.2537784576416016  
depth: 1, iteration: 714000, test\_RMSE: 1.1244537830352783, erank: 29.495450973  
510742, s1: 7.7098917961120605, s5: 3.2669525146484375  
depth: 1, iteration: 716000, test\_RMSE: 1.1244462728500366, erank: 29.563884735  
107422, s1: 7.730221748352051, s5: 3.2800824642181396  
depth: 1, iteration: 718000, test\_RMSE: 1.124438762664795, erank: 29.6319618225  
09766, s1: 7.750491619110107, s5: 3.2932262420654297  
depth: 1, iteration: 720000, test\_RMSE: 1.1244313716888428, erank: 29.699848175  
048828, s1: 7.770692348480225, s5: 3.3063881397247314  
depth: 1, iteration: 722000, test\_RMSE: 1.1244239807128906, erank: 29.767290115  
356445, s1: 7.7909135818481445, s5: 3.3195059299468994  
depth: 1, iteration: 724000, test\_RMSE: 1.1244165897369385, erank: 29.834512710

57129, s1: 7.811107158660889, s5: 3.3325788974761963  
depth: 1, iteration: 726000, test\_RMSE: 1.1244091987609863, erank: 29.901292800  
90332, s1: 7.831305503845215, s5: 3.345696210861206  
depth: 1, iteration: 728000, test\_RMSE: 1.1244019269943237, erank: 29.967775344  
848633, s1: 7.851471900939941, s5: 3.3587682247161865  
depth: 1, iteration: 730000, test\_RMSE: 1.1243947744369507, erank: 30.034015655  
517578, s1: 7.871580123901367, s5: 3.3718626499176025  
depth: 1, iteration: 732000, test\_RMSE: 1.124387502670288, erank: 30.0998458862  
3047, s1: 7.891739368438721, s5: 3.38493013381958  
depth: 1, iteration: 734000, test\_RMSE: 1.1243804693222046, erank: 30.165344238  
28125, s1: 7.911874771118164, s5: 3.39798641204834  
depth: 1, iteration: 736000, test\_RMSE: 1.124373197555542, erank: 30.2306518554  
6875, s1: 7.931849002838135, s5: 3.411025285720825  
depth: 1, iteration: 738000, test\_RMSE: 1.1243661642074585, erank: 30.295589447  
021484, s1: 7.951859951019287, s5: 3.4240939617156982  
depth: 1, iteration: 740000, test\_RMSE: 1.124359130859375, erank: 30.3601093292  
23633, s1: 7.97196626663208, s5: 3.4370968341827393  
depth: 1, iteration: 742000, test\_RMSE: 1.1243520975112915, erank: 30.424448013  
305664, s1: 7.991983413696289, s5: 3.4501430988311768  
depth: 1, iteration: 744000, test\_RMSE: 1.124345064163208, erank: 30.4884643554  
6875, s1: 8.011983871459961, s5: 3.463156223297119  
depth: 1, iteration: 746000, test\_RMSE: 1.124338150024414, erank: 30.5522212982  
17773, s1: 8.031923294067383, s5: 3.4761440753936768  
depth: 1, iteration: 748000, test\_RMSE: 1.1243312358856201, erank: 30.615602493  
286133, s1: 8.051898002624512, s5: 3.4891536235809326  
depth: 1, iteration: 750000, test\_RMSE: 1.1243243217468262, erank: 30.678798675  
53711, s1: 8.071761131286621, s5: 3.5021004676818848  
depth: 1, iteration: 752000, test\_RMSE: 1.1243174076080322, erank: 30.741693496  
7041, s1: 8.091611862182617, s5: 3.5150673389434814  
depth: 1, iteration: 754000, test\_RMSE: 1.1243107318878174, erank: 30.804151535  
03418, s1: 8.111534118652344, s5: 3.528048276901245  
depth: 1, iteration: 756000, test\_RMSE: 1.1243038177490234, erank: 30.866443634  
033203, s1: 8.131330490112305, s5: 3.5409841537475586  
depth: 1, iteration: 758000, test\_RMSE: 1.1242971420288086, erank: 30.928461074  
8291, s1: 8.151130676269531, s5: 3.5539348125457764  
depth: 1, iteration: 760000, test\_RMSE: 1.1242903470993042, erank: 30.989940643  
310547, s1: 8.171092987060547, s5: 3.566908836364746  
depth: 1, iteration: 762000, test\_RMSE: 1.124283790588379, erank: 31.0513858795  
166, s1: 8.190755844116211, s5: 3.5798230171203613  
depth: 1, iteration: 764000, test\_RMSE: 1.124277114868164, erank: 31.1125221252  
4414, s1: 8.210478782653809, s5: 3.5927107334136963  
depth: 1, iteration: 766000, test\_RMSE: 1.1242705583572388, erank: 31.173257827  
75879, s1: 8.230199813842773, s5: 3.6056087017059326  
depth: 1, iteration: 768000, test\_RMSE: 1.1242640018463135, erank: 31.233762741  
088867, s1: 8.249890327453613, s5: 3.6185178756713867  
depth: 1, iteration: 770000, test\_RMSE: 1.1242573261260986, erank: 31.293916702  
270508, s1: 8.269614219665527, s5: 3.631394624710083  
depth: 1, iteration: 772000, test\_RMSE: 1.124250888824463, erank: 31.3537826538  
08594, s1: 8.289316177368164, s5: 3.6442837715148926  
depth: 1, iteration: 774000, test\_RMSE: 1.1242444515228271, erank: 31.413463592  
529297, s1: 8.308931350708008, s5: 3.6571481227874756  
depth: 1, iteration: 776000, test\_RMSE: 1.1242380142211914, erank: 31.472871780  
395508, s1: 8.328526496887207, s5: 3.6699886322021484  
depth: 1, iteration: 778000, test\_RMSE: 1.1242315769195557, erank: 31.531944274



902344, s1: 8.348177909851074, s5: 3.6828339099884033  
depth: 1, iteration: 780000, test\_RMSE: 1.12422513961792, erank: 31.59074211120  
6055, s1: 8.367720603942871, s5: 3.6956698894500732  
depth: 1, iteration: 782000, test\_RMSE: 1.1242188215255737, erank: 31.649229049  
682617, s1: 8.387380599975586, s5: 3.7085185050964355  
depth: 1, iteration: 784000, test\_RMSE: 1.1242125034332275, erank: 31.707551956  
176758, s1: 8.40687084197998, s5: 3.7213332653045654  
depth: 1, iteration: 786000, test\_RMSE: 1.1242061853408813, erank: 31.765510559  
08203, s1: 8.426374435424805, s5: 3.734135627746582  
depth: 1, iteration: 788000, test\_RMSE: 1.1241999864578247, erank: 31.823259353  
637695, s1: 8.445881843566895, s5: 3.7469441890716553  
depth: 1, iteration: 790000, test\_RMSE: 1.1241936683654785, erank: 31.880760192  
871094, s1: 8.465350151062012, s5: 3.7597222328186035  
depth: 1, iteration: 792000, test\_RMSE: 1.1241875886917114, erank: 31.937906265  
25879, s1: 8.484834671020508, s5: 3.772512435913086  
depth: 1, iteration: 794000, test\_RMSE: 1.1241813898086548, erank: 31.994773864  
746094, s1: 8.504361152648926, s5: 3.7852842807769775  
depth: 1, iteration: 796000, test\_RMSE: 1.1241751909255981, erank: 32.051471710  
20508, s1: 8.523698806762695, s5: 3.798025131225586  
depth: 1, iteration: 798000, test\_RMSE: 1.124169111251831, erank: 32.1078643798  
8281, s1: 8.543113708496094, s5: 3.810781955718994

RUN: python /content/content/synth/main.py --method DLNN --data gaussian --N 10  
0 --rank 5 --reg\_norm ratio --initscale 1e-3 --sample\_size 4000 --log\_interval  
2000 --depth 1 --lam 1e-2 --optim Adam --lr 1e-3 --niters 30000  
depth: 1, iteration: 0, test\_RMSE: 1.13348388671875, erank: 80.00656127929688,  
s1: 0.01939358375966549, s5: 0.017589416354894638  
depth: 1, iteration: 2000, test\_RMSE: 1.1299279928207397, erank: 46.88607025146  
4844, s1: 16.388713836669922, s5: 9.12843132019043  
depth: 1, iteration: 4000, test\_RMSE: 1.1373224258422852, erank: 45.13441085815  
43, s1: 28.2651309967041, s5: 16.67180824279785  
depth: 1, iteration: 6000, test\_RMSE: 1.161454439163208, erank: 33.944564819335  
94, s1: 35.33620834350586, s5: 20.86817741394043  
depth: 1, iteration: 8000, test\_RMSE: 1.2263013124465942, erank: 19.56339073181  
1523, s1: 43.817752838134766, s5: 25.70183563232422  
depth: 1, iteration: 10000, test\_RMSE: 1.3281887769699097, erank: 8.02790737152  
0996, s1: 53.35487365722656, s5: 31.196672439575195  
depth: 1, iteration: 12000, test\_RMSE: 1.3776334524154663, erank: 4.96543359756  
4697, s1: 58.600799560546875, s5: 32.98215103149414  
depth: 1, iteration: 14000, test\_RMSE: 1.3782161474227905, erank: 4.92888116836  
54785, s1: 58.694461822509766, s5: 32.99470901489258  
depth: 1, iteration: 16000, test\_RMSE: 1.3782130479812622, erank: 4.92755842208  
8623, s1: 58.69486618041992, s5: 32.994720458984375  
depth: 1, iteration: 18000, test\_RMSE: 1.3782142400741577, erank: 4.92684078216  
5527, s1: 58.69489669799805, s5: 32.99480056762695  
depth: 1, iteration: 20000, test\_RMSE: 1.37821364402771, erank: 4.9282484054565  
43, s1: 58.69499969482422, s5: 32.99467468261719  
depth: 1, iteration: 22000, test\_RMSE: 1.3782159090042114, erank: 4.92764568328  
8574, s1: 58.69506072998047, s5: 32.994667053222656  
depth: 1, iteration: 24000, test\_RMSE: 1.3782117366790771, erank: 4.92663574218  
75, s1: 58.69490432739258, s5: 32.99445724487305  
depth: 1, iteration: 26000, test\_RMSE: 1.3782117366790771, erank: 4.92775011062  
6221, s1: 58.694923400878906, s5: 32.9947509765625  
depth: 1, iteration: 28000, test\_RMSE: 1.3782142400741577, erank: 4.92595005035

4004, s1: 58.69485855102539, s5: 32.99483108520508

```
In [11]: #Fetch ML-100k (safe no-op if present)
import os, urllib.request, zipfile, io, pathlib
ML_DIR = "/content/ml-100k"
if not os.path.exists(f"{ML_DIR}/u.data"):
    print("Downloading MovieLens 100k ...")
    data = urllib.request.urlopen("https://files.grouplens.org/datasets/movielens/ml-100k.zip")
    zip = zipfile.ZipFile(io.BytesIO(data)).extractall("/content")
    assert os.path.exists(f"{ML_DIR}/u.data"), "MovieLens 100k not found after download"
    print("✓ MovieLens ready.")

BASE_ML = dict(
    method="DLNN",
    data="ml-100k-sample",
    depth=1,
    optim="Adam",
    lr="5e-4", #working LR
    trainprop="0.8",
    reg_norm="ratio",
    initscale="1e-3",
    log_interval=1000
)

#λ = 0 vs 1e-3
run_and_log("ML_lam0_adam_long", **BASE_ML, lam="0.0", niters=40_000)
run_and_log("ML_lam1e-3_adam_long", **BASE_ML, lam="1e-3", niters=40_000)
```

✓ MovieLens ready.

```
RUN: python /content/content/synth/main.py --method DLNN --data ml-100k-sample
--depth 1 --optim Adam --lr 5e-4 --trainprop 0.8 --reg_norm ratio --initscale 1
e-3 --log_interval 1000 --lam 0.0 --niters 40000
depth: 1, iteration: 0, test_RMSE: 3.7128684520721436, erank: 675.819091796875,
s1: 0.06876151263713837, s5: 0.016600891947746277
depth: 1, iteration: 1000, test_RMSE: 3.7128684520721436, erank: 624.3471679687
5, s1: 66.41107940673828, s5: 15.898189544677734
depth: 1, iteration: 2000, test_RMSE: 3.7128684520721436, erank: 623.4058837890
625, s1: 128.39491271972656, s5: 30.638225555419922
depth: 1, iteration: 3000, test_RMSE: 3.7128684520721436, erank: 622.2479248046
875, s1: 186.6156463623047, s5: 44.45459747314453
depth: 1, iteration: 4000, test_RMSE: 3.7128684520721436, erank: 620.9565429687
5, s1: 241.38926696777344, s5: 57.60871505737305
depth: 1, iteration: 5000, test_RMSE: 3.7128684520721436, erank: 619.6657104492
188, s1: 292.7303466796875, s5: 70.26631927490234
depth: 1, iteration: 6000, test_RMSE: 3.7128684520721436, erank: 618.3209228515
625, s1: 340.2009582519531, s5: 82.28085327148438
depth: 1, iteration: 7000, test_RMSE: 3.7128684520721436, erank: 616.8640747070
312, s1: 383.0242919921875, s5: 93.44588470458984
depth: 1, iteration: 8000, test_RMSE: 3.7128684520721436, erank: 615.3244018554
688, s1: 420.49591064453125, s5: 103.4920425415039
depth: 1, iteration: 9000, test_RMSE: 3.7128684520721436, erank: 613.7203979492
188, s1: 451.6007995605469, s5: 112.14539337158203
depth: 1, iteration: 10000, test_RMSE: 3.7128684520721436, erank: 612.114135742
1875, s1: 475.905517578125, s5: 119.18619537353516
depth: 1, iteration: 11000, test_RMSE: 3.7128684520721436, erank: 610.703918457
0312, s1: 493.3720703125, s5: 124.4432144165039
depth: 1, iteration: 12000, test_RMSE: 3.7128684520721436, erank: 609.594909667
9688, s1: 504.42529296875, s5: 127.88113403320312
depth: 1, iteration: 13000, test_RMSE: 3.7128684520721436, erank: 608.879333496
0938, s1: 510.3301696777344, s5: 129.77371215820312
depth: 1, iteration: 14000, test_RMSE: 3.7128684520721436, erank: 608.576293945
3125, s1: 512.682373046875, s5: 130.48085021972656
depth: 1, iteration: 15000, test_RMSE: 3.7128684520721436, erank: 608.516296386
7188, s1: 513.135498046875, s5: 130.628662109375
depth: 1, iteration: 16000, test_RMSE: 3.7128684520721436, erank: 608.515991210
9375, s1: 513.149169921875, s5: 130.62303161621094
depth: 1, iteration: 17000, test_RMSE: 3.7128684520721436, erank: 608.514831542
9688, s1: 513.1483154296875, s5: 130.63018798828125
depth: 1, iteration: 18000, test_RMSE: 3.7128684520721436, erank: 608.513061523
4375, s1: 513.15771484375, s5: 130.63551330566406
depth: 1, iteration: 19000, test_RMSE: 3.7128684520721436, erank: 608.515136718
75, s1: 513.14453125, s5: 130.63031005859375
depth: 1, iteration: 20000, test_RMSE: 3.7128684520721436, erank: 608.514831542
9688, s1: 513.154541015625, s5: 130.6268768310547
depth: 1, iteration: 21000, test_RMSE: 3.7128684520721436, erank: 608.515136718
75, s1: 513.1485595703125, s5: 130.62176513671875
depth: 1, iteration: 22000, test_RMSE: 3.7128684520721436, erank: 608.514526367
1875, s1: 513.148681640625, s5: 130.63217163085938
depth: 1, iteration: 23000, test_RMSE: 3.7128684520721436, erank: 608.513977050
7812, s1: 513.1553955078125, s5: 130.6310272216797
depth: 1, iteration: 24000, test_RMSE: 3.7128684520721436, erank: 608.516296386
7188, s1: 513.1419067382812, s5: 130.6134033203125
```

depth: 1, iteration: 25000, test\_RMSE: 3.7128684520721436, erank: 608.5162963867188, s1: 513.1419067382812, s5: 130.6134033203125  
depth: 1, iteration: 26000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 27000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 28000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 29000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 30000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 31000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 32000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 33000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 34000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 35000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 36000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 37000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 38000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625  
depth: 1, iteration: 39000, test\_RMSE: 3.7128684520721436, erank: 608.515380859375, s1: 513.1487426757812, s5: 130.61676025390625

RUN: python /content/content/synth/main.py --method DLNN --data ml-100k-sample --depth 1 --optim Adam --lr 5e-4 --trainprop 0.8 --reg\_norm ratio --initscale 1e-3 --log\_interval 1000 --lam 1e-3 --niters 40000  
depth: 1, iteration: 0, test\_RMSE: 3.703817844390869, erank: 840.7400512695312, s1: 0.03829774633049965, s5: 0.03754178434610367  
depth: 1, iteration: 1000, test\_RMSE: 3.6616404056549072, erank: 492.5755920410156, s1: 74.02537536621094, s5: 16.605382919311523  
depth: 1, iteration: 2000, test\_RMSE: 3.6343634128570557, erank: 501.32574462890625, s1: 141.9091339111328, s5: 32.128509521484375  
depth: 1, iteration: 3000, test\_RMSE: 3.6053998470306396, erank: 498.4325256347656, s1: 206.66629028320312, s5: 46.96464538574219  
depth: 1, iteration: 4000, test\_RMSE: 3.570697069168091, erank: 490.08843994140625, s1: 269.34124755859375, s5: 61.4050407409668  
depth: 1, iteration: 5000, test\_RMSE: 3.526705741882324, erank: 477.32183837890625, s1: 330.79205322265625, s5: 75.61666107177734  
depth: 1, iteration: 6000, test\_RMSE: 3.46940279006958, erank: 460.18255615234375, s1: 391.6394958496094, s5: 89.64967346191406  
depth: 1, iteration: 7000, test\_RMSE: 3.3942551612854004, erank: 438.4794616699219, s1: 452.3440856933594, s5: 103.4718017578125  
depth: 1, iteration: 8000, test\_RMSE: 3.296700954437256, erank: 412.20001220703125, s1: 513.6458740234375, s5: 117.08761596679688  
depth: 1, iteration: 9000, test\_RMSE: 3.1729817390441895, erank: 381.82049560546875, s1: 576.2074584960938, s5: 130.39138793945312

depth: 1, iteration: 10000, test\_RMSE: 3.0217719078063965, erank: 348.213775634  
7656, s1: 640.8767700195312, s5: 143.31698608398438  
depth: 1, iteration: 11000, test\_RMSE: 2.845634698867798, erank: 313.0323181152  
344, s1: 708.5931396484375, s5: 155.6799774169922  
depth: 1, iteration: 12000, test\_RMSE: 2.6520071029663086, erank: 277.972595214  
84375, s1: 779.4852905273438, s5: 167.2338409423828  
depth: 1, iteration: 13000, test\_RMSE: 2.4524598121643066, erank: 245.481033325  
1953, s1: 853.2654418945312, s5: 177.8187713623047  
depth: 1, iteration: 14000, test\_RMSE: 2.2591652870178223, erank: 216.710433959  
96094, s1: 928.4568481445312, s5: 187.3521728515625  
depth: 1, iteration: 15000, test\_RMSE: 2.080876350402832, erank: 192.0294952392  
578, s1: 1003.4403076171875, s5: 195.9173583984375  
depth: 1, iteration: 16000, test\_RMSE: 1.9225038290023804, erank: 171.614852905  
27344, s1: 1076.968505859375, s5: 203.76495361328125  
depth: 1, iteration: 17000, test\_RMSE: 1.7855792045593262, erank: 155.024307250  
97656, s1: 1147.9334716796875, s5: 211.02337646484375  
depth: 1, iteration: 18000, test\_RMSE: 1.6695261001586914, erank: 141.253585815  
4297, s1: 1215.63623046875, s5: 217.72378540039062  
depth: 1, iteration: 19000, test\_RMSE: 1.5726906061172485, erank: 129.880065917  
96875, s1: 1279.745361328125, s5: 223.91879272460938  
depth: 1, iteration: 20000, test\_RMSE: 1.4926356077194214, erank: 120.296722412  
10938, s1: 1340.2816162109375, s5: 229.6568603515625  
depth: 1, iteration: 21000, test\_RMSE: 1.4266560077667236, erank: 112.251380920  
41016, s1: 1397.35546875, s5: 234.92999267578125  
depth: 1, iteration: 22000, test\_RMSE: 1.372292160987854, erank: 105.4084854125  
9766, s1: 1451.09033203125, s5: 239.8048858642578  
depth: 1, iteration: 23000, test\_RMSE: 1.3272801637649536, erank: 99.5703964233  
3984, s1: 1501.8026123046875, s5: 244.26324462890625  
depth: 1, iteration: 24000, test\_RMSE: 1.2897531986236572, erank: 94.5331573486  
3281, s1: 1549.7491455078125, s5: 248.3368682861328  
depth: 1, iteration: 25000, test\_RMSE: 1.258226752281189, erank: 90.15553283691  
406, s1: 1595.070068359375, s5: 252.0679931640625  
depth: 1, iteration: 26000, test\_RMSE: 1.2315638065338135, erank: 86.2925872802  
7344, s1: 1638.126708984375, s5: 255.44839477539062  
depth: 1, iteration: 27000, test\_RMSE: 1.2088348865509033, erank: 82.8650131225  
586, s1: 1679.1505126953125, s5: 258.4791564941406  
depth: 1, iteration: 28000, test\_RMSE: 1.189306378364563, erank: 79.80447387695  
312, s1: 1718.36767578125, s5: 261.26483154296875  
depth: 1, iteration: 29000, test\_RMSE: 1.1723880767822266, erank: 77.0820236206  
0547, s1: 1755.8427734375, s5: 263.7091369628906  
depth: 1, iteration: 30000, test\_RMSE: 1.1576611995697021, erank: 74.6286773681  
6406, s1: 1791.6536865234375, s5: 265.8998718261719  
depth: 1, iteration: 31000, test\_RMSE: 1.1447525024414062, erank: 72.4118270874  
0234, s1: 1826.0137939453125, s5: 267.876708984375  
depth: 1, iteration: 32000, test\_RMSE: 1.1333683729171753, erank: 70.4046020507  
8125, s1: 1858.9561767578125, s5: 269.5861511230469  
depth: 1, iteration: 33000, test\_RMSE: 1.1232737302780151, erank: 68.5699691772  
461, s1: 1890.73583984375, s5: 271.0729675292969  
depth: 1, iteration: 34000, test\_RMSE: 1.1142817735671997, erank: 66.8831863403  
3203, s1: 1921.355712890625, s5: 272.3211364746094  
depth: 1, iteration: 35000, test\_RMSE: 1.1062278747558594, erank: 65.3292312622  
0703, s1: 1950.9256591796875, s5: 273.40380859375  
depth: 1, iteration: 36000, test\_RMSE: 1.0989837646484375, erank: 63.8948631286  
6211, s1: 1979.4732666015625, s5: 274.29205322265625

```
depth: 1, iteration: 37000, test_RMSE: 1.0924348831176758, erank: 62.5656661987
3047, s1: 2007.2017822265625, s5: 274.9951171875
depth: 1, iteration: 38000, test_RMSE: 1.0864828824996948, erank: 61.3332443237
3047, s1: 2034.19775390625, s5: 275.5694274902344
depth: 1, iteration: 39000, test_RMSE: 1.081064224243164, erank: 60.19676208496
094, s1: 2059.987060546875, s5: 276.0526123046875
```

```
In [12]: import os, re, glob, pandas as pd, numpy as np

LOG_GLOBS = [os.path.join(LOGDIR, "*.log")]
files = sorted([p for g in LOG_GLOBS for p in glob.glob(g)])

pat = re.compile(
    r"depth:\s*(\d+).*?iteration:\s*(\d+).*?"
    r"test_RMSE:\s*([\d-0-9\.\Ee\+]+).*?erank:\s*([\d-0-9\.\Ee\+]+).*?"
    r"s1:\s*([\d-0-9\.\Ee\+]+).*?s5:\s*([\d-0-9\.\Ee\+]+)"
)

def infer_opt(name):
    n = name.lower()
    if "adam" in n: return "adam"
    if "gd" in n: return "gd"
    return "unk"

rows = []
for path in files:
    with open(path, "r", errors="ignore") as f:
        for line in f:
            m = pat.search(line)
            if not m: continue
            d,it,rmse,er,s1,s5 = m.groups()
            rows.append(dict(
                file=os.path.basename(path),
                optimizer=infer_opt(path),
                depth=int(d),
                iteration=int(it),
                test_RMSE=float(rmse),
                erank=float(er),
                s1=float(s1),
                s5=float(s5),
            ))

df = pd.DataFrame(rows).sort_values(["optimizer","depth","iteration"]).reset_i
print(f"Parsed {len(df)} rows from {len(files)} log files.")
if df.empty:
    raise RuntimeError("No rows parsed – make sure runs completed and s1/s5 ar
df.tail(10)
```

Parsed 2155 rows from 12 log files.

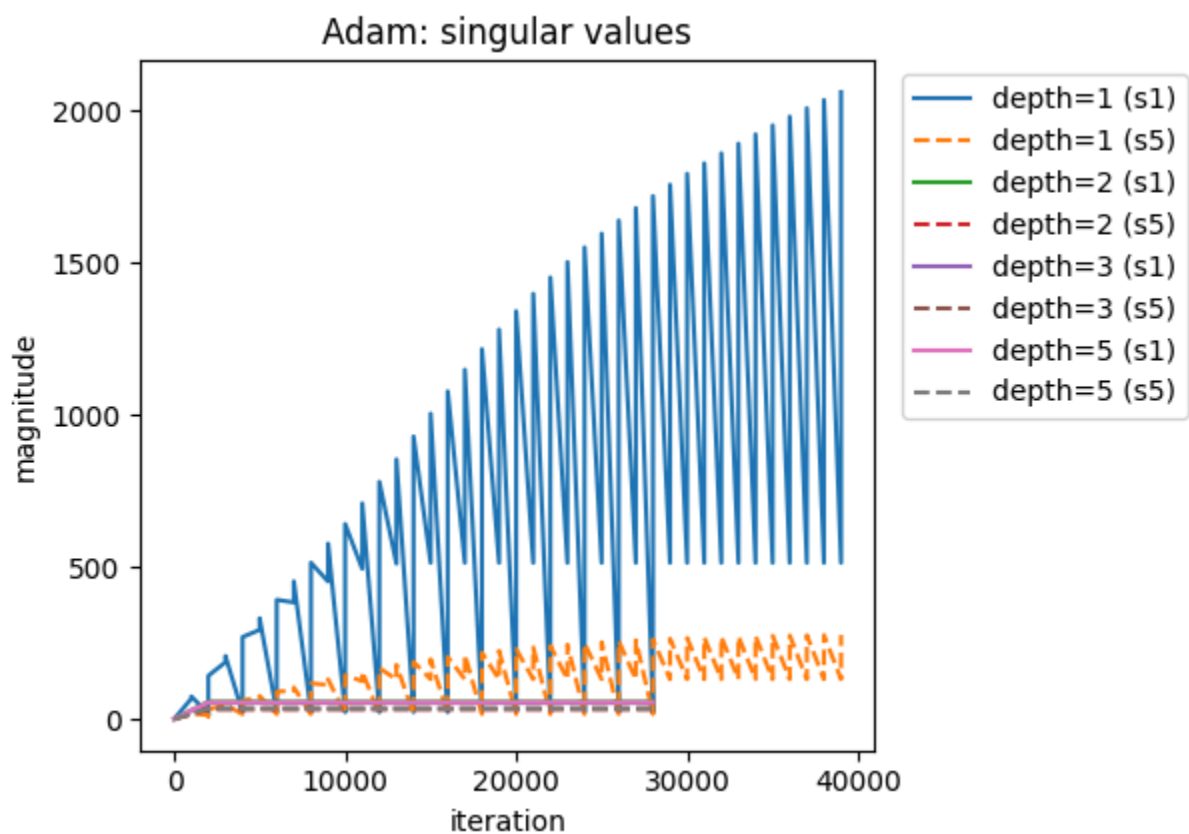
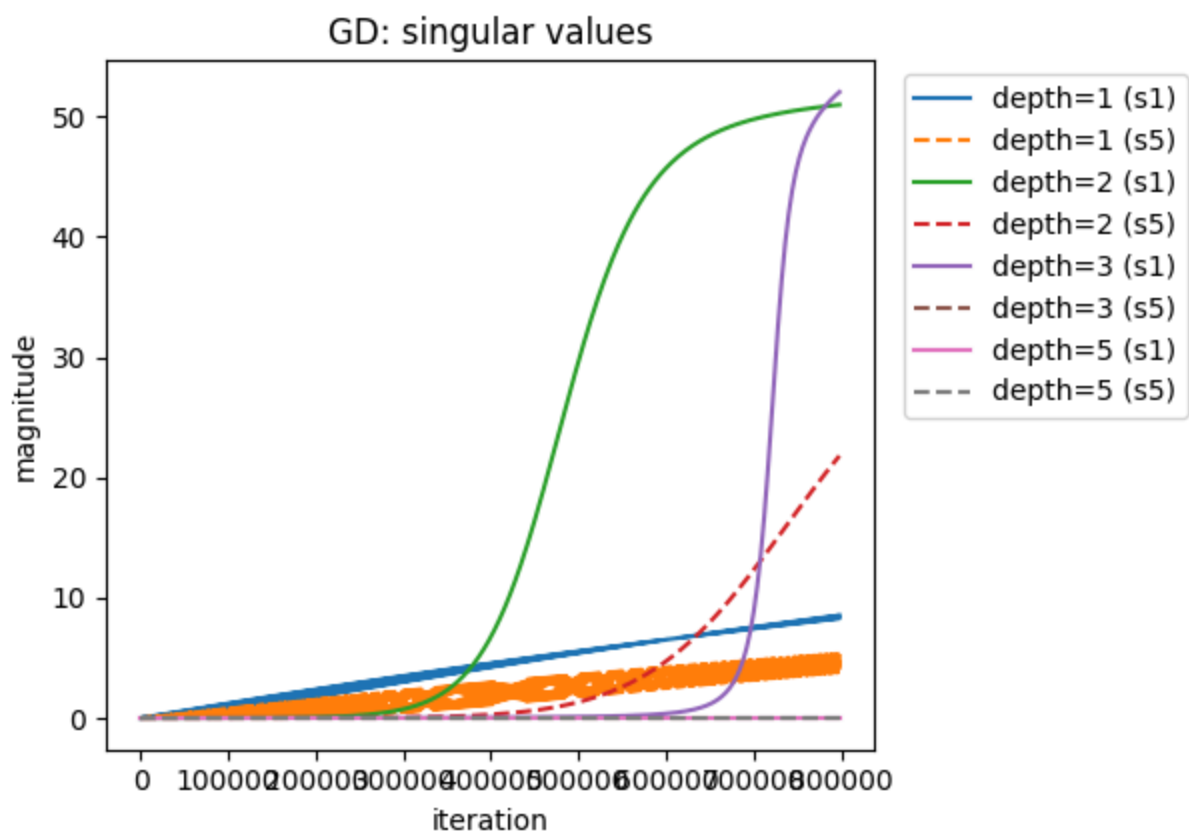
Out[12]:

	file	optimizer	depth	iteration	test_RMSE	erank	
<b>2145</b>	F1_gd_d5_lam0.log	gd	5	780000	1.119042	41.754005	0.004
<b>2146</b>	F1_gd_d5_lam0.log	gd	5	782000	1.119042	41.739948	0.004
<b>2147</b>	F1_gd_d5_lam0.log	gd	5	784000	1.119042	41.725899	0.004
<b>2148</b>	F1_gd_d5_lam0.log	gd	5	786000	1.119042	41.711735	0.004
<b>2149</b>	F1_gd_d5_lam0.log	gd	5	788000	1.119042	41.697536	0.004
<b>2150</b>	F1_gd_d5_lam0.log	gd	5	790000	1.119042	41.683300	0.004
<b>2151</b>	F1_gd_d5_lam0.log	gd	5	792000	1.119042	41.669014	0.004
<b>2152</b>	F1_gd_d5_lam0.log	gd	5	794000	1.119042	41.654690	0.004
<b>2153</b>	F1_gd_d5_lam0.log	gd	5	796000	1.119042	41.640285	0.004
<b>2154</b>	F1_gd_d5_lam0.log	gd	5	798000	1.119042	41.625851	0.004

In [13]: `import matplotlib.pyplot as plt`

```
def plot_sv_panel(opt_name, title):
    sub = df[df["optimizer"]==opt_name]
    if sub.empty: return
    plt.figure(figsize=(6.2,4.4))
    for d in sorted(sub["depth"].unique()):
        cur = sub[sub["depth"]==d]
        if cur.empty: continue
        plt.plot(cur["iteration"], cur["s1"], label=f"depth={d} (s1)")
        plt.plot(cur["iteration"], cur["s5"], linestyle="--", label=f"depth={d} (s5)")
    plt.title(title); plt.xlabel("iteration"); plt.ylabel("magnitude")
    plt.legend(bbox_to_anchor=(1.02,1), loc="upper left"); plt.tight_layout();

plot_sv_panel("gd", "GD: singular values")
plot_sv_panel("adam", "Adam: singular values")
```



```
In [14]: def plot_metric(metric, title):
plt.figure(figsize=(6.6,4.4))
```

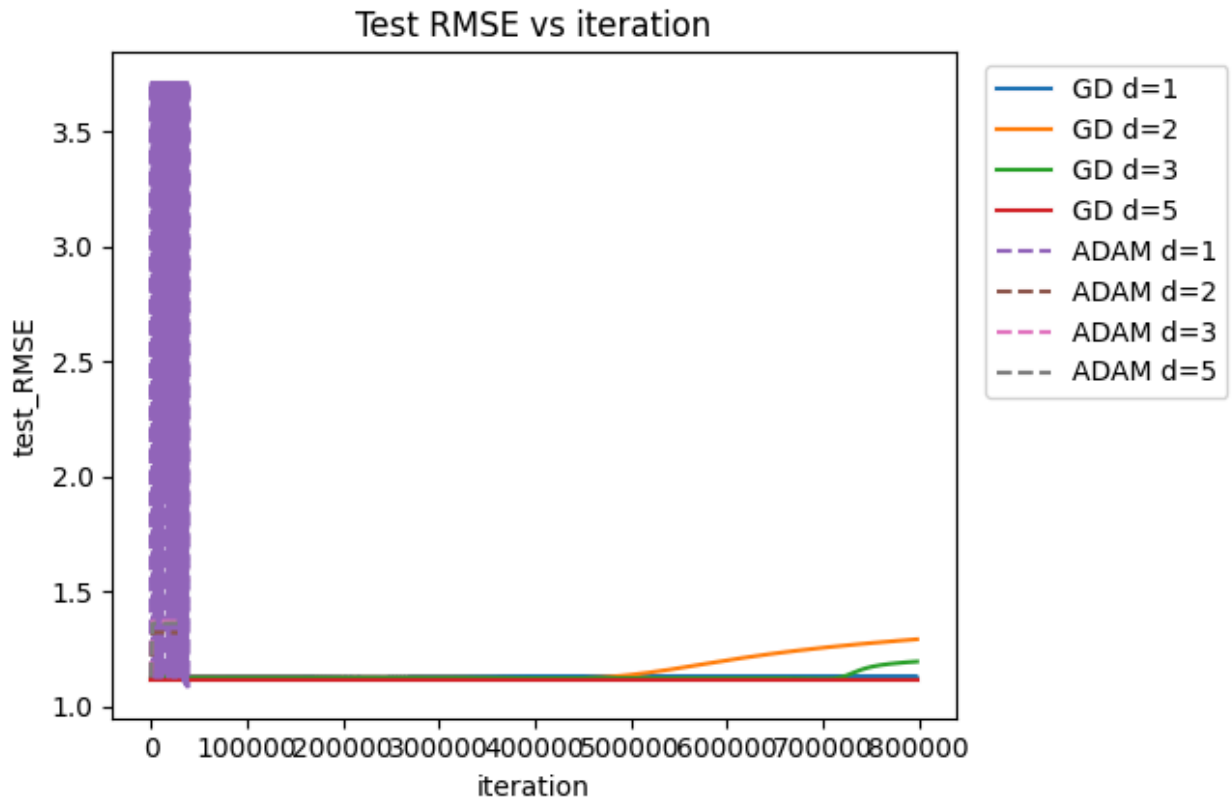


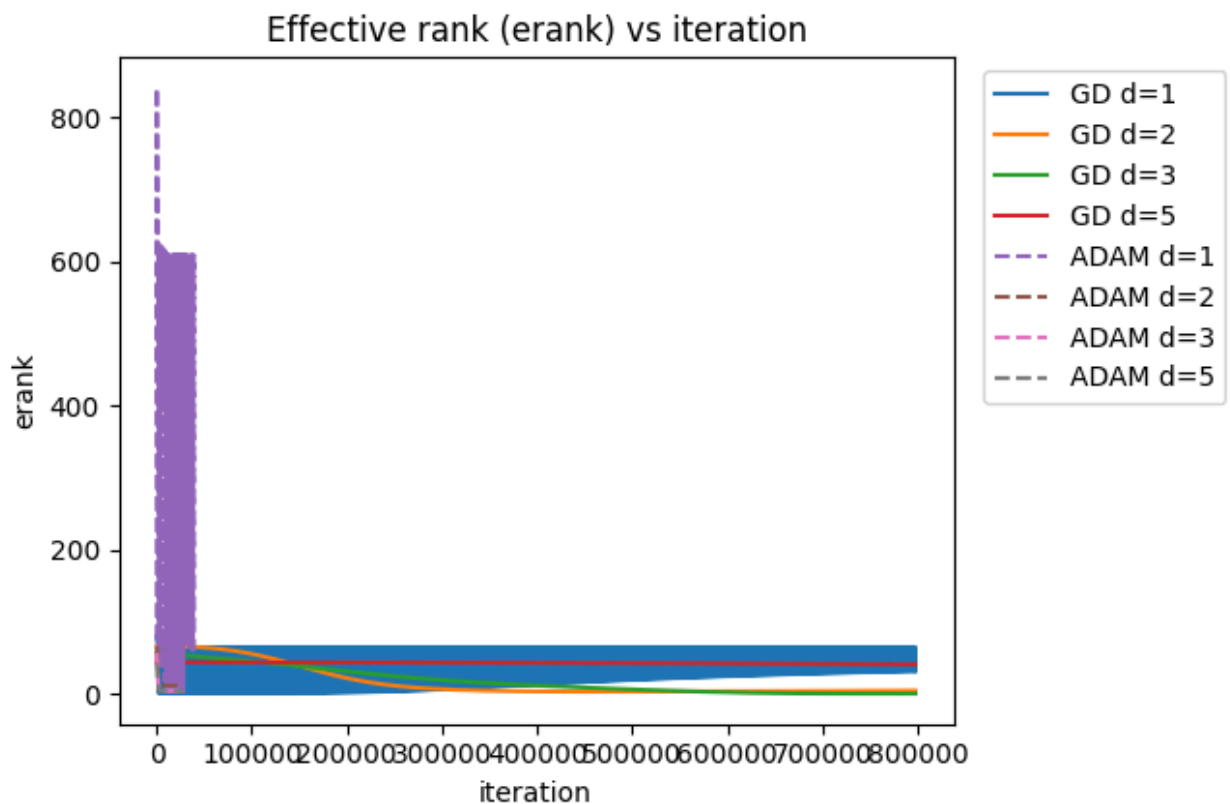
```

for opt in ("gd", "adam"):
    for d in sorted(df["depth"].unique()):
        cur = df[(df.optimizer==opt) & (df.depth==d)]
        if cur.empty: continue
        ls = "-" if opt=="gd" else "--"
        plt.plot(cur["iteration"], cur[metric], ls, label=f"{opt.upper()} {d}")
plt.xlabel("iteration"); plt.ylabel(metric); plt.title(title)
plt.legend(bbox_to_anchor=(1.02,1), loc="upper left"); plt.tight_layout();

plot_metric("test_RMSE", "Test RMSE vs iteration")
plot_metric("erank", "Effective rank (erank) vs iteration")

```





```
In [15]: ml = df[df["file"].str.contains("ML_", na=False)]
assert not ml.empty, "No MovieLens rows parsed. Run Cell 6 first."

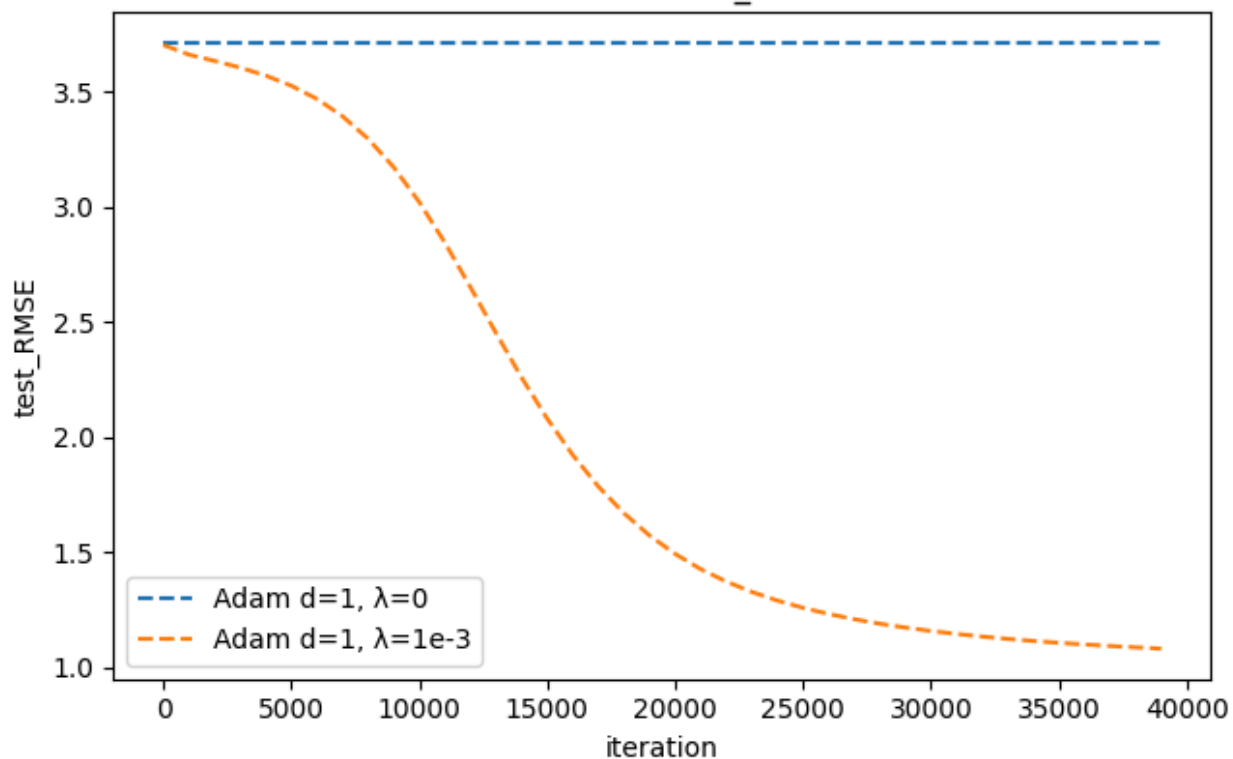
#Extract  $\lambda$  from filename for labeling
def lab(name):
    return " $\lambda=1e-3$ " if "lam1e-3" in name else " $\lambda=0$ "

def plot_ml(metric, title):
    plt.figure(figsize=(6.6,4.4))
    for key, g in ml.groupby("file"):
        g = g.sort_values("iteration")
        plt.plot(g["iteration"], g[metric], "--", label=f"Adam d=1, {lab(key)}")
    plt.xlabel("iteration"); plt.ylabel(metric); plt.title(title)
    plt.legend(); plt.tight_layout(); plt.show()

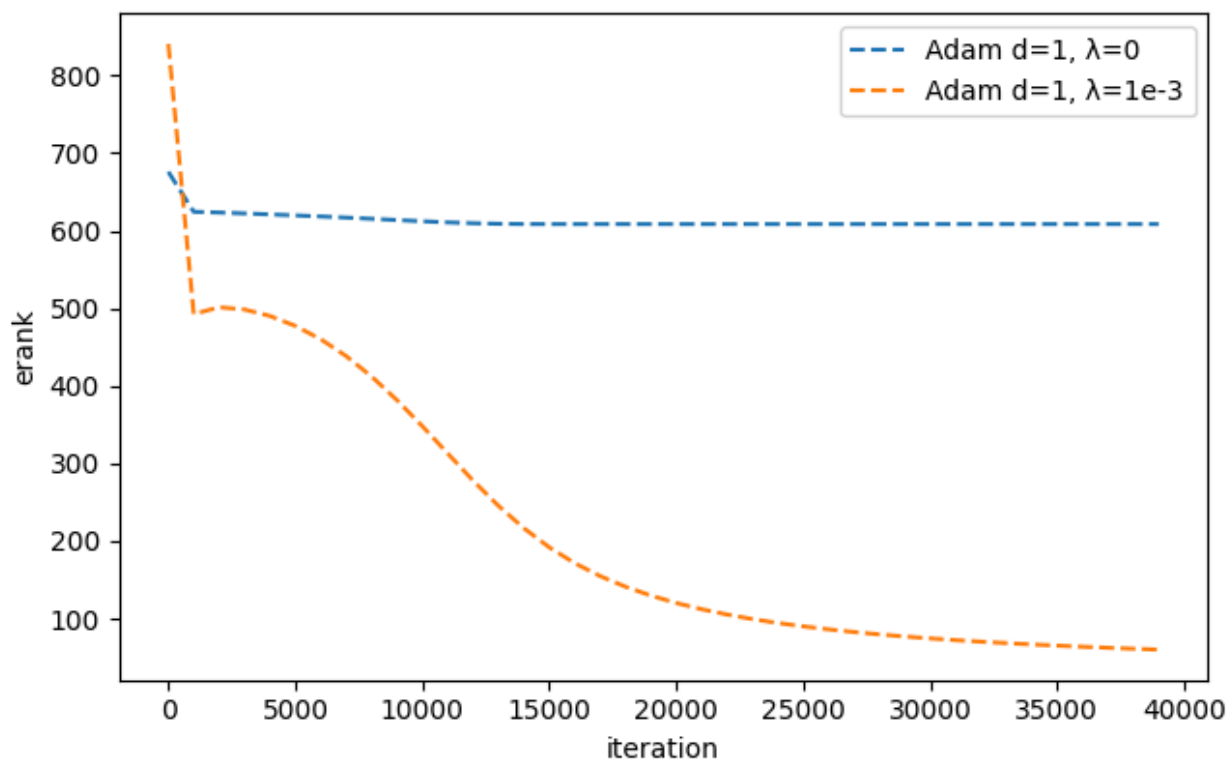
plot_ml("test_RMSE", "MovieLens: test_RMSE")
plot_ml("erank", "MovieLens: erank")

#summary table
last = (ml.sort_values(["file", "iteration"])
        .groupby("file").tail(1)
        [["file", "iteration", "test_RMSE", "erank", "s1", "s5"]])
print("=== MovieLens last metrics ===")
print(last.to_string(index=False))
```

MovieLens: test\_RMSE



MovieLens: erank



```

=== MovieLens last metrics ===
      file  iteration  test_RMSE      erank      s1      s
5  ML_lam0_adam_long.log      39000    3.712868  608.515381  513.148743  130.61676
0  ML_lam1e-3_adam_long.log      39000    1.081064   60.196762  2059.987061  276.05261
2

```

```

In [16]: last_syn = (df[~df["file"].str.contains("ML_", na=False)]
                  .sort_values(["optimizer", "depth", "iteration"])
                  .groupby(["optimizer", "depth"]).tail(1)
                  [["optimizer", "depth", "iteration", "test_RMSE", "erank", "s1", "s5"]])
print("=== Last metrics (synthetic, per optimizer & depth) ===")
print(last_syn.to_string(index=False))

```

```

=== Last metrics (synthetic, per optimizer & depth) ===
optimizer  depth  iteration  test_RMSE      erank      s1      s5
adam        1      28000    1.378214   4.925950  58.694859  32.994831
adam        2      28000    1.320843  12.232730  56.482361  31.388840
adam        3      28000    1.370288   4.952991  52.757309  35.784588
adam        5      28000    1.362176   4.940028  55.214802  33.268047
gd          1     798000    1.124169  32.107864   8.543114   3.810782
gd          2     798000    1.292061   5.181543  50.956833  21.791687
gd          3     798000    1.195019   1.039811  52.019512   0.008127
gd          5     798000    1.119042  41.625851   0.004569   0.002813

```