# HW2 Econometrics 3

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## Problem 2

Problem 2. Censoring/Truncation. Greene (2007) analyzed the default behavior and monthly behavior of a large sample of credit card users (13,444).

## (2.1)

Estimate the following model

 $\log spend = \beta_1 + \beta_2 \ln income + \beta_3 Age + \beta_4 Adepcnt + \beta 5ownrent + \varepsilon$ 

Table 1: Regression output used to answer Problem 2  $\,$ 

	Dependent variable:			
	LOGSPEND		NA	
	OLS	$censored \\ regression$	$Heckman \ selection$	
	(1)	(2)	(3)	
Ln_income	1.121***	1.117***	0.907***	
	(0.033)	(0.033)	(0.162)	
AGE	-0.015***	$-0.014^{***}$	-0.014***	
	(0.001)	(0.001)	(0.002)	
ADEPCNT	-0.027**	-0.027**	0.016	
	(0.011)	(0.011)	(0.034)	
OWNRENT	-0.203***	-0.201***	-0.281***	
	(0.030)	(0.030)	(0.065)	
logSigma		0.296***		
		(0.007)		
Constant	-3.363***	-3.340***	-1.419	
	(0.243)	(0.246)	(1.458)	
Observations	10,499	10,499	13,444	
$\mathbb{R}^2$	0.105		0.105	
Adjusted R <sup>2</sup>	0.104		0.104	
Log Likelihood		-18,012.210		
Akaike Inf. Crit.		36,036.430		
Bayesian Inf. Crit.		36,079.980		
$\rho$			-0.608	
Inverse Mills Ratio			-0.878(0.646)	
Residual Std. Error	1.330 (df = 10494)		, ,	
F Statistic	$306.358^{***}$ (df = 4; 10494)			
Note:		*p<0.1; **p<0.05; ***p<0.01		

### (2.1.a)

Using OLS. What is the effect of 10% increase in income on credit card expenditure?

• Since we are dealing with log-log we can simply multiply the paramater estimate on income by ten, which gives 11.2120776. So a 10% increase in income is estimated to increase credit card spending by 11.2120776%.

### (2.1.b)

Using Censored regression. What is the effect of 10% increase in income on credit card expenditure?

We will need to employ a Censored (Tobit) Regression and calculate the Partial Effects.

The general formulation for the Tobit Model (Greene 7th. ed., pg 848):

$$\begin{aligned} {y_i}^* &= {x_i}'\beta + \varepsilon_i \\ y_i &= 0 \\ {y_i} &= {y_i}^* \end{aligned} & \text{if } {y_i}^* \leqslant 0 \\ \text{if } {y_i}^* \geqslant 0 \end{aligned}$$

The proper Partial Effects formula:

$$\frac{\partial E[y|x]}{\partial x} = \beta \Pr{ob[a < y^* < b]}$$

Where I compute the partial effect at each observation and then compute the mean.

The parginal effect of Ln\_income on LOGSPEND is 1.1169911. Therefore, a 10% increase of income is estimated to increase credit card spending by 11.169911.

#### (2.1.c)

Using Heckman Two-Step Estimator. What the is effect of 10% increase in income on credit card expenditure?