

✳ 3.4 Equivalence Relations

• Equivalence Relation

◦ Def: Relations that are reflexive, symmetric, transitive

→ on Set A , $R \subset A \times A$ is "

ex) $A = \{1, 2, 3\}$ on Relation R ($x, y \in R$, $x \leq y$)

① Reflexive: \circ (R have $(1, 1), (2, 2), (3, 3)$)

② Symmetric: \times (R doesn't have $(2, 1), (3, 2)$)

③ transitive: \circ

⇒ R is not equivalence relation.

◦ features

□ The whole is partitioned into non-empty classes with no common-parts.

• Partition and equivalence class Subsets.

◦ Def: Set $\{S_1, S_2, \dots, S_n\}$ of a set S that is not empty satisfied the following three conditions.

① Each elements of S belongs to only one S_m .

② $S = S_1 \cup S_2 \cup \dots \cup S_n$

③ $i \neq j, S_i \cap S_j = \emptyset$

⇒ Let R be an equivalence relation on a set X .

For each $a \in X$, let $[a] = \{x \in X \mid x R a\}$.

Then $S = \{[a] \mid a \in X\}$ is a partition of X

 Equivalence classes of X given by the Relation R