

From all dwarfs, we can expect four groups of answers and assign them symbols:

- Green hats always telling truth – *green*
- Orange hats starting with answering the 1st question with a lie, therefore telling truth to the 2nd question and lying to the 3rd – *orange_{oddLie}*
- Orange hats starting with truth – opposite of the last group, truth to 1st and 3rd question and lie to 2nd question – *orange_{evenLie}*
- Red hats always lying – *red*

Graphically, we can represent them in a table of truth, which can be applied to any set of questions:

| Answers | <i>green</i> | <i>orange_{oddLie}</i> | <i>orange_{evenLie}</i> | <i>red</i> |
|-----------------|---------------------|---------------------------------------|--|-------------------|
| 1 st | Truth | Lie | Truth | Lie |
| 2 nd | Truth | Truth | Lie | Lie |
| 3 rd | Truth | Lie | Truth | Lie |

To build our system of equations, we can combine the table of truth with actual questions and answers:

| Question | <i>green</i> | <i>orange_{oddLie}</i> | <i>orange_{evenLie}</i> | <i>red</i> |
|-----------------|---------------------|---------------------------------------|--|-------------------|
| Green hat? | Positive | Positive | Negative | Positive |
| Orange hat? | Negative | Positive | Negative | Positive |
| Red hat? | Negative | Positive | Negative | Negative |

Now we can easily transpose the table to equations where the known number of positive answers is combined with proper addends:

$$\begin{cases} green + orange_{oddLie} + red = 34 \\ orange_{oddLie} + red = 26 \\ orange_{oddLie} = 11 \end{cases}$$

Last equation would be the sum of all dwarfs:

$$green + orange_{oddLie} + orange_{evenLie} + red = 43$$

Final system:

$$\begin{cases} green + orange_{oddLie} + orange_{evenLie} + red = 43 \\ green + orange_{oddLie} + red = 34 \\ orange_{oddLie} + red = 26 \\ orange_{oddLie} = 11 \end{cases}$$

The results are:

$$\begin{cases} green = 8 \\ orange_{oddLie} = 11 \\ orange_{evenLie} = 9 \\ red = 15 \end{cases}$$

So, the answer is: 20 dwarfs with orange hats attended the party