

Problem 1:

In this problem will test the engagement rate hypothesizes provided by the teacher for both knowledgeable and non-knowledgeable students. We will use hypothesis testing in order to challenge the given null hypothesizes of the teacher.

```
In [2]: import numpy as np
import matplotlib.pyplot
import scipy.stats as stats
from scipy.stats import ttest_1samp
from scipy.stats import norm
```

Q1:

Null hypothesis: The mean engagement of knowledgeable students who is = 0.75

Alternative hypothesis $H(1)$: The mean engagement of knowledgeable students is $\neq 0.75$

Therefore, we will be using hypothesis testing for a sample of size larger than 30.

```
In [3]: know_file = open('engagement_1.txt')
data1 = know_file.readlines()
data1 = [float(x) for x in data1]

nonknow_file = open('engagement_0.txt')
data0 = nonknow_file.readlines()
data0 = [float(x) for x in data0]
```

For data1 (knowledgeable student engagment data):

Q2:

```
In [4]: null_hyp1 = 0.75 #Null Hypothesis

n = len(data1) # data size
print("Knowledgeable engaged student data size: {}".format(n))

mean1 = np.mean(data1) # data mean
print("Knowledgeable engaged student sample Mean: {}".format(mean1))

std1 = np.std(data1, ddof=1) # sample std
print("Knowledgeable engaged student data Stander Deviation: {}".format(std1))

SE1 = std1/(n ** (0.5))
print("Knowledgeable engaged student data Stander Error: {}".format(SE1))

z1 = (mean1 - null_hyp1)/(std1/(n ** (0.5))) #stander-score
print("Knowledgeable engaged student data Stander Score: {}".format(z1))

p1 = 2 * stats.norm.cdf(-abs(z1))
# or (same result)
p1 = ttest_1samp(data1, null_hyp1)[1]
print("Knowledgeable engaged student p-value: {}".format(p1))

Knowledgeable engaged student data size: 937

Knowledgeable engaged student sample Mean: 0.7430304110448239

Knowledgeable engaged student data Stander Deviation: 0.12712605795317614

Knowledgeable engaged student data Stander Error: 0.004153027288269652

Knowledgeable engaged student data Stander Score: -1.6781948375012814

Knowledgeable engaged student p-value: 0.09364288349711912
```

```
In [6]: if p1 < 0.1:      # alpha value is 0.01
        print("Therefore, we reject the null hypothesis for 90% confidence interval")
        print("and p-value is not significant\n")

    else:
        print("Therefore, we accept the null hypothesis for 90% confidence interval")
        print("and p-value is significant\n")

    if p1 < 0.05:      # alpha value is 0.05
        print("Also, we reject the null hypothesis for 95% confidence interval")
        print("and p-value is not significant\n")
    else:
        print("Also, we accept the null hypothesis for 95% confidence interval")
        print("and p-value is significant\n")

    if p1 < 0.01:      # alpha value is 0.01
        print("Therefore, we reject the null hypothesis for 99% confidence interval")
        print("and p-value is not significant\n")
    else:
        print("Also, we accept the null hypothesis for 99% confidence interval")
        print("and p-value is significant\n")
```

Therefore, we reject the null hypothesis for 90% confidence interval and p-value is not significant

Also, we accept the null hypothesis for 95% confidence interval and p-value is significant

Also, we accept the null hypothesis for 99% confidence interval and p-value is significant

Q3:

For 95% confidance intervale The largest stander error, and the corresponding mimimum sample size, are as follows:

```
In [35]: alphas = 0.05 # significant level of 0.05
stdr_alphas = norm.ppf(alphas) # stander score at the given level
SE_alphas = (mean1 - null_hyp1) / stdr_alphas
print("At significant at a level of 0.05 \n\nThe largest standart error is:",SE_alphas)
size_alphas = (std1 / SE_alphas) ** 2
print("The minimum sample size is",int(size_alphas))

At significant at a level of 0.05
The largest standart error is: 0.004237209220916103
The minimum sample size is 900
```

Q4:

This question requires us to compare two datasets. We will work on comparing the statical results of the null hypothesis $H(0)$ which should be the same. On the other hand, the alternative hypothesis $H(1)$ will have different statical results.

Therefore, in this part we will use hypothesis testing since the sample size is larger than 30, as follows:

```
In [37]: null_hyp0 = 0.75 #Null Hypothesis

n0 = len(data0) # data size
print("Non Knowledgeable engaged student data size: {}".format(n0))

mean0 = np.mean(data0) # data mean
print("Non Knowledgeable engaged student sample Mean: {}".format(mean0))

std0 = np.std(data0, ddof=1) # sample std
print("Non Knowledgeable engaged student data Stander Deviation: {}".format(std0))

SE0 = std0/(n0 ** (0.5))
print("Non Knowledgeable engaged student data Stander Error: {}".format(SE0))

z0 = (mean0 - null_hyp0)/(std0/(n0 ** (0.5))) #stander-score
print("Non Knowledgeable engaged student data Stander Score: {}".format(z0))

p0 = 2 * stats.norm.cdf(-abs(z0))
# or (same result)
p0 = ttest_1samp(data0, null_hyp0)[1]
print("Non Knowledgeable engaged student p-value: {}".format(p0))

Non Knowledgeable engaged student data size: 1977

Non Knowledgeable engaged student sample Mean: 0.6399545077035914

Non Knowledgeable engaged student data Stander Deviation: 0.2541527210309046

Non Knowledgeable engaged student data Stander Error: 0.005715989588773277

Non Knowledgeable engaged student data Stander Score: -19.252220562568542

Non Knowledgeable engaged student p-value: 7.73562183240184e-76
```

```
In [38]: if p0 < 0.1:      # alpha value is 0.01
        print("Therefore, we reject the null hypothesis for 90% confidence interval")
        print("and p-value is not significant\n")

    else:
        print("Therefore, we accept the null hypothesis for 90% confidence interval")
        print("and p-value is significant\n")

    if p0 < 0.05:      # alpha value is 0.05
        print("Also, we reject the null hypothesis for 95% confidence interval")
        print("and p-value is not significant\n")
    else:
        print("Also, we accept the null hypothesis for 95% confidence interval")
        print("and p-value is significant\n")

    if p0 < 0.01:      # alpha value is 0.01
        print("Therefore, we reject the null hypothesis for 99% confidence interval")
        print("and p-value is not significant\n")
    else:
        print("Also, we accept the null hypothesis for 99% confidence interval")
        print("and p-value is significant\n")
```

Therefore, we reject the null hypothesis for 90% confidence interval and p-value is not significant

Also, we reject the null hypothesis for 95% confidence interval and p-value is not significant

Therefore, we reject the null hypothesis for 99% confidence interval and p-value is not significant

As the result, showed for each statical result the results are different. Then, the Alternative Hypothesis $H(1)$ takes place.

Q5:

Now we will combine the data and work to find the needed statistical results through hypothesis testing, as follows:

```
In [40]: null_hyp0 = 0.75 #Null Hypothesis

data = data1 + data0
n2 = len(data) # data size
print("Non Knowledgeable engaged student data size: {}".format(n2))

mean2 = np.mean(data) # data mean
print("Non Knowledgeable engaged student sample Mean: {}".format(mean2))

std2 = np.std(data, ddof=1) # sample std
print("Non Knowledgeable engaged student data Stander Deviation: {}".format(std2))

SE2 = std2/(n2 ** (0.5))
print("Non Knowledgeable engaged student data Stander Error: {}".format(SE2))

z2 = (mean2 - null_hyp0)/(std2/(n2 ** (0.5))) #stander-score
print("Non Knowledgeable engaged student data Stander Score: {}".format(z2))

p2 = 2 * stats.norm.cdf(-abs(z2))
# or (same result)
p2 = ttest_1samp(data, null_hyp0)[1]
print("Non Knowledgeable engaged student p-value: {}".format(p2))

Non Knowledgeable engaged student data size: 2914

Non Knowledgeable engaged student sample Mean: 0.673098681152711

Non Knowledgeable engaged student data Stander Deviation: 0.22655636936811666

Non Knowledgeable engaged student data Stander Error: 0.004196927844172565

Non Knowledgeable engaged student data Stander Score: -18.323240642334728

Non Knowledgeable engaged student p-value: 4.572608981610918e-71
```

Thus, the p-value is significant for all levels: 0.1, 0.05, 0.01

```
In [43]: know_file.close()
nonknow_file.close()
```