# Adv. Functional Programming: Assignment 1 Pure Functional Programming Card Games

Due: April 11, 2018

In these exercises, you will learn how to use functional programming to model the basic parts of a blackjack game.

# 1 Playing Cards (40 points)

Blackjack is a game that uses a standard deck of playing cards. Every playing card has one of four *suits*: hearts  $(\heartsuit)$ , diamonds  $(\diamondsuit)$ , clubs  $(\clubsuit)$ , or spades  $(\clubsuit)$ . In addition, each card comes in one of the following *ranks*:

- An ace (A).
- A numbered card, which has a number between 2 and 10 (inclusive).
- A face card, which has the face of one of the three royalty: king (K), queen (Q), or jack (J).

Some example playing cards are the ace of spades  $(A\spadesuit)$ , the five of clubs  $(5\clubsuit)$ , and the jack of hearts  $(J\heartsuit)$ .

Exercise 1.1 (10 points). Define some data types for representing playing cards. First, define a data type Suit that enumerates the four possible suits, and a data type Royalty that enumerates the three possible faces of royalty. Using Suit and Royalty, define a data type Card that represents each of the above three varieties (aces, numbers, and faces) of playing cards. In the case of a numbered card, the number can be represented as an Int.

**Exercise 1.2** (5 points). Both a deck of cards and a hand of cards can be represented as a list of cards. Define type synonyms **Deck** and **Hand** for lists of cards.

Exercise 1.3 (5 points). Derive an Eq instance for Suit, Royalty, and Card using the automated deriving mechanism. Likewise, derive an Enum instance for Suit and Royalty.

Exercise 1.4 (10 points). The Show type class informs Haskell how to render the values of a type as Strings using the associated function

```
show :: Show a => a -> String
```

The Enum type class informs Haskell how to enumerate through the values of a type, as used in a list enumeration like [1..10].

Manually define **Show** instances for **Suit**, **Royalty** and **Card**. **showing** a suit and royalty value should return the following string representations:

- heart:  $\heartsuit$
- diamond: ♦
- club: 🌲
- spade: •
- king: K
- queen: Q
- jack: J

showing a card should display a string signifying its rank immediately followed by the string signifying its suit. The string representations of ranks should be:

- ace: A
- number n: the string representation of the Int n
- face r: the string representation of the Royalty r

For example, a 10 of spades should be shown as "10 $\spadesuit$ " and a queen of diamonds should be shown as "Q $\diamondsuit$ ".

*Hint* 1.1. The unicode codes for characters corresponding to the card suits are (in hexadecimal):

- ♥: 2661
- \$: 2662
- ♣: 2663
- **\( \phi**: 2660

Hexadecimal unicode codes can be used in Haskell strings by escaping them with xn, where n is the code. For example, the string "x2660" corresponds to " $^*$ ".

Exercise 1.5 (10 points). Define the lists suits::[Suit], faces::[Royalty], and numbers::[Int] containing all suit, face, and valid numeric card values. Use these lists to create a full deck, fullDeck :: Deck, containing all playing cards: an ace for every suit, a numeric card for every suit and number between 2 and 10, and a face card for every suit and face. The order of fullDeck does not matter.

### 2 410: Simple Blackjack Scoring (20 points)

In the game of blackjack, each player's hand is given a numeric score and the goal is draw cards and achieve the highest score without going over 21. A hand with a score over 21 is called a "bust" is an automatic loss. Otherwise, when comparing two non-busted, the hand with the higher score wins.

Exercise 2.1 (10 points). Simplifying the rules of blackjack, each card can be assigned the following numeric score value based on its rank:

• ace: 11

• any face card: 10

• a numeric card n: the same n as its number

A card's suit does not affect its score. Define a function

```
cardValue :: Card -> Int
```

for calculating the numeric score value of a **Card** according to the above simplified rules.

Exercise 2.2 (10 points). Define a function

```
handValue :: Hand -> Int
```

for calculating the total score of a <code>Hand</code> by summing up the value of each card in the hand. For example, the value of an empty hand is 0, the value of a hand with exactly one card c is <code>cardValue</code> c, the value of a hand with two cards c and d is <code>cardValue</code> c + <code>cardValue</code> d and so on.

Bonus Exercise 2.1 (10 extra credit). Implement the full blackjack scoring rules, as described next in section 3, which supersedes the above simplified rules.

# 3 510: Full Blackjack Scoring (30 points)

In the full rules of blackjack, some scores are "soft," meaning that they can be lowered to avoid a bust. In particular, an ace is valued at *either* 11 or 1, depending on which results in the better, non-busted score. A score which cannot be lowered any more is "hard." For example, the hand  $A \spadesuit 4 \heartsuit$  has the soft score of 15 by valuing the ace as 11. Drawing an additional card to get the hand  $7 \clubsuit A \spadesuit 5 \heartsuit$  has the hard score of 13 by valuing the ace as 1, since valuing the ace as 11 would lead to the busted score 23.

**Exercise 3.1** (10 points). Define a **Score** data type that keeps separate track of soft parts of a score (which can be removed) and hard parts of the score (which are mandatory and cannot be removed). Define the functions

```
scoreValue :: Score -> Int
```

that calculate the total numeric value (including both the soft and hard parts) of the Score.

Define a function

```
improveScore :: Score -> Score
```

that "improves" a **Score** by lowering/eliminating soft scores to avoid a bust. improveScore should return either the **Score** with the highest value (according to scoreValue) that is less than or equal to 21 if possible, or otherwise the lowest possible busted score.

Exercise 3.2 (10 points). The Haskell type class Monoid defined as

```
class Monoid a where
  mempty :: a
  mappend :: a -> a -> a
  mconcat :: [a] -> a
  mconcat [] = mempty
  mconcat (x:xs) = mappend x mconcat xs
```

describes an interface for types that can be summed together. An example instance of Monoid is lists, where mempty is the empty list and mappend is list append as follows:

```
instance Monoid [a] where
  mempty = []
  mappend xs ys = xs ++ ys
```

Other examples of Monoid instances are numeric sums (where mempty is 0 and mappend is addition) and products (where mempty is 1 and mappend is multiplication). Many more instances can be found in the Data.Monoid module from the standard library.

Define a Monoid instance for Score by implementing mempty and mappend so they can be added together with mappend. As a guide, your Monoid Score instance should obey the following equalities (note, `mappend` means the mappend function used as an infix operator like +)

```
mempty `mappend` x == x
x `mappend` mempty == x
(x `mappend` y) `mappend` z == x `mappend` (y `mappend` z)
for any Scores x, y, and z.
```

Exercise 3.3 (10 points). Define the functions

```
cardScore :: Card -> Score
handScore :: Hand -> Score
```

for calculating the **Score** of an individual **Card** and the total **Score** of a **Hand**. Note that the score of an ace should include both a soft part (contributing a value of 10) and a hard part (contributing a value of 1), whereas all other cards only have a hard score value.

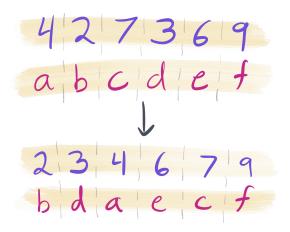
Define a function

#### handValue :: Hand -> Int

that calculates the value of a hand by first calculating its (potentially soft) **Score**, improving that **Score** to avoid a bust when possible, and then calculating the numeric value of the improved **Score**.

### 4 Deck Shuffling (30 points)

Of course, before playing a game, the deck of cards should be shuffled. One straightforward way to shuffle a deck is to sort the deck based on a random ordering. For example, consider the following illustration wherein two lists are rearranged pairwise by sorting:



At first, the purple list of numbers is in some "random" order, whereas the red list of letters is in order. After sorting the two lists pairwise, the purple numbers are put into ascending order, which forces the red letters into a "random" order.

Exercise 4.1 (5 points). Define a polymorphic data type Indexed i a which pairs together an item a with an index i. Derive a Show type class instance for this data type.

Exercise 4.2 (10 points). The Ord a type class specifies how values of a type a can be ordered relative to one another. Ord a includes many ordering operations (<, >, etc.) that are all derivable from the compare function

compare :: Ord a => a -> a -> Ordering

The Ordering type is an enumeration of the values LT (for "less than"), EQ (for "equal"), and GT (for "greater than"). To define an instance of Ord, only the compare function needs to be implemented.

Manually define an Ord (Indexed i a) which depends on Ord i by implementing the compare function for Indexed i a. Only the index part (of type i) of the Indexed i a value should be considered for the purposes of compareison, and the item part (of type a) should be completely ignored. Additionally, define an Eq (Indexed i a) instance by implementing the (==) function in a way that similarly only compares indexes for equality and ignores the item.

Exercise 4.3 (15 points). Define a shuffling function

```
shuffle :: [Int] -> [a] -> [a]
```

that permutes the given list [a] according to the "random" list of indexes [Int]. The shuffle function should

- 1. combine together each **Int** and **a**, pairwise, from the input lists to produce a list of **Indexed Int a**,
- 2. sort the list of Indexed Int a (according to the Ord (Indexed Int a) instance ordering) from step 1, and
- 3. return a list of as obtained from the items of the list from step 2.

For example,

```
shuffle [4, 2, 7, 3, 6, 9] "abcdef" == "bdaecf"
```

Hint 4.1. The list sorting function

```
sort :: Ord a => [a] -> [a]
```

can be found in the standard Data.List module included with GHC.