

Generating Uniform and Gradient 2D Lattices

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Abstract

One tissue regeneration, the geometry of bone scaffolds plays a crucial role. The mechanical strength of the scaffold is determined by this architecture, especially the pore size and form. The comparable model of the trabecular structure consisted of repeatable unit cells arranged in layers to fill the volume of the chosen scaffold. Cubic, triangular, and hexagonal polyhedral are among the three common unit cell structures studied. The use of porous cellular structures will provide mechanical and biological conditions closer to the host bone in the engineering of bone tissue. In this minor project we are discussing about: generating uniform and gradient 2D lattices and image-based uniform and gradient porous scaffold. First of all we will discuss about the bone and it's anatomy, scaffold and the designing of scaffold, spatially variant lattice and gradient, what are the materials used to design a porous scaffold and then code and the result. At the end we will discuss about the overall result, current challenges and progress and limitations.

Keywords-Bone scaffold, spatially variant lattice, Gradient, Meta material, Photonic material

1 Introduction

1.1 Bone and it's anatomy

A bone is a rigid organ that constitutes part of the vertebrate skeleton in animals. The part of the bone's organic connective tissue makes it resilient and the bone can thus afford resistance to tensile forces. A layer of connective tissue called the periosteum is composed of the outside of the long bone. The inner portion of the long bone is the medullary cavity, consisting (in adults) of yellow marrow with the inner center of the bone cavity. The long-bones are tubular in shape, such as the femur and tibia, and consist of following terms [1].

- Diaphysis: At the central part of Bone there's a rod like structure i.e. shaft of bone which is called Diaphysis.
- Epiphysis: The rounded plate like structure which is present at both the end i.e. the top and bottom of Bone is known as Epiphysis.
- Metaphysis: The cartilage which is sandwiched between epiphysis and the diaphysis known as Metaphysis.
- Epiphysical line: At complete growth of bone, A line is visible which is called Epiphysicanl line.

For better visualization all we can say is that Bone is basically a dumbbell kind of structure.

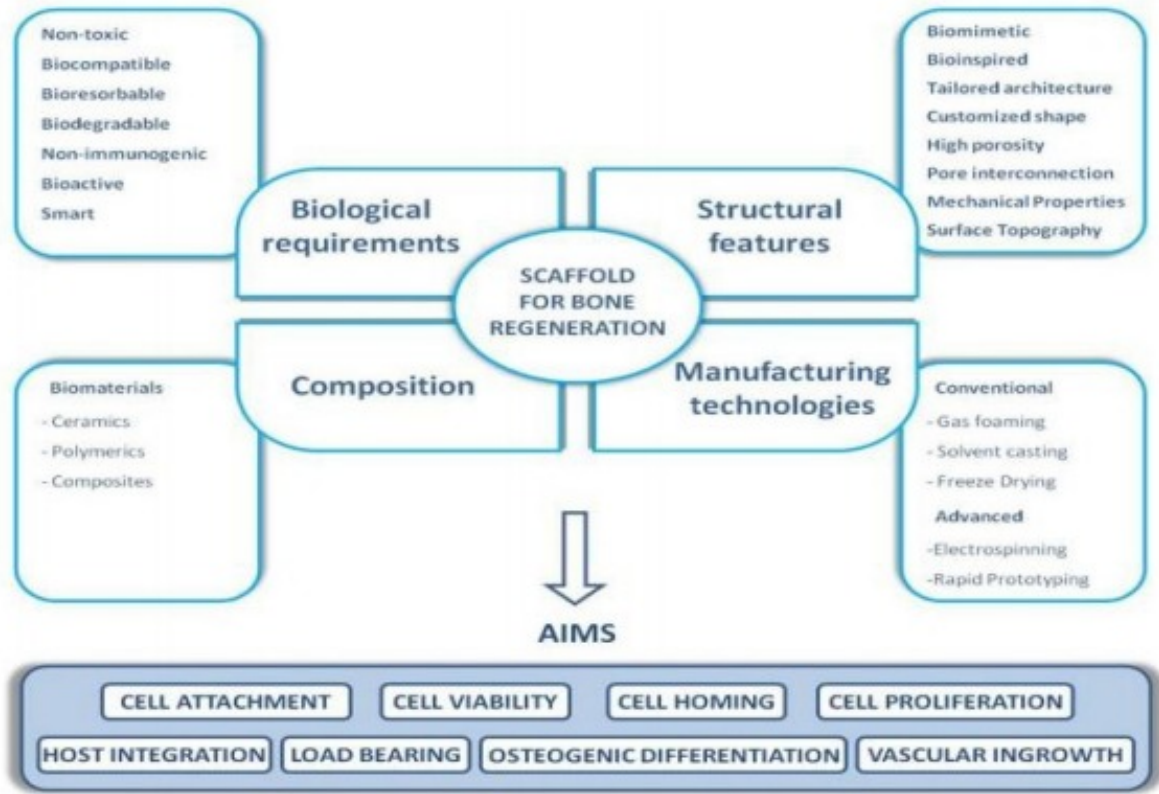


Figure 1: Requirements of Scaffold

1.2 Scaffolds

Scaffolds are the masterpiece of engineering of bone tissue. It's a 3D matrix that allows and stimulates the attachment and proliferation of osteoinducible cells on their surfaces is a bone scaffold. For making an ideal scaffold for BTE transplant we need to consider above parameters (given in Fig. 1)[5].

- The primary roles of scaffold are to serve as an adhesion substrate for cells, facilitate the localization and delivery of cells when implanted, and provide temporary mechanical support to the newly grown tissue by defining and maintaining a 3D structure.
- The scaffold needs to perfectly match the defect site within the patient's body. Medical imaging technologies are typically used to gather implant site external geometric data.
- An ideal scaffold suitable for BTE applications should allow or improve cell viability, attachment, osteogenic differentiation, vascularization, host integration and, where necessary, load bearing. In addition, it should allow for easy handling in the operation theatre without extensive preparatory procedures and allow for minimally invasive implantation. Industrial methods and techniques can be sterilizable [5].

2 Methodology

2.1 Scaffold Designing

For comparison, different 3D internal architectures were designed using a CAD software (SolidWorks, Fusion) to achieve:

- No enclosed pores after unit cell replication.
- Different strut orientations $[0^\circ/45^\circ/90^\circ]$ along the loading directions.
- Internal architecture similar to trabecular bone. Based on polyhedral geometries, three or four 3D internal architectures were designed

Small scale unit cells

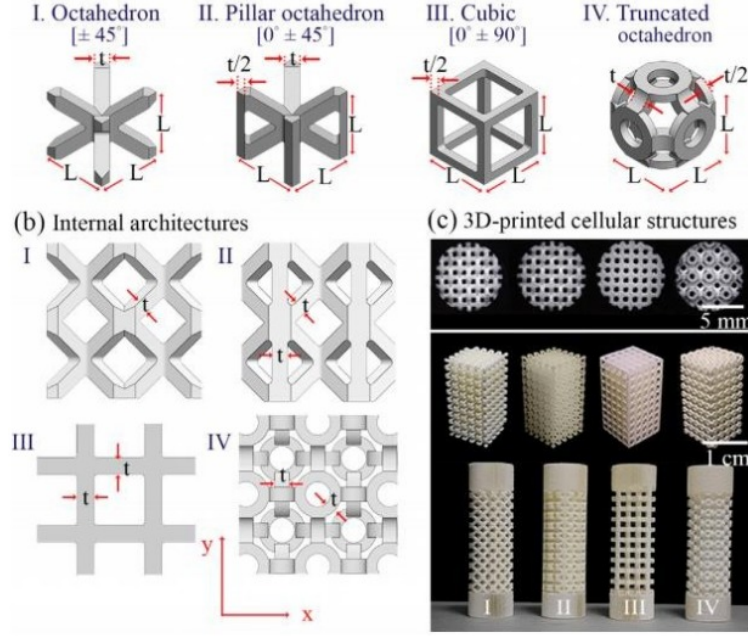


Figure 2: External and internal architectures of unit cells

The dimension of the unit (L) is 2 mm and the size of the strut (t) is 400 meter sand 500 meters. By repeating these unit cells along the x , y , and z axes, the cellular structures were planned and fabricated. To explore the mechanical properties, rectangular (10 mm * 20 mm) and cylindrical (10 mm * 30 mm) cellular structures were prepared shown inn In Fig. 2.

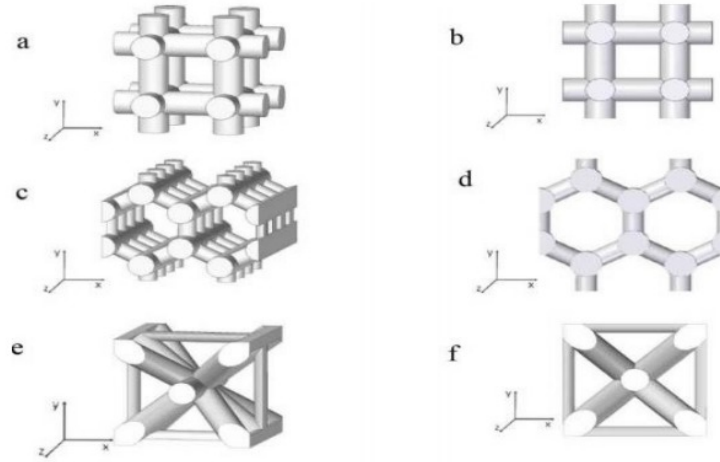


Figure 3: 2D and 3D view of Cubic, Triangular and hexagonal unit cell

There are 3-unit cell structure is used in paper: Cubic, Triangular, Hexagonal. The parameter which has been used to compare these scaffolds design is:

- Pore size: 120, 340 and 600 micrometer
- Porosity: 30
- Geometry: Cubic, triangular, Hexagonal, Octahedron, pillar octahedron, truncated, octahedron etc
- Rod and plate orientation
- Material propertie

2.2 Porous Structure

A porous structure contains pores (voids). The skeletal portion of the material is often called the "matrix" or "frame". The pores are typically filled with a fluid (liquid or gas). A porous medium is most often characterized by its porosity. Pore structure is a general term used to describe the porosity, pore size, pore size distribution, and pore morphology of a porous medium. The three-dimensional (3D) porous structure has always received considerable attention in different fields, such as materials science and bone tissue engineering, due to its ability to enhance the mechanical properties as well as its excellent bio mimetic design as bone scaffolds. For example, when forming this structure inside materials with a high Young's modulus, it can help enhance the deformability of the material system and improve the fracture strain [4].

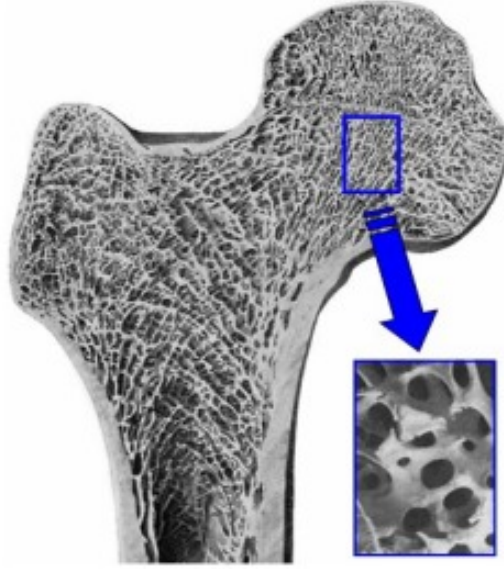


Figure 4: Porous Structure of Bone

2.3 Building of porous structure Scaffold implicit surface-based method

Implicit-surface-based (ISB) architectures are attractive candidates for designing biomorphic scaffold structures because they overcome the limitations of traditional chemistry-based methods (such as phase separation and salt-leaching, due to the uncontrollable porous morphology) and existing time-consuming computer aided design and fabrication strategies (due to the complicated processes of structural modeling and path planning) [8]. ISB methods are helpful to precisely control porous

architectures to quantitatively balance mass transport and mechanical function. One type of ISB method, the triply periodic minimal surfaces (TPMS) method allows for scaffold structures to be simply represented using a simple mathematical inequality. Using this method, different pore shapes and structural features, including pore sizes and porosities, can be introduced as needed, and the resulting models can be readily fabricated using AM techniques [6]. Regarding recent methods, much work has focused on generating regular structures and simple graded structures using periodic functions. Yoo proposed an effective method for arranging porosities using a thin-plate radial basis function based on distance field and TPMS-based functions. Fryazinov et al. proposed cellular structures based on periodic functions and obtained metamorphoses inside the structures by using gradient unit cells[6]. Furthermore, they systematically investigated the relationships between porosity and compressive or tensile strength of porous glass-ceramic scaffolds from morphological, architectural and mechanical viewpoints.

However, the capabilities of these current strategies are quite limited when it comes to constructing more complicated composite structures (such as those found in natural porous structures). Thus, the motivation for this paper was to develop a simple but generalized method for generating complex target structures[8].

2.4 Building of porous structure by using equation

As the framework of the method, we first need to find appropriate interface boundaries for subspaces based on given control elements (such as points, line segments, polylines, or polygons). Second, we arrange the needed substructures within each subspace to integrate a composite porous structure (such as hybrid structures, functionally gradient structures, hierarchical structures, random structures, and their combinations). Conveniently, these two steps can be integrated in one ISB expression. Based on the resulting models, we show that it is easy to fabricate desired porous structures using AM techniques.

Primitive(types P) TPMS

$$\phi_P = \cos(ax) + \cos(by) + \cos(cz) + p \quad (1)$$

Diamond (type D) TPMS

$$\phi_D = \cos(ax)\cos(by)\cos(cz) - \sin(ax)\sin(by)\sin(cz) + p \quad (2)$$

Gyroid(type G) TPMS

$$\phi_G = \cos(ax)\sin(by) + \cos(by)\sin(cz) + \cos(cz)\sin(ax) + p \quad (3)$$

and sheet TPMS

$$\phi = m - |\phi_\theta| \quad (4)$$

where inequality $\phi > 0$ represents the solids, $\phi < 0$ represents the interfaces. Parameters a,b, and c control the pore sizes in the x,y, and z directions, respectively. Parameter p controls the porosity. ϕ_θ can be replaced with ϕ_P, ϕ_D , and ϕ_G , and m is offset.

2.4.1 Generating anisotropic porous architecture using control elements

In Cartesian space R^3 , the subspaces that comprise each controlelement (e.g., points or line segments) are first constructed. Then,given ISB architectures are assigned to these subspaces. As a result,the final structure can be defined by $\phi \geq 0$, where ϕ is defined by

$$\phi = \sum_{i=1}^n W_i(x) \cdot \phi_i(x) \quad (5)$$

The weight functions, $w_i(x)$, are defined by

$$w_i(x) = \frac{\frac{1}{1+e^{k_i d_i(x)^2}}}{\sum_{j=1}^n \frac{1}{1+e^{k_i d_i(x)^2}}} \quad (6)$$

where $d_i(x)$ indicates the distance field of the i th control elements, the i th subspace comprises the i th control element, the i th substructure $\phi_i \geq 0$ is assigned to the i th subspace, k_i are transition factors for the i th subspace, n is the number of control elements, and x is the three-dimensional (3D) spatial coordinate vector. Obviously, we have $\sum_{i=1}^n w_i(x) = 1$. The smooth weight function in Eq. (6) guarantees the smooth transitions between the contact areas. Eq. (6) implies a spatial partition mechanism. The i th subspace is actually defined as the region.

$$w_i(x) \geq \max_{j \neq i} w_j(x) \quad (7)$$

where ‘=’ indicates the interface boundary. In the i th subspace, we have $w_i(x) \rightarrow 1$ and $w_j(x) \rightarrow 0$ ($j \neq i$) when k_i is sufficiently large; thus, based on Eqs. (5) and (6), we have $\phi \rightarrow \phi_i(x)$. Therefore, the i th substructure is assigned in the i th subspace. Furthermore, when control elements 1, 2, ..., and m indicate one subspace, this subspace can be defined by

$$\max w_i(x), i = 1 \text{ to } m \geq \max w_j(x), j = m + 1, \text{ to } n \quad (8)$$

Eqs. (7) and (8) are naturally included in Eqs. (5) and (6) when constructing a structure. Below, we introduce the different forms of $d_i(x)$ for different control elements.

Distance field of a control point. The distance field of a control point is defined by

$$d_i(x) = \|x - x_i\| \quad (9)$$

In essence, subspaces constructed by control points are Voronoi cells. Distance field of a control line segment. In Cartesian space, R^3 a control line segment generated by two points, x_1 and x_2 , can be defined by

$$x = x_1 + (x_2 - x_1)t \quad (10)$$

For different t , Eq. (10) represents the interior and exterior of the line segment, respectively. So the distance field of this line segment is defined in a piecewise manner.

$$d(x) = \begin{cases} \|x - x_1\| & t < 0 \\ \|x - x_t\| & 0 \leq t \leq 1 \\ \|x - x_2\| & t > 1 \end{cases} \quad (11)$$

where t and x_t are determined by the equation

$$\begin{cases} (x_t - x) \cdot (x_2 - x_1) = 0 \\ x_t = x_1 + (x_2 - x_1)t \end{cases} \quad (12)$$

where indicates the dot product operation for two vectors. We can approximate the piecewise function, i.e., Eq. (11), using a continuous function for structural smooth purpose by

$$d(x) = \frac{\|x - x_1\|}{1 + e^{k_d t}} + \frac{\|x - x_t\|}{(1 + e^{-k_d t})(1 + e^{k_d(t-1)})} + \frac{\|x - x_2\|}{1 + e^{-k_d(t-1)}} \quad (13)$$

2.5 Material Used

We have used two types of composite material:- Metamaterial and Photonic crystal.

2.5.1 Metamaterial

A metamaterial is any material engineered to have a property that is not found in naturally occurring materials. These are the materials that extract their properties from their structure rather than the material of which they are composed of. During the past ten years, a great interest in the research of metamaterials has been observed. Metamaterials are artificially invented materials that show the properties which are not detected in naturally occurring materials. Metamaterials exhibits negative permittivity and/ or negative permeability [2].

Metamaterials are artificial materials which have the electromagnetic properties that may not be found in nature. The unusual properties of a metamaterial have led to the development of metamaterial antennas, sensors and metamaterial lenses for miniature wireless systems which are more efficient than their conventional counterparts. Metamaterials exhibit a very sensitive response to the strain, dielectric media, chemical and biological sensing applications.

Metamaterials are artificial periodic structures with lattice constants that are much smaller than the wavelength of the incident radiation. Therefore providing negative refractive index characteristics [7]. A split-ring resonator (SRR) is one of the metamaterial particles that offer negative permeability, while complementary split-ring resonator (CSRR), the duality of SRR, interacts with the electric field and introduces negative permittivity [3].

Metamaterials are usually implemented in a periodic structure. It is a soft option to design and fabricate it by recurring structure of unit cells. A unit cell is a combination of SRR and wire structure which is shown in figure. An array of unit cells may be used to get this structure. Rectangular SRR is described below:

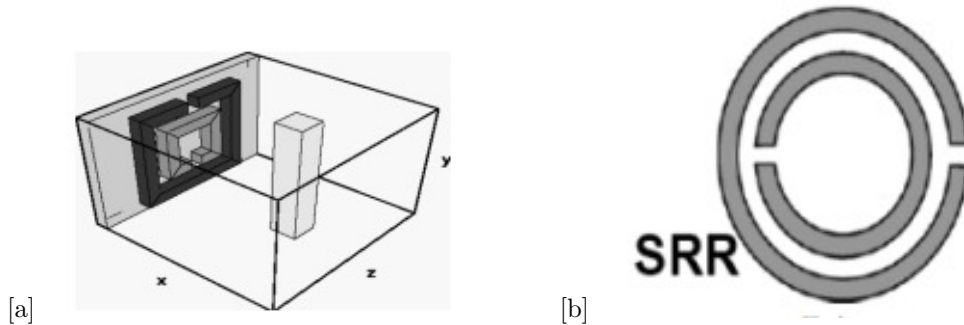


Figure 5: Structure of Unit Cell: (a)Combination of wire and SRR as unit cell, (b)Circular SRR

2.5.2 photonic crystal

A photonic crystal is an optical nanostructure in which the refractive index changes periodically. Photonic crystals are composed of periodic dielectric, metallo-dielectric or even superconductor microstructures or nanostructures that affect electromagnetic wave propagation. Photonic crystals are periodic optical nanostructures that can control light, specifically photons. Such crystals occur in nature in the form of structural coloration-like the natural microstructures.

3 Command and Output

3.1 Code

```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% MINIPROJECT IMAGE ONE
%%%%%%%% INITIALIZE MATLAB
close all;
clc;

%UNITS
degrees=pi/180;

%%%%%%%%%OPEN FIGURE WINDOW
figure('color','w','units','normalized','outerposition',[0 0 1 1]);

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% DASHBOARD %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

```

```

% PARAMETERS FOR THE PLANAR GRATING
a =1; %period of grating
theta = 30;%slant of the grating
ff = 0.6;

%%%%% GRID PARAMETERS %%%%%%%%%%%%%%
sx =10*a;
sy=10*a;
NRES = 10;

%%% GRID RESOLUTION
dx = a/NRES;
dy = a/NRES;

%%%%% NUMBER OF points
Nx = ceil(sx/dx);
dx = sx/Nx;
Ny = ceil(sy/dy);
dy = sy/Ny;

%%%%% GRID AXIS
xa = (0:Nx-1)*dx;
xa = xa -mean(xa);
ya = (0:Ny-1)*dy;
ya = ya -mean(ya);

%%%%% MESH GRID
[y,x]=meshgrid(ya,xa);

%%% GENERATE UNIFORM PLANAR FUNCTION

% CALCULATE GRATING VECTOR FUNCTION
kx =(2*pi /a) * cos(theta);
ky =(2*pi /a) * cos(theta);

% CALUCULATE ANALOG GRATING
GA=cos(kx*x+ky*y);

% CALUCULATE BINARY GRATING
gth=cos(pi*ff);
GB=double(GA>gth);

%% SHOW GRATING

% SHOW ANALOG GRATING
subplot(121);
pcolor(xa,ya,GA');
shading interp;
colorbar;
axis equal tight ;
title('analog grating ');

```



```

%%% SHOW BINARY GRATING
subplot(122);
pcolor(xa,ya,GB');
shading interp;
colorbar;
axis equal tight ;
title('binary grating ');

close all;
clc;

% units
degrees = pi/180;
%open figure window
figure('Color','w','Units','normalized','OuterPosition',[0 0 1 1]);

%%% Dashboard

% parameters of the planar grating
a=1 ; %period of grating
% grid parameters
sx=10*a;
sy=10*a;
NRESLO = 4;
NRESHI = 10;

%%% caluculate grids

% low resolution grid
dx= a/NRESLO;
dy= a/NRESLO;

Nx = ceil(sx/dx);
dx = sx/Nx;

Ny = ceil(sy/dy);
dy = sy/Ny;

xa=(0:Nx-1)*dx;
xa= xa - mean(xa);

ya=(0:Ny-1)*dy;
ya= ya - mean(ya);

[y,x] = meshgrid(ya,xa);

% HIGH RESOLUTION GRID

dx2 = a/NRESHI;
dy2 = a/NRESHI;

```

```

Nx2 = ceil(sx/dx2);
Ny2 = ceil(sy/dy2);

xa2 = linspace (xa(1),xa(Nx),Nx2);
dx2 = xa2(2) - xa2(1);

ya2 = linspace (ya(1),ya(Ny),Ny2);
dy2 = ya2(2) - ya2(1);

[y2,x2] = meshgrid (ya2,xa2);

%%% generate grids

%PERIOD
PER = X-Y;
PER = PER - min(PER(:));
PER = PER / max(PER(:));
PER = 0.5 * a + a * PER;

%ORIENTATION
r = 0.25 * sx;
RSQ = X.^2 +Y.^2;
THETA = (45 * degrees)*(RSQ < r ^2);
THETA =svlblur (THETA,[2 2]);

%FILL FACTOR
FF=X2+Y2;
FF = FF - min(FF(:));
FF = FF / max (FF(:));
FF = 0.2 +0.6 *FF;

%SHOW FF
subplot(231);
h= images (xa,ya,PER');
h2 = get(h,'Parent');
set(h2,'YDir','normal');
colorbar;
axis equal tight ;
title ('PER');

%SHOW THETA
subplot(232);
h= images (xa,ya,THETA');
h2 = get(h,'Parent');
set(h2,'YDir','normal');
colorbar;
axis equal tight ;
title ('THETA');

%SHOW FF
subplot(233);
h= images (xa,ya,THETA');
h2 = get(h,'Parent');

```

```

set(h2,'YDir','normal');
colorbar;
axis equal tight ;
title ('ff ');

%%generate spatially variant grating

%construct k function
kx= (2*pi./PER).*cos(THETA);
kY= (2*pi./PER).*sin(THETA);

%construct derivatives operations
NS = {Nx Ny};
RES = {dx dy};
[DX,DY]=svlder(NS,RES);

%solve for grating phase
A=[ DX ;DY];
b=[kx(:);ky(:)];
PHI =(A.'*A)\(A.'*b);
PHI = reshape(PHI,Nx,Ny);
%interpolate to high resolution
PHI = interp2(ya,xa',PHI,ya2,xa2');

%caluculate analog grating
GA = cos (PHI);

%caluculate binary grating
GTH=cos(PHI);
GB = (GA > GTH );

%SHOW ANALOG GRATING
subplot(235);
pcolor(xa2,ya2,GA');
shading interp;
colorbar;
axis equal tight ;
title ('ANALOG GRATING');

%SHOW BINARY GRATING
subplot(236);
h=imagec(xa2,ya2,GB');
h2=get(h,'parent');
set(h2,'ydir','normal');
colorbar;
axis equal tight ;
title ('BINARY GRATING');

% session2.m
%INITIALIZE MATLAB
close all;
clc;

```

```

% OPEN FIGURE WINDOW
figure('Color','W','Units','normalized','OuterPosition',[0 0.05 1 0.95]);
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% DASHBOARD %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% UNIT CELL PARAMETERS
a = 1;
w = 0.9*a;
% GRID PARAMETERS
Nx = 255;
Ny = Nx;
% FOURIER EXPANSION PARAMETERS
NP = 21;
NQ = 21;
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% BUILD UNIT CELL %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% GRID
dx = a/Nx;
dy = a/Ny;
xa = (0:Nx-1)*dx;
ya = (0:Ny-1)*dy;
xa = xa - mean(xa);
ya = ya - mean(ya);
[Y,X] = meshgrid(ya,xa);
% GRID INDICES OF TGRIANGLE
h = w*sqrt(3)/2;
ny = round(h/dy);
ny1 = 1 + floor((Ny - ny)/2);
ny2 = ny1 + ny - 1;
% BUILD TRIANGLE
UC = zeros(Nx,Ny);
for ny = ny1 : ny2
    f = 1 - (ny - ny1 + 1)/(ny2 - ny1 + 1);
    nx = round(f*w/dx);
    nx1 = 1 + floor((Nx - nx)/2);
    nx2 = nx1 + nx - 1;
    UC(nx1:nx2,ny) = 1;
end
% SHOW UNIT CELL
subplot(231);
hh = imagesc(xa, ya, UC');
h2 = get(hh, 'Parent');
set(h2, 'YDir', 'normal');
axis equal tight;
colorbar;
title('UNIT CELL');
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% COMPUTE FOURIER EXPANSION %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% CALCULATE FFT2
A = fftshift(fft2(UC))/(Nx*Ny);
% TRUNCATE FFT2
p0 = ceil(Nx/2);
q0 = ceil(Ny/2);
np1 = p0 - floor(NP/2);
np2 = p0 + floor(NP/2);

```

```

nq1 = p0 - floor(NP/2);
nq2 = p0 + floor(NP/2);
AT = A(np1:np2,nq1:nq2);
% AXES FOR AT
pa = (-floor(NP/2):floor(NP/2));
qa = (-floor(NQ/2):floor(NQ/2));
% CALCULATE GRATING VECTOR EXPANSION
KX = 2*pi*pa/a;
KY = 2*pi*qa/a;
[KY,KX] = meshgrid(KY,KX);
% SHOW FFT2
subplot(232);
hh = imagesc(xa, ya, real(A'));
h2 = get(hh, 'parent');
set(h2, 'YDir', 'normal');
axis equal tight;
colorbar;
title('FFT2');
% SHOW TRUNCATED FFT2
subplot(233);
hh = imagesc(pa, qa, real(AT'));
h2 = get(hh, 'parent');
set(h2, 'YDir', 'normal');
axis equal tight;
colorbar;
title('TRUNCATED FFT2');
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% RECONSTRUCT UNIT CELL
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% QUICK WAY
A = zeros(Nx,Ny);
A(np1:np2,nq1:nq2) = AT;
UCT = real(ifft2(ifftshift(A)))*(Nx*Ny);
% SHOW TRUNCATED FFT2
subplot(235);
hh = imagesc(xa, ya, real(A'));
h2 = get(hh, 'Parent');
set(h2, 'YDir', 'normal');
axis equal tight;
colorbar;
title('FFT2');
% SHOW TRUNCATED FFT2
subplot(233);
hh = imagesc(xa, ya, real(UCT'));
h2 = get(hh, 'Parent');
set(h2, 'YDir', 'normal');
axis equal tight;
colorbar;
title('TRUNCATED UNIT CELL');
% SLOW WAY
UCT = zeros(Nx,Ny);
for nq = 1 : NQ
    for np = 1 : NP
        % Calculate Planer Grating

```

```

G = exp(1i*(KX(np,nq)*X + KY(np,nq)*Y));
% Add Grating to Overall Unit Cell
UCT = UCT + AT(np,nq)*G;
% Show Truncated FFT
subplot(234);
hh = imagesc(pa,qa,real(AT'));
h2 = get(hh,'Parent');
set(h2,'YDir','normal');
axis equal tight;
colorbar;
title('TRUNCATED FFT2');
hold on;
x = pa(np) - 0.5 + [0 1 1 0 0];
y = qa(nq) - 0.5 + [0 0 1 1 0];
line(x,y,'color','k','LineWidth',2);
hold off;
% Show Planer Grafting
subplot(235);
hh = imagesc(xa,ya,real(G'));
h2 = get(hh,'Parent');
set(h2,'YDir','normal');
axis equal tight;
colorbar;
title(['P = ' num2str(pa(np)) ', Q = '...
num2str(qa(nq))]);
% Show Reconstruction Unit Cell
subplot(236);
hh = imagesc(xa,ya,ifftshift(real(UCT')));
h2 = get(hh,'Parent');
set(h2,'YDir','normal');
axis equal tight;
colorbar;
title('RECONSTRUCTED UNIT CELL');
% Force MATLAB to Draw Graphics
drawnow;
end
end

```

3.2 Output

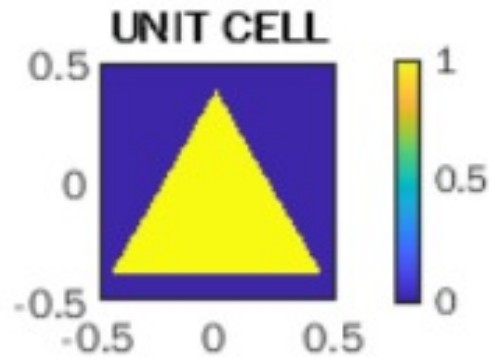


Figure 6: 2D Unit Cell

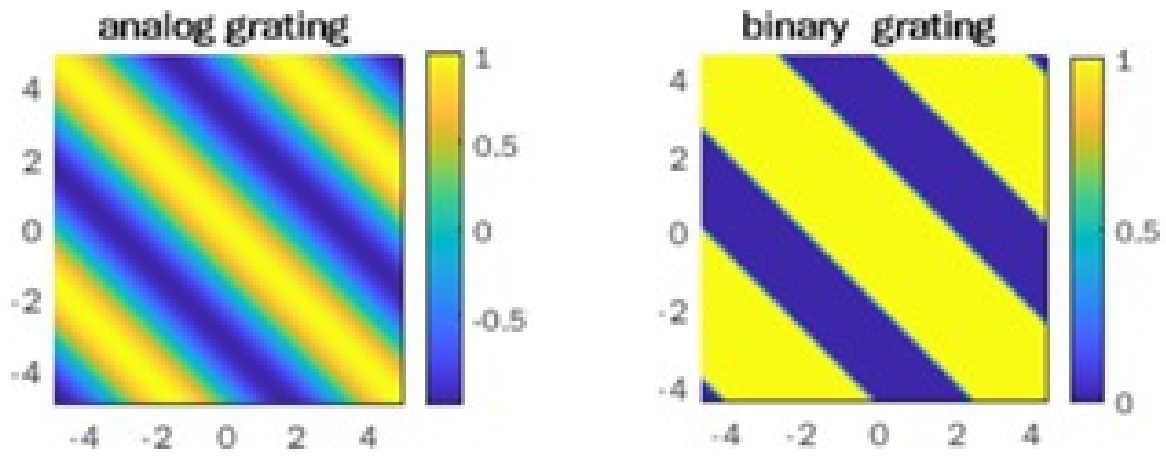


Figure 7: Analog Grating , Binary Grating

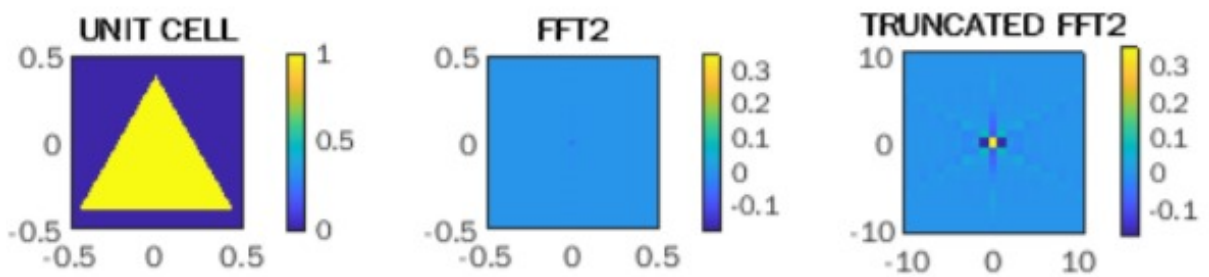


Figure 8: Unit Cell , FFT2, Truncated FFT2

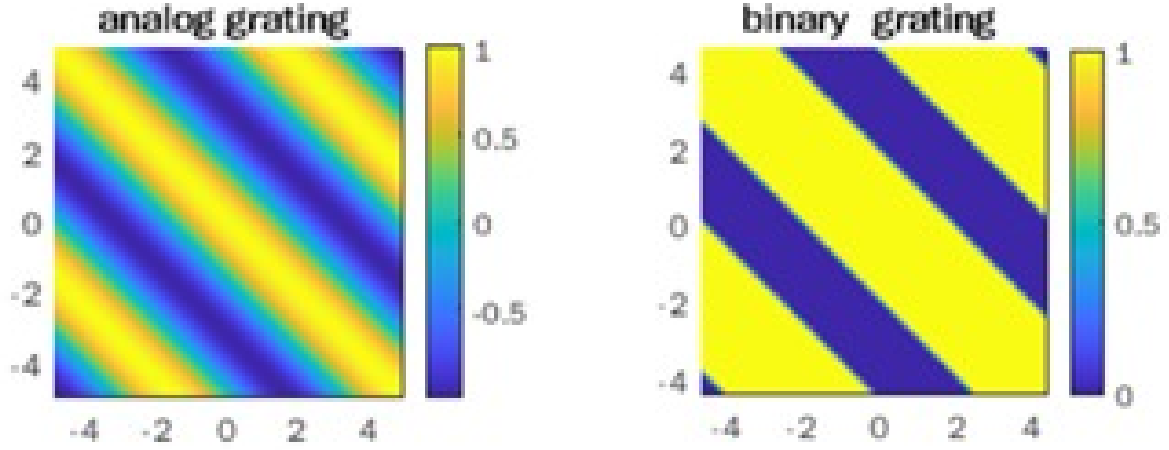


Figure 9: Unit Cell , FFT2, Truncated Unit Cell,Truncated FFT2, Reconstructed Unit Cell

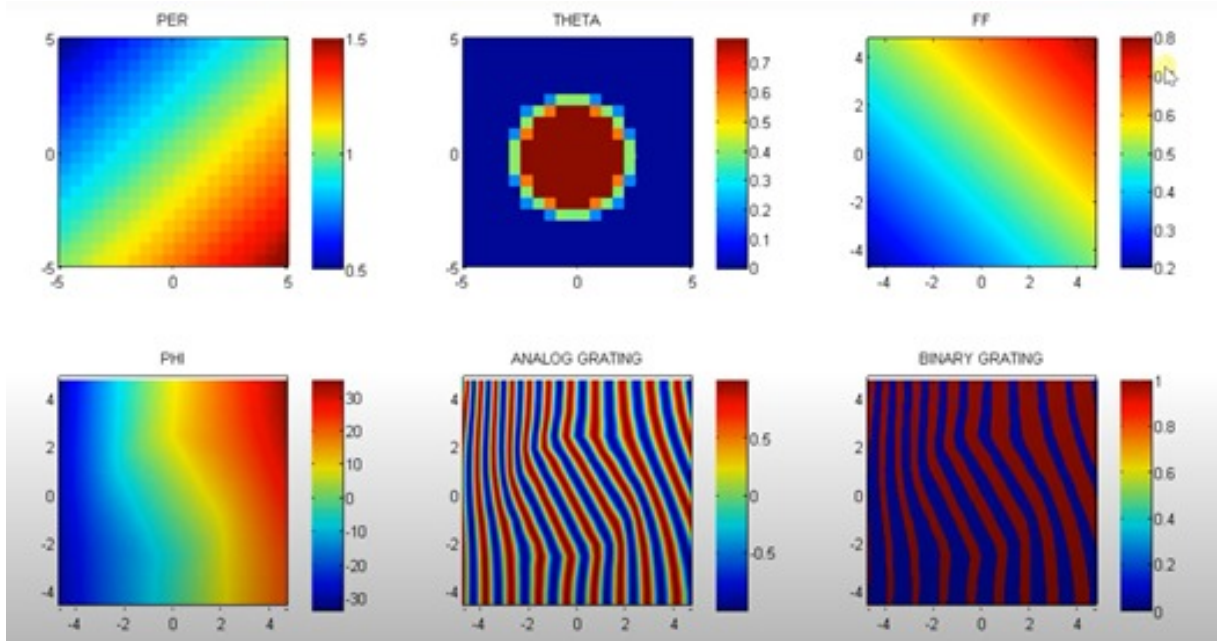


Figure 10: Spatially Variant Lattice

4 Results and Discussions

We prepared an unit cell ,calculated grating vectors and generated spatially variant lattices. Mainly we created a 2D and a 3D structure of crystal lattices using MATLAB code which resembles like a bone. We also studied and found about the porous structure of the bone.

5 Conclusion

Cellular structures consist of lattices. Lattices have many outstanding properties such as lightweight, high strength, absorbing energy, and reducing vibration, which has been extensively studied and concerned. The mechanical properties of lattice structure are the fundamental aspects for the design of lattices. Only when the lattice structure with good mechanical properties is designed, because of excellent properties, lattice structures have been widely used in bio-engineering field.

6 Acknowledgement

We made an effort to do this project. However, without the kind help and assistance of Dr. Nishant Kumar Singh, it would not have been possible. To him, we would like to extend our heartfelt thanks For his guidance and continuous monitoring, as well as providing necessary information about the project and also for their assistance in completing the project.

References

- [1] Geoffrey H Bourne. *The biochemistry and physiology of bone*. Elsevier, 2014.
- [2] Wenshan Cai and Vladimir M Shalaev. *Optical metamaterials*. Vol. 10. 6011. Springer, 2010.
- [3] Xiaoyu Cheng et al. “A compact omnidirectional self-packaged patch antenna with complementary split-ring resonator loading for wireless endoscope applications”. In: *IEEE Antennas and Wireless Propagation Letters* 10 (2011), pp. 1532–1535.
- [4] M Gelinsky et al. “Porous three-dimensional scaffolds made of mineralised collagen: Preparation and properties of a biomimetic nanocomposite material for tissue engineering of bone”. In: *Chemical Engineering Journal* 137.1 (2008), pp. 84–96.
- [5] Toktam Ghassemi et al. “Current concepts in scaffolding for bone tissue engineering”. In: *Archives of bone and joint surgery* 6.2 (2018), p. 90.
- [6] Scott J Hollister, RD Maddox, and Juan M Taboas. “Optimal design and fabrication of scaffolds to mimic tissue properties and satisfy biological constraints”. In: *Biomaterials* 23.20 (2002), pp. 4095–4103.
- [7] V Koushick and C Divya. “Investigation of Metamaterial and its Design Approaches”. In: *2018 International Conference on Recent Innovations in Electrical, Electronics & Communication Engineering (ICRIEECE)*. IEEE. 2018, pp. 2422–2427.
- [8] Nan Yang et al. “Building implicit-surface-based composite porous architectures”. In: *Composite Structures* 173 (2017), pp. 35–43.