Package 'compGeometeR'

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Type Package

Title Create Computational Geometry Algorithms for use in R

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Description Create Computational Geometry Algorithms for use in R

License GPU

Depends R (>= 3.5.1)

Imports devtools

Encoding UTF-8

LazyData true

RoxygenNote 7.1.0

Suggests testthat

NeedsCompilation no

R topics documented:

alpha_complex *Alpha complex*

Description

This function calculates the alpha complex of a set of n points in d-dimensional space using the Qhull library.

Usage

```
alpha_complex(points = NULL, alpha = Inf)
```

Arguments

points	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.
alpha	a real number between zero and infinity that defines the maximum circumradii for a simplex to be included in the alpha complex. If unspecified alpha defaults to infinity and the alpha complex is equivalent to a Delaunay triangulation.

Value

Returns a list consisting of:

- input_points: the input points used to create the Voronoi diagram.
- simplices: a s-by-$d+1$ matrix of point indices that define the s simplices that make up the alpha complex.
- circumcentres: a s-by-d matrix of coordinates that define the centre of the circumcircle associated with each simplex.
- circumradii: the radius of each circumcircle.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

Edelsbrunner H, Mücke EP (1994) Three-dimensional alpha shapes. ACM Transactions on Graphics, 13(1):43-72 https://dl.acm.org/doi/abs/10.1145/174462.156635.

Examples

```
# Define points
x <- c(30, 70, 20, 50, 40, 70)
y <- c(35, 80, 70, 50, 60, 20)
p <- data.frame(x, y)
# Create alpha complex and plot
a_complex <- alpha_complex(points = p, alpha = 20)
plot(p, pch = as.character(seq(nrow(p))), xlim=c(0,80), ylim=c(10,90), asp=1)
for (s in seq(nrow(a_complex$simplices))) {
  polygon(a_complex$input_points[a_complex$simplices[s,],], border="red")
}
text(a_complex$circumcentres, labels=seq(nrow(a_complex$simplices)), col="blue")
```

```
symbols(a_complex$circumcentres, circles = a_complex$circumradii,
        inches = FALSE, add = TRUE, fg="blue", lty="dotted")
```

`compGeometeR` *Computational geometry algorithms for R*

Description

Implementation of various computation geomtery algorithms for use in R

Package:	compGeometeR
Date:	2020-05-20
License:	GPL-2
LazyLoad:	yes

Author(s)

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References

http://www.qhull.org/html/qh-code.htm

`convex_hull` *Convex hull*

Description

This function calculates the convex hull around a set of n points in d-dimensional space using the Qhull library.

Usage

```
convex_hull(points = NULL)
```

Arguments

`points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.

Value

Returns a list consisting of:

- `input_points`: the input points used to create the convex hull.

- `hull_simplices`: a s-by-d matrix of point indices that define the s simplices that make up the convex hull.
- `hull_indices`: a vector of the point indices that form the convex hull.
- `hull_vertices`: a matrix of point coordinates that form the convex hull.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

See Also

`convex_layer`

Examples

```
# Define points
x <- c(30, 70, 20, 50, 40, 70)
y <- c(35, 80, 70, 50, 60, 20)
p <- data.frame(x, y)
# Create convex hull and plot
ch <- convex_hull(points=p)
plot(p, pch = as.character(seq(nrow(p))))
for (s in seq(nrow(ch$hull_simplices))) {
  lines(ch$input_points[ch$hull_simplices[s, ], ], col = "red")
}
```

`convex_layer` *Convex layer*

Description

This function calculates a convex layer of specified depth from a set of n points in d-dimensional space using the Qhull library.

Usage

```
convex_layer(points = NULL, layer = 1)
```

Arguments

`points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.
`layer`	an integer that specifies the desired convex layer. If left unspecified convex layer 1 is returned that is equivalent to the convex hull.

Value

Returns a list consisting of:

- `input_points`: the input points used to create the convex layer.
- `hull_simplices`: a s-by-d matrix of point indices that define the s simplices that make up the convex layer.
- `hull_indices`: a vector of the point indices that form the convex layer.
- `hull_vertices`: a matrix of point coordinates that form the convex layer.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

See Also

convex_hull

Examples

```
# Create some random example data
set.seed(1) # to reproduce figure exactly
x = 20 + rgamma(n = 100, shape = 3, scale = 2)
y = rnorm(n = 100, mean = 280, sd = 30)
p <- data.frame(x, y)
plot(p)
cols <- c("red", "blue", "orange", "lightseagreen", "purple")
for (i in seq(5)) {
  cl <- convex_layer(points = p, layer = i)
  for (s in seq(nrow(cl$hull_simplices))) {
    lines(cl$input_points[cl$hull_simplices[s, ], ], col = cols[i], lwd = 2)
  }
}
legend("topright", legend = seq(5), lwd = 2, col = cols, bty = "n",
       title = "Convex layers")
```

---

delaunay *Delaunay triangulation*

Description

This function calculates the Delaunay triangulation of a set of n points in d-dimensional space using the Qhull library.

Usage

```
delaunay(points = NULL)
```

Arguments

`points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.

Value

Returns a list consisting of:

- `input_points`: the input points used to create the Delaunay triangulation .
- `simplices`: a s-by-$d+1$ matrix of point indices that define the s simplices that make up the Delaunay triangulation.
- `simplex_neighs`: a list containing for each simplex the neighbouring simplices.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

Examples

```
# Define points
x <- c(30, 70, 20, 50, 40, 70)
y <- c(35, 80, 70, 50, 60, 20)
p <- data.frame(x, y)
# Create Delaunay triangulation and plot
dt <- delaunay(points = p)
plot(p, pch = as.character(seq(nrow(p))))
for (s in seq(nrow(dt$simplices))) {
  polygon(dt$input_points[dt$simplices[s,],], border="red")
  text(x=colMeans(dt$input_points[dt$simplices[s,],])[1],
       y=colMeans(dt$input_points[dt$simplices[s,],])[2],
       labels=s, col="red")
}
```

`find_simplex` *Find simplex*

Description

Returns the simplices of a Delaunay triangulation or alpha complex that contain the given set of test points.

Usage

```
find_simplex(simplices, test_points)
```

Arguments

`simplices`	A Delaunay trigulation list object created by `delaunay` or a alpha complex list object created by `alpha_complex` that contain simplices.
`test_points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.

Value

A n length vector containing the index of the simplex the test point is within, or a value of NA if a test point is not within any of the simplices. If any of the test point coordinates contain NA then the output is also NA.

Examples

```
# Define points and create a Delaunay triangulation
x <- c(30, 70, 20, 50, 40, 70)
y <- c(35, 80, 70, 50, 60, 20)
p <- data.frame(x, y)
a_complex <- alpha_complex(points = p, alpha = 20)
# Check which simplex the test points belong to
p_test <- data.frame(c(20, 50, 60, 40), c(20, 60, 60, 50))
p_test_simplex <- find_simplex(simplices = a_complex, test_points = p_test)
plot(p, pch = as.character(seq(nrow(p))), xlim=c(0,90))
for (s in seq(nrow(a_complex$simplices))) {
  polygon(a_complex$input_points[a_complex$simplices[s,],], border="red")
  text(x=colMeans(a_complex$input_points[a_complex$simplices[s,],])[1],
       y=colMeans(a_complex$input_points[a_complex$simplices[s,],])[2],
       labels=s, col="red")
}
points(p_test[,1], p_test[,2], pch=c("1", "2", "3", "4"), col="blue")
legend("topright", legend = c("input points", "simplices", "test points"),
       text.col=c("black", "red", "blue"), title = "Indices for:", bty="n")
print(p_test_simplex)
```

---

grid_coordinates *Grid Coordinates*

Description

Create an n-dimensional grid of coordinates across space.

Usage

```
grid_coordinates(mins, maxs, nCoords)
```

Arguments

mins	Vector of length n listing the point space minimum for each dimension.
maxs	Vector of length n listing the pointspace maximum for each dimension.
nCoords	Number of coordinates across the point space in all dimensions.

Details

This function creates a grid of coordinates systematically located throughout the specified point space to enable visualisation of alpha shape . The extent of the grid is given by the mins and maxs, and the number of coordinates for each dimension is given by nCoords.

Value

A matrix with n columns.

Examples

```
# Point space grid coordinates usage
xy = grid_coordinates(mins=c(15,0), maxs=c(35,200), nCoords=5)
```

`in_convex_hull` *In convex hull*

Description

Given a d-dimensional convex hull this function checks to see which of a set of n test points are within the convex hull. This function uses the Qhull library.

Usage

```
in_convex_hull(hull = NULL, test_points = NULL)
```

Arguments

`hull`	A convex hull list object created by `convex_hull`
`test_points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.

Value

A n length vector containing `TRUE` if test point n lies within the hull and `FALSE` if it lies outside the hull. If any of the test point coordinates contain NA then the output is also NA.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

See Also

`convex_hull`

Examples

```
# Define points to create the convex hull
x <- c(30, 70, 20, 50, 40, 70)
y <- c(35, 80, 70, 50, 60, 20)
p <- data.frame(x, y)
ch <- convex_hull(points = p)
plot(p, pch = as.character(seq(nrow(p))), xlim=c(0,100), ylim=c(0,100))
for (s in seq(nrow(ch$hull_simplices))) {
  lines(ch$input_points[ch$hull_simplices[s, ], ], col = "red")
}
# Check if some test points are in the convex hull
p_test <- data.frame(c(20, 50, 60, 90), c(20, 60, 60, 40))
```

```
points(p_test[,1], p_test[,2], pch=c("1", "2", "3", "4"), col="blue")
legend("topright", legend = c("input points", "test points"),
       text.col=c("black", "blue"), title = "Indices for:", bty="n")
p_test_hull <- in_convex_hull(hull = ch, test_points = p_test)
print(p_test_hull)
```

`voronoi` *Voronoi diagram*

Description

This function calculates the Voronoi digram of a set of n points in d-dimensional space using the Qhull library.

Usage

```
voronoi(points = NULL, delaunay = FALSE)
```

Arguments

`points`	a n-by-d dataframe or matrix. The rows represent n points and the d columns the coordinates in d-dimensional space.
`delaunay`	a boolean indicating if the Delaunay triangulation, which is the dual of the Voronoi diagram should also be returned, defaults to `FALSE`.

Value

Returns a list consisting of:

- `input_points`: the input points used to create the Voronoi diagram.
- `voronoi_vertices`: a i-by-d matrix of point coordinates that define the verticies that make each Voronoi region v.
- `voronoi_regions`: a list of length p that for each input point contains indices for the Voronoi vertices that define the Voronoi region v for each input point - if the indices include zeros then the Voronoi region is infinite.

Additionally, if `delaunay = TRUE` the returned list also inclues:

- `simplices`: a s-by-$d+1$ matrix of point indices that define the s simplices that make up the Delaunay triangulation.
- `circumradii`: for each simplex the radius of the associated circumcircle (note: the `voronoi_vertices` are equivalent to the the centres of the circumcircles).
- `simplex_neighs`: a list containing for each simplex the neighbouring simplices.

References

Barber CB, Dobkin DP, Huhdanpaa H (1996) The Quickhull algorithm for convex hulls. ACM Transactions on Mathematical Software, 22(4):469-83 https://doi.org/10.1145/235815.235821.

See Also

delaunay

Examples

```
# Define points
x <- c(30, 70, 20, 50, 40, 70, 20, 55, 30)
y <- c(35, 80, 70, 50, 60, 20, 20, 55, 65)
p <- data.frame(x, y)
# Create Voronoi diagram and plot
vd <- voronoi(points = p)
cols = c("red", "blue", "green", "darkgrey", "purple", "lightseagreen",
         "brown", "darkgreen", "orange")
plot(vd$input_points, pch = as.character(seq(nrow(p))), col=cols,
     xlim=c(0,100), ylim=c(0,100))
text(vd$voronoi_vertices[,1], vd$voronoi_vertices[,2],
     labels = as.character(seq(nrow(vd$voronoi_vertices))))
r = 0
for (vd_region in vd$voronoi_regions) {
  r = r + 1
  if (!0 %in% vd_region) {
    polygon(vd$voronoi_vertices[vd_region,], density=20, col = cols[r])
  }
}
```

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