

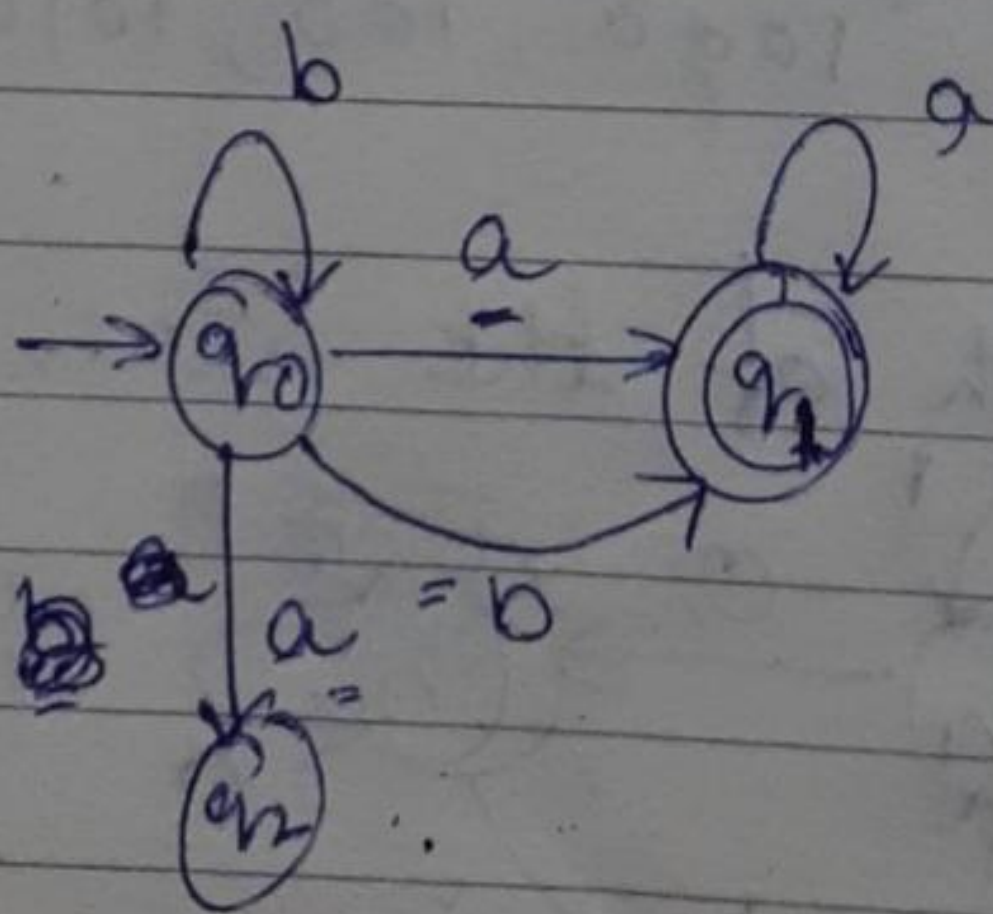
NFA / NDFA

Non-Deterministic FA

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- The FA are called NFA when there exist many paths to specific i/p from the current state to the next state.
- It is easy to construct NFA that DFA from a given regular language.
- Every NFA is not DFA, But each NFA can be transmitted to DFA.
- NFA is defined in the same way as DFA, but with two exceptions.
 - It contains multiple next ~~next~~ state.
 - It contains ϵ transitions.



⇒ Formal Definition of NFA

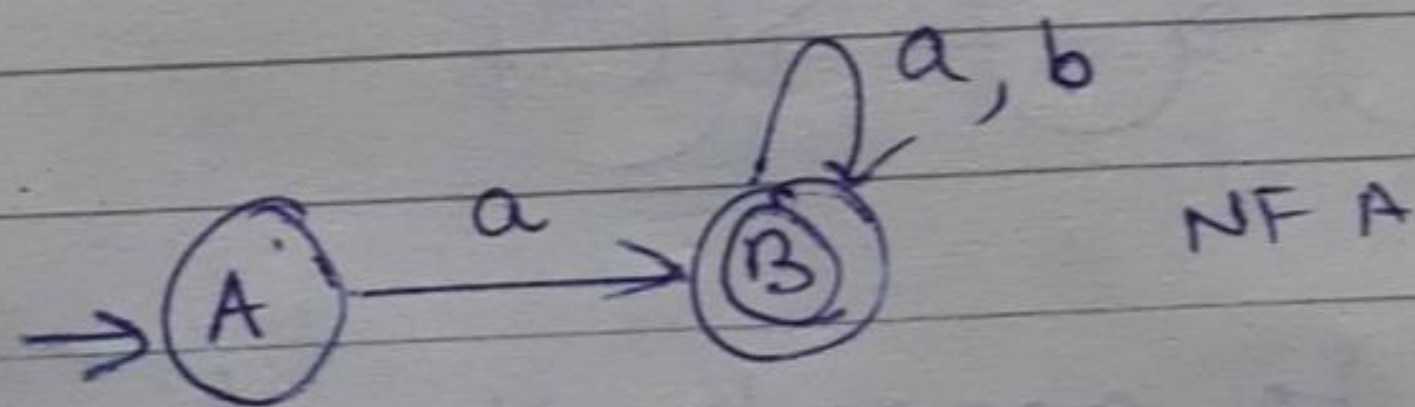
NFA also have 5 tuples same as DFA, but with different transition fn.

$\delta : Q \times \Sigma \subseteq 2^Q$	DFA
↓ Transition fn.	$\delta : Q \times \Sigma \rightarrow Q$
	Multiple states

Example:

$\Sigma = \{a, b\}$

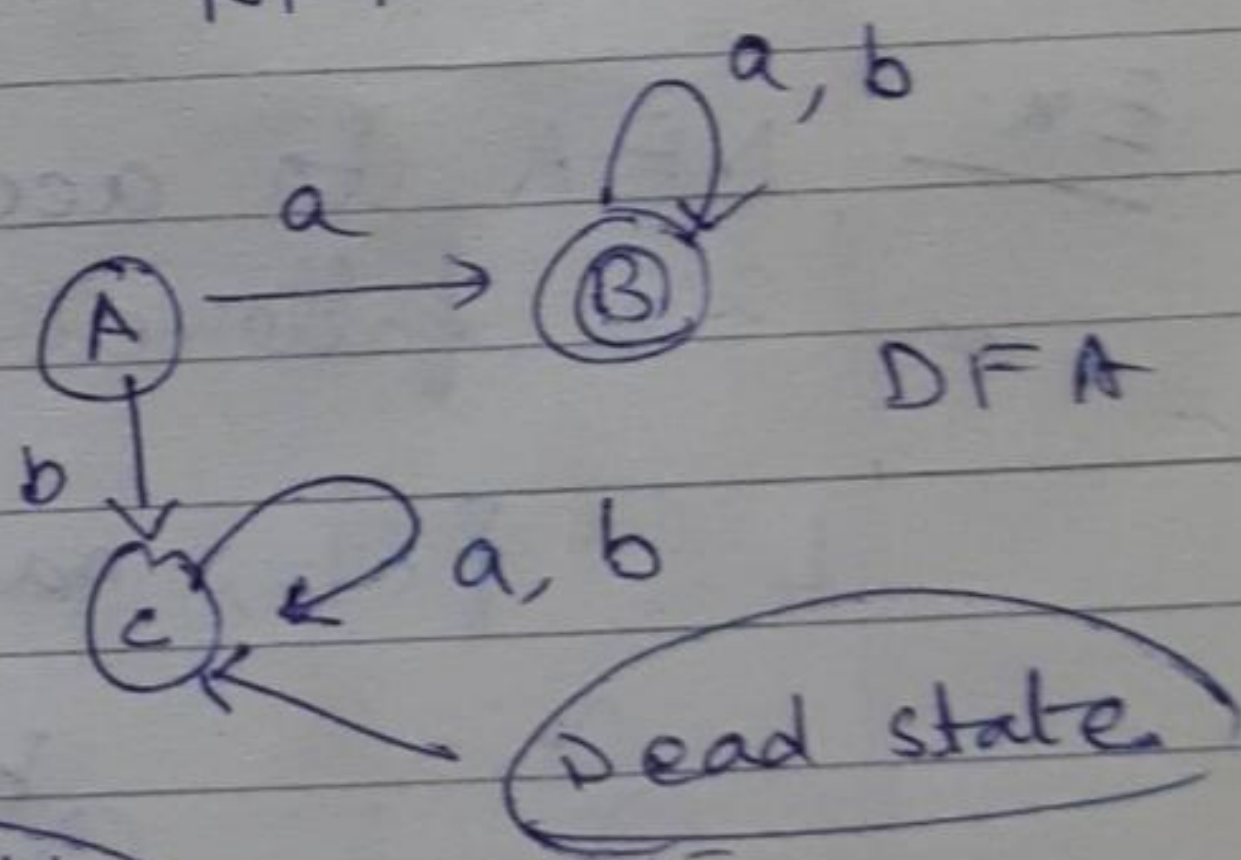
Ex. 1 $L_1 = \{ \text{start-s with 'a'} \}$



check for ab
 $A \rightarrow B$.

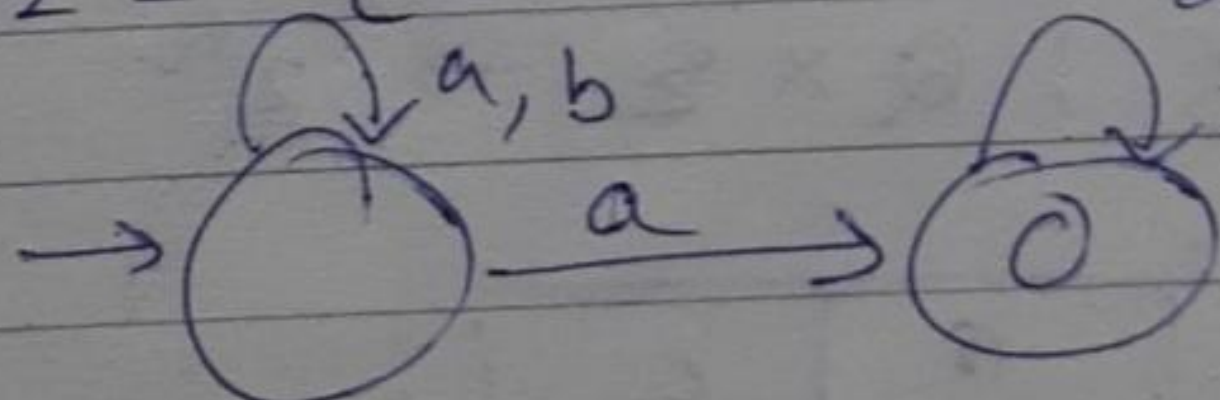
check for b
No input for b.

It is Dead configuration.

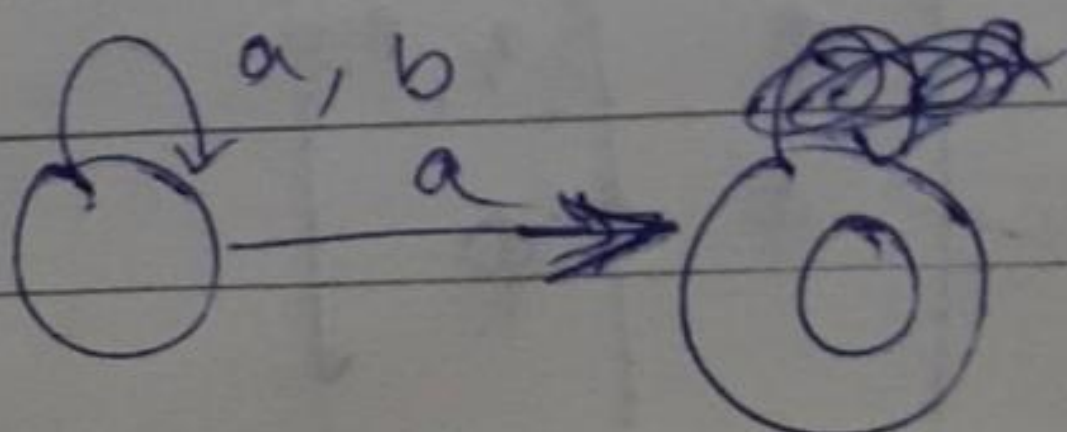


Ex. 2

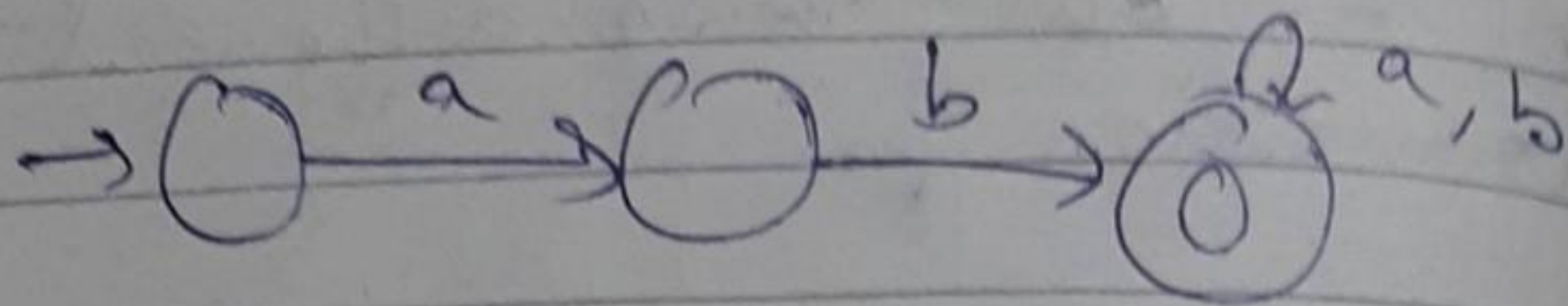
$L_2 = \{ \text{contain 'a'} \}$



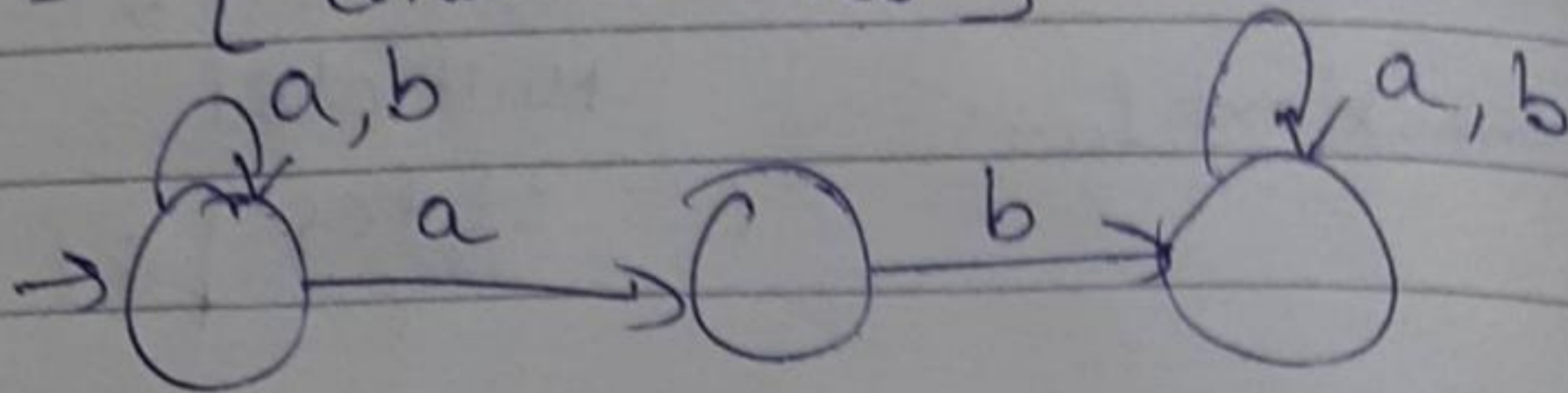
$L_3 = \{ \text{End-s with 'a'} \}$



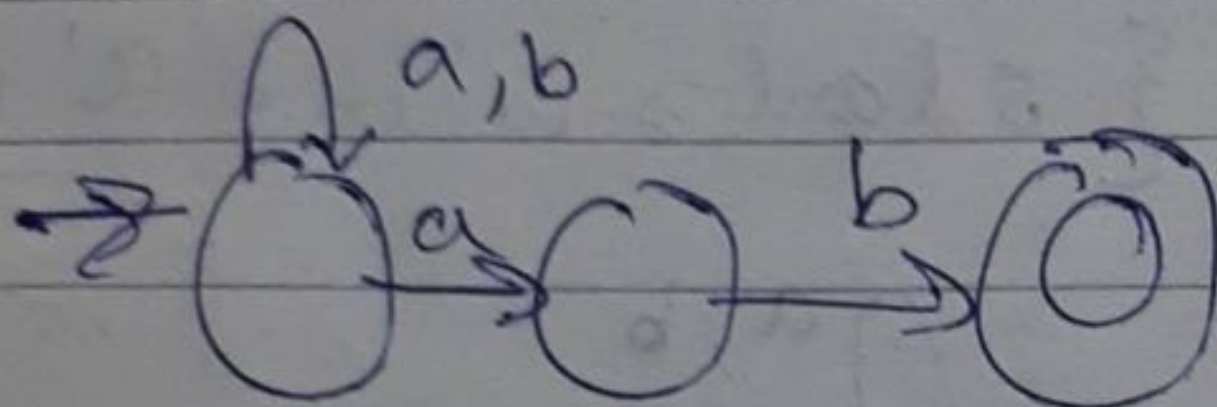
$L_4 = \{ \text{starts with 'ab'} \}$



$L_5 = \{ \text{contains 'ab'} \}$

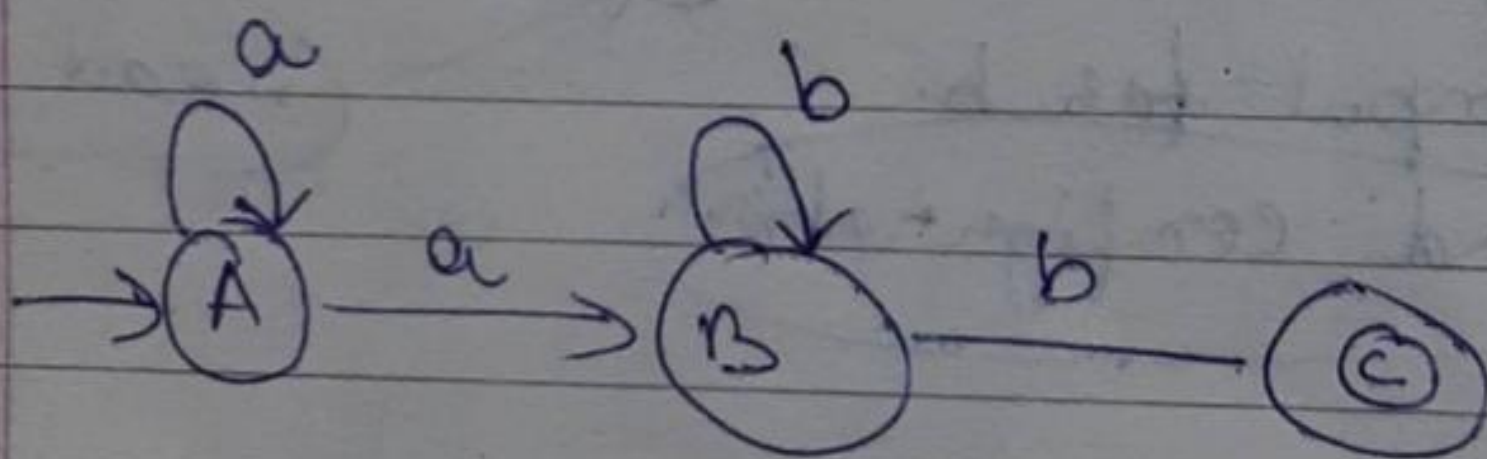


$L_6 = \{ \text{Ends with 'ab'} \}$



Ex NFA to accept the strings of all a's followed by all b's.

$L = \{ ab, aab, aaaaabbbb, abbb \dots \}$



Transition Table.

$$\delta : Q \times \Sigma \rightarrow 2^Q$$

$q \backslash \Sigma$	a	b
q_0	$\{q_0, q_1\}$	\emptyset
q_1	\emptyset	$\{q_1, q_2\}$
q_2	\emptyset	\emptyset

Definition

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$$M = (Q, \Sigma, \delta, q_0, F)$$

$$Q = \{q_0, q_1, q_2\}$$

$$\Sigma = \{a, b\}$$

$$\delta = Q \times \Sigma \rightarrow Q$$

$$q_0 = q_0$$

$$F = \{q_2\}$$

String verification

check abb

$$\delta(q_0, abb) \rightarrow q_1$$

$$\delta(q_1, bb) \rightarrow q_1$$

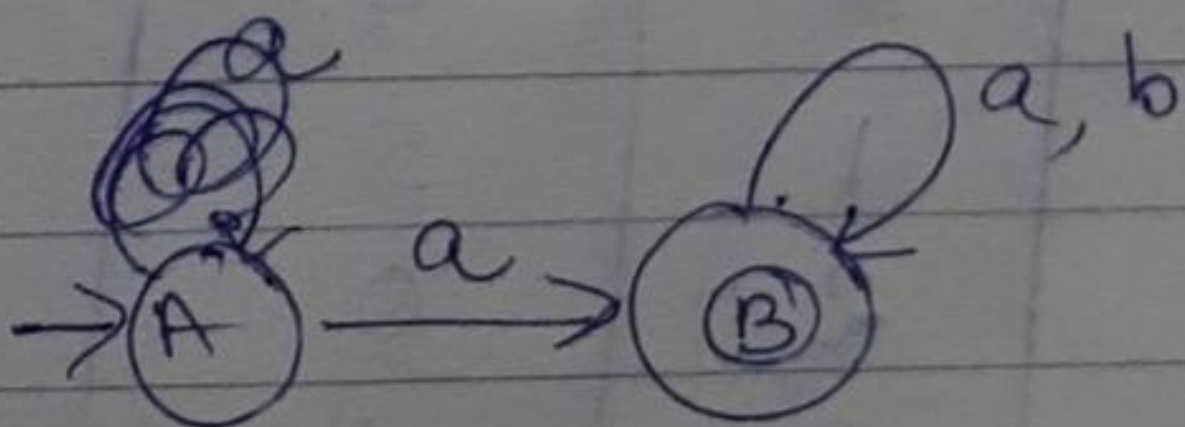
$$\delta(q_1, b) \rightarrow q_2$$

$$\delta(q_2, \epsilon) \rightarrow \text{Accepted}$$

Ex.

NFA to accept string that start with 'a', $\Sigma = \{a, b\}$

$$L = \{a, aa, aaaa, ab, abab, aabaa, \dots\}$$



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Ex.

NFA contain any no. of 0's
or 1's followed by either
'00' or '11'

$L = \{00, 11, 01011, 01000, 0100011, 1100, \dots\}$

