

Qtext :

Consider the space-time diagram shown in Fig. 1. The scalar clock values of the events **a**, **b**, **c** and **d** are 3, 2, 2 and 4 respectively. Identify the scalar timestamps of the rest of the events and the scalar timestamps of the messages exchanged among the 4 processes. Use **R1** and **R2** for updating the scalar clocks. Assume increment value  $d = 2$ . [10]

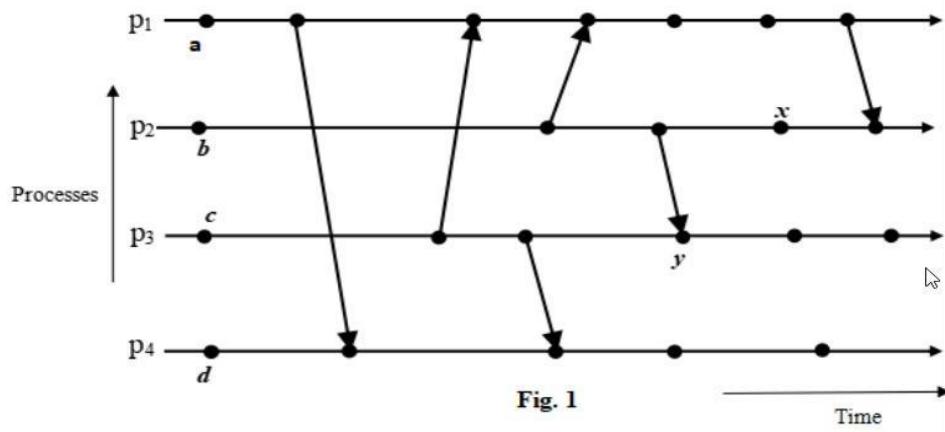
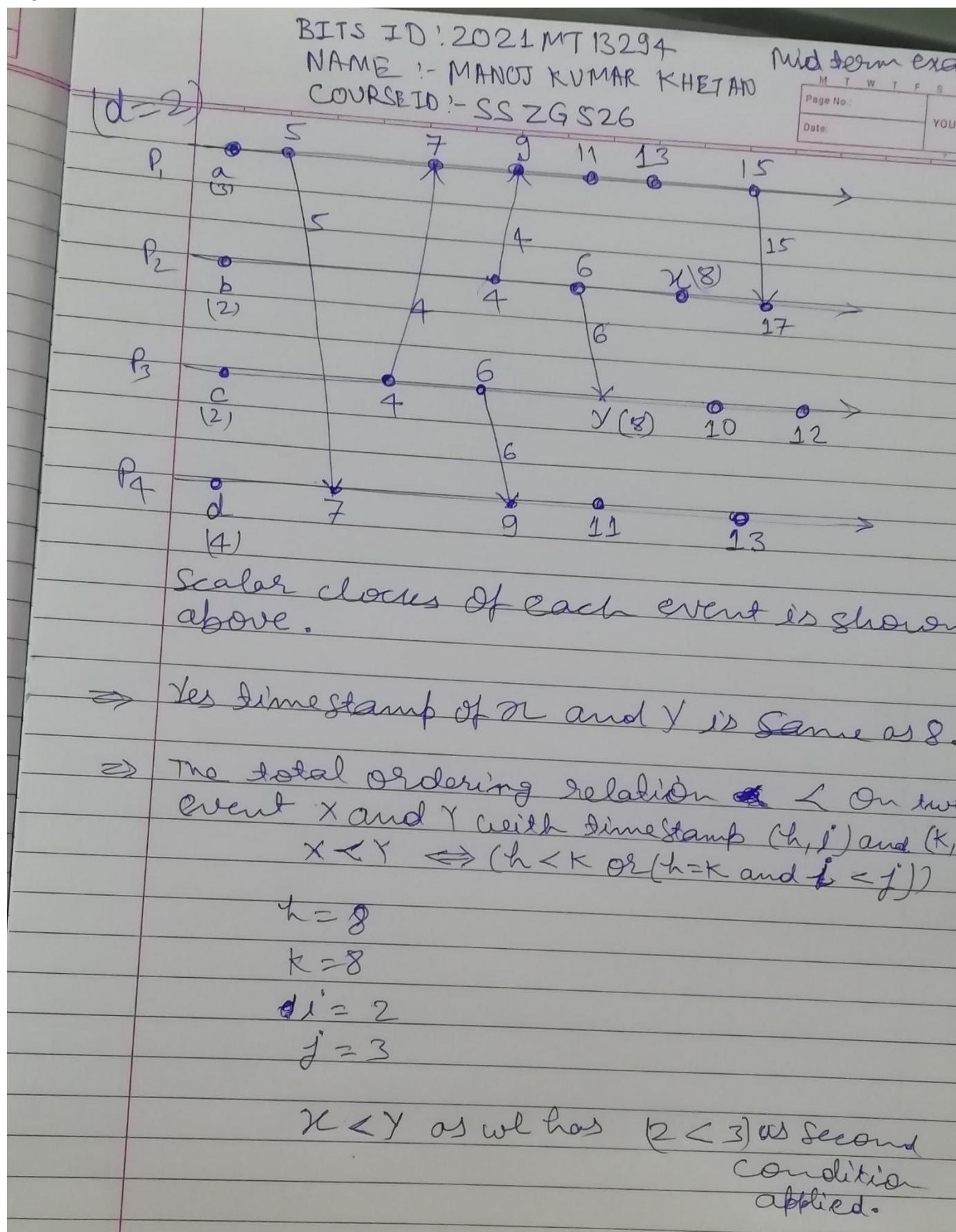


Fig. 1

Are the scalar timestamps of events **x** and **y** same? If yes, then with proper justification, show how you can totally order **x** and **y**?

[ $1 + 1 = 2$ ]

Ans :



Barsha Ma'am feedback : 1st part answer is correct, 2<sup>nd</sup> part answer is not clear. You have to write the order in tuple form.

Correction for part 2

x has time stamp as (8, 2) and y as time stamp as (8, 3). As  $(8, 2) < (8, 3)$  since  $2 < 3$ .

Hence  $x < y$ .

Qtext :

Consider the timing diagram of Fig. 3. The timing diagram shows 2 processes P1 and P2 of a distributed system.  $C_{12}$  is the communication channel from P1 to P2 and  $C_{21}$  is the communication channel from P2 to P1. P1 has 2 local variables A and B. P2 has 2 local variables X and Y. The dashed vertical lines denote the different time instants of this timing diagram. Initially, at time instant  $t_1$ , the values of the local variables of P1 are – A = 30, B = 9 and the values of the local variables at P2 are – X = 50, Y = 20. Between time instants  $t_1$  and  $t_2$ , P1 sends message m1 to P2. The content of m1 is “change X to 60”. P2 receives m1 between  $t_2$  and  $t_3$  and accordingly changes the value of X. P2 sends message m2 to P1 between  $t_1$  and  $t_2$ . The content of m2 is “change B to 29” and P1 receives this message between  $t_2$  and  $t_3$ . P1 changes the value of B accordingly. Between  $t_3$  and  $t_4$ , P1 sends message m3 to P2. The content of m3 is “change Y to 90”. P2 receives m3 between  $t_4$  and  $t_5$  and accordingly changes the value of Y. The messages m1, m2 and m3 are shown using bold arrows in the diagram. Assume that the Chandy-Lamport algorithm is executed on this distributed system for recording the global snapshot. P1 initiates the snapshot recording algorithm by sending a marker to P2 after time instant  $t_4$ . P2 receives this marker after time instant  $t_5$  and sends a marker to P1. P1 receives this marker after  $t_6$ . The sending and the receiving of markers are shown using dotted arrows in the Figure. Describe how the Chandy-Lamport algorithm records the local states of P1 and P2 and the states of the channels  $C_{12}$  and  $C_{21}$ . Note that the values of the individual local variables constitute the state of each process. [6]

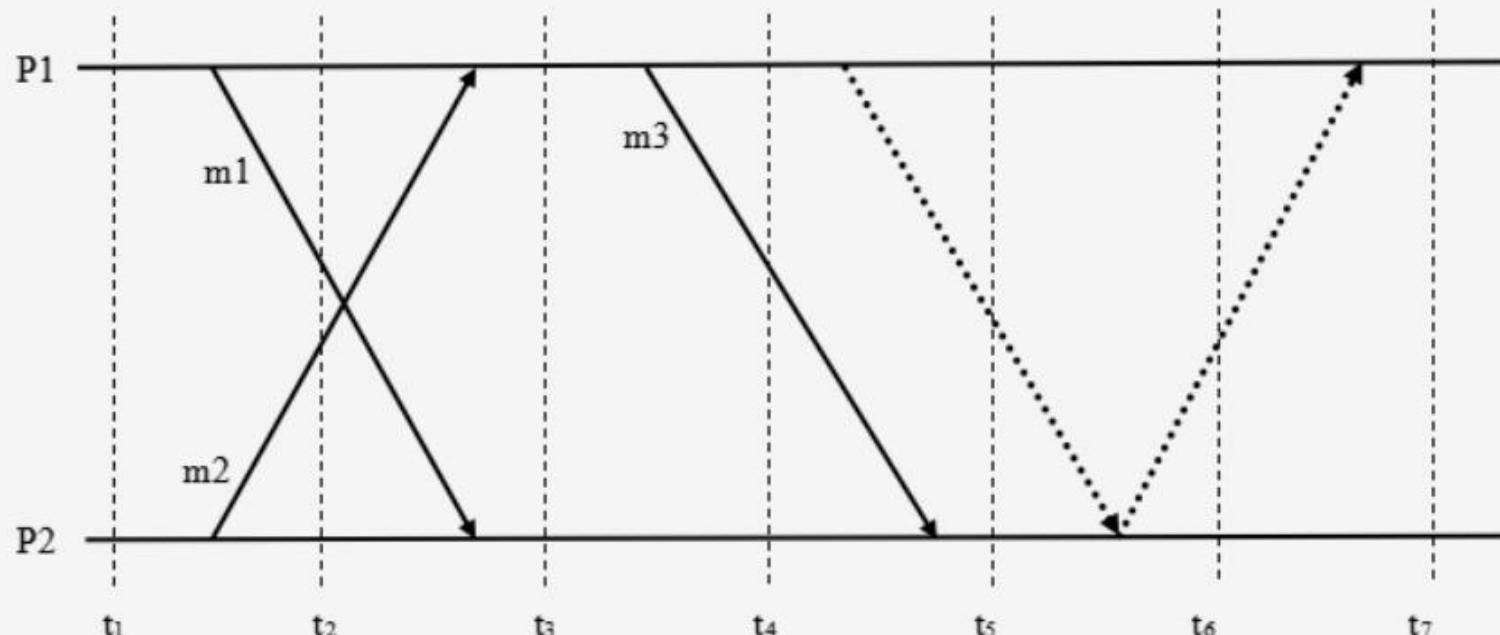
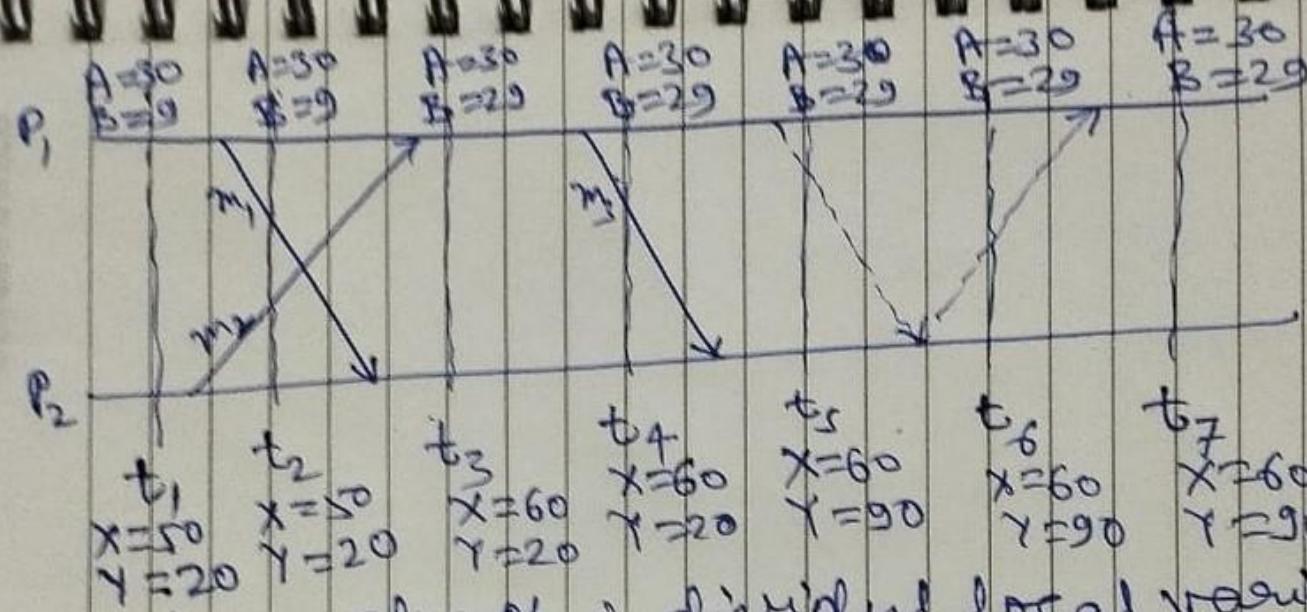


Fig. 3

Ans :

Barsha Ma'am feedback : The sum of the variables are not to be computed. The state of each process is the values

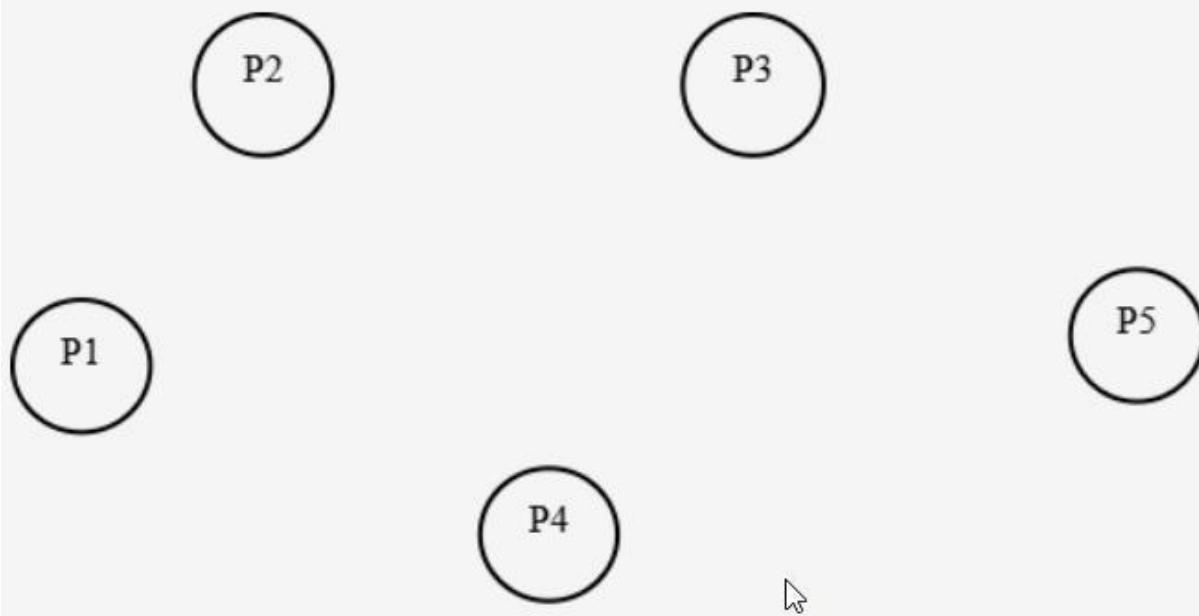
Redone the solutions of problem as below:



- ⇒ As per given value of individual local variable constitute the state of each process.
- ⇒ As per Chandy-Lamport Algorithm, process  $P_1$  record the state ~~of~~<sup>LSP</sup> snapshot as  $\{A=30, B=29\}$  before sending marker message, later sends marker to  $P_2$
- ⇒ On receiving marker process  $P_2$  record the state/snapshot later sends marker to  $P_1$ .  $LSP_2 = \{X=60, Y=90\}$
- ⇒ State of channel  $C_{12}$  as  $SC_{12} = \emptyset \rightarrow$  as there are both messages  $m_1, m_3$  were already reached to  $P_2$ .
- ⇒ State of channel  $C_{21}$  as  $SC_{21} = \emptyset \rightarrow$  as  $m_2$  already reached to  $P_1$ .

**Qtext :**

Consider a distributed system consisting of 5 processes as depicted in Fig. 4. The sites have not been shown in the diagram. You are not required to consider any site for answering the questions.



**Fig. 4**

The following dependencies exist among the processes:

- P1 is blocked and is waiting for P4 to release some resource
- P4 is blocked and is waiting for P3 to release some resource
- P3 is blocked and is waiting for P2 to release some resource
- P2 is blocked and is waiting for P1 to release some resource
- P5 is blocked and is waiting for P3 to release some resource

Draw the WFG for the above scenario.

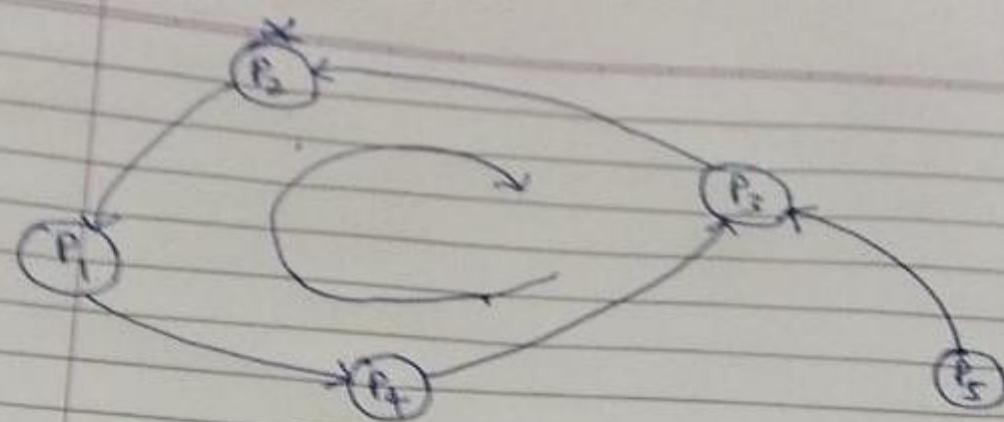
[1]

Execute Chandy-Misra-Haas algorithm for the OR model on this distributed system to determine whether any deadlock exists in the system. Assume P2 initiates the algorithm. Note that the deadlock is to be detected by using the algorithm and not by any other means. [9]

**Ans :**

Barsha Ma'am feedback : You have to write the steps of the CMH algorithm. You have to mention the messages exchanged in text, not in diagram. Follow the lecture content.

[Redone the solutions of problem as below:](#)



Since process  $P_2 \rightarrow P_1 \rightarrow P_4 \rightarrow P_3$  cycle is present as well as process  $P_5$  is dependent on  $P_3$ , so knot is present in the WFG.

presence of knot represents a deadlock in pse CMH OR model.

Step 1 Since  $P_2$  is initiating the CMH OR Algorithm

$$\text{Num}_{P_2} = 1$$

$$|D_{S_{P_2}}| = 1$$

$$\text{Wait}_{P_2} = T$$

Query sent  ~~$\nabla(P_2, P_2, P_4)$~~   $\nabla(2, 2, 1)$

as engaged query

Step 2 at  $P_3$

$$\text{Num}_{P_3} = 1$$

$$|D_{S_{P_3}}| = 1$$

$$\text{Wait}_{P_3} = T$$

Query sent  $\nabla(2, 1, 4)$

Step 3 at  $P_4$

$\text{Num}_{P_4} = 1$  Engaged Query sent  $\nabla(2, 4, 3)$

$$|D_{S_{P_4}}| = 1$$

$$\text{Wait}_{P_4} = T$$

Step 4: Since  $P_5$  is not part of knot, so it will not send engaged query.

Step 5: at  $P_3$

$$\text{Num}_{P_3} = 1$$

$$|D_{S_{P_3}}| = 1$$

$$\text{Wait}_{P_3} = T$$

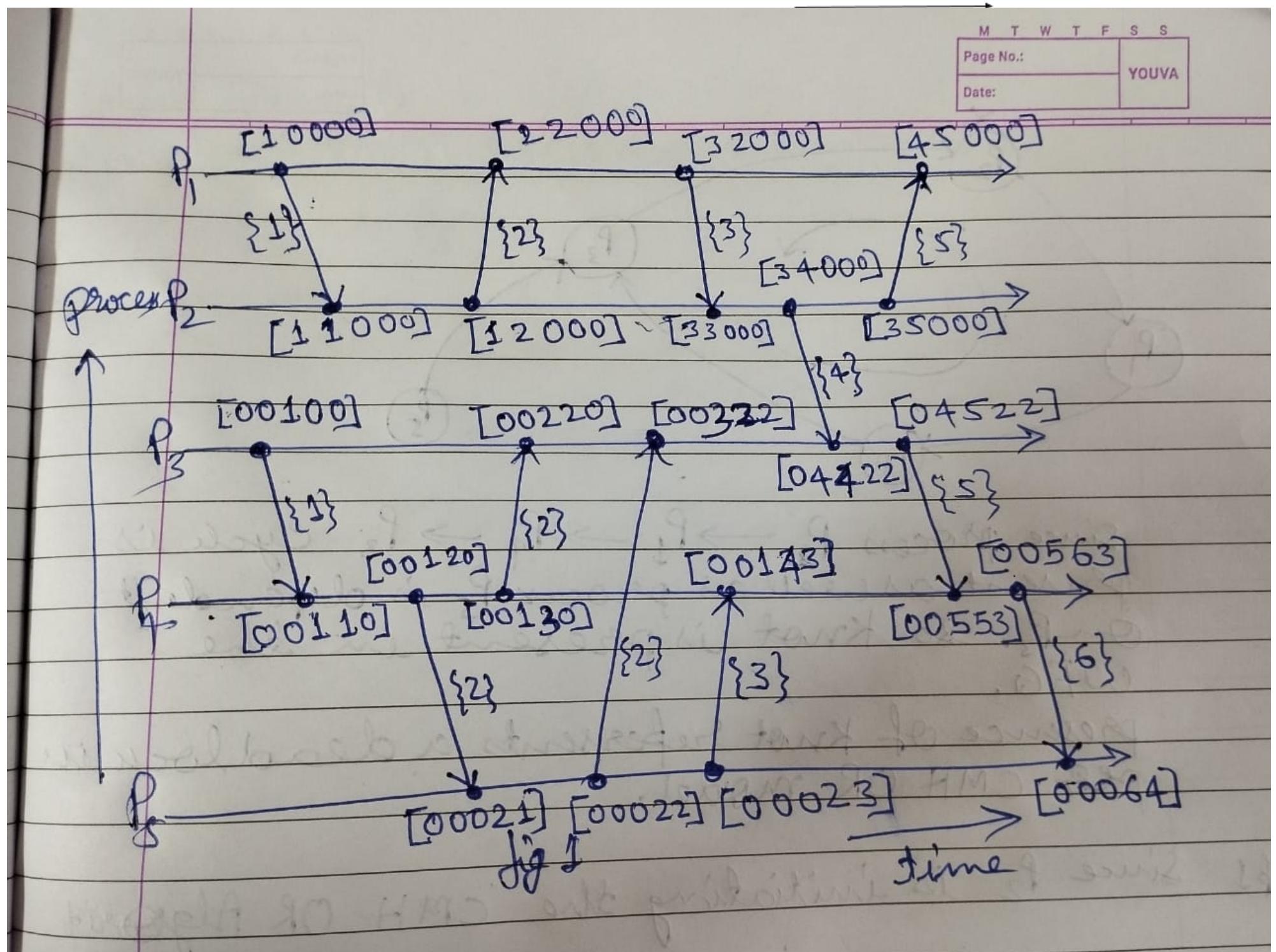
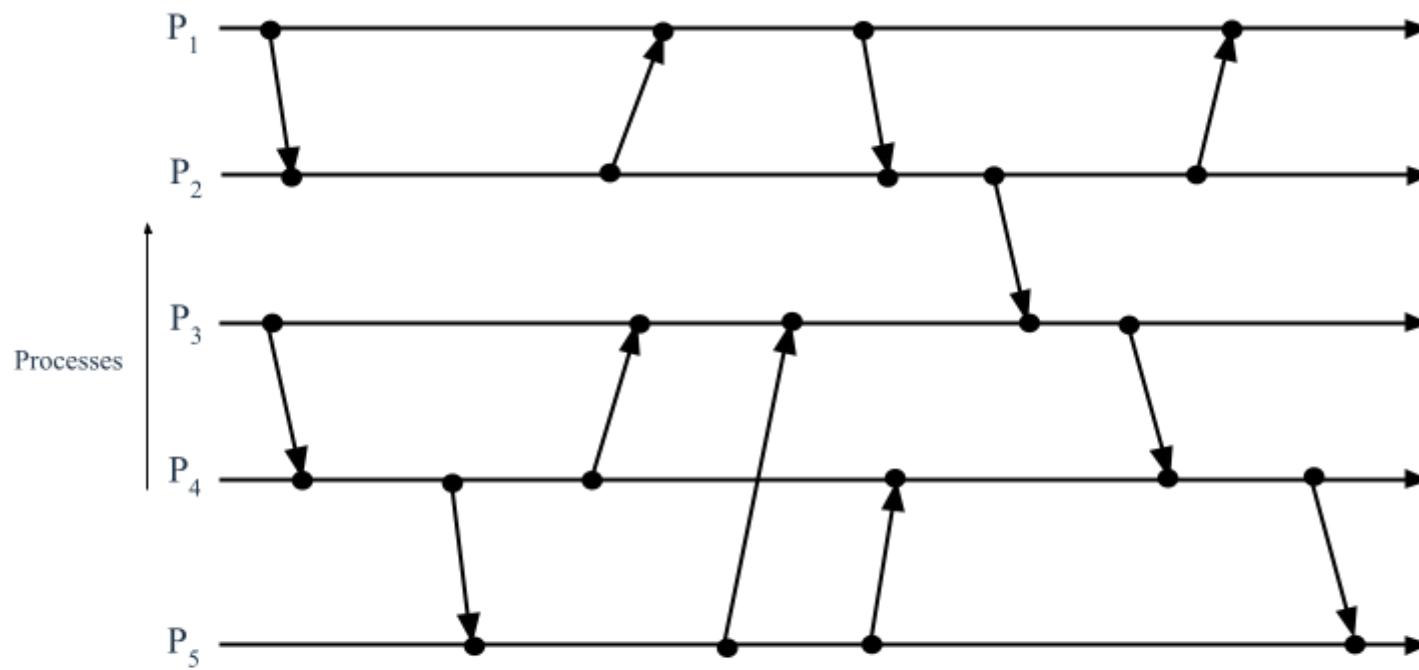
Query sent  $\nabla(2, 3, 2)$   
Engaged query

Step 6:  $P_2$  will send reply message to  $P_3$  as it send Engaged query



Q.1 Set.(A)

Apply Fowler-Zwaenepoel's direct-dependency technique to determine the progress of vector clocks at each of the 5 processes shown in Fig. 1 and also the contents of the messages exchanged among them. Assume that initially the vector clocks of each of the 5 processes is [0 0 0 0] and the increment value  $d = 1$ . [9]



Q.2 Set.(A) Suppose a distributed system consists of 8 processes – P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>, P<sub>5</sub>, P<sub>6</sub>, P<sub>7</sub> and P<sub>8</sub>. Consider the following 4 events –

- e<sub>1</sub> has occurred on P<sub>2</sub> and has a height of 7
- e<sub>2</sub> has occurred on P<sub>5</sub> and has a height of 10
- e<sub>3</sub> has occurred on P<sub>6</sub> and has a height of 7
- e<sub>4</sub> has occurred on P<sub>8</sub> and has a height of 5

You do not have to consider the other events of this distributed system.

Calculate the scalar timestamps of e<sub>2</sub> and e<sub>4</sub>. Assume d = 1 and the scalar clocks of each of the processes before the occurrence of any events in the distributed system was 0.

How will you totally order  $e_1$  and  $e_3$ ? Clearly mention the timestamp representations of the 2 events and the reason for your manner of total ordering.

$$[1 + 2 = 3]$$

Ans:

$e_2$  has height as 10 and value of  $d = 1$ , so scalar timestamp :  $10 + 1 = 11$

$e_4$  has height as 5 and value of  $d = 1$ , so scalar timestamp :  $5 + 1 = 6$

$e_1$  has height as 7 and value of  $d = 1$ , so scalar timestamp :  $7 + 1 = 8$

$e_3$  has height as 7 and value of  $d = 1$ , so scalar timestamp :  $7 + 1 = 8$

So time stamp for  $e_1$  is (8, 1) and  $e_3$  is (8, 3).

Since (8, 1) < (8, 3) as per total ordering second as below:

$$x \prec y \Leftrightarrow (h < k \text{ or } (h = k \text{ and } i < j))$$

So  $e_1 < e_3$

Q 3Set(A) Consider the spanning tree shown in Fig. 2. Each node of this tree stores an integer value. For each node, the node label corresponds to the stored integer value. The objective is to determine the sum of all the integer values stored in the tree. Describe the step-by-step procedure by which the root node notifies all the nodes of the spanning tree to initiate the procedure for computation of the sum of all integers and how the sum is computed over all the integers. Write the steps of the algorithm as is applicable to the given scenario. DO NOT ANNOTATE IN THE DIAGRAM. If you annotate in the diagram without writing the steps of the algorithm, NO MARKS WILL BE AWARDED.

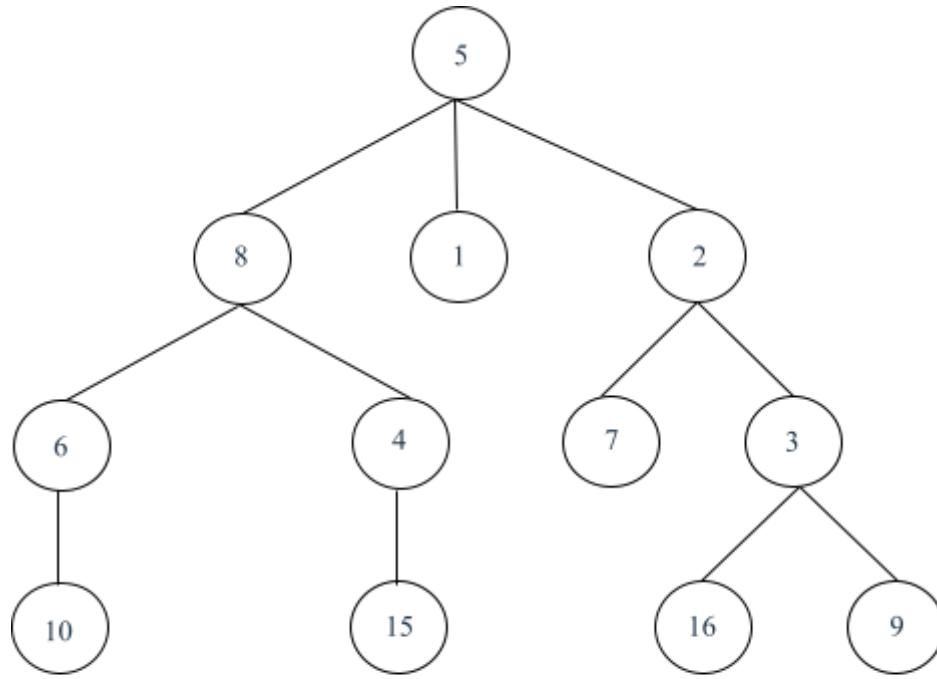
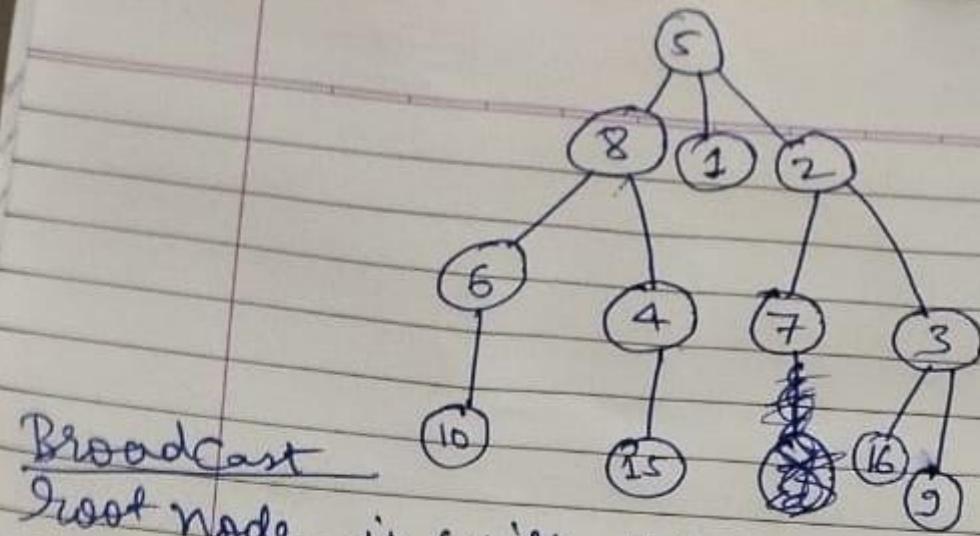


Fig. 2



Broadcast

- ⇒ Root node is with stored value as 5 & labelled as sum.
- ⇒ Root node 5 will send notify to children (to compute sum) 8, 1, 2. Node 8, 2 has further children, so will send notification.
- ⇒ 8 node send notification (to compute sum) to node 6, 4, node 6 further sends notification to 10. node 7 send further to node 15.
- ⇒ 2 node send notification to 7 and 3. Node 3 has children, so send notification further.
- ⇒ 3 node send notification to node 16 and 9.

Converge cast

- ⇒ Node 15 and 9 sends calculated sum as 18 and 9 to parent 3. Node 3 calculates sum as  $3 + 16 + 9 = 28$  and send values to parent 2.
- ⇒ Node 2 gets values from 7 as value 7 & 3 as 28. Calculates sum  $28 + 7 = 37$  and sends to parent 5.
- ⇒ Node 6 gets value as 10 from 10 & sends  $6 + 10 = 16$  to parent node 8.
- ⇒ Node 4 gets values as 15 from 15 & sends  $15 + 4 = 19$  value to parent node 8.
- ⇒ Node 8 gets values as 19 from 4 and 16 from 6 & send value  $8 + 19 + 16 = 43$  to parent 5.

root node (5) receives values as 43 from node (8)  
and 1 from (1), 37 from (2).

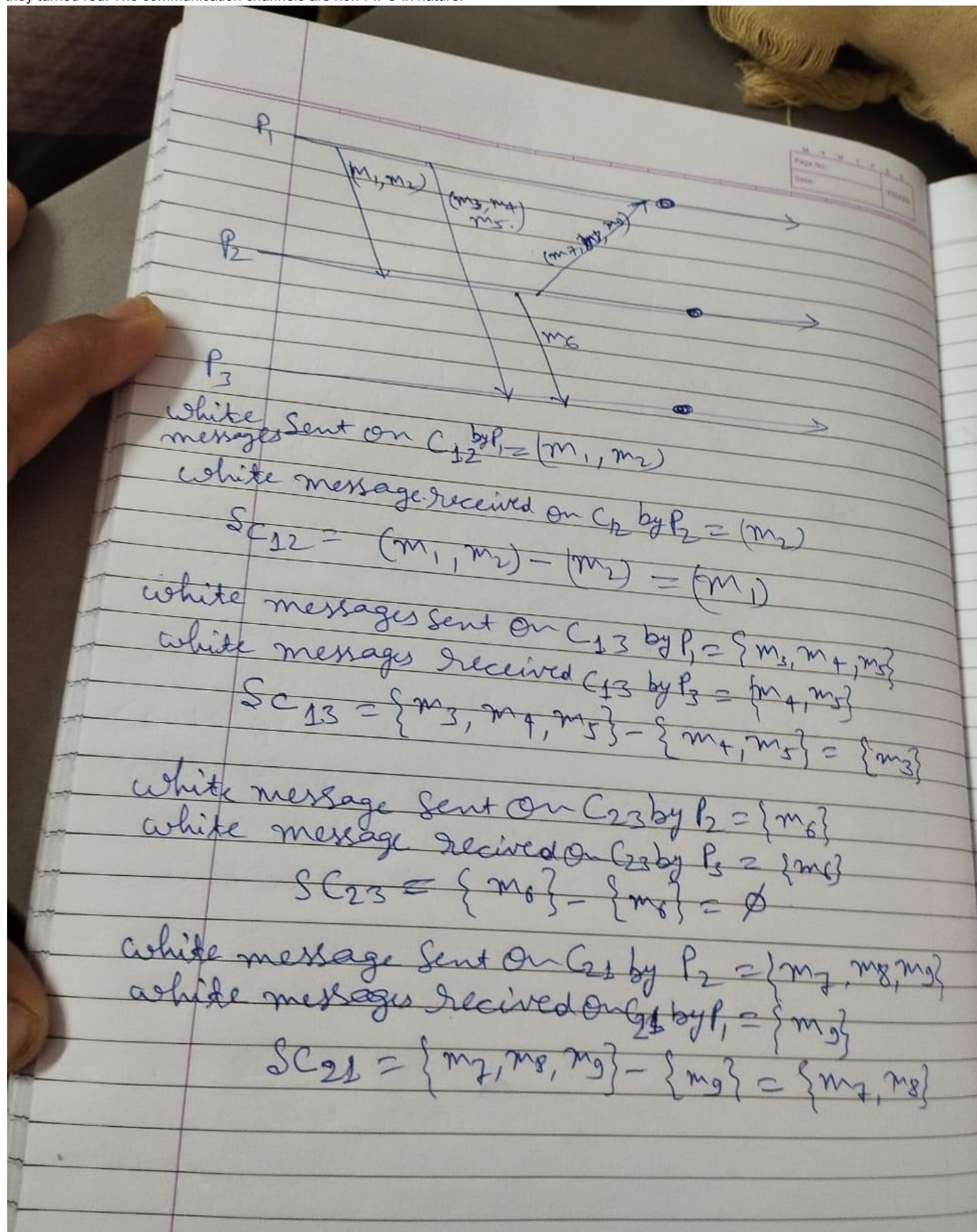
root node calculates final sum as  $5 + 43 + 1 + 37$   
 $= 86.$

Q.4 Set.(A) Consider a distributed system consisting of 3 processes – P1, P2 and P3. The communication channel from P1 to P2 is denoted as  $C_{12}$ , the communication channel from P2 to P1 is denoted as  $C_{21}$ , the communication channel from P1 to P3 is denoted as  $C_{13}$ , the communication channel from P3 to P1 is denoted as  $C_{31}$ , the communication channel from P2 to P3 is denoted as  $C_{23}$ , and the communication channel from P3 to P2 is denoted as  $C_{32}$ . Now consider the following history of white messages exchanged.

- P1 has sent  $m_1$  and  $m_2$  on  $C_{12}$
- P1 has sent  $m_3$ ,  $m_4$  and  $m_5$  on  $C_{13}$
- P2 has sent  $m_6$  on  $C_{23}$
- P2 has sent  $m_7$ ,  $m_8$  and  $m_9$  on  $C_{21}$
- P2 has received  $m_2$  on  $C_{12}$
- P3 has received  $m_4$  and  $m_5$  on  $C_{13}$
- P3 has received  $m_6$  on  $C_{23}$
- P1 has received  $m_9$  on  $C_{21}$

Determine the states of the channels  $C_{12}$ ,  $C_{13}$ ,  $C_{23}$  and  $C_{21}$  using your knowledge of the Lai-Yang algorithm for global snapshot recording. You have to properly show how you are determining each of the channel states along with appropriate justification. Assume that P1, P2 and P3 have turned red and have recorded their respective local states. Note that all the messages mentioned above are white messages and were exchanged among the processes before

they turned red. The communication channels are non-FIFO in nature.



- Q.5 Set.(A) For a synchronous system consisting of 5 Byzantine/faulty processes, what is the minimum total number of processes that should be present in the system so that the Byzantine agreement problem can be solved? Do not simply write the answer. Show your calculations.

If the recursive Byzantine Agreement Tree algorithm is executed on the above synchronous distributed system, then calculate the number of rounds/phases for which the algorithm will execute. Do not simply write the answer. Show your calculations.

Based upon the minimum total number of processes that you had calculated above, determine the total number of messages exchanged in round number 3.  $[1 + 1 + 1 = 3]$

Ans :

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⇒ No. of faulty/Byzantine processes = 5  
 formula for  $\min_{\text{Total nodes}} N = 3m + 1$  (where m is  
 faulty/Byzant  
Proc)  
 minimum no. of proc(N) =  $3 \times 5 + 1 = 16$ .

⇒ for 5 faulty/Byzantine processes recursive calls will be  $O(m^5)$  to  $O(m^0)$   
 So, the number of rounds =  $5 + 1 = 6$

⇒ Total number of messages exchanged in Round 3 =  $(N-1)(N-2)(N-3)$  messages  
 $= (16-1)(16-2)(16-3)$   
 $= 15 \times 14 \times 13 = 2730$  messages

Q.6 Set.(A) Consider a distributed system consisting of 11 processes as depicted in Fig. 3.

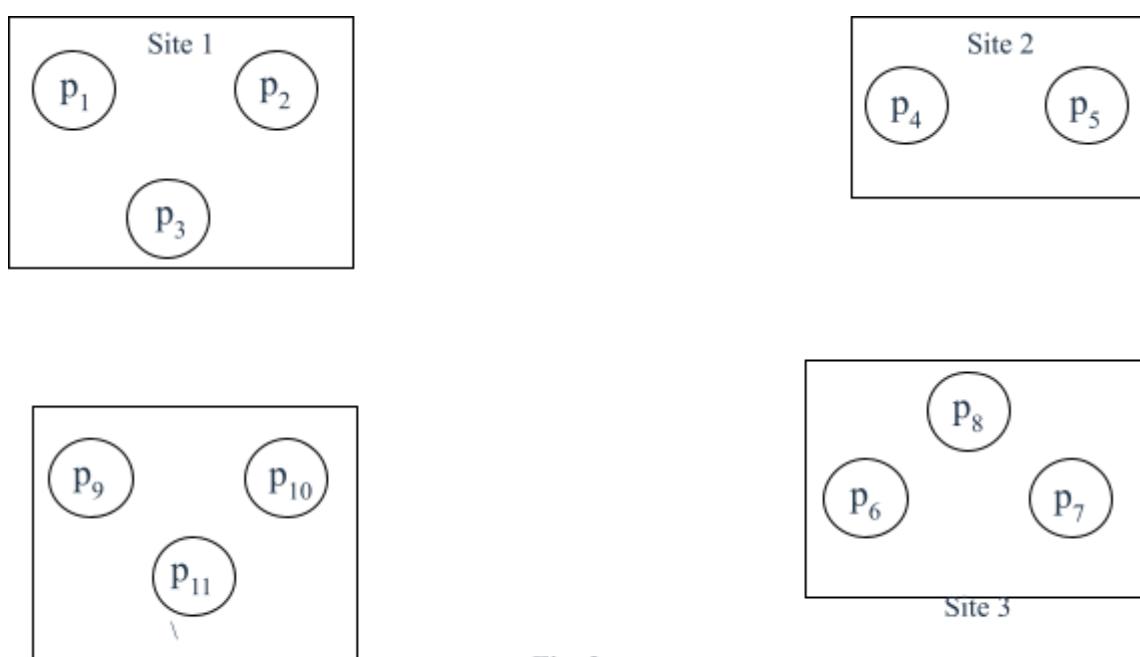


Fig. 3

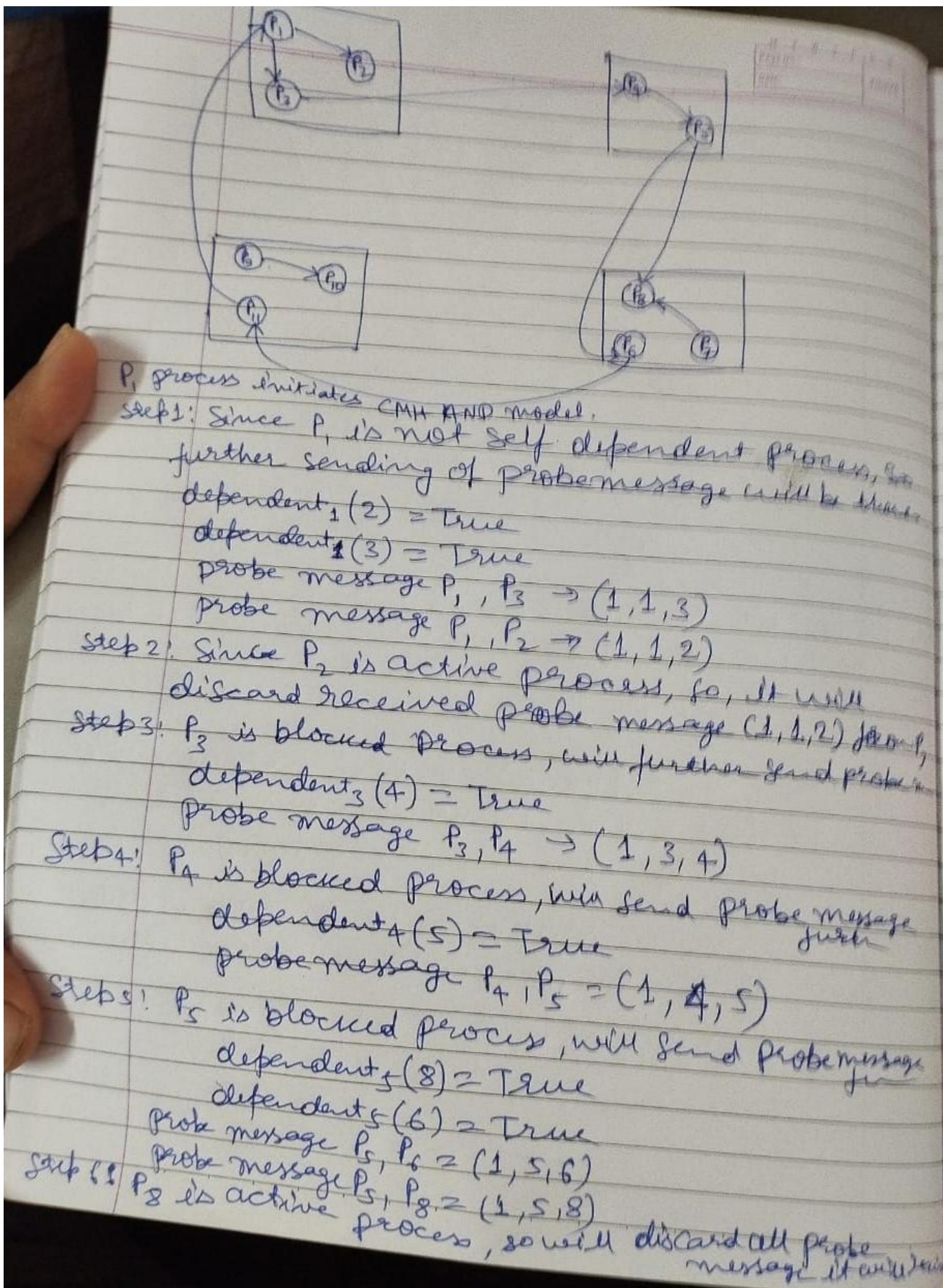
The following dependencies exist among the processes:

- p<sub>1</sub> is blocked and is waiting for p<sub>2</sub> and p<sub>3</sub> to release some resources
- p<sub>3</sub> is blocked and is waiting for p<sub>4</sub> to release some resource
- p<sub>4</sub> is blocked and is waiting for p<sub>5</sub> to release some resource
- p<sub>5</sub> is blocked and is waiting for p<sub>6</sub> and p<sub>8</sub> to release some resources
- p<sub>7</sub> is blocked and is waiting for p<sub>8</sub> to release some resource
- p<sub>6</sub> is blocked and is waiting for p<sub>11</sub> to release some resource
- p<sub>9</sub> is blocked and is waiting for p<sub>10</sub> to release some resource
- p<sub>11</sub> is blocked and is waiting for p<sub>1</sub> to release some resource

Draw the WFG for the above scenario.

Execute Chandy-Misra-Haas algorithm for the AND model on this distributed system to determine whether any deadlock exists in the system. Assume p<sub>1</sub> initiates the deadlock detection and initially, the dependent arrays of all the processes contain false as values. Also, assume that all nodes of the WFG

obtained above are AND nodes. Note that if a deadlock exists, it is to be detected by using the algorithm and not by any other means. Write the steps of the algorithm as is applicable to the scenario given above. DO NOT ANNOTATE IN THE DIAGRAM. If you annotate in the diagram without writing the steps of the algorithm or detect deadlock without applying the algorithm, NO MARKS WILL BE AWARDED.



Step 7:  $P_7$  is not part of global WFG, so will not send probe message

Step 8:  $P_6$  is blocked process and send probe message  
 $\text{dependent}_6(N) = \text{True}$   
 probe message  $P_6, P_{11} = (1, 6, 1)$

Step 9:  $P_9$  and  $P_{10}$  are not part of global WFG, so will not send probe message

Step 10:  $P_{11}$  is blocked and send probe message  
 $\text{dependent}_{11}(1) = \text{True}$   
 probe message  $P_{11}, P_1 = (1, 11, 1)$

Step 11: On receiving probe message  
 as  $(1, 11, 1)$  from  $P_{11}$  to  $P_1$ , since  
 $K = i$  ( $i=1$ ),  $P_1$  will declare deadlock

- Q.7Set.(A) Consider a synchronous distributed system consisting of 8 processes –  $P_1, P_2, P_3, P_4, P_5, P_6, P_7$  and  $P_8$ . Every process puts forth an initial integer value. The initial values put forth by  $P_1, P_2, P_3, P_4, P_5, P_6, P_7$  and  $P_8$  are 1, 3, 4, 4, 2, 3, 1 and 6 respectively. Out of the 8 processes,  $P_2, P_5$  and  $P_7$  are faulty processes and the non-faulty processes are aware of this fact. Using your knowledge of the interactive consistency problem, determine the 8 values of the final agreement array. Assume that for a faulty process, the agreed upon value by all the non-faulty processes is 0. You do not need to consider how many maximum faulty processes can be tolerated by the system. [4]

⇒ Define processes as faulty with doing  
Circle on it.

P<sub>1</sub> - 1

(P<sub>2</sub>) - 3

P<sub>3</sub> - 4

P<sub>4</sub> - 4

(P<sub>5</sub>) - 2

P<sub>6</sub> - 3

(P<sub>7</sub>) - 1

P<sub>8</sub> - 6

with 3 processes as faulty  
minimum no. of total nodes/proc  
expected as  $3 \times 3 + 1 = 10$  processes  
for consensus.

Since except (P<sub>2</sub>), (P<sub>5</sub>), (P<sub>7</sub>) all processes are healthy, so will continue same values further.  
Since agreed values for faulty processes for ~~(P<sub>2</sub>, P<sub>5</sub>, P<sub>7</sub>)~~ non-faulty are 0.

Final values as (1, 0, 4, 4, 0, 3, 0, 6)  
assume P<sub>2</sub> will send \$ value, P<sub>5</sub> will send #, P<sub>7</sub> will send &, P<sub>1</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>2</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>3</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>4</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>5</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>6</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>7</sub> will get (1, \$, 4, 4, #, 3, &, 6)

P<sub>8</sub> will get (1, \$, 4, 4, #, 3, &, 6)

Final values as (1, 0, 4, 4, 0, 3, 0, 6).

as final agreed values for faulty processes to non-faulty process as

Q.8Set.(A) For a Chord ring of  $m = 6$ , the nodes as shown in Fig. 4 are present.

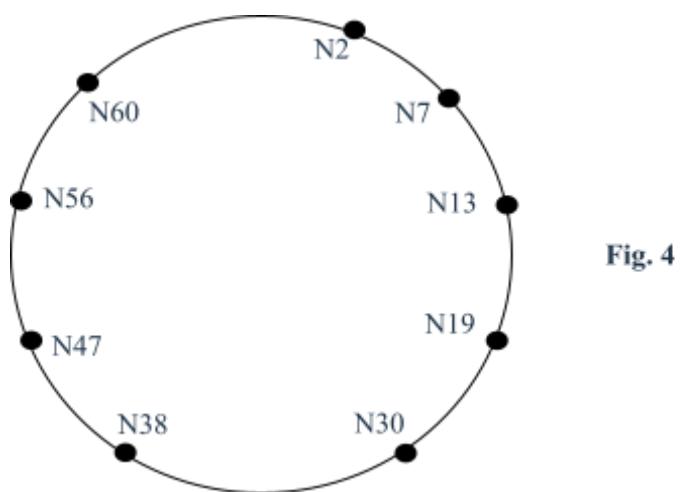


Fig. 4

Consider the following 9 keys – K5, K7, K12, K27, K38, K45, K53, K60 and K62. Identify on which node each of the above mentioned keys will be placed for this Chord ring. You should clearly mention the reason for placing each key on a particular node.

Determine the entries of the finger tables of N7, N19 and N47.

[ $4.5 + 4.5 = 9$ ]

# chord Ring, m=6

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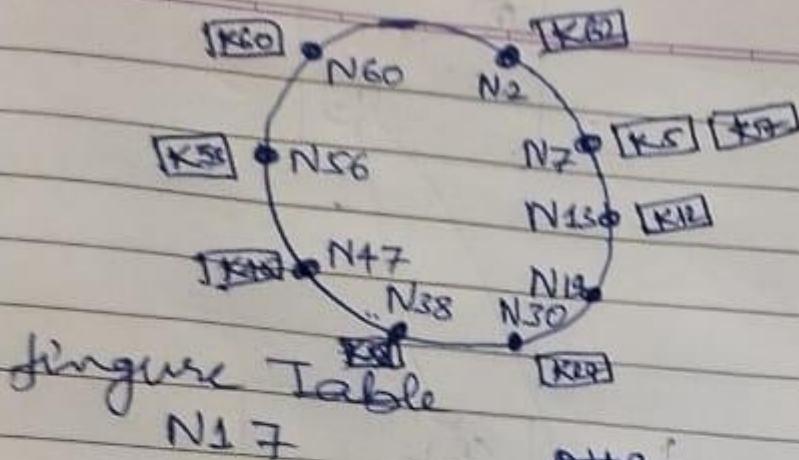


figure Table

N17

$$17 + 1 = 18 \rightarrow N19$$

$$17 + 2 = 19 \rightarrow N19$$

$$17 + 4 = 21 \rightarrow N30$$

$$17 + 8 = 25 \rightarrow N30$$

$$17 + 16 = 33 \rightarrow N38$$

$$17 + 32 = 49 \rightarrow N56$$

~~17 + 67~~

N49

$$19 + 1 = 20 \rightarrow N30$$

$$19 + 2 = 21 \rightarrow N30$$

$$19 + 4 = 23 \rightarrow N30$$

$$19 + 8 = 27 \rightarrow N30$$

$$19 + 36 = 35 \rightarrow N38$$

$$19 + 32 = 51 \rightarrow N56$$

N47

$$47 + 1 = 48 \rightarrow N51$$

$$47 + 2 = 49 \rightarrow N56$$

$$47 + 4 = 51 \rightarrow N56$$

$$47 + 8 = 55 \rightarrow N56$$

$$47 + 16 = 63 \rightarrow N2$$

$$47 + 32 = 79 \rightarrow N19$$

m=6

$$\text{succ}(5) = N7 \leftarrow K5$$

$$\text{succ}(7) = N7 \leftarrow K7$$

$$\text{succ}(12) = N13 \leftarrow K12$$

$$\text{succ}(27) = N30 \leftarrow K27$$

$$\text{succ}(38) = N38 \leftarrow K38$$

$$\text{succ}(45) = N45 \leftarrow K45$$

$$\text{succ}(53) = N56 \leftarrow K53$$

$$\text{succ}(60) = N60 \leftarrow K60$$

$$\text{succ}(62) = N2 \leftarrow K62$$

Keys are as below

K5, K7, K12, K27,  
K38, K45, K53, K60  
and K62.

**Qtext :**

Suppose a synchronous system consists of 10 processes out of which 3 processes are faulty. Assume that the Byzantine agreement tree algorithm is executed on this system.

What will be the total number of rounds for the algorithm? [1]

Each message will be sent to how many nodes in the last round? [1]

Ans: As number of faulty processes are 3, so the number of rounds will be  $3 + 1 = 4$

Number of messages in last round =  $(10-1) * (10-2) * (10-3) * (10-4) = 9 * 8 * 7 * 6 = 3024$

**Qtext :**

A Chord ring with  $m = 8$  contains the following nodes – N10, N25, N42, N56, N80, N101, N137, N159, N210, N242, and N251.

The chord ring contains the following keys – K10, K57, K201 and K230. Identify on which node each of the above-mentioned keys will be placed for this Chord ring. You should clearly mention the reason for placing each key on a particular node. You are not required to draw any diagram for answering this question. [4]

Suppose for this Chord ring, a lookup for K230 is initiated at N101. Describe the step-by-step procedure by which K230 can be located using the simple lookup algorithm. Write the steps of the algorithm clearly in text. You are not required to draw any diagram. If you answer this question by only drawing a diagram, no marks will be awarded. [4]

**Ans :**

$m = 8$ ;

Successor (10) = N10 ==> K10

Successor (57) = N80 ==> K57

Successor (201) = N210 ==> K201

Successor (230) = N242 ==> K230

