

Demand and Pricing for Telecom Services with Network and Price Effects

Q3) How does Apple manage to continuously increase the price of iPhones over the years?

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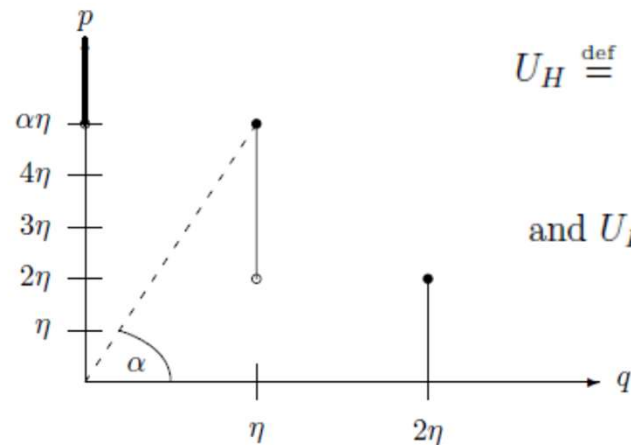
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Chapter 5 “Telecommunications”, In Shy, Oz (1999). *The Economics of Network Industries*,
Cambridge University Press.

Kinked Demand Curves and Critical Mass

- Monopoly Service Provider
- Utility as a function of the network size and price
 - H: η number of High Value Subscribers
 - L: η number of Low Value Subscribers
 - $\alpha > 4$

Groups of users behave similarly



$$U_H \stackrel{\text{def}}{=} \begin{cases} \alpha q - p & \text{connected} \\ 0 & \text{disconnected} \end{cases}$$

$$\text{and } U_L \stackrel{\text{def}}{=} \begin{cases} q - p & \text{connected} \\ 0 & \text{disconnected,} \end{cases} \quad (5.1)$$

Price Ranges



Low-price range ($0 \leq p < 2\eta$): At this range, the quantity demanded is unique at the level of 2η consumers. To see this we need to show that both types of consumers gain a nonnegative utility. That is, $U_H = \alpha(2\eta) - p > 0$ and that $U_L = 2\eta - p > 0$, which follow directly from (5.1).

Medium-price range ($2\eta < p \leq \alpha\eta$): At this range the consumer equilibrium involves only the type H consumers, whereas the type L are better off not buying. Suppose that $q = \eta$; then $U_H = \alpha\eta - p > 0$. However, even if all type L consumers also subscribe, $U_L = 2\eta - p < 0$, hence $q = \eta$ constitutes a consumer equilibrium at this price range.

High-price range ($p > \alpha\eta$): In this range no one subscribes since $U_H = \alpha\eta - p < 0$ and $U_L = 2\eta - p < 0$.

Social Welfare



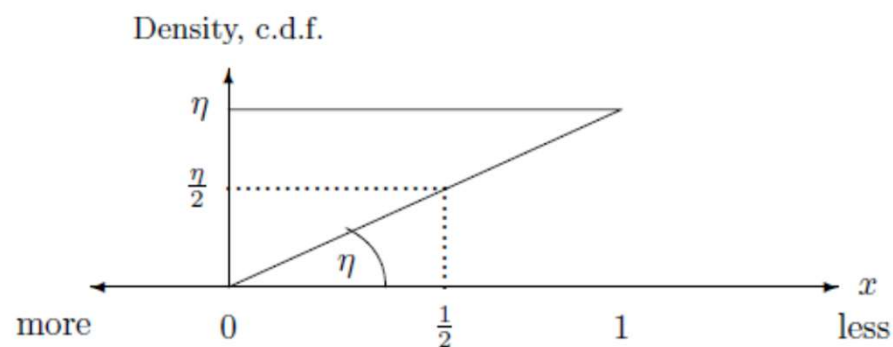
$$\begin{aligned} W &\stackrel{\text{def}}{=} \eta U_H + \eta U_L + \pi && (5.5) \\ &= \begin{cases} \eta(\alpha\eta - p) + \eta 0 + \eta(p - \mu) - \phi & H \text{ connect} \\ \eta(\alpha 2\eta - p) + \eta(2\eta - p) + 2\eta(p - \mu) - \phi & \text{All connect} \end{cases} \\ &= \begin{cases} \alpha\eta^2 - \eta\mu - \phi & \text{Only } H \text{ connect} \\ 2\eta^2(\alpha + 1) - 2\eta\mu - \phi & \text{All connect.} \end{cases} \end{aligned}$$

Problem



- No. of High-value customers: 200
- No. of low-value customers: 400
- Utility function of high-value customers: $5q-p$
- Utility function of low-value customers: $q-p$
- Derive the kinked demand curve
- What is the net utility of each type of customers
- What is the profit (assuming cost of zero) for service providers
- What is the Social Welfare?

Demand for Telecom Services: Calculus Analysis

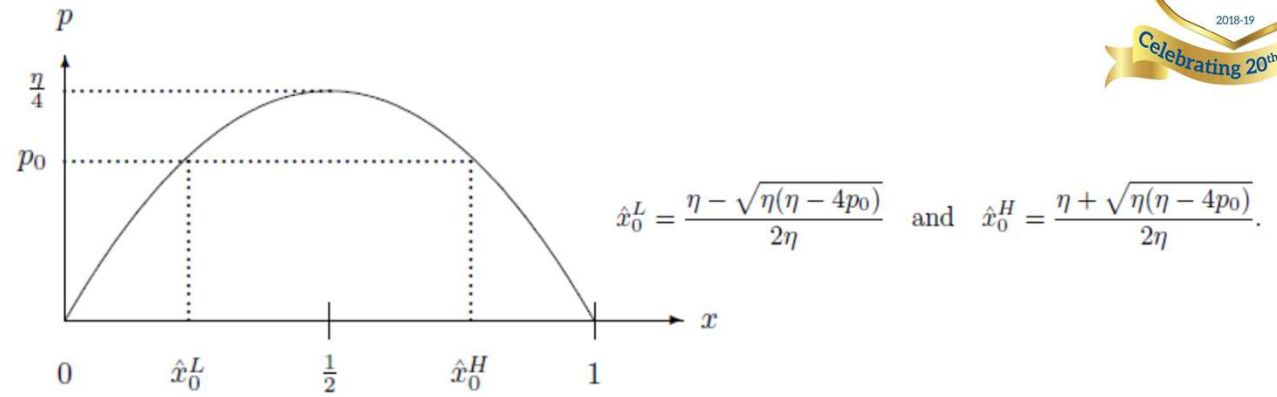


$$U_x = \begin{cases} (1-x)q^e - p & \text{if she subscribes} \\ 0 & \text{if she does not subscribe,} \end{cases}$$

$$0 = (1-\hat{x})q^e - p, \quad \text{or} \quad \hat{x} = \frac{q^e - p}{q^e}$$

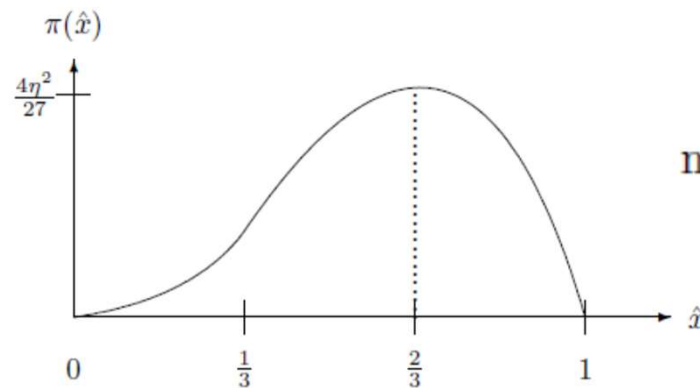
$$p = (1-\hat{x})\eta\hat{x}$$

Demand for Telecom Services



- **Low levels: High-valuation customers subscribe to network**
 - Smaller network size
 - Network effect dominates the price effect (inverse of typical downward sloping demand curve)
- **High levels: Low-valuation customers also subscribe**
 - Larger network size
 - Price effect dominates the network effect (downward sloping demand curve)

Profit Maximizing Monopoly



$$\max_{\hat{x}} \pi(\hat{x}) \stackrel{\text{def}}{=} p\eta\hat{x} = (1 - \hat{x})(\eta\hat{x})^2.$$

- A monopoly phone company maximizes its profit by setting its connection fee so that the number of customers exceeds half of the consumer population but is less than the entire population.

Connection cost case



$$\max_{\hat{x}} \pi(\hat{x}) \stackrel{\text{def}}{=} (p - \mu)\eta\hat{x} - \phi = [(1 - \hat{x})(\eta\hat{x}) - \mu]\eta\hat{x} - \phi,$$

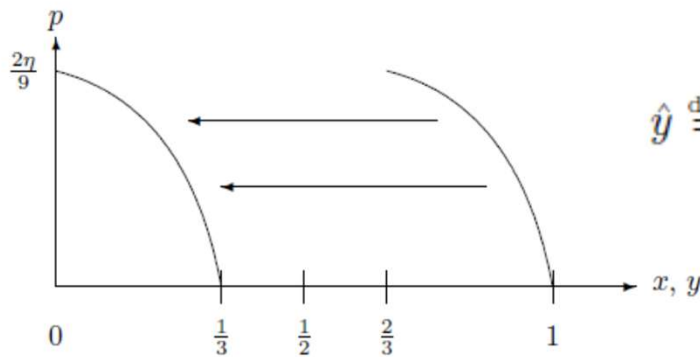
$$\hat{x} = \frac{\eta + \sqrt{\eta(\eta - 3\mu)}}{3\eta}.$$

Invitations to Enter



- Realization of network externalities by a monopoly requires a high output
 - Monopolist may be unable to commit to higher output
- May license the technology to a number of firms and invites them to enter and compete
- Competition Effect vs. Network Effect
 - Competitive effect: Expected increase in competition because of the increase in number of firms
 - Network Effect: Increases willingness to pay
- Invite when network effect > competitive effect

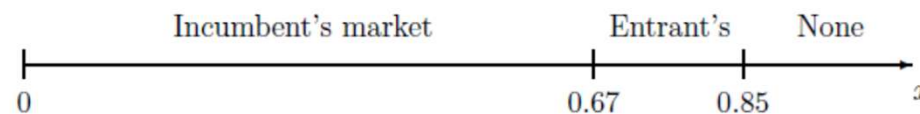
Second Entrant case



$$\hat{y} \stackrel{\text{def}}{=} \hat{x} - \frac{2}{3} = \frac{\eta + \sqrt{\eta(\eta - 4p_0)}}{2\eta} - \frac{2}{3}.$$

$$p = \frac{\eta(2 - 3\hat{y} - 9\hat{y}^2)}{a}, \quad \text{hence} \quad \pi = \frac{\eta(2 - 3\hat{y} - 9\hat{y}^2)}{a} \eta \hat{y}.$$

$$\hat{y} = \frac{\sqrt{7} - 1}{9} \approx 0.182, \quad p = \frac{\eta(23 - \sqrt{7})}{81} \approx 0.128, \quad \pi = \eta^2 \frac{14\sqrt{7} - 20}{729}. \quad (5.20)$$



Entry of New Service Providers



- Entry into the telecommunication industry increases the utility of old and newly connected consumers, as well as the profit of the entering firm.
 - The proposition follows from the fact that old users gain because of the increase in the network size; new users gain because they are connected to this service; and the entering firm makes above normal profit.

How does Apple manage to continuously increase the price of iPhones over the years?
What is the pricing strategy behind iPhone 7, iPhone 7 Plus, iPhone X

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Leveraging Network Effect of one product in another



- Initially, there are profits to be made in both markets.
- But subsidizing market one with a free good can increase demand and profits in market two more than the loss in market one.

