Control System - 1

Nyquist Problem

Ques 1. A unity feedback system has a loop transfer function

G(s) = 50

(s H)(s+2)

Use myg nyquist criteria to comment on its stability

Ans) G(s) = 50 (s+1)(s+2)

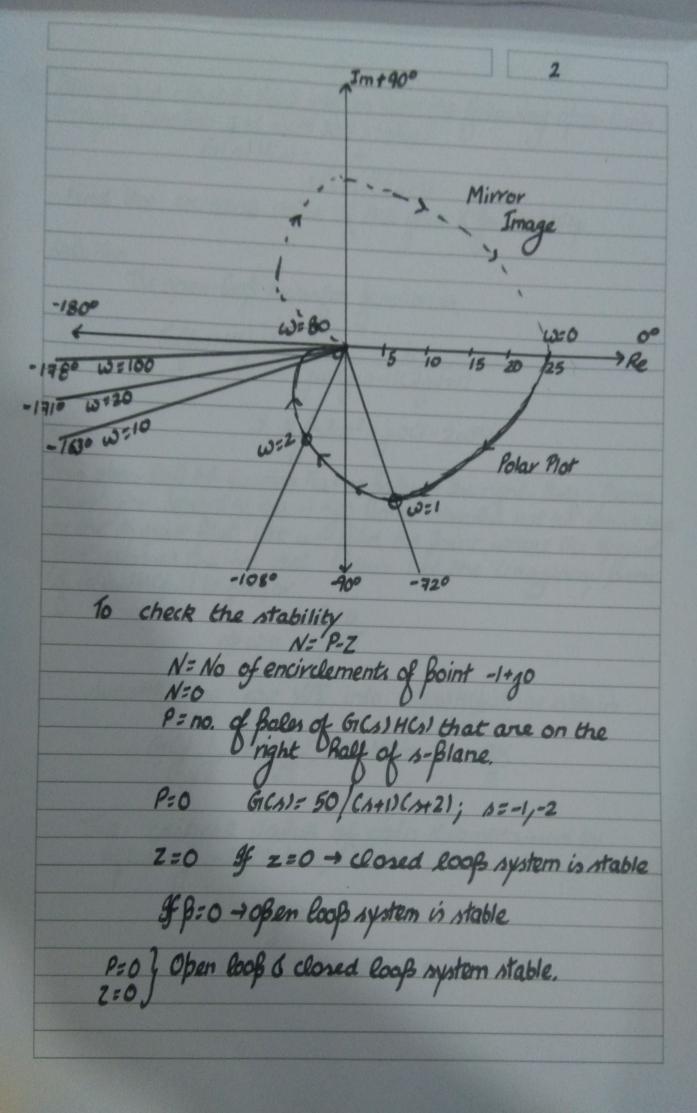
G(Jw) - 50/ (jw+1)(jw+2)

M = | GGW) = 50 / [1+w2 54+w2

 $\phi = \tan^{-1}(\omega) - \tan^{-1}(\omega | \omega) - \omega$

w varies from 0 to 00

SNO $W = |4G|w| = \phi$ 1. $O = 2F = D^{\circ}$ 2. $I = I6 = -72^{\circ}$ 3. $2 = 8 = -108^{\circ}$ 4. $I0 = 0.5 = -168^{\circ}$ 5. 20 = 0.1 = -17106° $100 = 0.05 = -180^{\circ}$

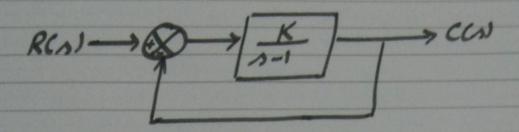


Pr) Below is a closed-loop system with the following open-loop transfer function and with K=2 stable?

G(s)H(s) = K Find the critical value of the gain K for stability. Solution. The open-loop transfer function is $G(j\omega)H(j\omega)=\frac{K}{j\omega Cj\omega-1)(2j\omega+1)}$ = K/-3w2+jwc1-2w2) This open-loop tif. function has no boles in the right-Roll's Blane.
Thus, for stability, the -1 + jo Boint should not be encircled Blot absses the -ive real Danis. Let the imaginary Bant of Gi(jw)H(jw) be zero,ov 1-242=0 => w= ± 1/52 substitutiong w= 1/52 into G(jw)H(jw), we obtain GIG 1 HG 1, we obtain = -2K The critical value of gain K is obtained by equating -2K/3 to-1, 00 or -2 K=-1

Hence K = 3/2 = 1.5

The system is stable if OKK(3/2. Hence, the systemwith K=2 is unstabble



Consider the closed loop system as show.