

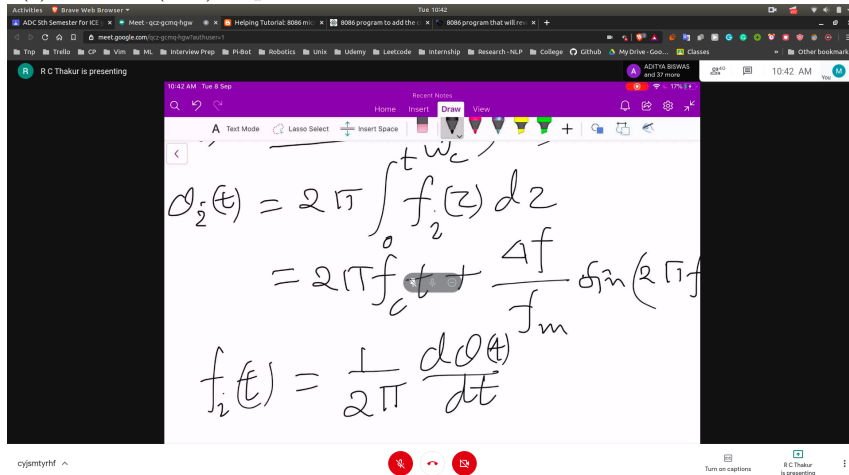
Analysis of FM and PM

Modulation Index in FM and PM

- We have assumed $m(t)$
 - $m(t) = A_m \cos(\omega_m * t)$
- $f(t) = f_c + K * A_m \cos(\omega_m * t)$

Frequency Deviation

- $\Delta f = K * A_m$
- Δf can take values max and min depending on the values of magnitude of $m(t)$
- $c(t) = A_c \cos(\omega_c t + \phi_0)$



- here $\Delta f/f_m$ will be called modulation index \Rightarrow beta
- if beta is small then it is called -> **Narrow Band**
- if beta is large then it is called -> **Wide Band**

Carrier Wave

- The final carrier wave can be written as

various i → Wideband

$$C(t) = A_c \cos[2\pi f_c t + \beta \sin 2\pi f_m t]$$

- Expanded form

$$C(t) = A_c \cos[2\pi f_c t + \beta \sin 2\pi f_m t]$$

$$= A_c \cos(2\pi f_c t) \cos(\beta \sin 2\pi f_m t) - A_c \sin(2\pi f_c t) \sin(\beta \sin 2\pi f_m t)$$

$$\approx A_c \cos(2\pi f_c t) \left[1 - \frac{\beta^2 \sin^2(2\pi f_m t)}{2} \right] - A_c \sin(2\pi f_c t) \left[\beta \sin 2\pi f_m t - \frac{\beta^3 \sin^3(2\pi f_m t)}{6} \right]$$

For Narrow Signal

- $\cos(\theta) \rightarrow 1$
- $\sin(\theta) \rightarrow \theta$

$$C(t) = A_c \cos(2\pi f_c t + \beta) + B \sin(2\pi f_m t)$$

$$= A_c \cos(2\pi f_c t) \cdot \cos(\beta) + B \sin(2\pi f_m t)$$

$$\text{If } \beta \ll \frac{\pi}{2} \Rightarrow \sin(\frac{\pi}{2} - \beta) \approx \cos(\beta)$$

$$= A_c \cos(2\pi f_c t) \cdot \cos(\beta) + B \sin(2\pi f_m t)$$

$$= A_c \cos(2\pi f_c t) \cdot \cos(\beta) + B \sin(2\pi f_m t)$$

In terms of freq band

