LATEX ASSIGNMENT

ANAND

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EXERCISE 12.11.4

- 1. Show that the link joining the origin to the point (2, 1, 1) is perpendicular to the point (2, 1, 1) is perpendicular to the line determined by the points (2, 1, 1) is perpendicular to the line determined by the points (3, 5, -1), (4, 3, -1).
- 2. If l_1, m_1, n_1 and l_2, m_2, n_2 are the direction cosines of two mutually perpendicular lines, show that the direction cosines of the line perpendicular to Both of these are $m_1n_2 m_2n_1, n_1l_2 n_2l_2 n_2l_1, l_1m_2 l_2m_1$.
- 3. Find the angle between the lines whose direction ratios are a, b, c and b c, c a, a b.
- 4. Find the equation of a line parallel to x-axis and passing through the origin.
- 5. If the co-ordinates of the points A, B, C, D be (1, 2, 3), (4, 5, 7), (-4, 3, -6) and (2, 9, 2) respectively, then find the angle between the lines AB and CD.
- 6. If the lines $\frac{x-1}{-3} = \frac{y-2}{2k} = \frac{z-3}{2}$ and $\frac{x-1}{3k} = \frac{y-1}{1} = \frac{z-6}{-5}$ are perpendicular, Find the value of k.
- 7. Find the vector equation of the line passing through (1, 2, 3) and perpendicular to the plane $\overrightarrow{y} \cdot (\hat{i} + 2\hat{j} 5\hat{k}) + 9 = 0$.
- 8. Find the equation of the plane passing through (a, b, c) and parallel to the plane $\overrightarrow{r}(\hat{i} + \hat{j} + \hat{k}) = 2$.
- 9. Find the shortest distance between the lines $\vec{r} = 6\hat{i} + 2\hat{j} + 2\hat{k} + \lambda(\hat{i} 2\hat{j} + 2\hat{k})$ and $\vec{r} = 4\hat{i} \hat{k} + \mu(3\hat{i} 2\hat{j} 2\hat{k})$.
- 10. Find the co ordinates of the point where the line through (5, 1, 6) and (3, 4, 1) crosses the YZ-plane.
- 11. Find the co ordinates of the point where the line through (5, 1, 6) and (3, 4, 1) crosses the ZX-plane.
- 12. Find the co ordinates of the point where the line through (3, -4, -5) and (2, -3, 1) crosses the plane 2x + y + x = 7.

- 13. Find the equation of the plane passing through the point (-1, 3, 2) and perpendicular to each of the planes x + 2y + 3z = 5 and 3x + 3y + z = 0.
- 14. If the points (1, 1, p) and (-3, 0, 1) be equidistant from the plane $\overrightarrow{r} \cdot (3\hat{i} + 4\hat{j} 12\hat{k}) + 13 = 0$, then find the value of p.
- 15. Find the equation of the plane passing through the line of intersection of the planes $\vec{r} \cdot (\hat{i}\hat{j} + \hat{k}) = 1$ and $\vec{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 1$ and $\vec{r} \cdot (2\hat{i} + 3\hat{j} \hat{k}) + 4 = 0$ and parallel to *x*-axis.
- 16. If 0 be the origin and the coordinates of p be (1, 2, -3), then find the equation of the plane passing through P and perpendicular to OP.
- 17. Find the equation of the plane which contains the line of intersection of the planes $\vec{r} \cdot (2\hat{i} + \hat{j} \hat{k}) + 5 = 0$ and which is perpendicular to the plane $\vec{r} \cdot (5\hat{i} + \hat{j} 6\hat{k}) + 8 = 0$
- 18. Find the distance of the point (-1, -5, -10) from the point of intersection of the line $\overrightarrow{r} = 2\hat{i} \hat{j} 2\hat{k} + \lambda(3\hat{i} + 4\hat{j} + 2\hat{k})$ and the plane $\overrightarrow{r} \cdot (\hat{i} \hat{j} + \hat{k}) = 5$.
- 19. Find the vector equations of the line passing through the point (1, 2, -4) and perpendicular to the two lines:

$$\frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7} \text{ and } \frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}.$$
 (1)

20. Prove that if a plane has the intercept a, b, c and is at a distance of p units from the origin, then

$$\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} = \frac{1}{p^2}.$$
 (2)

Choose the correct answer in Excercises ?? and ??

- 21. Distance between the two planes: 2x + 3y + 4z = 4 and 4x + 6y + 8z = 12 is
 - (a) 2 units
 - (b) 4 units
 - (c) 8 units
 - (d) $\frac{2}{\sqrt{29}}$ units
- 22. The planes: 2x y + 4z = 5 and 5x 2.5y + 10z = 6 are
 - (a) Perpendicular
 - (b) Parallel
 - (c) Intersect y axis
 - (d) Passes through $[0, 0, \frac{5}{4}]$