

Sep 2022

MATRIX ASSIGNMENT

0.1 Problem:

Construct a triangle ABC in which $BC = 7\text{cm}$, $\angle B = 75^\circ$ and $AB + AC = 13\text{ cm}$.

0.2 Solution:

Theory:

Construct a triangle ABC in which $BC = 7\text{cm}$, $\angle B = 75^\circ$ and $AB + AC = 13$

To Prove:

- Draw base $BC = 7\text{cm}$, and at point, B make an angle $\angle CBX$ of $\angle B = 75^\circ$ using a protractor.
- With B as center and radius $BD = 13\text{ cm}$, draw an arc to intersect ray BX at D.
- Join DC.
- Let's construct a perpendicular bisector of DC. With D and C as the center and radius greater than half of DC, draw arcs above and below the line DC to intersect ray BX at A.
- Join AC.

ABC is the required triangle.

Verification:

On measuring we see that, $BC = 7\text{cm}$, $\angle B = 75^\circ$ and $AB + AC = 13\text{cm}$

0.3 TermuxCommands:

`python3 matrix.py`

To Prove:

Given BC length is $a = 7\text{cm}$, so the coordinates of B are $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

X_1, Y_1 respectively and the coordinates of C are, $\begin{pmatrix} a \\ 0 \end{pmatrix}$

X_3, Y_3 respectively and also given the angle is $B = 75^\circ$, so by finding the coordinates of the other side we can form a required triangle.

Calculating Other Coordinate:

Let the coordinates of A are X_2, Y_2 respectively.

Let $A = \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix}$

Using the Cosine formula in $\triangle ABC$,
 $b^2 = a^2 + c^2 - 2ac \cos B$.

$$(b+c)(b-c) = a^2 - 2 \times a \times 0.25c$$

$$b - 1.26c = 3.76 \dots 1$$

Upon Simplification we get:-

$$b + c = 13 \dots 2$$

and the above 2 equations can be written as:-

$$\begin{pmatrix} 1 & -1.26 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} b \\ c \end{pmatrix} = \begin{pmatrix} 3.76 \\ 13 \end{pmatrix}$$

$$\text{from this, } \begin{pmatrix} b \\ c \end{pmatrix} = \begin{pmatrix} 5.333 \\ 7.66 \end{pmatrix}$$

Thus, the vertices of $\triangle ABC$ are

$$\text{Let } A = 7.66 \begin{pmatrix} \cos 75^\circ \\ \sin 75^\circ \end{pmatrix}$$

$$\text{Let } B = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$\text{Let } C = \begin{pmatrix} 7 \\ 0 \end{pmatrix}$$

The below python code realizes the above construction:

<https://github.com/manasareddy442002/fwc-moudle1/blob/master/matrix-lines/matrix.py>

0.4 Construction

