

Sep 2022

MATRIX ASSIGNMENT

0.1 Problem:

Construct a triangle ABC in which $BC=7\text{cm}$, $\angle B = 75^\circ$ and $AB + AC = 13 \text{ cm}$.

$$\begin{pmatrix} 1 & -1.26 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} b \\ c \end{pmatrix} = \begin{pmatrix} 3.76 \\ 13 \end{pmatrix}$$

$$\begin{pmatrix} b \\ c \end{pmatrix} = \begin{pmatrix} 5.333 \\ 7.66 \end{pmatrix}$$

The vertices of ΔABC are

$$\mathbf{A} = c \begin{pmatrix} \cos 75^\circ \\ \sin 75^\circ \end{pmatrix} = \begin{pmatrix} 1.33 \\ 5.15 \end{pmatrix}$$

$$\mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$\mathbf{C} = \begin{pmatrix} 7 \\ 0 \end{pmatrix}$$

Below python code realizes the above construction :

<https://github.com/manasareddy442002/fwc-moudle1/blob/matrix-lines/matrix.py>

0.2 Solution

The input parameters for this construction are

Symbol	Value	Description
BC	a	where a is 7cm
AB	b	AB distance is b
AC	c	AC distance is c
$\angle BC$	75°	ΔABC
\mathbf{C}	$\begin{pmatrix} a \\ 0 \end{pmatrix}$	BC length is equal to a
\mathbf{A}	$\begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix}$	using the cosine formula in ΔABC

termux commands :

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bash line.sh.....using shell command
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Caluclating Other Coordinate:

Let the coordinates of A are X_2, Y_2 respectively.

$$\text{Let } \mathbf{A} = \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix}$$

Using the Cosine formula in ΔABC ,

$$b^2 = a^2 + c^2 - 2accosB \quad (1)$$

$$(b+c)(b-c) = a^2 - 2 \times a \times 0.25c \quad (2)$$

Upon Simplifaction we get:-

$$b - 1.26c = 3.76 \quad (3)$$

$$b + c = 13 \quad (4)$$

From the above, we obtain the matrix equation:-

0.3 Construction

