CS343: Data Communication



Spread Spectrum

by

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Spread Spectrum



- Essential idea is to spread the information signal over a wider bandwidth
- Modulation using spreading sequence is performed
 - To increase significantly the bandwidth (spread the spectrum) of the signal to be transmitted
- It is an important form of encoding for wireless communications
- It can be used to transmit either analog or digital data, using an analog signal

Types:

- frequency hopping spread spectrum (FHSS)
- direct sequence spread spectrum (DSSS)

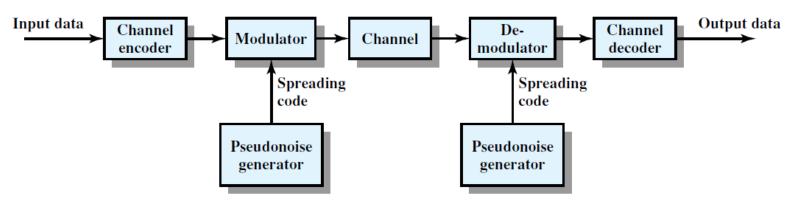


Figure 9.1 General Model of Spread Spectrum Digital Communication System

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- Pseudorandom numbers
 - generated by an algorithm using some initial value called the seed
 - produce sequences of numbers that are not statistically random, but passes reasonable tests of randomness
 - unless you know the algorithm and the seed, it is impractical to predict the sequence

- Gain from this apparent waste of spectrum
 - The signals gains immunity from various kinds of noise and multipath distortion.
 - Immune to jamming attack
 - It can also be used for hiding and encrypting signals.
 - Several users can independently use the same higher bandwidth with very little interference. (e.g. CDMA)

FHSS

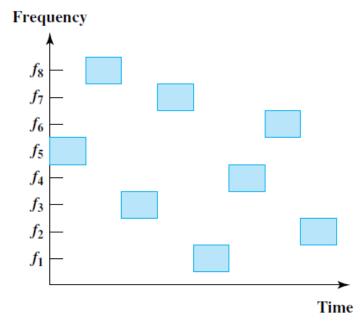


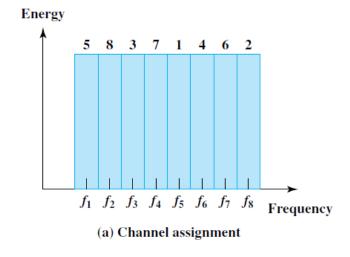
the signal is broadcast over a seemingly random series of radio frequencies, hopping from frequency to frequency at fixed intervals.

 The transmitter operates in one channel at a time for a fixed interval

 A receiver, hopping between frequencies in synchronization with the transmitter, picks up the message

 width of each channel usually corresponds to the bandwidth of the input signal





BFSK



BFSK modulated signal:

$s(t) = \begin{cases} A\cos(2\pi f_1 t) & \text{binary 1} \\ A\cos(2\pi f_2 t) & \text{binary 0} \end{cases}$

where f_1 and f_2 are typically offset from the carrier frequency f_c by equal but opposite amounts

BFSK modulated signal:

$$s_d(t) = A\cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f)t)$$
 for $iT < t < (i + 1)T$

where

A =amplitude of signal

 f_0 = base frequency

 b_i = value of the *i*th bit of data (+1 for binary 1, -1 for binary 0)

 Δf = frequency separation

T = bit duration; data rate = 1/T

Thus, during the *i*-th bit interval, the frequency of the data signal is:

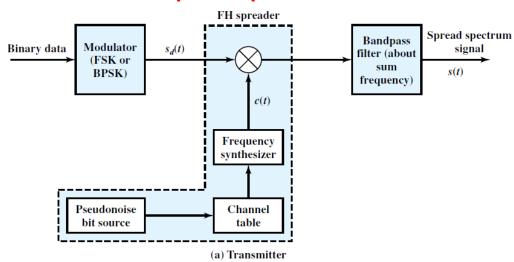
 f_0 if the data bit value is -1 $f_0+\Delta f$ if the data bit value is +1

FHSS



FSK + Spread Spectrum

The frequency synthesizer generates a constant-frequency tone whose frequency hops among a set of 2^k frequencies, with the hopping pattern determined by k bits from the PN sequence.



product of data signal and spreading signal during the i-th hop (during the i-th bit) is

$$p(t) = s_d(t)c(t) = A\cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f)t)\cos(2\pi f_i t)$$

$$= 0.5A \left[\cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f + f_i)t) + \cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f - f_i)t)\right]$$

where f_i is the frequency of the signal generated by the frequency synthesizer during the i-th hop

A bandpass filter blocks the difference frequency and pass the sum frequency, we get the FHSS signal: $s(t) = 0.5A \cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f + f_i)t)$

Cont...



Thus, during the *i*-th bit interval, the frequency of the data signal is

$$f_0 + f_i$$
 if the data bit value is -1 $f_0 + f_i + \Delta f$ if the data bit value is +1

At the receiver: multiplied by a replica of the spreading signal

$$s(t)c(t) = 0.5A\cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f + f_i)t)\cos(2\pi f_i t)$$

$$= 0.25A[\cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f + f_i + f_i)t) + \cos(2\pi(f_0 + 0.5(b_i + 1) \Delta f)t)]$$

A bandpass filter blocks the sum frequency and pass the difference frequency, we get the data signal:

$$s_d(t) = 0.25A\cos(2\pi(f_0 + 0.5(b_i + 1)\Delta f)t)$$

FHSS Using MFSK



- Multiple FSK uses $M=2^{L}$ different frequencies to encode the digital input L bits at a time
- Transmitted Signal $s_i(t) = A\cos 2\pi f_i t, \quad 1 \leq i \leq M$ $f_i = f_c + (2i-1-M)f_d$ $f_c = \text{denotes the carrier frequency}$ $f_d = \text{denotes the difference frequency}$ $M = \text{number of different signal elements} = 2^L$
- For FHSS, the MFSK signal is translated to a new frequency every T_c seconds by modulating the MFSK signal with the FHSS carrier signal.
- For a data rate of R, the duration of a bit is T=1/R seconds and the duration of a signal element is $T_s = LT$ seconds.

L = number of bits per signal element

Slow-frequency-hop spread spectrum	$T_c \geq T_s$
Fast-frequency-hop spread spectrum	$T_c < T_s$





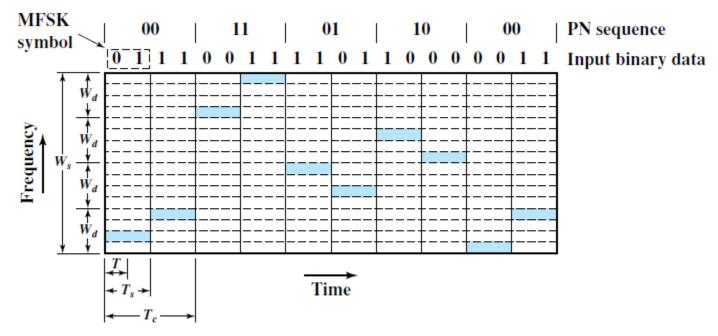


Figure 9.4 Slow Frequency Hop Spread Spectrum Using MFSK (M = 4, k = 2)

- we have M=4 which means that four different frequencies are used to encode the data input 2 bits at a time
- Each signal element is a discrete frequency tone, and the total MFSK bandwidth is $W_d = M f_d$
- We use an FHSS scheme with k=2. That is, there are $2^k = 4$ different channels, each of width W_d
- The total FHSS bandwidth is $W_s = 2^k W_d$
- $T_c = 2T_s = 4T$

Tc < Ts



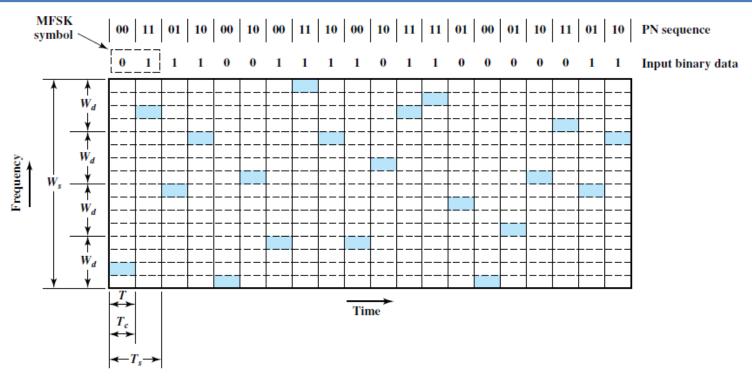


Figure 9.5 Fast Frequency Hop Spread Spectrum Using MFSK (M = 4, k = 2)

- we have M=4 which means that four different frequencies are used to encode the data input
- each signal element is represented by two frequency tones
- Each signal element is a discrete frequency tone, and the total MFSK bandwidth is $W_d = M f_d$
- We use an FHSS scheme with k=2. That is, there are $2^k = 4$ different channels, each of width W_d
- The total FHSS bandwidth is W_s = 2^k W_d
- $T_s = 2T_c = 4T$

FHSS Performance Considerations

- a large number of frequencies is used in FHSS
- So, W_s is much larger than W_d
- suppose we have an MFSK transmitter with bandwidth W_d
- a jammer of the same bandwidth and fixed power S_i on the signal carrier frequency
- we have a ratio of signal energy per bit to noise power density per Hertz of

$$\frac{E_b}{N_j} = \frac{E_b W_d}{S_j}$$

- If frequency hopping is used, the jammer must jam all 2^k frequencies.
- With a fixed power, this reduces the jamming power in any one frequency band to $S^{j}/2^{k}$
- The gain in signal-to-noise ratio, or processing gain, is

$$G_P = 2^k = \frac{W_s}{W_d}$$

DSSS



- Direct Sequence Spread Spectrum (DSSS)
 - each bit in the original signal is represented by multiple bits in the transmitted signal, using a spreading code
 - spreading code spreads the signal across a wider frequency band in direct proportion to the number of bits used

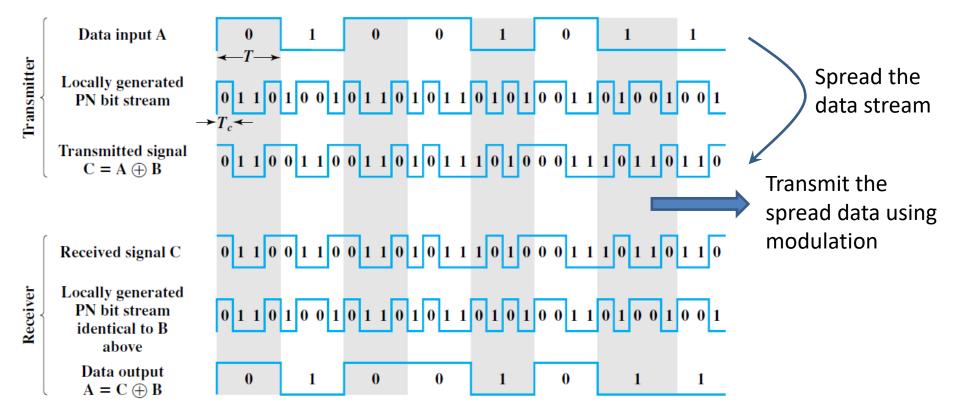
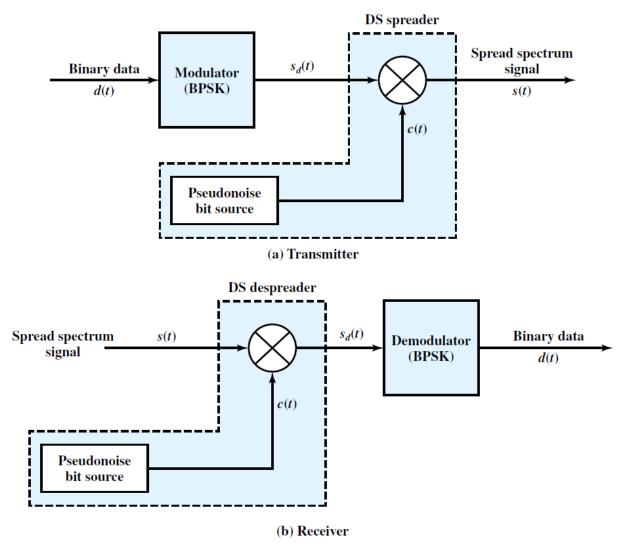


Figure 9.6 Example of Direct Sequence Spread Spectrum

DSSS System





Two ways used in spread spectrum:

- Spread the data and then modulate to transmit
- Perform modulation and then spread the modulated signal

(This figure using the 2nd approach)

Figure 9.7 Direct Sequence Spread Spectrum System

DSSS using BPSK



- Let a BPSK signal $s_d(t) = Ad(t)\cos(2\pi f_c t)$ where, A = amplitude of signal, $f_c = \text{carrier frequency},$ d(t) = the discrete function d(t) = +1 if the corresponding bit in the bit stream is 1 d(t) = -1 if the corresponding bit in the bit stream is 0
- the DSSS signal $s(t) = A \ d(t)c(t) \cos(2\pi f_c t)$ where, c(t) is the PN sequence taking on values +1 and -1.
- At the receiver, the incoming signal is multiplied again by c(t). As, $c(t) \times c(t) = 1$, the original signal is recovered.

Cont...



This figure using the 1st approach:

- first perform the BPSK modulation on the data stream d(t) to generate the data signal s_d(t).
- This signal can then be multiplied by spreading code c(t).

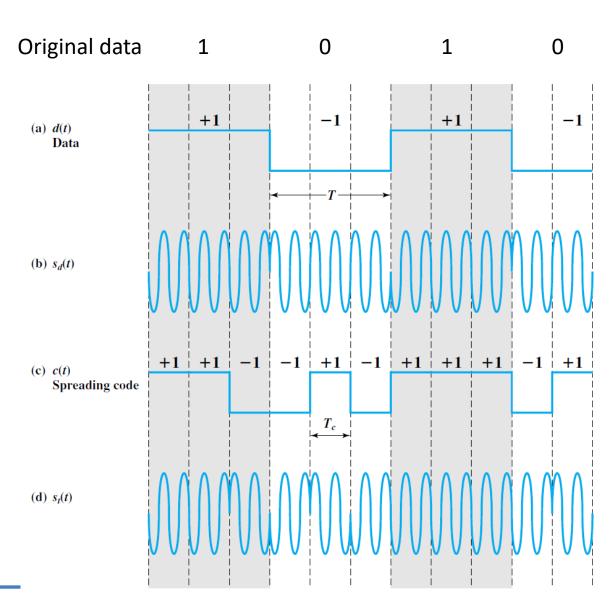


Figure 9.8 Example of Direct-Sequence Spread Spectrum Using BPSK

DSSS Performance Considerations

- Let us assume a simple jamming signal at the center frequency of the DSSS system.
- The jamming signal has the form $s_j(t) = \sqrt{2S_j}\cos(2\pi f_c t)$

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then, the received signal is s_r(t) = s(t) + s_j(t) + n(t)
where, s(t) = \text{transmitted signal}
s_j(t) = \text{jamming signal}
n(t) = \text{additive white noise}
S_j = \text{jammer signal power}
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- The de-spreader at the receiver multiplies $s_r(t)$ by c(t).
- so the signal component due to the jamming signal is $y_j(t) = \sqrt{2S_j}c(t)\cos(2\pi f_c t)$
- Thus, the jamming carrier power S_i is spread over a bandwidth of approximately $2/T_c$.

Cont...



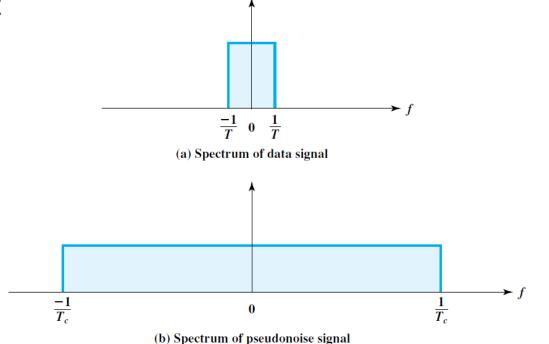
- the BPSK demodulator includes a bandpass filter matched to the BPSK data, with bandwidth of 2/T
- Thus, most of the jamming power is filtered out.
- the jamming power passed by the filter is

$$S_{jF} = S_j(2/T)/(2/T_c) = S_j(T_c/T)$$

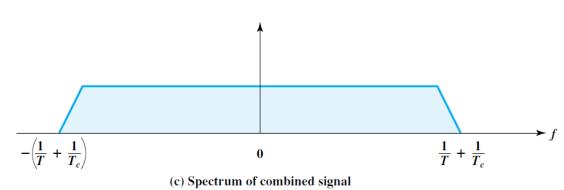
- The jamming power has been reduced by a factor of (T_c/T)
- the gain in signal-to-noise ratio

$$G_P = \frac{T}{T_c} = \frac{R_c}{R} \approx \frac{W_s}{W_d}$$

where, R_c is the spreading bit rate, R is the data rate, W_d is the signal bandwidth, and W_s is the spread spectrum signal bandwidth.



Signal energy



CDMA



- CDMA is a multiplexing techniques used with spread spectrum.
- Let 4 stations: 1,2,3,4
- Their data frames: d₁, d₂, d₃, d₄
- Assigned codes: c₁, c₂, c₃, c₄ (chip sequence)
 - Property-1: $c_i \cdot c_k => 0$
 - Property-2: $c_i \cdot c_j => 4$ (number of chips present in the chip sequence)
- Channel carrying:

$$- (d_1.c_1)+(d_2.c_2)+(d_3.c_3)+(d_4.c_4)$$

- Let stations 1 and 3 are talking,
- Station1 wants data from station3
- Station1 multiply the received string by station3 code: $(d1.c1)+(d2.c2)+(d3.c3)+(d4.c4).c_3 = 4.d_3$

Chip Sequences & Operations



$$C_1$$
 C_2 C_3 C_4 [+1 +1 +1] [+1 -1 +1 -1] [+1 +1 -1 -1] [+1 -1 -1 +1]

- Multiply by number:
- $2 \bullet [+1 +1 -1 -1] = [+2 +2 -2 -2]$

Inner product:

$$[+1+1-1-1] \bullet [+1+1-1-1] = 1+1+1+1=4$$

$$[+1 +1 -1 -1] \bullet [+1 +1 +1 +1] = 1 +1 -1 -1 = 0$$

• Addition: $[+1+1-1-1] + [+1+1+1+1] = [+2+2 \ 0 \ 0]$

Encoding Rules:

$$0 => -1;$$
 $1 => 1;$ silence $=> 0$

Example



Stations wants to send:

Station1: 0

– Station2: 0

Station3: silent

Station4: 1

Encoded to: [-1, -1, 0, 1]

Transmitted:

$$[-1.(+1+1+1+1)] + [-1.(+1-1+1-1)] + [0.(+1+1-1-1)] + [+1.(+1-1-1+1)]$$

= $[-1-1-1-1] + [-1+1-1+1] + [0000] + [+1-1-1+1]$
= $[-1-1-31]$

Let station4 wants to listen station2

- Station4 do: [-1 -1 -3 +1].[+1 -1 +1 -1] = -4

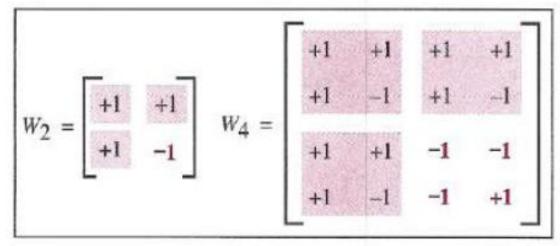
- Receive: $-4/4 = -1 \rightarrow bit 0$

Walsh Table



$$w_1 = \begin{bmatrix} +1 \end{bmatrix} \ w_{2N} = \begin{bmatrix} w_N & w_N \\ w_N & \overline{w_N} \end{bmatrix}$$

a. Two basic rules



b. Generation of W_2 and W_4

CDMA for DSSS



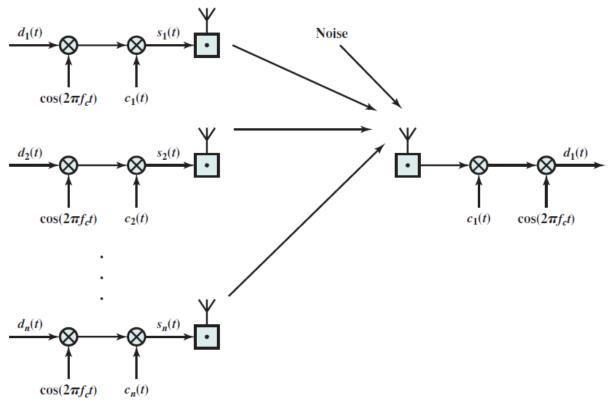


Figure 17.14 CDMA in a DSSS Environment for Receiving User 1

- There are *n* users, each transmitting using a different, orthogonal, PN sequence.
- For each user, the data stream to be transmitted, di(t), is BPSK modulated to produce a signal with a bandwidth of Ws and then multiplied by the spreading code for that user, ci(t). All of the signals, plus noise, are received at the receiver's antenna.



Thanks!

Figure and slide materials are taken from the following sources:

- 1. W. Stallings, (2010), Data and Computer Communications
- 2. B. A. Forouzan, (2013), Data Communication and Networking