

## CS 6301 Implementation of data structures and algorithms

### Long Project 3: Skip Lists and RBT

Ver 1.0: Initial description (Thursday, March 23).

**Due: 11:59 PM, Sun, April 9.**

**Max excellence credits: 2.0**

- Submission procedure is same as the same as that of prior projects.
- For each group, only its last submission is kept and earlier submissions are discarded.
- Your code must be of good quality, well commented, and pass all test cases within certain time limits to earn excellence credits.
- If you have implemented any EC problem, please mention in the README file.
- All relevant code and testcases are under folder LP3 in the shared box folder.

### Project Description

In this long project, implement skip lists and red-black tree, and then perform comparison study of both the data structures over a large number (several millions) of add, contain, remove operations.

#### 1. Skip Lists

Implement the following operations of skip lists. Some are optional. Starter code is provided. Do not change the signatures of public methods declared. You can add additional fields, nested classes, and methods as needed. Driver code is also provided along with the several testcases.

`add(x)`: Add a new element `x` to the list. If `x` already exists in the skip list, replace it and return `false`. Otherwise, insert `x` into the skip list and return `true`.

`contains(x)`: Does list contain `x`?

`remove(x)`: Remove `x` from the list. If successful, removed element is returned. Otherwise, return `null`.

`size()`: Return the number of elements in the list.

`isEmpty()`: Is the list empty?

`ceiling(x)`: Find smallest element that is greater or equal to `x`.  
(optional)

`first()`: Return first element of list. (optional)

`floor(x)`: Find largest element that is less than or equal to `x`. (optional)

`get(n)`: Return element at index `n` of list. First element is at index 0. Call either `getLinear` or `getLog`. (optional)

`getLinear(n)`:  $O(n)$  algorithm for `get(n)`. (optional)

`getLog(n)`:  $O(\log n)$  expected time algorithm for `get(n)`. **This method is optional, but code it correctly to earn an EC.** Need to implement `get(n)` too if you implement this.

`iterator()`: Iterator for going through the elements of list in sorted order. (optional)

`last()`: Return last element of list. (optional)

`rebuild()`: Reorganize the elements of the list into a perfect skip list. A search operation in a perfect skip list, will emulate binary search in a sorted array. (optional)

## 2. Red-black Tree

Extend BST to Red-Black Tree. Implement add and remove operations. You need to implement the algorithms discussed in the class. If you implement any other algorithm, you will not get any credit. Do not declare field for parent in a node. Also, as discussed in the class, just create one nil black node. If you create a new nil node for every leaf node, your space usage will double. Also, implement method `verifyRBT()` to verify whether the tree satisfies all the properties of RB tree. Starter code (`RedBlackTree.java`) and driver code are provided. Some of the test cases given for skip lists can be used to test your code for RB tree.

## 3. Comparison Study (optional for EC)

Do a comparison study of the performances of your implementation of skip list, your implementation of RB tree and java's `TreeSet` over a large number of add/contain/remove operations. Do the study over large tree sizes such as 4M, 16M, 64M, 256M till you run out of memory. Write a good report on your comparison study and the results. **An excellent comparison study with a good report will earn you an EC.**