

3MHS01I(24)

Operations Research 3

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Ans 2

let, x_1 = explosive for P x_2 = " " 9 x_3 = " " 8

explosive	Bombs			capacity
	P	Q	R	
A	3	1	4	600 Kg
B	2	4	2	480 Kg
C	2	3	3	540 Kg

$$\text{max } Z = 2x_1 + 3x_2 + 4x_3$$

the max 600 Kg for A

$$3x_1 + x_2 + 4x_3 \leq 600$$

at least 480Kg of B

$$2x_1 + 4x_2 + 2x_3 \geq 480$$

exactly 540 Kg of C

$$2x_1 + 3x_2 + 3x_3 = 540$$

$$x_1, x_2, x_3 \geq 0$$

Ans 2

$$\text{max } Z = 2x_1 + 5x_2$$

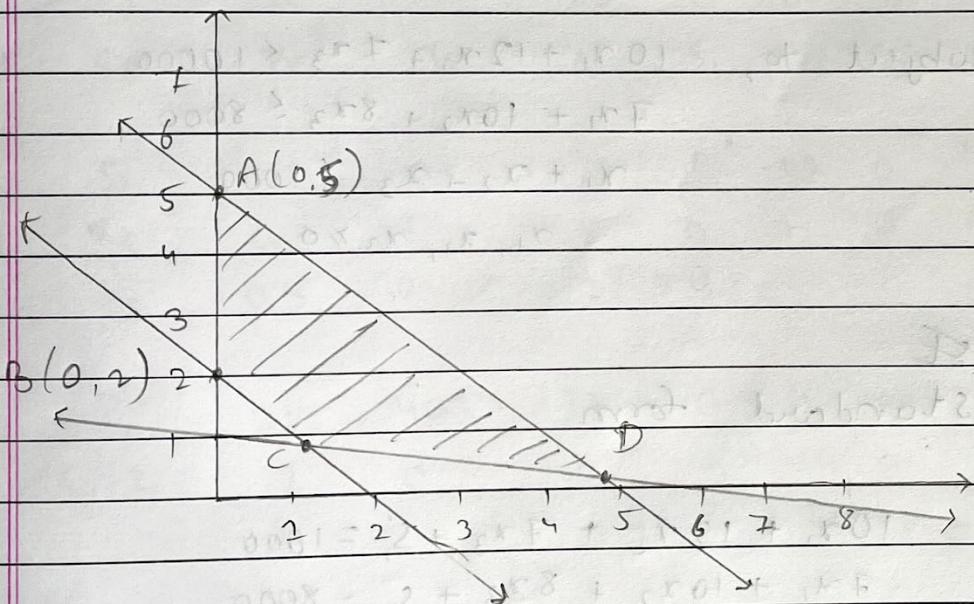
$$\text{subject to } x_1 + x_2 \geq 2$$

$$x_1 + x_2 \leq 5$$

$$x_1 + 6x_2 \geq 6$$

$$x_1, x_2 \geq 0$$

$x_1 + x_2 = 2$	$x_1 + x_2 = 5$	$x_1 + 6x_2 = 6$
$x_1 \ 0 \ 2$	$x_1 \ 0 \ 5$	$x_1 \ 0 \ 6$
$x_2 \ 2 \ 0$	$x_2 \ 5 \ 0$	$x_2 \ 1 \ 0$



$$x_1 + x_2 = 2$$

$$x_1 + 6x_2 = 6$$

$$-5x_2 = -4$$

$$x_2 = \frac{4}{5}$$

$$C\left(\frac{6}{5}, \frac{4}{5}\right)$$

$$x_1 + \frac{4}{5} \geq 2$$

$$x_1 + x_2 = 5$$

$$x_1 + 6x_2 = 6$$

$$-5x_2 = -1$$

$$x_2 = \frac{4}{5}, x_1 = \frac{24}{5}$$

$$D\left(\frac{24}{5}, \frac{4}{5}\right)$$

CP

Z-value

(0,5)

25

(0,2)

10

(6/5, 4/5)

~~6.4~~

6.4

(24/5, 4/5)

10.8

max Z = 25 at (0,5)

Ay3max Z = 30x₁ + 40x₂ + 20x₃Subject to, 10x₁ + 12x₂ + 7x₃ ≤ 100007x₁ + 10x₂ + 8x₃ ≤ 8000x₁ + x₂ + x₃ ≤ 1000x₁, x₂, x₃ ≥ 0~~ST~~

standard form

$$10x_1 + 12x_2 + 7x_3 + s_1 = 1000$$

$$7x_1 + 10x_2 + 8x_3 + s_2 = 8000$$

$$x_1 + x_2 + x_3 + s_3 = 1000$$

$$x_1, x_2, x_3, s_1, s_2, s_3 \geq 0$$

	C_j	30	40	20	0	0	0	0	
B_j	C_B	x_1	x_2	x_3	S_1	S_2	S_3	S_0	Ratio

0	S_1	10	12	7	1	0	0	10000	83333
0	S_2	7	10	8	0	1	0	8000	800 ←
0	S_3	1	1	1	0	0	1	1000	1000

	Z_j	0	0	0	0	0	0	0	
	$C_j - Z_j$	30	40	20	0	0	0		

	C_j	30	40	20	0	0	0		
B_j	C_B	x_1	x_2	x_3	S_1	S_2	S_3	S_0	Ratio

0	S_1	1.6	0	-2.6	1	-1.2	0	400	250 ←
40	x_2	0.7	1	0.8	0	0.1	0	800	1142.8
0	S_3	0.3	0	0.2	0	-0.1	1	200	666.6

	Z_j	28	40	32	0	4	0	32000	
	$C_j - Z_j$	2	0	-12	0	-4	0		

	C_j	30	40	20	0	0	0		
B_j	C_B	x_1	x_2	x_3	S_1	S_2	S_3	S_0	Ratio
30	x_1	1	0	-1/8	5/8	-3/4	0	250	
40	x_2	0	1	1.93	-7/16	0.625	0	625	
0	S_3	0	0	0.98	-3/16	7/8	1	125	

	Z_j	30	40	28.45	1.25	2.5	0	32500	
	$C_j - Z_j$	0	0	-8.45	-1.25	-2.5	0		

Solution of LPP is.

$$x_1 = 250, x_2 = 625, x_3 = 0$$

& solution = 32500

Ans 4 solve by 2-phase method

$$\text{minimize } z = 600x_1 + 800x_2$$

$$\text{subject to : } 2x_1 + x_2 \geq 80$$

$$x_1 + 2x_2 \geq 60$$

$$x_1, x_2 \geq 0$$

convert to standard LPP.

$$z = -600x_1 - 800x_2$$

$$2x_1 + x_2 - s_1 + A_1 = 80$$

$$x_1 + 2x_2 - s_2 + A_2 = 60$$

$$x_1, x_2, s_1, s_2, A_1, A_2 \geq 0$$

$$z^* = -A_1 - A_2$$

C_j	0	0	0	0	-1	-1		
C_B	Basic	x_1	x_2	s_1	s_2	A_1	A_2	Ratio
-1	A_1	2	1	-1	0	1	0	80
-1	A_2	1	2	0	-1	0	1	40
	Z_j	-3	-3	1	1	-1	-1	60
	$C_j - Z_j$	3	3	-1	-1	0	0	60
		↑						

x_1	1	$\frac{1}{2}$	$-\frac{1}{2}$	0	-	0	40	80
A_1	0	$\boxed{\frac{3}{2}}$	$\frac{1}{2}$	-1	-	1	20	$40/3 \leftarrow$
Z_j	0	$\frac{-3}{2}$	$-\frac{1}{2}$	$\frac{1}{3}$	-	$-\frac{1}{3}$	-20	
$C_j - Z_j$	0	$\frac{3}{2}$	$\frac{1}{2}$	-1	-	1		
.								

x_1	1	0	$-\frac{2}{3}$	$\frac{1}{3}$	-	-	$100/3$
x_2	0	1	$\frac{1}{3}$	$-\frac{2}{3}$	-	-	$40/3$
Z_j	0	0	0	0	-	-	0
$C_j - Z_j$	0	0	0	0	-	-	

All $C_j - Z_j \leq 0$ optimum solⁿ of phase-I
is optimized.

$Z^* = 0$, no artificial variable appear

Phase-II

C_B	-600	-500	0	$\frac{10}{3}$			
C_j	Basic	x_1	x_2	S_1	S_2	$20/3$	Ratio
-600	x_1	1	0	$-\frac{2}{3}$	$\frac{1}{3}$	$100/3$	
-500	x_2	0	1	$\frac{1}{3}$	$-\frac{2}{3}$	$40/3$	
Z_j	-600	-500	$\frac{700}{3}$	$\frac{400}{3}$	$-\frac{8000}{3}$		
$C_j - Z_j$	0	0	$-\frac{700}{3}$	$-\frac{400}{3}$			

All $c_j - z_j \leq 0$, so optimum solution is optimized

$$\text{optimize } z = \frac{100}{3}x_1 + \frac{40}{3}x_2$$

$$z_{\max} = -\frac{80000}{3}$$

$$z_{\min} = -z_{\max} = \frac{80000}{3}$$

Ans 5

Destination

Source	D ₁	D ₂	D ₃	D ₄	D ₅	Availability
S ₁	12	15	14	18	20	50
S ₂	25	15	20	12	8	30
S ₃	12	14	16	20	15	10
S ₄	15	22	25	24	30	20

Demand 25 20 28 27 10

	D ₁	D ₂	D ₃	D ₄	D ₅	Penalty
S ₁	12	15	14	18	20	50/22/17/13/3/3/2/2/13/3
S ₂	x 25	x 15	x 20	x 12	x 8	30/20/0/4/3/3/-/-
S ₃	x 12	x 14	x 16	x 20	x 15	10/0/2/2/2/2/2/16
S ₄	15	x 22	x 25	x 24	x 30	20/0/7/7/-/-
	25	20	28	27	10	
	5/0	10/0	6	7/0	10	

Penalty

0	0	2	6	7
0	0	2	6	-
0	0	2	16	-
0	1	2	2	-
0	1	2	2	-

$$\begin{aligned}
 \text{Cost} &= 5(12) + 10(15) + 28(14) + 7(18) + 20(12) + 10(8) \\
 &\quad + 10(14) + 20(15) \\
 &= \boxed{1488}
 \end{aligned}$$

Ans 6

Tasks

Persons	P	I	II	III	IV	V
P	102	110	145	125	90	.
Q	80	95	120	110	80	
R	78	105	100	88	92	
S	50	58	46	65	70	
T	0	0	0	0	0	

Row Reduction.

	I	II	III	IV	V
P	12	20	55	35	0
Q	0	15	40	30	0
R	0	27	22	10	14
S	4	12	0	19	24
T	0	0	0	0	0

Column Reduction, both are same.

I II III IV V

P	12	20	55	35	10	✓
Q	10	15	40	30	0	✓
R	8	27	22	10	14	✓
S	4	12	10	19	24	
T	0	10	0	0	0	✓

min. value = 10

I II III IV V

P	2	10	45	25	10
Q	10	5	30	20	0
R	8	17	12	10	14
S	0	12	10	19	34
T	0	0	0	0	0

Optimal assignment

$$\text{cost} = 90 + 80 + 88 + 46 + 0 \\ = 304$$

Ans 7

$J_1 \quad J_2 \quad J_3 \quad J_4 \quad J_5 \quad J_6 \quad J_7$

m_1	(12)	10	(13)	(12)	30	10	(16)
m_2	17	8	13	15	32	8	11
	X	X	X	X	X	X	X

optimum sequence,

$[J_7 | J_1 | J_4 | J_3 | J_5 | J_6 | J_2]$

	Machine-1	Machine-2	Idle time for m_2
	Time In	Time Out	In Out
J_7	0	10	10 21 10
J_1	10	22	22 39 1
J_4	22	34	34 54 0
J_3	34	47	54 67 0
J_5	47	77	77 109 10
J_6	47	87	109 117 0
J_2	87	97	117 125 0
			total = 21

total time elapse = 125 hr

ideal time of $m_1 = 125 - 97 = 28$ hr

ideal time of $m_2 = 21$ hr

Ans 8

OR is set of math-based method for making best possible decisions. It provides mathematical framework for optimizing complex system & enhancing efficiency. Its applications are widespread, touching nearly every domain of the field.

In computer network, OR is fundamental for routing protocols. Algorithm like Dijkstra's and Bellman-Ford, rooted in graph theory, are used to find shortest path for data packets to travel from source to destination.

In AI & ML heavily rely on optimization, a core concept of OR. Training a neural network minimizing a loss function, an optimization problem typically solved using techniques like gradient descent.

In operating system, OR is applied to process scheduling (e.g. shortest Job first) & resource allocation to prevent deadlocks & maximize system performance.