

Compression

Compared to text files, other media files like image, audio + video take up a huge amount of disk space.

It is extremely difficult working with such huge files; of 2 reasons:-

- (1) Due to their huge sizes, storage requirements increases rapidly with multiple such media files thereby ~~ring~~ the cost. During mm dev work, one can quickly run out of disk space
- (2) Even if there is adequate storage space, such files require a large data transfer rate that may be beyond the capabilities of both the processor + hard disk.

Due to these facts, it is customary to subject media files to a process called compression.

Compression reduces their file size using mathematical algorithms which becomes much easier to manipulate these files. The amount of compression depends on both original media data as well as compression

Technique applied:

CODC

After an analog quantity has been digitized, it is stored on the disk as a digital file. Such files are referred to as raw or uncompressed media data. To compress the file and reduce its size, it needs to be filtered.

For this, a specialized program called CODC (which stands for Compression/Decompression, or Coder/Decoder) reads the media data and applies the mathematical algorithm to reduce its size.

Dif:

This also works by finding the redundant info within the media files.

- Redundant info is that which can either be discarded without affecting the media quality by appropriate measures or data can be expressed in more compact form.

Amt of reduction depends on large no. of factors including both media data and CODEC used.

- The compressed media is then again stored on the disk or other storage media frequently, as a diff. type of file with another extension.
- When the media needs to be played back, either as stand-alone or as part of presentation, the same CODEC is again used to decompress the data which was previously compressed. Hence, the compression process needs to be essentially reversible. However, depending on type of CODEC used, the decompressed data may or may not be exactly identical to original uncompressed data.
- Decompression is necessary as the playback devices like the monitor or speakers cannot directly handle compressed data. After compressing the raw digital data is usually converted to analog form before being played back.

Types of Compression

Based on methodologies
compression can be divided into
Lossless vs Lossy compression

- * Lossless compression :- means the original data is not changed permanently during compression. After decompression therefore the original data can be retrieved back exactly. Codecs used for lossless compression are called lossless CODECS.
- * The algo within these CODECS attempts to represent the existing information in a more compact form without actually discarding any data.
- Adv:- Original data stays intact without degradation of quality and can be reused.
- Disadv:- Compression achieved is not very high + may be typically of order of 2 to 5 times.

{ Lossless compression is used where media quality is of utmost importance and large space requirements may be justified.

e.g. quality plays an imp. part in diagnosing faults from digitally stored medical images like X-ray plates & ultra-sonographs.

Lossy compression

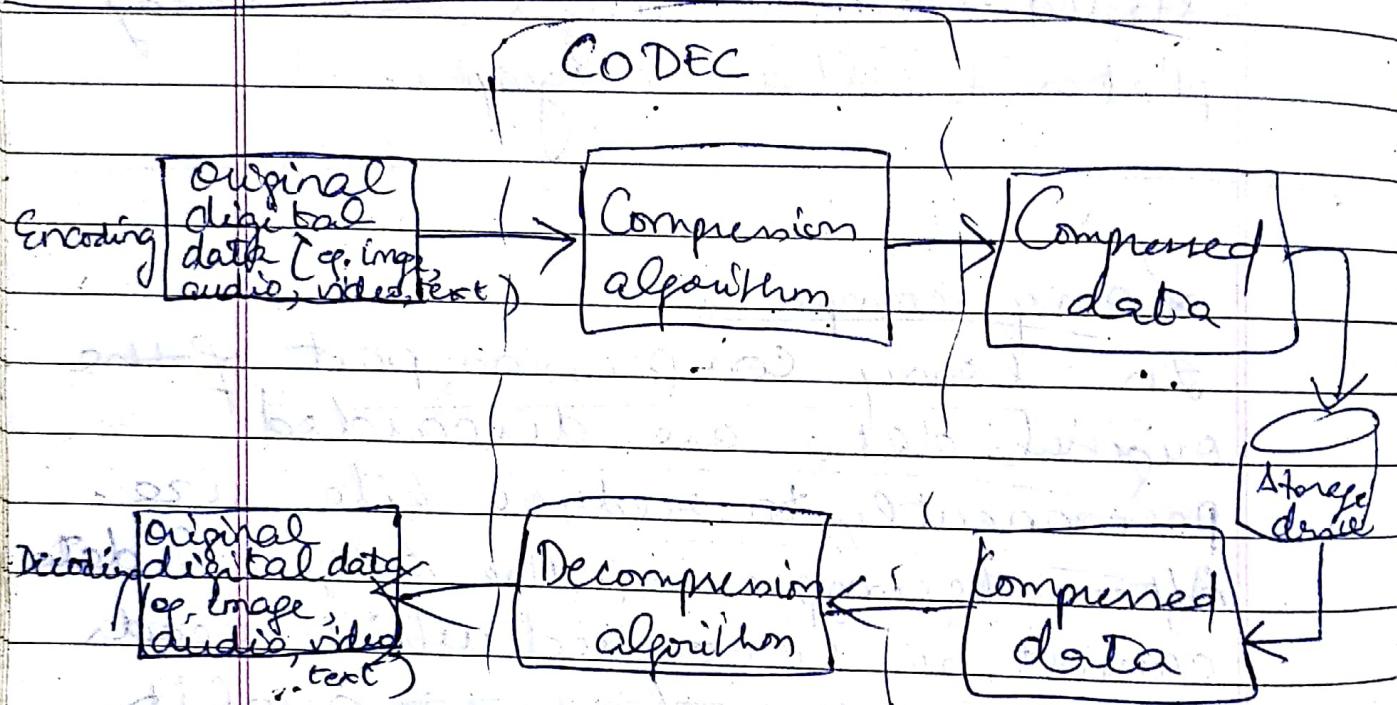
In lossy compression, parts of the original data are discarded permanently to reduce file size.

After decompression, the original data cannot be recovered which leads to degradation of media quality.

However if done correctly, the quality loss may not be immediately apparent because of the limitations of human eye and ear + also because of tendency of human senses to bridge gaps in information.

An imp. consideration is how much "info" can be lost before human eye can tell the diff. Compression ratios of order of 10 to 50 times can be achieved.

Voice compression is usually used while media quality may be sacrificed to a certain extent for reducing space requirements like in mm presentations & web page content.



Now a Codec works

Types of Compression

based on kind of redundancies exploited
compression can be divided into
Intraframe Interframe

Intraframe compression, It is applicable either a still image or a single video frame. Here, spatial redundancies are detected + exploited to reduce the file size. Such redundancies occur when diff. portions of an image are identical or similar to each other. e.g. an ^{area} of flat color in an image has pixels of identical values.

Interframe compression

It exploits the redundancies b/w adjacent frames in a video sequence, referred to as temporal redundancy. Such redundancies occur when subsequent frames of a video sequence are also identical or very similar.

e.g. in video of a never reader, most of time in b/w adjacent frames remain unchanged with minor variations in lip movement + facial expression of reader.

Types of Redundancies

Statistical
(Lorley)

Psycho-visual
(Loy)

Statistical redundancy

There some statistical relationships exists b/w media data.

It may be related either to actual "info" content - e.g. intensity values of adjacent pixels along row in an image may be similar or it may be related to representation of information - e.g. frequently occurring data may be represented by small no. of bits.

Statistical relationships within static media like images are spatial in nature, while those in time-varying media like sound are temporal in nature. In video clips, they may both be spatial-temporal.

Psycho-visual redundancy
It originates from the characteristics of the HVS. In the HVS, visual information is not perceived equally, some infoⁿ may be more imp. than other infoⁿ, so, if we apply fewer data to represent less important visual infoⁿ, perception will not be affected. e.g. some colors in an image or specific sounds within an audio clip may not be detectable by human senses. Such infoⁿ can be eliminated to reduce file size, without an appreciable variation in quality perception.

Lossless / statistical Compression Techniques

Lossless compression techniques are also known as Entropy Coding. It refers to techniques which do not take into account the nature of infoⁿ to be compressed. They treat all data as sequence of bits & tries to achieve compression by statistical manipulation of reordering of bits i.e. they ignore semantics of infoⁿ to be compressed.

Entropy

Entropy

It is measure of energy in physical system that cannot be used to do useful work. It is also used to depict disorder in the system.

The SI unit of entropy is

Joules per Kelvin (J/K) name as heat capacity.

Entropy is used to depict randomness in a signal which in turn provides a measure of how much useful info can be carried by a signal.

Suppose e.g. a signal is used to transmit a text string from a source to a destination. It cannot be predicted with accuracy what the next char would be.

Entropy in terms of a discrete random event x having possible states $1 - n$ can be defined as:-

$$\text{Entropy } H(x) = - \sum_{i=1}^n p(i) \log_2 p(i)$$

where n is the no. of diff. states
and $p(i)$ is the prob. of state i .
This is called Shannon's law of
entropy And can be used to
provide a measure of min^{avg.}
no. of bits reqd. to transmit
particular byte stream.

The efficiency of a particular
encoding scheme is often computed
as a ratio of entropy of source to
avg. no. of bits/codeword that are
reqd. with scheme.

Latter is computed acc to relation:

Avg. no. of bits/codeword -

$$\sum_{i=1}^n N_i p(i)$$

where N_i is no. of bits, $p(i)$ is
prob. of occurrence of i^{th} symbol.

Run Length Encoding (RLE)

Here, any sequence of repetitive characters may be replaced by a more compact form. A series of n successive characters may be replaced by a single instance of char. and no. of occurrences.

To depict the fact that it has a special meaning & not part of normal text, a special char is used as a flag.

i) Uncompressed data:

UNNNNNN I MAN N U E Z M

Compressed data:

U 16 N I M A N N H E I M

→ Flag

N N N N N N → replaced
by

16 N

This method should only be used if no. of occurrences is equal to a more than a specific no. (e.g., if, it was 4).

Huffman Coding (or Statistical coding)

- * This method consists of identifying the most frequent bit or byte patterns in a given file & coding these patterns with fewer bits than initially represented.
- * Less frequent patterns will be coded with more bits whereas most frequent patterns will use shorter codes.
- * A table of correspondence called code-book b/w initial patterns & their new representations must be available at both encoding & decoding ends.
- * This table is generated by analyzing frequencies of the occurrences of each char in the encoding process.

AAAAAA AA AAAA AABCD

(12 A's, 2 B's, 1 C, 1 D)

Free of

Prob. of occurrence of 4 characters

$$P(A) = 3/4, P(B) = 1/8,$$

$$P(C) = P(D) = 1/16$$

To transmit string without compression using 7-bit

ASCII code requires total

$$7 \times 16 = 112 \text{ bits}$$



$$P(BCD) = 1/4, P(A) = 3/4$$

$$P(CD) = 1/8, P(B) = 1/8$$



$$P(D) = 1/16, P(C) = 1/16$$

Codewords are determined from paths from root node to leaf node.

Codewords are:

A : 1

B : 01

C : 001

D : 000

After compression, total no. of bits required to represent documents is,

$$12 \times 1 + 2 \times 2 + 1 \times 3 + 1 \times 3 = 22 \text{ bits}$$

$$\text{Compression ratio} = \frac{112}{22.8}$$

~ about 5, 1

Q1

$$\begin{array}{c}
 A12 \longrightarrow A12 \xrightarrow{S} A12(1) \\
 B2 \longrightarrow B2(1) \quad \left. \begin{array}{l} \\ \end{array} \right\} \xrightarrow{} 4(0) \\
 C1(1) \quad \left. \begin{array}{l} \\ \end{array} \right\} \xrightarrow{} 2(0) \quad \left. \begin{array}{l} \\ \end{array} \right\} \xrightarrow{} 4(0) \\
 D1(0) \quad \left. \begin{array}{l} \\ \end{array} \right\}
 \end{array}$$

Godewards from Lt.-Col. + several

A is not a function. A represents B.

B 310 ~~several~~

B : 10 *liver* B : 01

15:10 15:01

$C_1 1000 \times 10^3$ $C_2 0010 \times 10^3$

D 2000-9 D 2000-10

q,

A document contains letters A thru F with frequencies as indicated:

$$A = 0.25, B = 0.1, C = 0.2,$$

$$D = 0.15, E = 0.26, F = 0.04$$

Use Huffman Coding to derive a codeword set.

$$A: 0.25 \quad 10 \quad 0011010$$

$$B: 0.1 \quad 11$$

$$C: 0.2 \quad 110$$

$$D: 0.15 \quad 1110$$

$$E: 0.26 \quad 11110 \quad 0011010$$

$$F: 0.04 \quad 11111 \quad 0011010$$

↓ decreasing order of frequency

$$E: 0.26 \quad 11110 \quad 0011010$$

$$A: 0.25 \quad 10 \quad 0011010$$

$$C: 0.20 \quad 110$$

$$D: 0.15 \quad 1110$$

$$B: 0.10(1) \quad 11110$$

$$F: 0.04(0) \quad 11111$$

$$B: 0.26 \quad 11110 \quad 0011010$$

$$A: 0.25 \quad 10 \quad 0011010$$

$$C: 0.20 \quad 110$$

$$D: 0.15 \quad 1110$$

$$E: 0.14 \quad 11110 \quad 0011010$$

$$F: 0.04 \quad 11111$$

20.29

20.26

A: 0.25 (1)

C: 0.26 (0)

0.45

20.29 (1), 20.26 (0)

B: 0.26 (0)

0.55 (1)

0.45 (0)

A: 0.1 (0) → 0.1

B: 1 (0) (1) (1) (1) → 1101

C: (0) (0) → 00

D: (1) (1) (1) → 111

E: (0) (1) → 10

F: (0) (0) (1) (1) → 1100

20.29 3.0 A 20.26

Program a counter with 02.26

20.26 and 0.26

~~E: 0.26~~ ~~E: 0.26~~
~~A: 0.25~~ ~~R: 0.25~~ ~~B: 0.26~~
~~C: 0.26 (0)~~ ~~= 0.49 (0)~~
~~- 0.29 (0)~~

Lempel-Ziv (LZ) Codes

- * LZ Coding uses codes documents by considering a string of characters at a time instead of single characters.
- * Both encoder + decoder holds a table containing all possible words in the document.
- * As each word occurs in the text encoder stores the index of the word in table instead of actual word. The decoder then uses the index to access the corresponding word from table in order to reconstruct the document.
- * Table is used as a dictionary and the LZ algo is called as dictionary-based compression algo.
- * Most word processing packages have a dictionary annotated with freq which is used for both spell checkers & for compression. Typically they contain in range of 25,000 words.
- * To generate an index for each word would require a 15-bit no ($2^{15} = 32,768$).

q. to encode word 'compression',
would just require 15 bits
instead of 77 bits, corresponding to
11 7 bit ASCII codes

- Basic req. of LZ algo is that a copy of dictionary is held by both encoder + decoder.

Lempel-Ziv-Welch (LZW) Coding

* Efficiency of LZ coding depends on how many of words in document to be encoded actually is included within the dictionary.

If small subset of words could be replaced by an index, the overall compression factor might be quite low as remaining words would need to be stored without compression.

To address this problem, a variation of the scheme has been developed known as LZW algo.

* This scheme allows dictionary to be built up dynamically by encoder-decoder as compressed text is stored.

* Initially dictionary contains only ASCII char set. The remaining entries are then dynamically added as each word is encountered.

{ Cf. suppose dictionary is a 8-bit table → therefore contains 256 entries

- * The first 128 table cells are populated with ASCII char set, while remaining 128 is empty initially.

* When 1st word is encountered in document, at 1st the word is interpreted as a collection of characters → each char is replaced by its index in table.

* At end of word when white space character is encountered, encoder stores word in next available free slot of table + uses that index no. to represent word hence forth.

* This procedure is repeated for each word, however prior to encoding characters individually encoders checks if word is already stored in table.

* If its word is represented by its index no. only. Decoder has access to same table & uses index no to retrieve original word.

LZW provides a technique for building a dynamic table lengths. Initially no. of entries is kept low, but if space is used up, the no. of slots can be increased.

e.g. If all 256 entries are used, encoder & decoder double size of table to 512 entries.

Q: LZ compression scheme is used to compress a text document. The dictionary table contains 1024 entries. The avg. char/word in document is 5. Calculate compression achieved.

1024 entries, so rep. by 10 bit codeword (as $2^{10} = 1024$)

Index of each word is 10 bit no.
As compression is not there, each char is rep. by 7 bits.
As 5 char/word, so each word rep. by 35 bit no. ($5 \times 7 = 35$)

$$\text{Compression ratio} = \frac{35}{10} = 3.5 : 1$$

Lossy Perceptual Compression Technique

It is also known as Source Coding.
Here, the human audio-visual
capabilities + limitations are
considered to isolate poor
portions of the media that
cannot be perceived by avg.
human senses + then
selectively discard them to
reduce file size. If done
correctly, the user will not be
able to detect any perceptual
change b/w original + changed re-
sp. in an image certain colors whch
cannot be perceived by human
eye could be discarded
while in sound clip certain
freq. not audible by human
ear may be filtered out.

They produce higher compression ratios than entropy encoding.

The main processes involved in coding are:

- ① transform coders → which convert the ip data into a diff form from where it is easier to identify redundancies
- ② Psycho - analysis, which identifies the redundant portions according to the known characteristics of human sense organs

~~JPEG, Image Coding Standard~~

- * JPEG (Joint Photographic Expert Group) is a compression standard for images.
- * Its performance depends on the complexity of image. Normally, image compression ratios are around 20:1.
- * It does not perform well on line drawings.

Modes of Operations

- (1) Sequential Encoding: It is the simplest lossy mode. It involves a single scan, left to right to bottom.
- (2) Progressive Encoding: It is also lossy mode. It also image to be built in multiple scans.
- (3) Lossless Encoding: It does not have any data loss.
- (4) Hierarchical Encoding: It has multiple resolution levels which can be decompressed separately.

Overview of Compression Steps

Compression process consists of following steps:

- (1) Preparation of data blocks.
- (2) Source encoding step involving forward DCT + quantization.
- (3) Entropy encoding step involving RLE and Huffman encoding.

Decompression process is made up of following

(1) Entropy decoding steps involves Huffman decoding + Run length decoding.

(2) Source decoding steps involves dequantization + inverse DCT.

Block Preparation

- * An image is represented by 1 or more 2D array of pixel values.
- * For continuous tone grayscale image using a CLUT, there will be a single array consisting of 8 bit values for each pixel of image.
- * For color image, without a CLUT, there will be 3 2D arrays of pixel values corresponding R, G and B subcomponents.
- * The block preparation step breaks each 2D array of image into individual blocks of 8×8 pixels / block.

Discrete Cosine Transform (DCT)

* It is used to transform each block from spatial domain to the freq. domain.

* Each block is composed of 64 values which represents amplitude of sampled signal. This amplitude is a function of 2 spatial coordinates $a = f(x, y)$ where x and y are 2 spatial dimensions and a represents the amplitude of pixel at sampled posⁿ (x, y) .

* After DCT, this f^n is turned into another $f^m c = g(F_x, F_y)$ where c is coefficient and F_x and F_y are respective spatial freq. for each direction.

DCT of each 8x8 block is computed using as:

$$R[i, j] = \sum_{x=0}^7 \sum_{y=0}^7 P[x, y] - \cos[\pi i(2x+1)/16] \cdot \cos[\pi j(2y+1)/16]$$

where x, y, i and j all vary from 0 to 7.

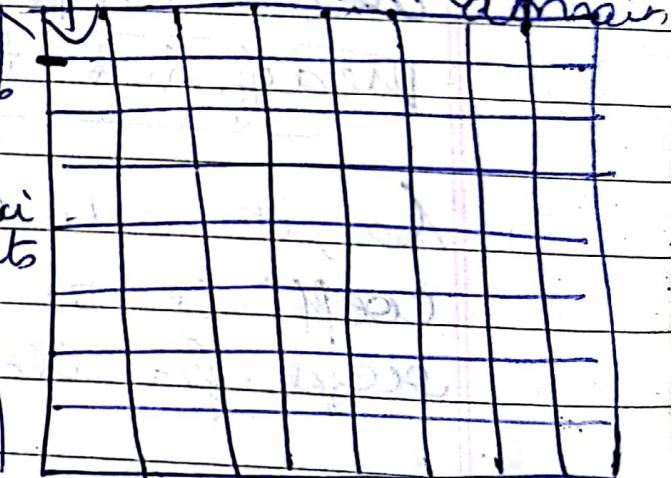
- * For $i=j=0$ two cosine terms become 0 and $\cos(0)=1$. This term obtained is called DC coefficient.
- * Since values in other locations of transformed array have a freq. coefficient associated with them, they are called AC coefficient.

$P(x, y)$: Spatial domain

$F(i, j)$: free domain

DC coefficient

↑
freq
coeffi
-ents



for Vertical freq,
in Horizontal,

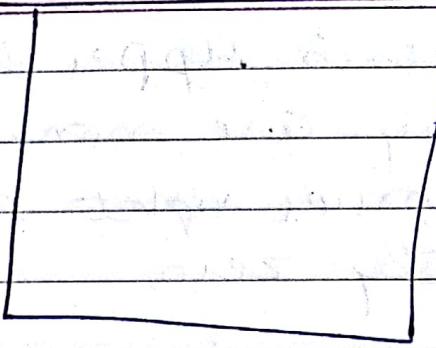
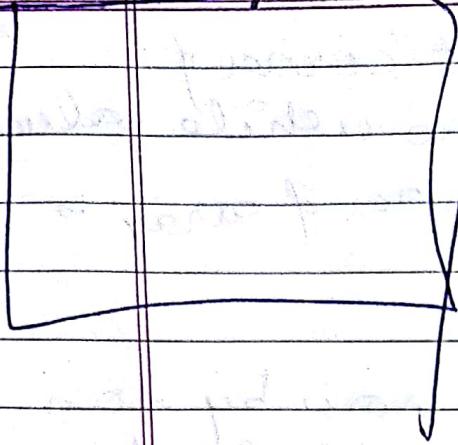
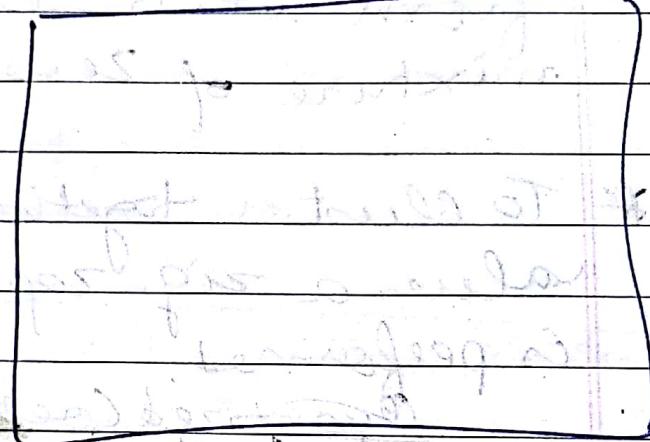
Quantization

So far no info is lost. If the image is stored as such & inverse transform is applied, initial image is recovered in exact form. The human eye responds primarily to DC coefficient. If magnitude of a higher freq. coefficient is below a certain threshold, eye will not detect it. This property is exploited in quantization by dropping the higher spatial freq. coefficients whose amplitudes are less than predefined threshold value.

So, it reduces size of DC + AC coefficients so that less bytes reqd. for its transmission.

← Here, a division operation is performed using defined threshold value as divisor.

If resulting quotient is zero the coefficient is less than threshold value while if it is non zero this indicates no. of times the coefficient is greater than threshold. These values are stored in SQT Table called quantization.

DCT coefficientsQuantization coefficientsQuantized coefficient

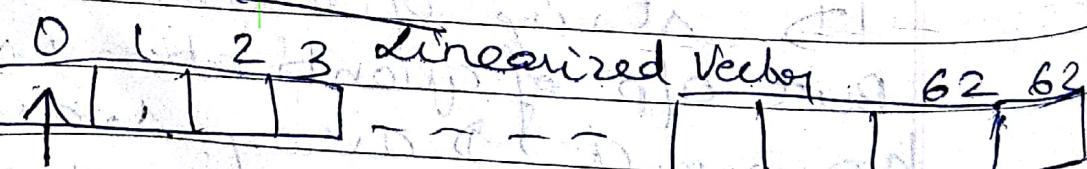
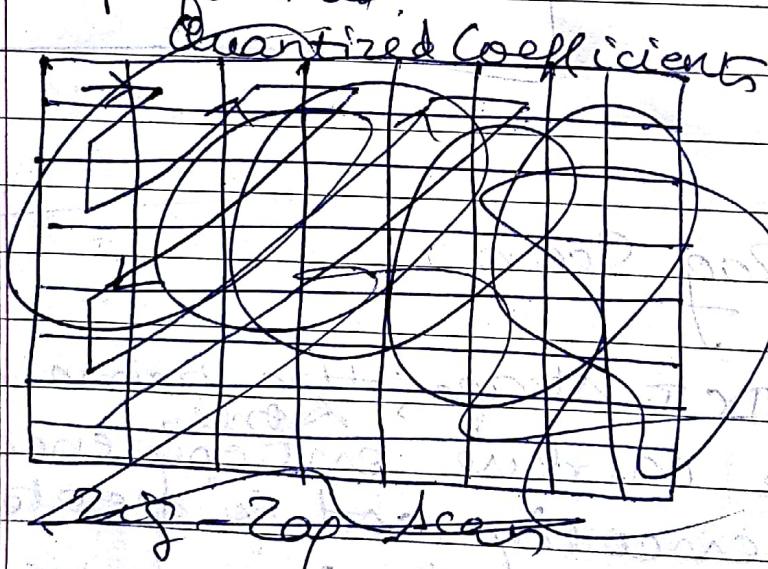
Zig-Zag Scan

After DCT stage, the remaining stage involve entropy encoding. The encoding coding operate on 1D strip of values ie vector. But o/p of quantization is however a 2D array. So array is converted to 1D array, this is called vectorizing.

Talib

* Values in upper left corner of array are non-zero while values in lower right corner of array are mostly zero.

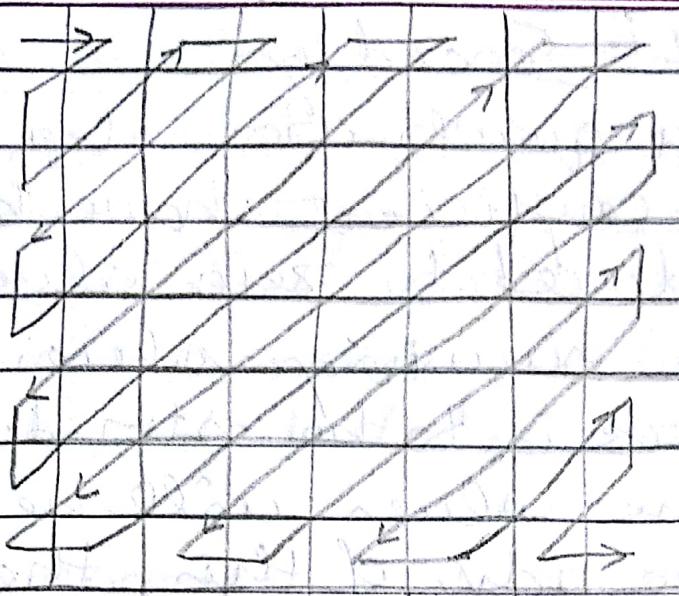
- * Thus, a simple scan row by row from left to right would lead to mixture of zeros + non-zero values.
- * To cluster together zeros + nonzeros values a zig-zag scan of array is performed.



DC coefficient

AC coefficient is
in zig order of freq.

Quantized Coefficients



Zig-Zag Scanning Order

Differential Pulse code modulation, DPCM Encoding

- * There is one DC coefficient / block.
- * DC coefficient is measure of mean value of 64 values of that block.
- * the sequence of DC coefficients is encoded in DPCM mode.
- * This means that the difference b/w the DC coefficient of each block and adjacent block is computed + stored.
- * This reduces the no. of bits reqd. to encode the relatively large magnitude of DC coefficient.

RLE Encoding

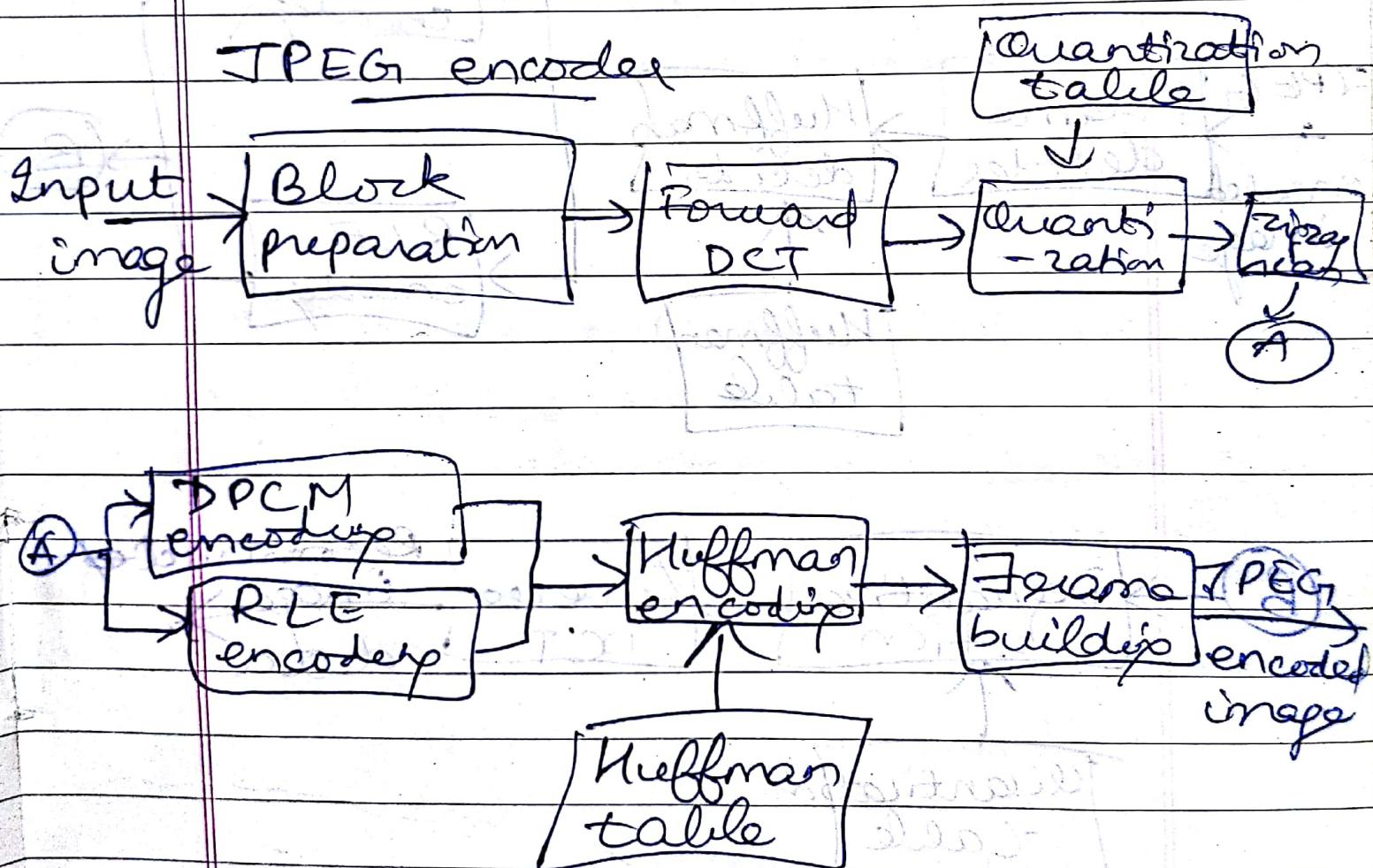
- * After quantization step, most of the coefficients have been reduced to zero values.
- * The surviving values of each block is to be stored. Many of these values will be zero and take adv. of this, they are run length encoded.
- * Due to zig-zag scan of AC coefficients of each block have been grouped in a way that zero values have been clustered together. To exploit this, for each strip of repeated zero values, a single value is stored along with count of how many times value is to be repeated.

Huffman Encoding

- * The final step is to apply huffman coding which allocates codes & is applied both to DC and AC coefficients.

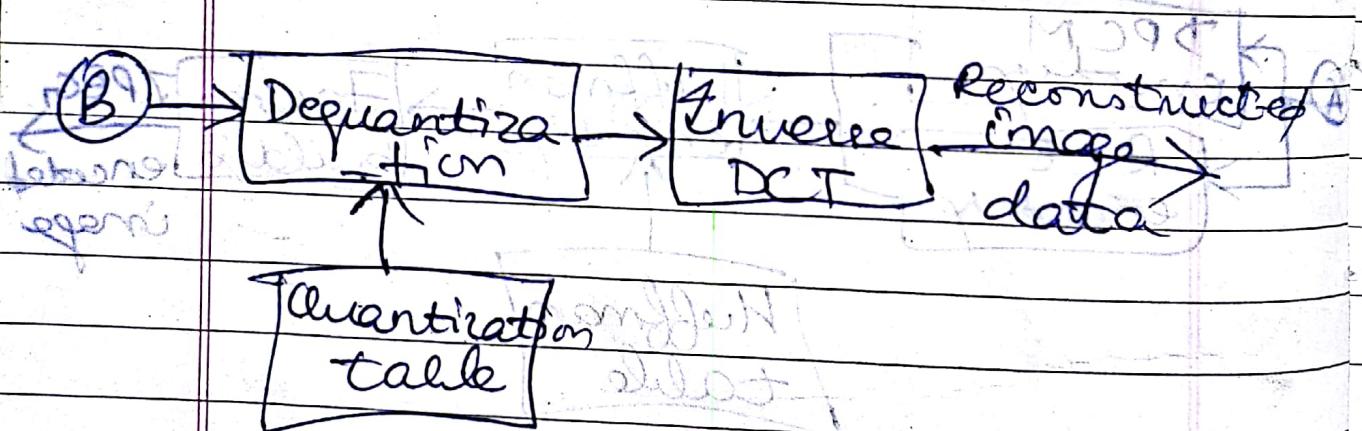
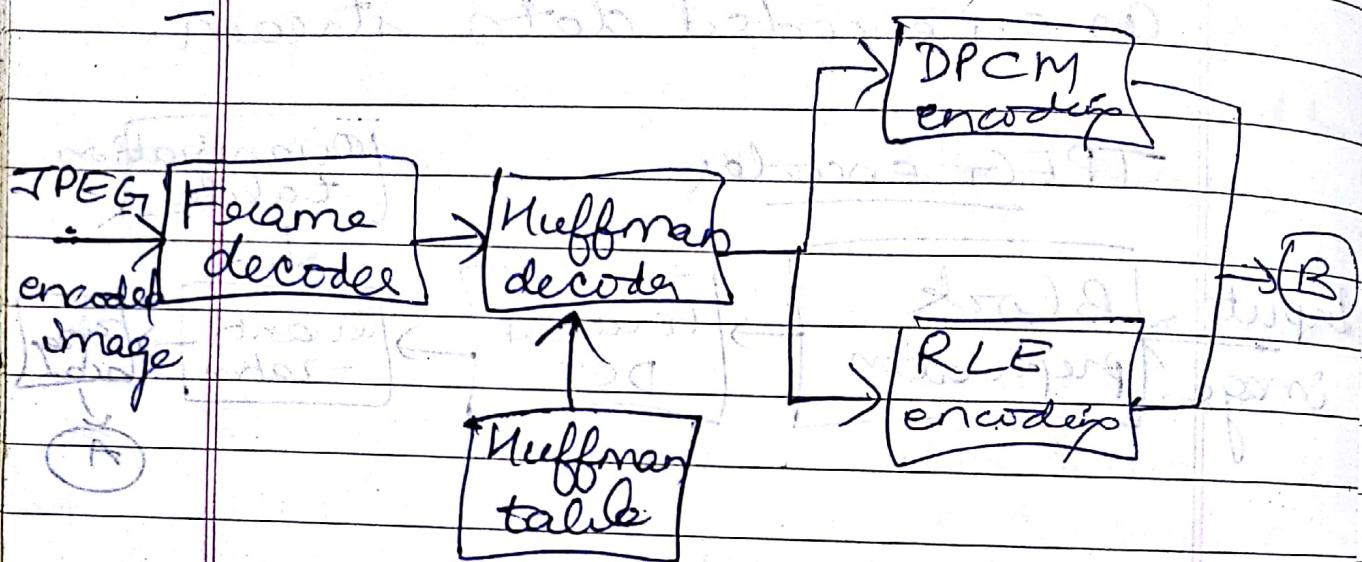
Frame building

The frame packing block does the final assembling of data and adds additional error check codes before sends data to O/p as an encoded data stream



Decoder

JPEG decoder is made up of no. of stages which are corresponding decoder section of those used in encoder.



JPEG decode

JPEG does not work well with black + white images. To address this limitation, another group called Joint Bi-level Experts Group (JBIG) was formed whose main goal is to define lossless compression also for these images.

MPEG (Motion Pictures Expert Group)

MPEG's working gp. under ISO/IEC
(International Standards Organization)
(International Electrotechnical
Commission) set up to formulate a
set of standards relating to a large
num applications involving audio +
video.

MPEG-1 standard was developed by
MPEG dev. the ISO/IEC international
standard 11172 for reduced
data rate coding of video + audio
signals. This standard is called
MPEG-1. It is used for Video CD.
It includes popular MP3 audio format.

It has 5 diff. parts:-

Part-1 Systems (ISO/IEC 11172-1:
1993) :- It addresses problem of
combining 1 or more data streams
from video + audio parts of MPEG-1
standard with timing info to form
single stream.

Part 2 - Video (ISO/IEC 11172-2; 1993)
It is used for compressing video sequences at bit rates about 1.5Mbit/s.

Part 3 - Audio (ISO/IEC 11172-3; 1993)
It is used for compressing audio sequences, both mono + stereo.

Part 4 - Compliance Testing
(ISO/IEC 11172-4; 1995)
It specifies how tests can be designed to verify whether bitstreams + decoders meet the requirements as specified in Part 1, 2 and 3 of MP3 standard.

Part 5 - Software Simulation
(ISO/IEC TR 11172-5; 1998)
It is a technically report giving full software implementation of parts of standard.

MPEG-2

Video + audio storage + transmission standard for broadcast quality television. Used for digital TV Tx, digital satellite TV service, digital cable TV signals + for DVD applications. It has series of documents which are subsets of ISO Recommendation 13818. It has 8 parts.

MPEG-3

Designed for HDTV, but abandoned when it became apparent that MPEG-2 was sufficient for that purpose.

MPEG-4

The primary uses for MPEG-4 standard are web + CD distribution, conversational (videophone) + broadcast television.

- It absorbs many features of MPEG-1 and MPEG-2.
- It adds new features such as VRML support.

→ It has 21 parts -

Most of features included in MPEG-4 are left to individual developers to decide whether to implement them.

MPEG-7

- * Also called Multimedia Content Description Interface which provides a set of descriptors (D) ie quantitative measures of audio-visual features DS (description schemes) (DS) ie structure of descriptors + their relationship * A language called DDL (Description Definition Language) can be used to specify scheme
- * The images, audio, video that have MPEG-7 data associated with them can be indexed + searched for.
→ It has 10 parts.

MPEG-21

- Defined as ISO/IEC 21000-1
- It defines an open framework for mm delivery + consumption
- It is based on 2 essential concepts :-

9 parts

- (a) definition of fundamental units of distribution & draw
- (b) Concept of users interacting with digital items.

MPEG-1 Audio

This standard for digital audio.

It has 3 diff. layers pertaining to 3 levels of complexities for algorithms.

Layer I is basic mode + layer II +

layer III has 1 esp. levels of complexities associated with them which in turn produces a corresponding 1st layer of compression.

Layer I: 192 kbps / channel, compression 4:1, quality same as digital audio cassette.

Layer II: 128 kbps / channel, compression 6:1 to 8:1, quality same as digital audio broadcasting.

Layer III: 64 kbps / channel, compression 16:1 to 128:1, quality same as audio CD quality.

Bit rates are for a single audio channel
There are 4 diff. audio channel formats. They are -

- Monophonic (mono), where only a single channel carries audio signal.
- Dual mono - where same mono signal is carried over 2 channels
- Stereophonic (stereo) - 2 channels carry different signals
- Joint stereo - stereo signals are combined & carried over a single channel.

For stereo + dual mono format, bit rates are doubled.

MPEG-1 Audio layer I (MP 1)

- Least sophisticated method
- Requires high data rate of 192 kbps/ channel.
- Compression ratio is about 4:1.
- Quality same as digital audio cassette.

MPEG-1 Audio Layer II (MP2)

- MP2 files first appeared on Internet
- were played back using Xiph MPEG player & on UNIX, in a program called MPlayer.
- Bitrate is 128 kbps / channel
- Compression ratio ranges from 6:1 to 8:1.
- Quality is same as that of digital audio broadcasting.

MPEG-1 Audio Layer III (MP3)

It is used to compress files prior to electronic distribution. The MP3

CODEC is lossy in nature.

The crucial point is which data to keep and which to discard. To decide MP3 depends on the perceptual characteristics of human acoustic system.

Specific sounds may not be audible to human ear, it's called masking.

As masked sounds are removed & remaining data forms the compressed file.

(\rightarrow) MP3 encoder 1st converts input audio from the temporal domain using DFT (Discrete Fourier transform) after which a psycho acoustic block (contains info about characteristic of human auditory system) identifies + removes masked audio components.

- The remaining data is sent to quantizer + coding block for code word generation.
- The frame packing block adds error checking codes before storing compressed data as an MP3 file.
- Data must be passed through MP3 decoder for playback which dequantizes codewords + converts them back to temporal domain from freq. domain.
- Bit rates of 256, 64, 128, 192 and 320 kbps may be allowed.

ID3 Tag → It's format for storing textual metadata for MP3 files such as title, artist, album, track no etc.

The various variants are:-

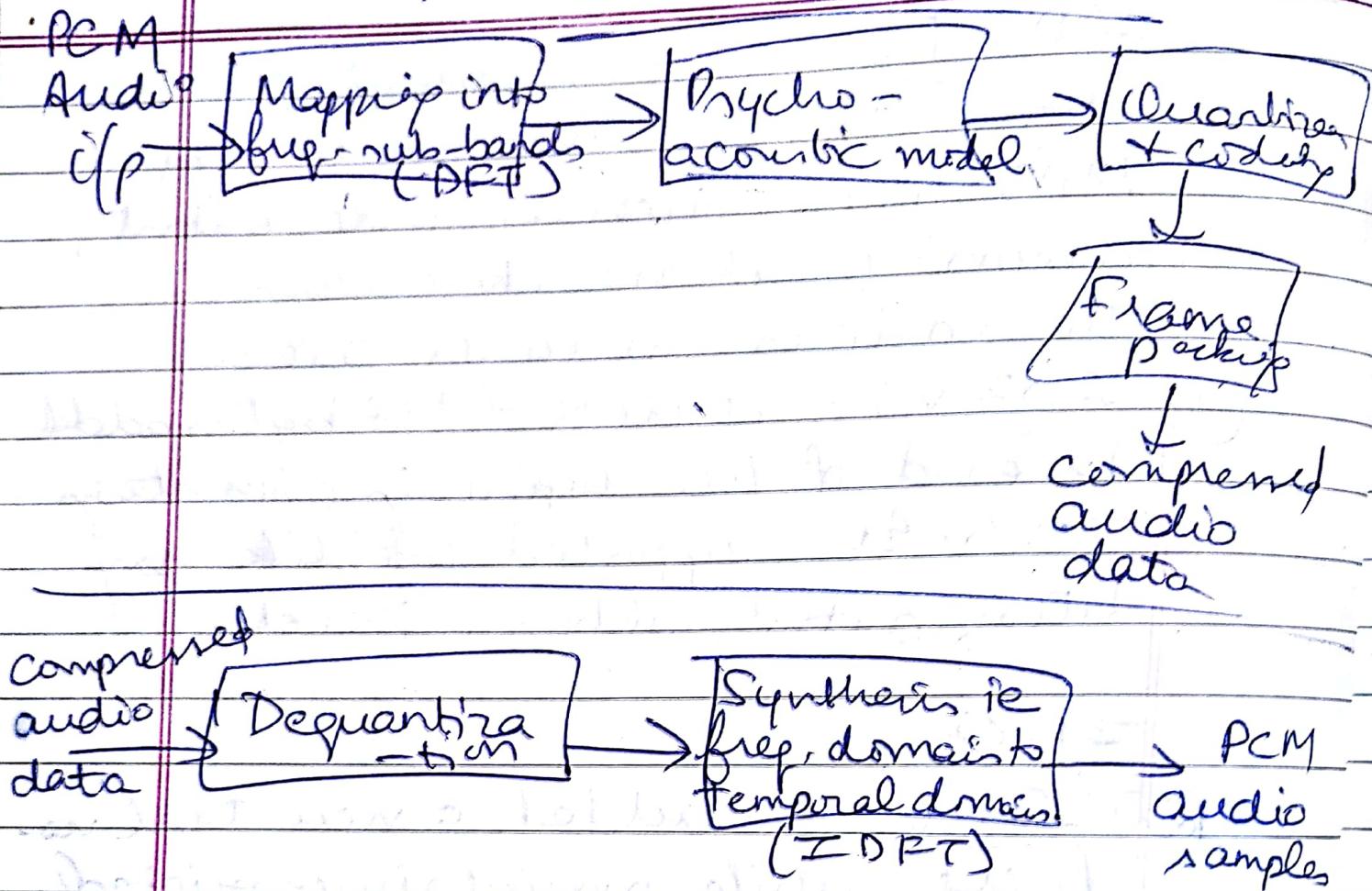
- (1) ID3 v1, consists of 128 bytes added to end of file beginning with string TA 0, It supported info like song title, artist, album, year etc.

ID3v1.1

- (2) ID3v1.1 → added a new track no field while maintaining original size of 128 bytes.

- (3) ID3v2 :- expanded ID3 format with addn of many more fields such as strip of lyrics within file. The tags are included at beginning instead of the end which has an advantage that related info can be read without reaching end of file.

MPEG-1 audio encoder



MPEG-1 audio decoder