$$hP = \sum_{j} \sum_{k} (S_{j,k} \cdot F_{j,k}) / \sum_{k} (S_{k,k} \cdot F_{+,k})$$

$$hR = \sum_{j} \sum_{k} (S_{j,k} \cdot F_{j,k}) / \sum_{j} (S_{j,j} \cdot F_{j,+})$$

$$hF = [(\beta^{2} + 1) \cdot hP \cdot hR] / (\beta^{2} \cdot hP + hR)$$

$$hP_{k} = \sum_{j} (S_{j,k} \cdot F_{j,k}) / (S_{k,k} \cdot F_{+,k})$$

$$hR_{j} = \sum_{k} (S_{j,k} \cdot F_{j,k}) / (S_{j,j} \cdot F_{j,+})$$

$$hF_{j=k} = [(\beta^{2} + 1) \cdot hP_{k} \cdot hR_{j}] / (\beta^{2} \cdot hP_{k} + hR_{j})$$

- j An observed class
- k A predicted class
- $m{S}_{j,k}$ The length of the path from the first common ancestor of classes $m{j}$ and $m{k}$ to the root. For $m{S}_{j,j}$ and $m{S}_{k,k}$ the depth of class $m{j}$ or $m{k}$, respectively
- $\mathbf{\textit{F}}_{\textit{j},k}$ The number of cases observed in class j that were classified as class k
- $extbf{\emph{F}}_{ ext{+},k}$ The total number of cases classified as class $extbf{\emph{k}}$
- ${m F_{j,+}}$. The total number of cases observed as class ${m j}$
- β The relative weight of precision and recall (beta.h.F as defined above)