

# Lesson 19 — Logic

## Problem 1: translation (20 points)

Write the statements below in symbolic form using  $\neg$ ,  $\wedge$ ,  $\vee$ , and the letters:

- $h$  = "Jon is healthy"
- $w$  = "Jon is wealthy"
- $s$  = "Jon is wise"

- (a) "Jon is wealthy and healthy but not wise."
- (b) "Jon is not wealthy but he is healthy and wise."
- (c) "Jon is neither healthy, wealthy, nor wise."
- (d) "Jon is neither wealthy nor wise but he is healthy."
- (e) "Jon is wealthy, but he is not both healthy and wise."

## Problem 2: de Morgan's laws (5 points)

Which of the following is the correct negation of "Both Abe and Ben are tall."?

- (a) "Abe is tall, and Ben is tall."
- (b) "Abe is not tall, and Ben is not tall."
- (c) "Abe is tall, or Ben is tall."
- (d) "Abe is not tall, or Ben is not tall."

## Problem 2: de Morgan's laws (5 points)

Which of the following is the correct negation of "Both Abe and Ben are tall."?

- (a) "Abe is tall, and Ben is tall."
- (b) "Abe is not tall, and Ben is not tall."
- (c) "Abe is tall, or Ben is tall."
- (d) "Abe is not tall, or Ben is not tall."

## Problem 3: de Morgan's laws (5 points)

Which of the following is the correct negation of "Jon is wealthy, but he is not both healthy and wise."?

- (a) "Jon is not wealthy, but he is both healthy and wise."
- (b) "Jon is not wealthy, or he is both healthy and wise."
- (c) ""Jon is not wealthy, and he is both healthy and wise.""
- (d) "Jon is not wealthy, or he is neither healthy nor wise."