

# Lesson 23

Arbitrage betting

# Arbitrage: General idea

Buy low in one market.

Sell high in another market.

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**Example 1.** Argentina peso historically has high inflation.



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**Example 1.** To stop this,  
Milei artificially props up  
the peso:

<https://archive.ph/7RHMG>

The image shows a screenshot of the Bloomberg news website. At the top, there is a dark navigation bar with the Bloomberg logo in white. Below the logo, there is a horizontal menu with several items: 'Live TV' (in red), 'Markets' (with a dropdown arrow), 'Economics', 'Industries', 'Tech', 'Politics', 'Businessweek', and 'Opinion'. The main content area has a light gray background. At the top of this area, there is a headline: 'Argentina's Javier Milei: Approval Rises | US Trade Deal | Midterm Win | Trump Support'. Below the headline, there is a sub-headline: 'Markets | Currencies'. The main title of the article is 'Currency Arbitrage Costs Milei \$2 Billion a Month in Argentina'. At the bottom of the article, there is a call-to-action: 'Subscribe now for uninterrupted'. Below this, it says 'Get the context behind every story for \$1.99/month.' and a 'Claim this offer' button.

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Step 3: ???

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Step 2. Sell the still “worthy” peso at banks to buy dollars.

Step 3: ???

Step 4: Profit

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## **Example 2.** Sports Betting: Eagles vs Chargers Game.

- Betting Site 1 underestimates Eagles and gives too-good-to-be-true payout. → You bet on this.
- Betting Site 2 underestimates Chargers and gives too-good-to-be-true payout. → You bet on this.

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- Betting Site 2 underestimates Chargers and gives too-good-to-be-true payout. → You bet on this.
- Either Eagles or Chargers win → You win more than you pay in.

# Sports betting: Decimal Odds

Payout (includes your stake) = Decimal Odds × Bet

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**Example.** If you bet \$100 on a game with decimal odds of 3.00, then your payout is

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$$\text{Your gain: } \$300 - \$100 = \$200$$

# Arbitrage: Math

	Eagles to Win	Chargers to Win	Best Odds	Implied Probability
Betting Site 1	1.20	6.00		
Betting Site 2	1.50	2.80		

**Step 1.** Find big odd & take both sides.

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**Step 2.** Invert odds to get probability the site thinks the outcome happens.

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# Arbitrage: Math

	Eagles to Win	Chargers to Win	Best Odds	Implied Probability
Betting Site 1	1.20	<b>6.00</b>	<b>6.00</b>	<b>0.167</b>
Betting Site 2	<b>1.50</b>	2.80	<b>1.50</b>	<b>0.667</b>

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**Step 3.** Arbitrage if probabilities add to < 1 (Betting Sites collectively underestimate & undervalue chosen outcomes). Otherwise, don't bet.

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**Step 3.** Arbitrage if probabilities add to < 1.

**Step 4. Bet:**

$$\frac{0.167}{0.834} = 20\% \text{ of wealth on Chargers to Win on Betting Site 1, and}$$

80% of wealth on Eagles to Win on Betting Site 2.

# Arbitrage Risks

- Sports betting websites (“sportsbooks”) limit your account if you are too successful. Your effective salary will then be less than minimum wage.
- Odds change before you respond.

# Other logistics for today

# Next meeting (December 8 or 9)

- Review for final exam aka quiz make-ups/retakes
- Go over more homework questions.

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Three assignments will be dropped.

# This meeting (now)

Course survey (15 minutes) first, then homework questions

<https://rowan.campuslabs.com/eval-home/>

