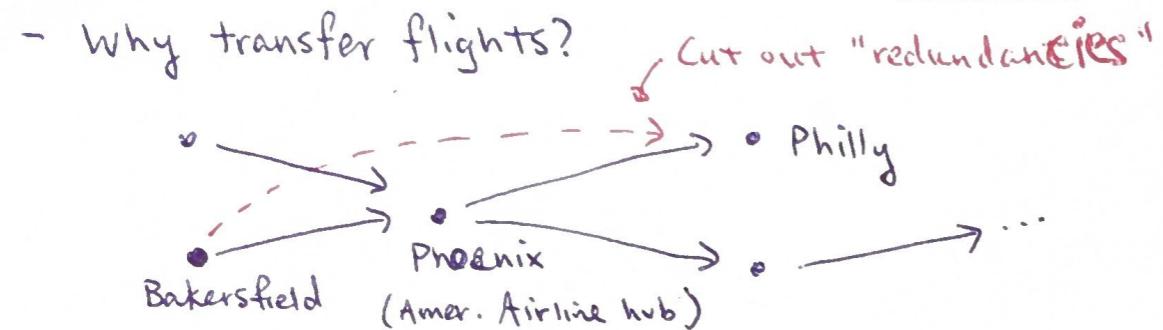


## Minimum cost spanning tree (MST)

- Why no In-N-Out in NJ? No distribution network



Structure is a "tree"

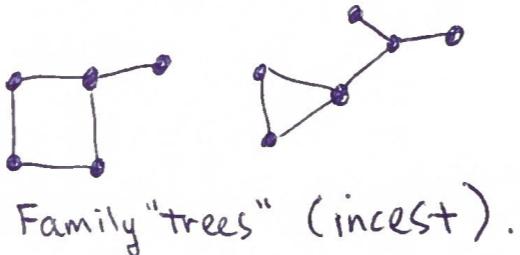
A structure without such redundancies is a "tree".

Definition A tree is a graph without circuits / loops.

### Ex of trees



### Not examples of trees



### Definitions

- A spanning tree of a graph  $G$  is a subgraph of  $G$  that includes every vertex of  $G$ .

- A minimum spanning tree (MST) is a spanning tree with minimal total cost.

Kruskal's algorithm To get MST, added smallest edges without forming circuits until you get a spanning tree.

Ex

1	4	5		
	5	3		4
1	3	8	2	6
	10	4		

First pick lowest cost edge (1's)

1			

Then pick next lowest cost edges (2's).

1			
			2

Then pick next lowest cost edges (3's)

1			
	3		2
	3		

Then pick next lowest cost edges (4's)

1			
	3	3	4
	4		
	3		

We can't pick 5's (form circuits) so we add 6's, which now touch every vertex so completes our spanning tree