

$$y = 4x$$

$$\begin{aligned}\text{Cov}(x, y) &= E(xy) - E(x)E(y) \\ &= E(4x^2) - E(x)E(4x) \\ &= E(4x^2) - 4E(x^2) \\ &= 4[\text{Var}(x)] \\ &= 4 \times 1 \\ &= 4\end{aligned}$$

$$\rho = \frac{\text{Cov}(x, y)}{\sigma_x \sigma_y} = \frac{4}{1 \times \sqrt{17}} = 4/\sqrt{17}$$

Bivariate Normal Conditional distribution takes the following form

$$x|y = N\left(\mu_x + \frac{\sigma_x}{\sigma_y}(y - \mu_y)\rho, (1 - \rho^2)\sigma_x^2\right)$$

$$\mu_x = 0, \sigma_x = 1$$

$$\mu_y = 0, \sigma_y = \sqrt{17} \rightarrow \text{From 4.2.6}$$

Setting  $y = 2$

$$\mu_{x|y} = 0 + \frac{1}{\sqrt{17}} \times \frac{4}{\sqrt{17}} \times (2 - 0)$$

$$\mu_{x|y} = \frac{8}{17}$$

$$\sigma_{x|y}^2 = \left(1 - \left(\frac{4}{\sqrt{17}}\right)^2\right) \times 1$$

$$= \left(1 - \frac{16}{17}\right)$$

$$= 1/17$$