

$$\beta_{-}=\sin[\pi/\theta_w(\pi-\theta-\theta_o)]\times\{1-2\exp(-\pi Y/\theta_w)\cos[\pi/\theta_w(\pi-\theta-\theta_o)]+\exp(-2\pi Y/\theta_w)\}^{-1}$$