$$\beta_{++} = \sin[(\pi/\theta_w)(\pi+\theta+\theta_o)] \times \{1 - 2\exp(-\pi Y/\theta_w)\cos[(\pi/\theta_w)(\pi+\theta+\theta_o)] + exp(-2\pi Y/\theta_w)\}^{-1}$$