$$Y = \text{arcCosh} \, \frac{c^2 t^2 - (r^2 + r_o^2 + Z^2)}{2 r r_o}$$