$\beta = \sin[(\pi/\theta_w)(\pi \pm \theta \pm \theta_o)] \times \{1 - 2\exp(-\pi Y/\theta_w)\cos[(\pi/\theta_w)(\pi \pm \theta \pm \theta_o)] + \exp(-2\pi Y/\theta_w)\}^{-1}$