

## Bernoulli Naïve Bayes

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

$P(A|B)$  = probability of A given B

$P(B|A)$  = Probability of B given A

$P(A)$  = Probability that A will occur.

$P(B)$  = probability that B will occur.

Confident	Studied	sick	Result.
yes	No	No	fail
yes	No	yes	Pass
No	yes	yes	Fail
No	yes	No	Pass
yes	yes	yes	Pass

step 1 -

calculate class probabilities

$$P(\text{Pass}) = 3/5$$

$$P(\text{fail}) = 2/5$$

Step 2 -

Calculate Individual probability with Respect to each features.

$$P(\text{Confident} = \text{yes} | \text{Result} = \text{Pass}) = 2/3$$

$$P(\text{Studied} = \text{yes} | \text{Result} = \text{Pass}) = 2/3$$

$$P(\text{sick} = \text{yes} | \text{Result} = \text{Pass}) = 1/3$$

Similarly,

$$P(\text{Confident} = \text{Yes} | \text{Result} = \text{Fail}) = 1/2$$

$$P(\text{Studied} = \text{Yes} | \text{Result} = \text{Fail}) = 1/2$$

$$P(\text{Sick} = \text{Yes} | \text{Result} = \text{Fail}) = 1/2$$

Step 3 -

$$P(X | \text{Result} = \text{Pass}) \times P(\text{Result} = \text{Pass}) = (2/3) \times (2/3) \times (1/3) \times (3/5) = \underline{0.088}$$

$$P(X | \text{Result} = \text{Fail}) \times P(\text{Result} = \text{Fail}) = (1/2) \times (1/2) \times (1/2) \times (2/5) = \underline{0.05}$$

Step 4 -

Calculate probability of estimator

$$P(X) = P(\text{Confident} = \text{Yes}) \times P(\text{Studied} = \text{Yes}) \times P(\text{Sick} = \text{No}) = (3/5) \times (3/5) \times (2/5) = 0.144$$

Step 5 -

$$P(\text{Result} = \text{Pass} | X) = 0.088 / 0.144 = \underline{0.611}$$

$$P(\text{Result} = \text{Fail} | X) = 0.05 / 0.144 = \underline{0.34}$$

Result →

As  $0.611 > 0.31$

Instance with

Confident = Yes, Studied = Yes, Sick = No

Result is 'Pass'