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EE24BTECH11040 - Mandara Hosur

Question:

Point P(x, 4) lies on the line segment joining the points A(-5, 8) and B(4, -10). Find the ratio in which point P divides the line segment AB. Also, find the value of x.

Solution: Given that all 3 points lie on the same line. Therefore,

$$\mathbf{A} - \mathbf{B} = r(\mathbf{A} - \mathbf{P})$$

where r is some constant of proportionality.

$$\binom{-5}{8} - \binom{4}{-10} = r \left(\binom{-5}{8} - \binom{x}{4} \right)$$

$$\implies \begin{pmatrix} -9 \\ 18 \end{pmatrix} = r \begin{pmatrix} -5 - x \\ 4 \end{pmatrix}$$

Now,

$$18 = 4r$$

$$\implies r = \frac{18}{4} = \frac{9}{2}$$

Also,

$$9 = r(5 + x)$$

$$\implies 9 = \frac{9}{2}(5 + x)$$
or, $x = -3$

By section formula,

$$\mathbf{P} = \frac{1}{1+k} \left(\mathbf{A} + k \mathbf{B} \right)$$

Here, k denotes the ratio in which the line segment AB has been divided by \mathbf{P} .

$$\begin{pmatrix} -3\\4 \end{pmatrix} = \frac{1}{1+k} \left(\begin{pmatrix} -5\\8 \end{pmatrix} + k \begin{pmatrix} 4\\-10 \end{pmatrix} \right)$$

$$\implies \begin{pmatrix} -3\\4 \end{pmatrix} = \frac{1}{1+k} \begin{pmatrix} 4k-5\\8-10k \end{pmatrix}$$
or, $k = \frac{2}{7}$

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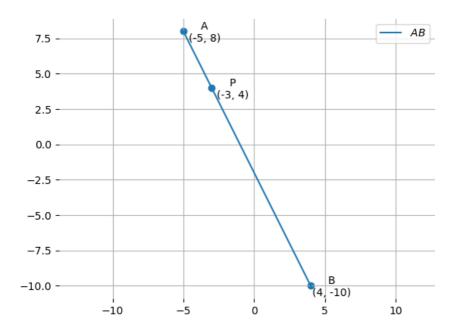


Fig. 0.1: Plot of line segment AB along with point \mathbf{P}