EE24BTECH11040 - Mandara Hosur

Question:

Show that the points (-2,3,5), (1,2,3) and (7,0,-1) are collinear. **Solution:**

Given Points	Description
(-2, 3, 5)	Point A
(1, 2, 3)	Point B
(7,0,-1)	Point C

TABLE 0: Given Information

The matrix

$$(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A})^{\mathsf{T}} = \begin{pmatrix} 3 & -1 & -2 \\ 9 & -3 & -6 \end{pmatrix}$$

$$\xrightarrow{R_2 = R_2 - 3R_1} \begin{pmatrix} 3 & -1 & -2 \\ 0 & 0 & 0 \end{pmatrix}$$

$$(0.1)$$

$$\stackrel{R_2=R_2-3R_1}{\longleftrightarrow} \begin{pmatrix} 3 & -1 & -2 \\ 0 & 0 & 0 \end{pmatrix} \tag{0.2}$$

has rank of 1.

Hence, it has been proved that the three given points are collinear.

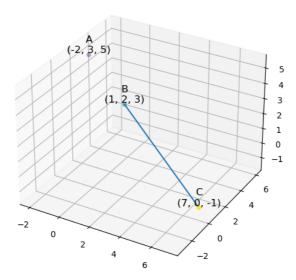


Fig. 0.1: 3D plot of line through points A, B, C