



Branch: ALL

Academic Year: 2020-21

Course Code: FE-C

201 Course Name: Engineering Mathematics II [Choice Based]

Assignment 2

Ques. No.	Question	Module	Level*	PI	CO
1	<p>Choose the correct answer from the options below:</p> <p>1. The roots of the auxiliary equation are imaginary and repeated ($m = \alpha \pm i\beta$) in the differential equation $f(D)y = 0$ then its solution is</p> <p>a) $y = e^{\alpha x}(C_1 \cos \beta x + C_2 \sin \beta x)$</p> <p>b) $y = e^{\alpha x}[(C_1 + C_2 x) \cos \beta x + (C_3 + C_4 x) \sin \beta x]$</p> <p>c) $y = e^{\alpha x}(C_1 \cosh \sqrt{\beta} x + C_2 \sinh \sqrt{\beta} x)$</p> <p>d) $y = e^{\alpha x}[(C_1 + C_2 x) \cosh \sqrt{\beta} x + C_3 \sinh \sqrt{\beta} x]$</p> <p>2. $e^{-x}(c_1 \cos \sqrt{3}x + c_2 \sin \sqrt{3}x) + c_3 e^{2x}$ is the general solution of</p> <p>a. $\frac{d^3 y}{dx^3} + 4y = 0$ b. $\frac{d^3 y}{dx^3} - 8y = 0$</p> <p>c. $\frac{d^3 y}{dx^3} + 8y = 0$ d. $\frac{d^3 y}{dx^3} - 2 \frac{d^2 y}{dx^2} y + \frac{dy}{dx} - 2 = 0$</p> <p>3. The D.E. whose auxiliary equation has the roots 0, -1, -1 is-</p> <p>a. $\frac{d^4 y}{dx^4} + 4y = 0$ b. $\frac{d^3 y}{dx^3} - 8y = 0$</p> <p>c. $\frac{d^3 y}{dx^3} + 8y = 0$ d. $\frac{d^3 y}{dx^3} + 2 \frac{d^2 y}{dx^2} y + \frac{dy}{dx} = 0$</p> <p>4. If $f(D) = D^2 - 2$, $\frac{1}{f(D)} e^{2x} = \dots$</p> <p>a) $\frac{1}{4} e^{2x}$ b) $\frac{1}{2} e^{2x}$</p> <p>c) $\frac{1}{-4} e^{2x}$ d) $2e^{2x}$</p> <p>5. If $f(D) = (D - a)^r \phi(D)$ then $\frac{1}{f(D)} e^{ax} = \dots \dots \dots$</p> <p>a) $\frac{x^r}{r!} \cdot \frac{1}{\phi(a)} e^{ax}$ b) $x \cdot \frac{1}{\phi(a)} e^{ax}$</p> <p>c) $\frac{1}{f(a)} e^{ax}$ d) $e^{ax} \frac{1}{f(D+a)}$</p>	2	1	1.1.1	2
		2	1	1.1.1	2
		2	1	1.1.1	2
		2	1	1.1.1	2

2	<p>Match the following</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>A</p> <p>1. $\frac{1}{f(D)} e^{ax}$</p> <p>2. $\frac{1}{f(D)} \cdot a^x$</p> <p>3. $\frac{1}{(D^2+a^2)^2} \cos ax$</p> <p>4. $\frac{1}{f(D)} e^{-ax} \cdot V$</p> <p>5. U (variation of parameter)</p> <p>6. V (variation of parameter)</p> <p>7. W</p> <p>8. $\frac{\sin ax}{f(D^2+a^2)}$</p> <p>9. $\frac{X}{(D-a)}$</p> </div> <div style="text-align: center;"> <p>B</p> <p>a) $\int \frac{y_1 X}{W} dx$</p> <p>b) $-\int \frac{y_2 X}{W} dx$</p> <p>c) $\frac{-x \cos ax}{2a}$</p> <p>d) $\begin{vmatrix} y_1 & y_2 \\ y_1' & y_2' \end{vmatrix}$</p> <p>e) $\frac{1}{f(\log a)} \cdot a^x$</p> <p>f) $e^{ax} \int e^{-ax} x dx$</p> <p>g) $\frac{x^r}{r!} \cdot \frac{1}{\phi(a)} e^{ax}$</p> <p>h) $\frac{-x^2 \sin ax}{4a^2}$</p> <p>i) $e^{-ax} \frac{1}{f(D-a)} V$</p> </div> </div>	2	1	1.1.1	2
3	<p>Fill in the blanks</p> <p>1. P.I. of $(D^2 + 4)y = \sin 3x$ is</p> <p>2. P.I. of $(D^2 - 2D + 1)y = e^x$ is</p> <p>3. If the characteristic equation of the D.E.</p> $\frac{d^2 y}{dx^2} + 2\alpha \frac{dy}{dx} + y = 0$ <p>Have two equal roots, then $\alpha = \dots$</p>	2	1	1.1.1	2
4	<p>Define the following</p> <p>i) Complementary function</p> <p>ii) Particular integral</p>	2	1	1.1.1	2
5.	<p>State True or False</p> <p>i) The differential equation $y'' - \sin y y' + 2y = 0$ is a linear equation with constant coefficient.</p> <p>ii) The method of variation of parameters can be used to solve the equation $y'' + e^t y' + t^2 y = \sin t$</p> <p>iii) General solution of the differential equation</p> $\frac{d^3 y}{dx^3} + 4y = 0$ <p>must contain four arbitrary constants.</p>	3	2	1.1.1	3

6.	i. Solve $(D^2 - 2D + 1)y = e^x + 1$	2	2	1.1.1	2
	ii. Solve $(D^4 + 1)y = \cosh 4x \cdot \sinh 3x$	2	2	1.1.1	2
	iii. Solve: $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = x^2 + e^x + \cos 2x$	2	2	1.1.1	2
	iv. Solve $(D^2 + 2)y = e^x \cos x + x^2 e^{3x}$	2	2	1.1.1	2
	v. Solve $\frac{d^3y}{dt^3} + \frac{dy}{dt} = \cos t + t^2 + 3$	1	2	1.1.1	1
7	i. Solve. $(D^2 - D - 2)y = 2\log x + \frac{1}{x} + \frac{1}{x^2}$	3	2	1.1.1	3
	ii. Solve $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = xe^x \sin x$	3	2	1.1.1	3
	iii. Solve by method of variation of parameters $\frac{d^2y}{dx^2} + y = \frac{1}{1 + \sin x}$	3	2	1.1.1	1
	iv. Solve by method of variation of parameters $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = e^{e^x}$	3	2	1.1.1	1
8	i) Application of first order and first degree differential equation	2	3	1.1.1	2