

1. Show where the distribution is centered at and compare it to the theoretical center of the distribution.

```
n <- 40
lambda <- 0.2
reps <- 1000

Exp <- 0
for (i in 1:reps)
{
  Exp <- Exp + rexp(n,lambda)
}
Exp <- Exp / reps

summary(Exp)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      4.57   4.94   5.03   5.02   5.08   5.45
```

```
#theoretical mean = 1/lambda = 5
#simulated mean:
mean <- mean(Exp)
mean
```

```
## [1] 5.019
```

2. Show how variable it is and compare it to the theoretical variance of the distribution.

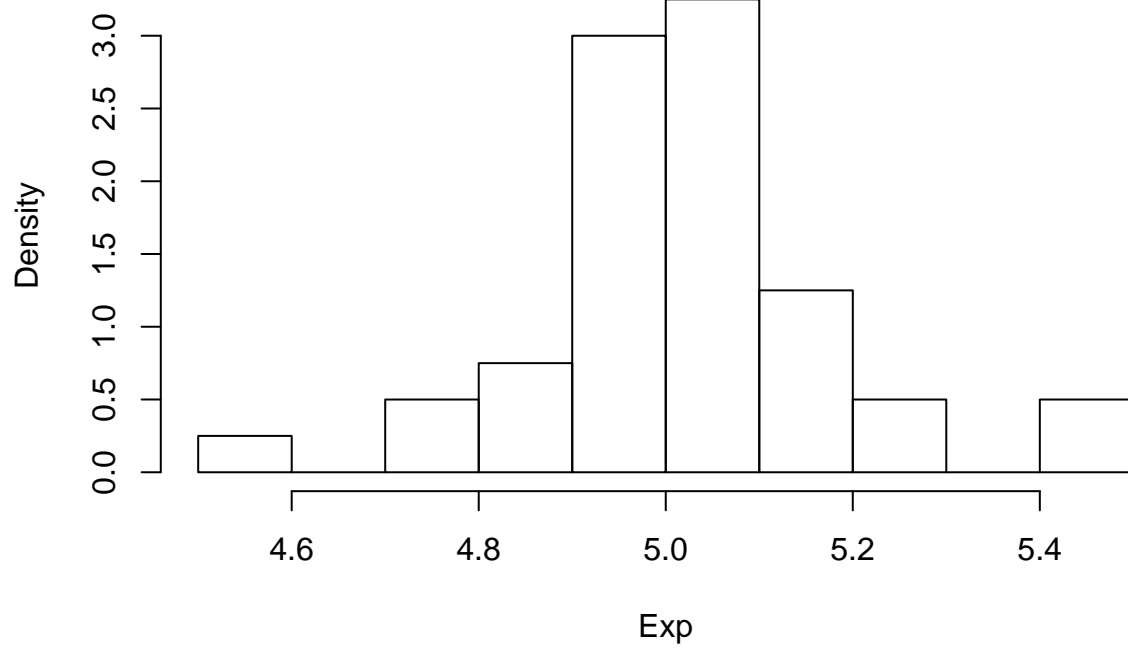
```
#theoretical variance = lambda^-2 = 0.04
#simulated variance:
1/(mean(Exp))^2
```

```
## [1] 0.0397
```

3. Show that the distribution is approximately normal.

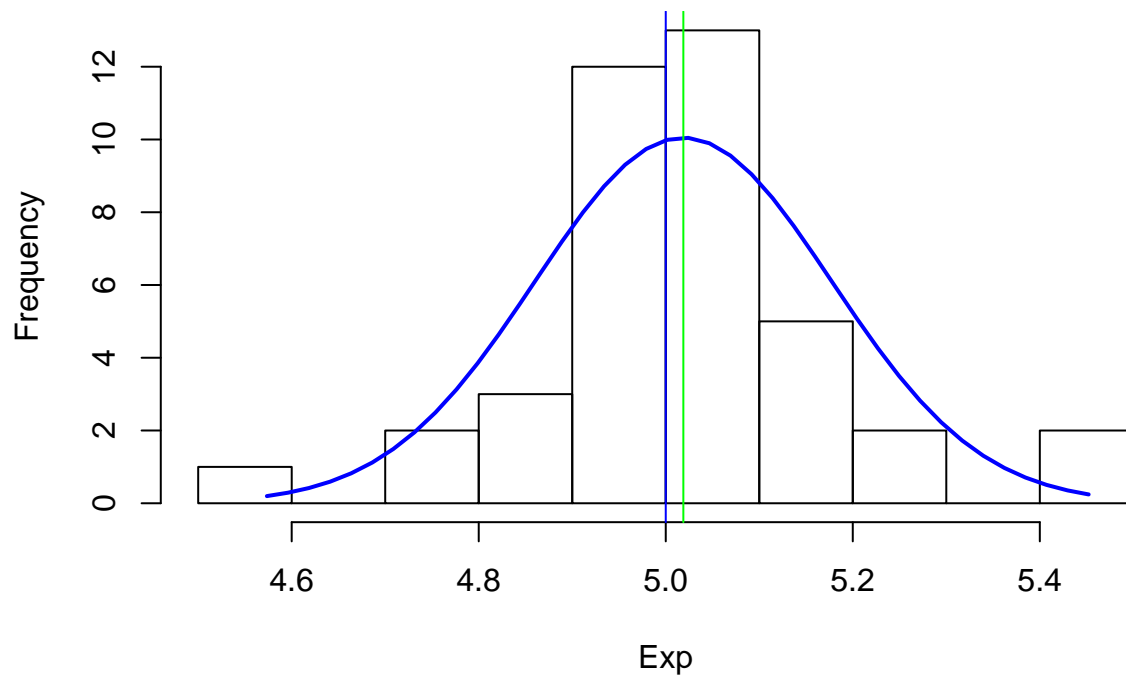
```
h <- hist(Exp,freq=FALSE)
```

Histogram of Exp



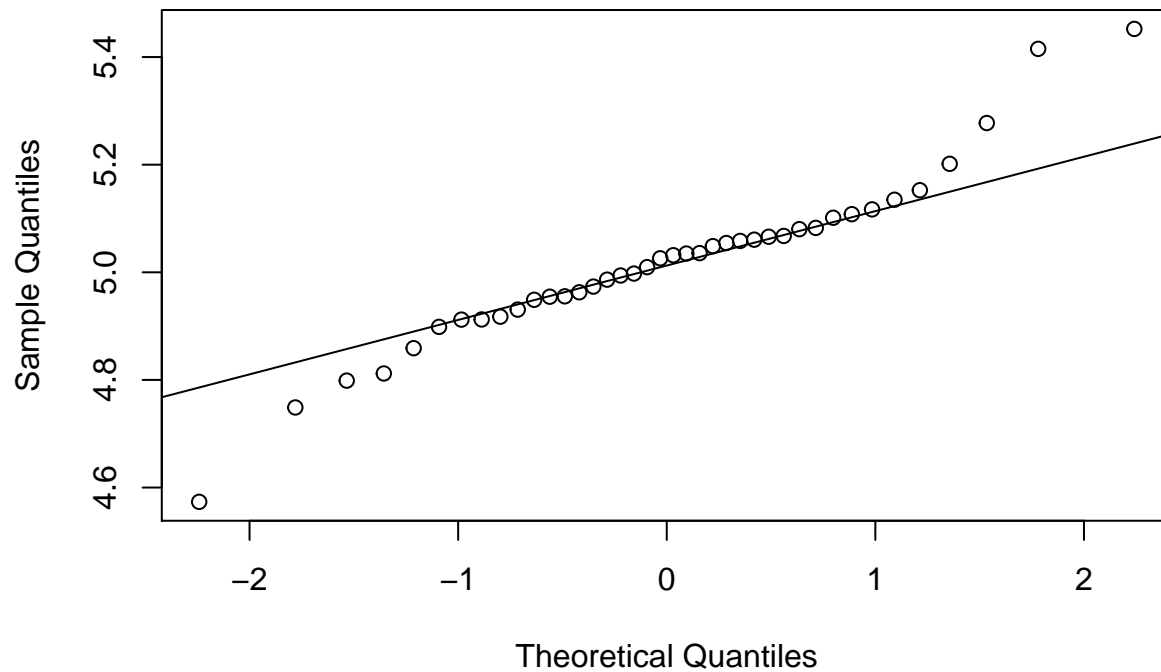
```
xfit<-seq(min(Exp),max(Exp),length=40)
yfit<-dnorm(xfit,mean=mean(Exp),sd=sd(Exp))
yfit <- yfit*diff(h$mids[1:2])*length(Exp)
plot(h, main="Comparison to Normal Distribution")
lines(xfit, yfit, col="blue", lwd=2)
abline(v=1/lambda,col="blue")
abline(v=mean,col="green")
```

Comparison to Normal Distribution



```
qqnorm(Exp)  
qqline(Exp)
```

Normal Q-Q Plot



4. Evaluate the coverage of the confidence interval for $1/\lambda$

```
left <- mean - qt(.95,40)*sd(Exp)/sqrt(n)
right <- mean + qt(.95,40)*sd(Exp)/sqrt(n)
left
```

```
## [1] 4.977
```

```
right
```

```
## [1] 5.061
```