

# Practical Work number 4:

Problem number 6, Manea Robert-Petrisor Group 914.

**Prim's** algorithm is a popular algorithm used to find the minimum spanning tree (MST) of a weighted undirected graph. The minimum spanning tree is a tree that spans all the vertices of the graph while minimizing the total weight or cost of the tree.

```
def prim(graph, start_vertex):
    visited = {start_vertex}
    edges = []
    current_node = start_vertex

    while len(visited) < graph.numberOfVertices():
        for neighbor in graph.Outbound_of_vertex(current_node):
            weight = graph.Costs_of_vertices(current_node, neighbor)
            if neighbor not in visited:
                heappush(edges, (weight, current_node, neighbor))

        while edges:
            weight, u, v = heappop(edges)
            if v not in visited:
                visited.add(v)
                yield u, v, weight
                current_node = v
                break
```

Start with a variable **start\_vertex** (this is the vertex inputted by the user) and add it to the set of visited vertices.

Create an empty list named **edges** to store potential edges for expanding the MST.

While there are unvisited vertices:

- For each neighbor of the current vertex, calculate the weight of the edge connecting them.
- If the neighbor is not visited, add the edge to the **edges** list.
- Choose the edge with the minimum weight from the **edges** list.
- If the destination vertex of the chosen edge is not visited, add it to the set of visited vertices and yield the edge as part of the MST.
- Set the current vertex to the destination vertex of the chosen edge.

Repeat until all vertices are visited.

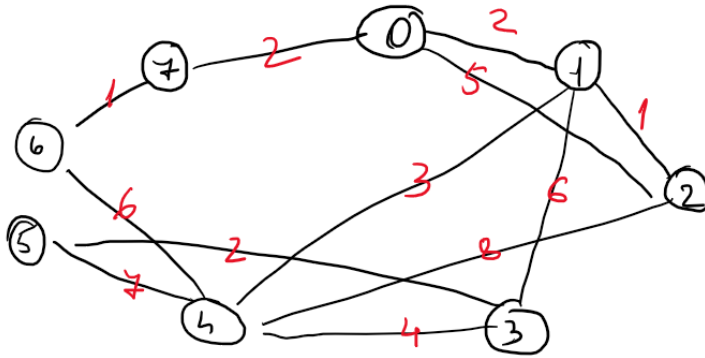
In summary, Prim's algorithm starts from a specified vertex and repeatedly selects the minimum-weight edge that connects visited vertices to unvisited vertices. It grows the minimum spanning tree by adding these edges until all vertices are included.

Manual Executions:

Graph:

Vertices:  $0 \rightarrow 7$

Edges: (first vertex, second vertex, weight):  
 $(0, 1, 2), (0, 2, 5), (1, 2, 1), (1, 3, 6), (1, 4, 3), (2, 4, 8),$   
 $(3, 4, 4), (3, 5, 2), (4, 5, 7), (4, 6, 6), (6, 7, 1), (7, 0, 2)$



Iteration	Visited Vertices	Current node	Edges in Heap	Adding edges to Heap	Selected Edge
1	0	0	$[\ ]$	$[(2, 0, 1), (5, 0, 2), (2, 0, 7)]$	$(0, 1, 2)$
2	0, 1	1	$[(2, 0, 7), (5, 0, 2)]$	$[(1, 1, 2), (3, 1, 4), (2, 1, 3), (6, 1, 3), (5, 1, 2)]$	$(1, 2, 1)$
3	0, 1, 2	2	$[(2, 0, 7), (3, 1, 4), (5, 0, 2), (6, 1, 3)]$	$[(2, 0, 7), (3, 1, 4), (5, 0, 2), (6, 1, 3), (3, 2, 4)]$	$(0, 7, 2)$
4	0, 1, 2, 7	7	$[(3, 1, 4), (6, 1, 3), (5, 0, 2), (3, 2, 4)]$	$[(1, 7, 6), (3, 7, 4), (5, 0, 2), (6, 7, 1), (6, 1, 3)]$	$(7, 6, 1)$

$$5 \quad 0, 1, 2, 6, 7 \quad 6 \quad [(3, 1, 4), (6, 1, 3), (5, 0, 2), (8, 2, 4)] \quad [(3, 1, 4), (6, 1, 3), (5, 0, 2), (8, 2, 4), (6, 6, 4)] \quad (4, 3)$$

$$6 \quad \{0, 1, 2, 4, 6, 7\} \quad 4 \quad [(5, 0, 2), (6, 1, 3), (6, 6, 4), (8, 2, 4)] \quad [(4, 4, 3), (5, 0, 2), (6, 6, 4), (8, 2, 4), (6, 1, 3), (7, 4, 5)] \quad (4, 3, 4)$$

$$4 \quad \{0, 1, 2, 3, 4, 6, 7\} \quad 3 \quad [(5, 0, 2), (6, 1, 3), (6, 6, 4), (8, 2, 4), (7, 4, 5)] \quad [(2, 3, 5), (6, 1, 3), (5, 0, 2), (8, 2, 4), (7, 4, 5), (6, 6, 4)] \quad (3, 5, 2)$$

Edges + Costs

(0, 1) : 4

(0, 2) : 7

(1, 2) : 7

(1, 3) : 5

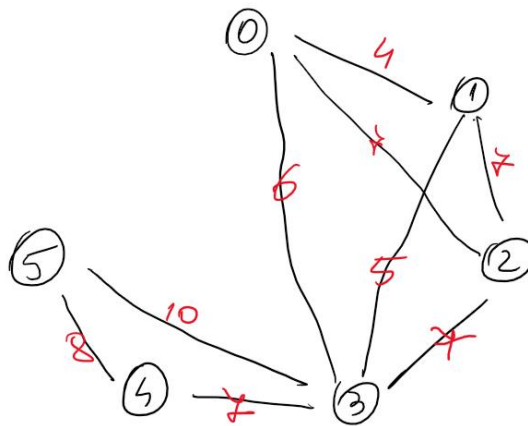
(0, 3) : 6

(2, 3) : 7

(3, 4) : 7

(4, 5) : 8

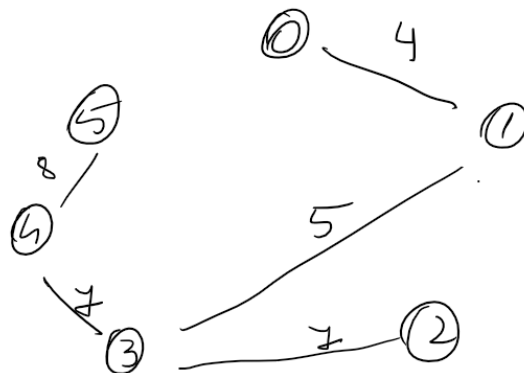
(5, 3) : 10



1st MST:

Total cost:

31



2nd MST:

Total cost:

31

