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Quantum assisted Secure Multiparty Computation

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Abstract

Start with no indent.

Then you can write another paragraph.

Key-words: quantum cryptography, quantum oblivious transfer, quantum obliious linear evaluation, secure multiparty computation.

Resumo

Escrever a mesma coisa que est no Abstract, mas em Portugus.

Palavras-chave: criptografia quântica, passeios quânticos, memórias quânticas, transições de fase topológicas, estados de fronteira

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I dedicate this thesis to my loving wife Teresinha and my two children Henrique and Helena who came to life during this journey to help me finish it.

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List of Abbreviations

A – Alice

B – Bob

BCS – Bardeen-Cooper-Schrieffer

BG – Boltzmann-Gibbs

CS – Chiral symmetry

DTQW – Discrete-time quantum walk

DQPT – Dynamical quantum phase transition

E – Eve

EB – Entanglement based

LE – Loschmidt Echo

MDM – Massive Dirac model

PHS – Particle-hole symmetry

PT – Phase transition

PM – Prepare and measure

SSH – Su-Schrieffer-Heeger

TI – Topological insulator

TSC – Topological superconductor

TRS – Time-reversal symmetry

QKD – Quantum Key Distribution

QW – Quantum walk

Chapter 1

Introduction

The emerging fields of Data Mining and Data Analysis have deeply benefited from the increasing power of computers [1]. However, its need for a massive and methodical collection of data can lead to the complete or partial leak of private sensitive information, such as in the case of the genomics field [2–5]. As a consequence, the aggregation of data from different sources is most of the times blocked due to legally imposed regulations such as the General Data Protection Regulation (GDPR) [6]. Although this has the benefit of protecting people’s privacy, it also has the downside of preventing honest players from accessing data necessary to tackle some of the most important issues in our society.

Secure Multiparty Computation

To overcome the privacy-related issues described above, several privacy-enhancing technologies have been proposed [7–9]. One important area of research is Secure Multiparty Computation (SMC). This technology allows a set of n parties P_i to jointly compute some function $f(x_1, \dots, x_n) = (y_1, \dots, y_n)$ without disclosing their inputs to the other parties. The security requirements of SMC are equivalent to an ideal case, where every party P_i sends his inputs to some independent and trusted third party, who computes $f()$ and sends back to each party their corresponding output.

Since Yao seminal work [10], several SMC protocols have been developed, rendering different framework implementations [11–13]. However, they can generally be separated into two types according to the circuit logic being used: boolean or arithmetic. In each case, the efficiency and security of SMC heavily rely on the efficiency and security of important cryptographic primitives. Boolean-based SMC protocols rely on Oblivious Transfer (OT) [14] and arithmetic-based rely on Oblivious Linear Evaluation (OLE) [15]. Impagliazzo and Rudich [16] proved that both OT and OLE protocols require public cryptography and cannot just rely on symmetric cryptography. This is an unfortunate

result both from an efficiency and security perspective. Indeed, symmetric cryptography is lighter than asymmetric cryptography and requires less computational assumptions. Moreover, with the emergence of quantum computers, Shors algorithm [17] jeopardizes all the current public-key methods based on RSA, Elliptic Curves or Diffie-Hellman, in which many OT and OLE implementations rely on. This puts at risk the deployment of classical OT and OLE, which ultimately leads to the exposure of the SMC parties private inputs. Thus, it is essential to develop SMC methods secure against quantum computers while not compromising state-of-the-art performance levels.

A Quantum Era

We are now in the beginning of what is known to be the second quantum revolution. Quantum technology has evolved to a point where we can integrate quantum exotic features into complex engineering systems. Most of the applications lie in the field of quantum cryptography, where one thrives to find protocols that offer some advantage over their classical counterparts. As analysed in [18, 19], these advantages can be of two types:

1. Improve the security requirements, rendering protocols that are information-theoretically secure or require fewer computational assumptions;
2. Achieve new primitives that were previously not possible just with classical techniques.

Despite the most famous use-case of quantum cryptography being quantum key distribution (QKD), other primitives play an important role in this quest. Some examples of these cryptographic tasks are bit commitment [20], coin flipping [21], delegated quantum computation [22], position verification [23], and password-based identification [24, 25].

Also, the intrinsic randomness provided by quantum phenomena is an ideal resource to develop quantum communication protocols for oblivious transfer (OT) [26]. Remarkably, there is a distinctive difference between classical and quantum OT from a security standpoint, as the latter is proved to be possible assuming only the existence of quantum-hard one-way functions [27, 28]. This means quantum OT can be based only on symmetric cryptography, requiring weaker security assumptions than classical OT. Moreover, these quantum protocols frequently have a desirable property that guarantees information-theoretic security after the execution of the protocol. This property is commonly called everlasting security. This greatly improves the security of SMC protocols, allowing them to have their security based on symmetric cryptography alone and with this important feature of everlasting security. Regarding oblivious linear evaluation (OLE) primitive, it is known that it can be reduced to OT [29] through classical methods that do not require further

assumptions. Therefore, it seems natural to use quantum OT to generate quantum-secure OLE instances.

Contributions and Outline

Despite the many advances, the adoption of quantum cryptography by secure multiparty computation (SMC) systems is still reduced. This is due to the efficiency challenges imposed by quantum technology and the need of high throughput of both OT and OLE primitives in boolean- and arithmetic-based SMC, respectively.

The overall goal of this dissertation is to give one step closer to the adoption of quantum cryptography by SMC systems. We do this with three contributions. In our first contribution, we start the studying of comparing the efficiency of both classical and quantum protocols. Our second contribution is the first quantum OLE protocol which does not rely on OT. Our last contribution is an implementation of a special-purpose SMC system applied to genomics analysis assisted with quantum OT. Along the way, we produced a review dedicated to quantum OT protocols alone. Usually, its analysis is integrated into more general surveys under the topic of quantum cryptography, leading to a less in-depth exposition of the topic.

We describe the contributions in a bit more detail.

Efficiency of classical and quantum OT protocols. To the best of our knowledge, there is no comparative study on the efficiency of quantum and classical approaches. This is mainly caused by two reasons. From a theoretical perspective, the use of different types of information (quantum and classical) makes it difficult to make a fair comparison based on the protocols' complexity. Also, from a practical standpoint, there is still a discrepancy in the technological maturity between quantum and classical techniques. Quantum technology is still in its infancy, whereas classical processors and communication have many decades of development.

Despite these constraints, we compare the complexity and operations efficiency of classical and quantum protocols. To achieve this, we realize that both classical and quantum protocols can be divided into two phases: offline and online. The offline phase is characterized by the fact that it is independent of the parties' inputs. This means that, from a practical point-of-view, this phase produces the resources necessary to use during the online phase, where we take into consideration the parties' inputs. It can be argued that the offline phase is not so hungry-efficient as the online phase. As a consequence, for comparison purposes, we can focus on the online phase. Fortunately, the online phase of quantum OT is solely based on classical communications. Therefore, it is possible and

fair to compare the online phase of both classical and quantum protocols.

We make a detailed comparison between the complexity of the online phase of two state-of-the-art classical OT protocols [30, 31] and an optimized quantum OT protocol. We conclude that the online phase of quantum OT competes with its classical counterparts and has the potential to be more efficient.

Quantum oblivious linear evaluation protocol. Our second contribution is a quantum protocol for OLE with quantum universally composable (quantum-UC) security in the \mathcal{F}_{COM} -hybrid model, i.e. when assuming the existence of a commitment functionality, \mathcal{F}_{COM} . To obtain a secure protocol, we take advantage of the properties of Mutually Unbiased Bases in high-dimensional Hilbert spaces with prime and prime-power dimension. Such a choice is motivated by recent theoretical and experimental advances that pave the way for the development and realization of new solutions for quantum cryptography [32–36].

To the best of our knowledge our protocol is the first quantum-UC secure quantum OLE proposal. Moreover, it is not based on any quantum OT implementation which would be the standard approach. We consider the static corruption adversarial model with both semi-honest and malicious adversaries. We develop a weaker version of OLE, which may be of independent interest. We also modify the proposed protocol to generate quantum-UC secure vector OLE (VOLE). We give bounds on the possible size of VOLE according to the security parameters.

Quantum assisted secure multiparty computation. Individuals privacy and legal regulations demand genomic data be handled and studied with highly secure privacy-preserving techniques. In this contribution, we propose a feasible secure multiparty computation (SMC) system assisted with quantum cryptographic protocols that is designed to compute a phylogenetic tree from a set of private genome sequences. This system adapts several distance-based methods (Unweighted Pair Group Method with Arithmetic mean, Neighbour-Joining, Fitch-Margoliash) into a private setting where the sequences owned by each party are not disclosed to the other members present in the protocol. We do not apply a generic implementation of SMC to the problem of phylogenetic trees. Instead, we develop a tailored private protocol for this use case in order to improve efficiency.

We theoretically evaluate the performance and privacy guarantees of the system through a complexity analysis and security proof and give an extensive explanation about the implementation details and cryptographic protocols. We also implement a quantum-assisted secure phylogenetic tree computation based on the Libscapi implementation of the Yao protocol, the PHYLIP library and simulated keys of two quantum systems: quantum

oblivious key distribution and quantum key distribution.¹. This demonstrates its effectiveness and practicality. We benchmark our implementation against a classical-only solution and we conclude that both approaches render similar execution times. The only difference between the quantum and classical systems is the time overhead taken by the oblivious key management system of the quantum-assisted approach.

The results are presented as follows. We start presenting SMC protocols based on OT and OLE at Chapter 2. Then, at Chapter 3 we introduce some quantum information concepts and security definitions used throughout the thesis. Chapter 4 is devoted to quantum oblivious transfer protocols. Then, in Chapter 5 we compare classical and quantum approaches for OT. In Chapter 6 we present our quantum OLE protocol along with its security proof. Finally, in Chapter 7, we presented our implementation of quantum-assisted SMC system applied to phylogeny analysis.

Published research

This thesis is based on research published in various journals. During my PhD I was involved in the following projects.

- [37] Manuel B. Santos, Paulo Mateus, and Armando N. Pinto. Quantum Oblivious Transfer: A Short Review. In: *Entropy* 24.7 (July 2022), p. 945.
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¹ The code can be accessed at the following repo: <https://github.com/manel1874/QSHY/tree/dev-cq-phylip>

Chapter 4 is based on [37]. Chapter 5 is based on the work developed on both [37] and [39]. Chapter 6 presents all the results from [38]. Finally, Chapter 7 is the combination of [39–41]

Chapter 2

Technical Overview

2.1 Secure Multiparty Computation

Estrutura da introdução:

- Comentar que não sabemos mais do que o output da computação. Dar o exemplo da média de pesos. 2 pessoas sabemos o resultado. 3 não. Ainda assim, pode revelar alguma coisa a mais. Note that, practically, we can put together other PET such as Differential Privacy in order to do this.

Talk about two approaches: boolean and arithmetic. Discuss the advantages and disadvantages of each.

2.1.1 Boolean approach

Boolean approach is based on the Yao protocol. In order to do it we need OT. We start by presenting OT and then we describe the Yao protocol.

Oblivious Transfer

The study of oblivious transfer (OT) has been very active since its first proposal in 1981 by Rabin [42]. The importance of OT comes from its wide number of applications. More specifically, one can prove that OT is equivalent to the secure two-party computation of general functions [10, 14], i.e. one can implement a secure two-party computation using OT as its building block. Additionally, this primitive can also be used for secure multiparty computation (SMC) [29], private information retrieval [43], private set intersection [44], and privacy-preserving location-based services [45].

Definition

Small classical review

Base OT vs Extended OT

Yao protocol

Description

Optimizations

Security

Generalizations of Yao: GMW, BMR

2.1.2 Arithmetic approach

Oblivious Linear Evaluation

SPDZ

2.2 Quantum Information

2.2.1 Mathematical preliminaries

2.2.2 Quantum states representation

2.2.3 Entropy

2.2.4 Two-universal functions

2.2.5 Mutually Unbiased Basis

2.3 Universal Composability

2.4 Functionality definitions

Chapter 3

Quantum Oblivious Transfer

In a recent survey on classical oblivious transfer (OT) [46], all the analysed protocols require some form of asymmetric cryptography. Indeed, in the classical setting, it is impossible to develop information-theoretic secure OT or even reduce it to one-way functions, requiring some public-key computational assumptions. As shown by Impagliazzo and Rudich [47], one-way functions (symmetric cryptography) alone do not imply key agreement (asymmetric cryptography). Also, Gertner et al. [48] pointed out that since it is known that OT implies key agreement, this sets a separation between symmetric cryptography and OT, leading to the conclusion that OT cannot be generated alone by symmetric cryptography. Otherwise, one could use one-way functions to implement key agreement through the OT construction. This poses a threat to all classical OT protocols [49–51] that are based on mathematical assumptions provably broken by a quantum computer [17]. Besides the security problem, asymmetric cryptography tends to be computationally more complex than symmetric cryptography, creating a problem in terms of speed when a large number of OTs are required. The classical post-quantum approach, thrives to find protocols resistant against quantum computer attacks. However, these are still based on complexity problems and are not necessarily less computationally expensive, than the previously mentioned ones.

In parallel to the classical post-quantum approach, the quantum cryptography community presented some OT protocols based on quantum technologies to tackle this security issue. Intriguingly enough, more than a decade before the first classical OT by Rabin (1981, [42]) was published, Wiesner proposed a similar concept. However, at the time it was rejected for publication due to the lack of acceptance in the research community. The first published quantum OT (QOT) protocol, known as the BBCS (Bennett-Brassard-Cr peau-Skubiszewska) protocol [26] was only presented in 1992. Remarkably, there is a distinctive difference between classical and quantum OT from a security standpoint, as the latter is proved to be possible assuming only the existence of quantum-hard one-way

functions [27, 28]. This means quantum OT requires weaker security assumptions than classical OT.

In this chapter, we review the particular topic of quantum OT. We mainly comment on several important OT protocols, their underlying security models and assumptions. To the best of our knowledge, there is no prior survey dedicated to quantum OT protocols alone. Usually, its analysis is integrated into more general surveys under the topic of “quantum cryptography”, leading to a less in-depth exposition of the topic. For reference, we provide some distinctive reviews on the general topic of quantum cryptography [18, 52–58].

This chapter is divided as follows. We start by giving a brief overview of the impossibility results related to quantum OT. Then, we provide an exposition about some of the most well-known quantum OT protocols based on assumptions. Finally, we give a brief overview of OT protocols not covered throughout this thesis.

3.1 Impossibility results

The beginning of the development of quantum OT (QOT) came hand in hand with the development of quantum bit commitment (QBC). In fact, the first proposed QOT protocol (BBCS [26]) reduces QOT to QBC. This sets a distinctive difference between classical and quantum protocols. Although bit commitment (BC) can be reduced to oblivious transfer (OT) [14], the reverse is not true using only classical communication [59]. Therefore, Yao’s proof [60] of BBCS protocol [26] gives quantum communications the enhanced quality of having an equivalence between QOT and QBC - they can be reduced to each other - a relation that is not known in the classical realm.

At the time of the BBCS protocol, the quest for unconditionally secure QOT was based on the possibility of unconditional secure QBC. A year later, Brassard et al. presented a QBC protocol [61] named after the authors, BCJL (Brassard-Crpeau-Jozsa-Langlois). However, this work presented a flawed proof of its unconditional security which was generally accepted for some time, until Mayers spotted an issue on it [62]. Just one year after, Lo and Chau [63], and Mayers [64] independently proved unconditional QBC to be impossible. Nevertheless, the existence of unconditionally secure QOT not based on QBC was still put as an open question [52] even after the so-called no-go theorems [63, 64]. However, Lo was able to prove directly that unconditionally secure QOT is also impossible [65]. He concluded this as a corollary of a more general result that states that secure two-party computations which allow only one of the parties to learn the result (one-side secure two-party computation) cannot be unconditionally secure. Lo’s results triggered a line of research on the possibility of two-sided secure two-party computation (both parties are allowed to learn the result without having access to the other party’s inputs), which

was also proved by Colbeck to be impossible [66] and extended in subsequent works [67–69]. For a more in-depth review of the impossibility results presented by Lo, Chau and Mayers, we refer the interested reader to the following works [59, 70].

Although the impossibility results have been well accepted in the quantum cryptography community, there was some criticism regarding the generality of the results [71–74]. This line of research reflects the view put forward by Yuen [71] in the first of these papers: “Since there is no known characterization of all possible QBC protocols, logically there can really be no general impossibility proof, strong or not, even if it were indeed impossible to have an unconditionally secure QBC protocol.” In parallel, subsequent analyses were carried out, reaffirming the general belief of impossibility [75–77]. However, most of the discord has ended with Ariano et al. proof [78] in 2007, giving an impossibility proof covering all conceivable protocols based on classical and quantum information theory. Subsequent work digested Ariano et al. [78] work, trying to present more succinct proofs [79–81] and to translate it into categorical quantum mechanics language [82–84].

Facing these impossibility results, the quantum cryptography community followed two main paths:

1. Develop OT protocols under some assumptions. These could be based on limiting the technological power of the adversary (e.g. noisy-storage model, relativistic protocols, isolated-qubit model) or assuming the security of additional functionalities (e.g. bit commitment).
2. Develop OT protocols with a relaxed security definition. These allow the adversary to extract, with a given probability, some information (partial or total) about the honest party input/output. This approach leads to the concepts of weak OT and weak private database query.

In the next section, we explore protocols that produce a special primitive called *oblivious keys* as an intermediate step.

3.2 QOT BBKS-based protocols

In this section, we explore protocols that circumvent the no-go theorems [63, 64] utilizing some assumptions. Some of the presented solutions are based on one-way functions, which are believed to be quantum-hard [27, 28], and others rely on some technological or physical limitation of the adversaries [29–34]. The latter are qualitatively different from complexity-based assumptions on which post-quantum protocols rely. Also, all these assumptions have the important property that they only have to hold during the execution of the protocol for its security to be preserved. In other words, even if the

assumptions lose their validity at some later point in time, the security of the protocol is not compromised, which also makes a major distinction from classical cryptographic approaches. This property is commonly known as *everlasting* security [?].

We start by presenting the first QOT protocol. Then, we see how this leads to the development of two assumption models: \mathcal{F}_{COM} –hybrid model and the limited-quantum-storage model.

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