

6:30 - 7:50 HUMN 1B50

6:30 ————— ECES 116 1%

13 Mult. Choice x 3pts each 39%

- 3 code

- 10 other

- basic defns

- med.

- hard

3 Free response x 20 each. 60%

① Pinned Piazza

②
$$\beta^3 - \alpha^3 = (\beta - \alpha)(\beta^2 + 2\alpha\beta + \alpha^2)$$

Calc: yes. No phones.
2-sided page of notes.

1. Quadratic $ax^2 + bx + c$

yes know
this.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

2. Basic Integration.

$$\int_a^b x^2 dx = \left. \frac{x^3}{3} \right|_a^b \quad \checkmark$$

Discrete RVs

- discrete outcomes

- finite # of outcomes

✓ $\text{Ber}(p)$

✓ $\text{Bin}(n, p)$

$$P(X = \pi) = \frac{1}{\pi}$$

$$P(X = e) = 1 - \frac{1}{\pi}$$

- infinite (countable)
of outcomes.

$\text{Geop}(p)$

P M F

- sums

Continuous RVs

- continuous outcomes

- uncountably infinite # of outcomes.

$U[\alpha, \beta]$

P D F

- integrals

Both:

• C D F

cumulative distribution function

$$CDF(a) = P(X \leq a)$$

↑
particular #

↑
R.V.

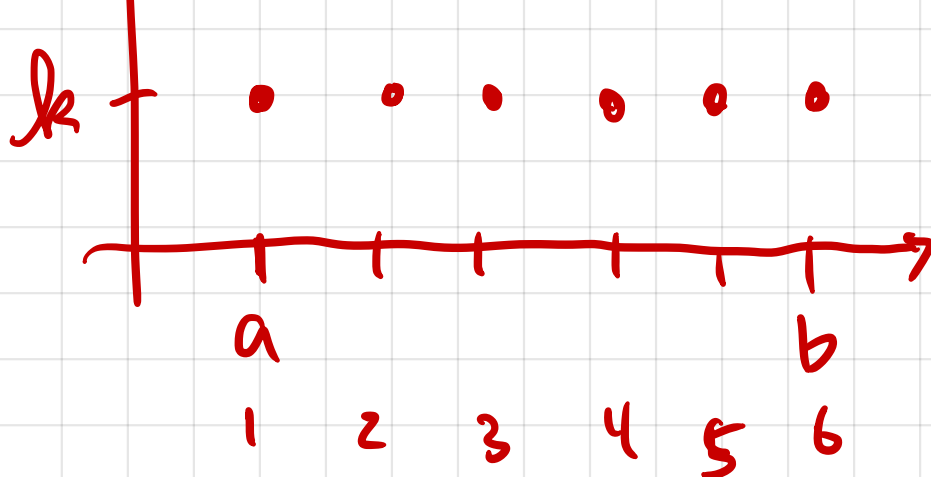
Both:

- Uniform distribution

- continuous

$$\text{PDF } f(x) = \frac{1}{\beta - \alpha} \quad \alpha \leq x \leq \beta$$
$$0 \quad \text{otherwise}$$

$$\text{PMF } f(x) = \frac{1}{n} \quad n \text{ is \# of points or outcomes.}$$



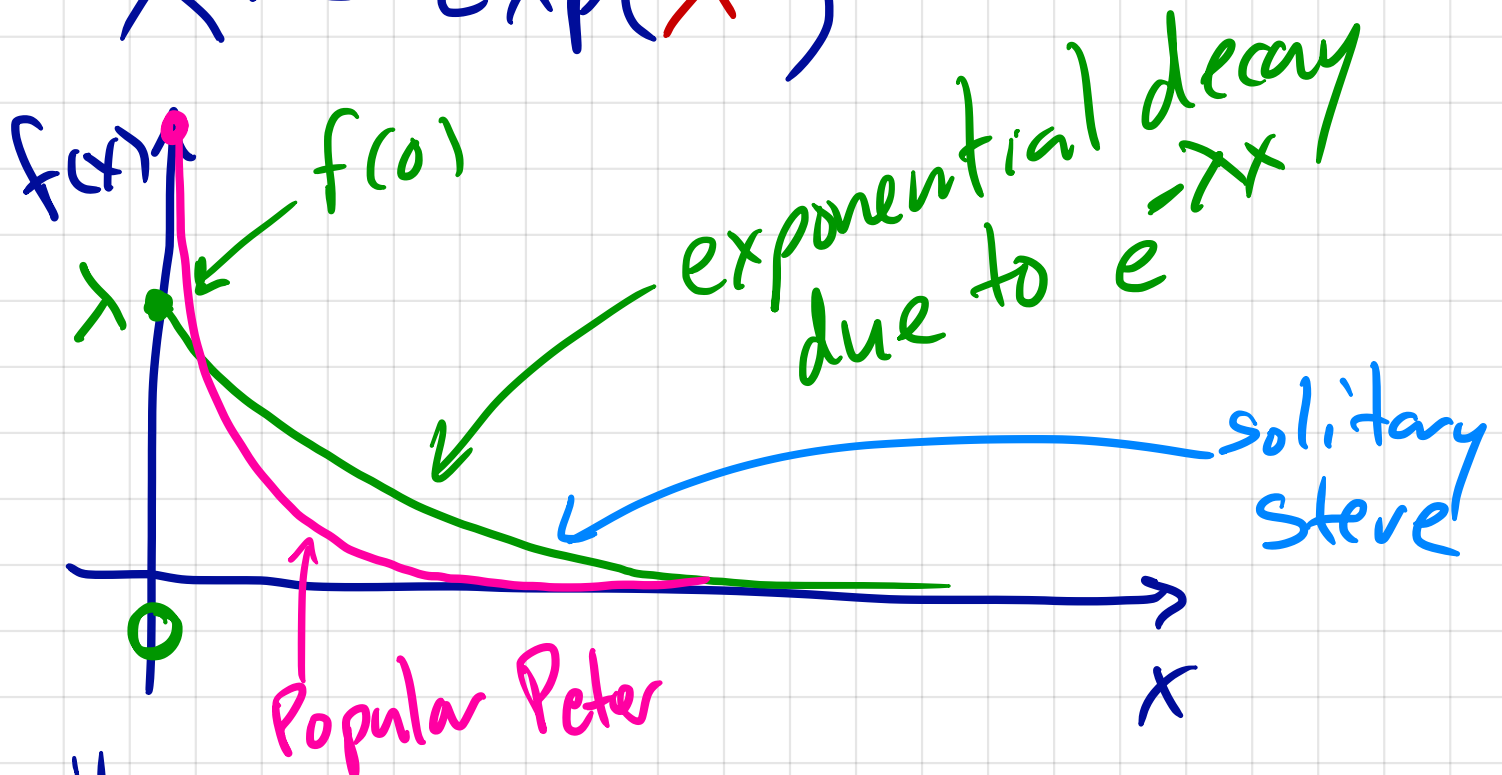
- $E[X]$, $\text{Var}(X) = E[X^2] - E[X]^2$

$$\sum_{\text{outcomes } i} a_i p(a_i) \quad \int_{-\infty}^{\infty} x f(x) dx$$

Exponential Distribution

$$\text{PDF: } \lambda e^{-\lambda x}$$

$$X \sim \text{Exp}(\lambda)$$



"Opposite of Poisson"

Poisson and Exponential Cousins

Discrete

↓
of texts
in some time
period.

Continuous

↓
Inter-arrival time
of texts.

What is the typical or expected waiting time for your 1st text?

Assume you get, on average, 10 texts per hour.

Waiting times $\sim \text{Exp}(10)$

In python, exponential (1/10)

$$E[\text{Exp}(10)] = \int_0^{\infty} x \lambda e^{-\lambda x} dx = \boxed{\frac{1}{\lambda}}$$

integ. by parts! :-

What is the probability that you wait between 30 and 60 minutes for that 1st text?

→ convert rate to mins: $\frac{1}{6}$ texts per min

or → convert times to hrs.

30 to 60 mins → $\frac{1}{2}$ to 1 hrs.

$$\int_{1/2}^1 \lambda e^{-\lambda x} dx = \int_{1/2}^1 10 e^{-10x} dx$$

$$= 10 \int_{1/2}^1 e^{-10x} dx = \cancel{10} \frac{e^{-10x}}{\cancel{-10}} \bigg|_{x=1/2}^{x=1}$$

anti deriv.

$$\frac{e^{-10x}}{-10}$$

$$= -1 \left(e^{-10 \cdot 1} - e^{-10 \cdot \frac{1}{2}} \right)$$

$$= e^{-5} - e^{-10}$$