

Things to study:

- Point.
- Distance between points.
- Line.
- Plane.
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## 1 Linear algebra

**Definition 1.1.** *(Dot). is an abstract idea to represent a place on a  $n$ th dimension.*

On one dimension we can say that a dot is an  $x \in S$  on which  $S$  is a set. Similarly on the two and three dimension we have:

$$(x, y) \in S^2,$$
$$(x, y, z) \in S^3,$$

In general we will be working from now on with the real numbers:  $\mathbb{R}^n$ , where  $n$  is the dimension.

### 1.1 Operations

**Definition 1.2.** *Addition (+) Given two points  $P_1$  and  $P_2$ , we say that the addition of these two points will be equal to some other point. And it is represented as:*

$$P_1 + P_2 = P_3,$$

*also a more general on  $n$ th dimension sum will be:*

$$(x_1, y_1, z_1, \dots, m_1) + (x_2, y_2, z_2, \dots, m_2) = (x_1 + x_2, y_1 + y_2, z_1 + z_2, \dots, m_1 + m_2)$$

**Definition 1.3.** *Dot Product ( $\cdot$ ) Given two points  $P_1$  and  $P_2$ , we say that the addition of these two points will be equal to some scalar  $k$ . Then*

$$P_1 = (x_1, y_1, z_1, \dots, m_1), P_2 = (x_2, y_2, z_2, \dots, m_2)$$

$$P_1 \cdot P_2 = P_3$$

$$(x_1, y_1, z_1, \dots, m_1) \cdot (x_2, y_2, z_2, \dots, m_2) = x_1x_2 + y_1y_2 + z_1z_2 + \dots + m_1m_2$$

**Definition 1.4.** *Scalar product The scalar product is...*