

Programming Languages
CSCI-GA.2110.001 Fall 2021

Scheme Assignment
Due Tuesday, March 26 at 11:55pm

Your assignment is to write a number of small Scheme functions. All code must be purely functional (no use of `set!`, `set-car!`, or `set-cdr!` allowed) and should be concise and elegant.

Scheme programming will be on the mid-term exam on October 27, so it is essential that you finish this assignment on time. Do not work on the code with anyone else. Put all your code into single file (with a “.scm” extension) and upload it to Brightspace.

Additionally, unless otherwise noted, each recursive function that you write must be preceded by a comment that shows your reasoning about the recursion. For example, the comment before the solution to problem 1 below might be:

```
;; (byTwos n m) returns the list of every other integer starting with n up to m.
;; Base Case:  if n > m, the result is the empty list.
;; Hypothesis: Assume (byTwos (+ n 2) m) returns the list of every other integer
;;               from n+2 up to m.
;; Recursive step: (byTwos n m) returns (cons n (byTwos (+ n 2) m))
```

1. Define the function (`byTwos n m`) that returns the list of integers starting with `n` such that each successive element is two greater than the previous element and no element is greater than `m`. For example,

```
> (byTwos 1 20)
(1 3 5 7 9 11 13 15 17 19)
```

This function should be around 3 or 4 lines of code. If you are writing more than that, you are probably thinking about it incorrectly.

2. Write the function (`compress L`) that returns a list of all the atoms (non-list values) contained in `L` or in any nested list within `L`. For example,

```
> (compress '(1 (2 3 (4 5) (6 7 (8))) 9) 10))
(1 2 3 4 5 6 7 8 9 10)
```

This function should be around 6 lines of code. Note: (`list? x`) returns true if `x` is a list (including the empty list), false otherwise.

3. Write a linear-time reverse function, (`rev-all L`) which reverses the elements of a list `L` and, if the `L` contains nested lists, reverses those nested lists as well. For example,

```
> (rev-all '(1 2 (3 4) (5 6 (7 8) 9) 10))
(10 (9 (8 7) 6 5) (4 3) 2 1)
```

To make sure it is linear time (in the total number of atoms in the list at any level of nesting), you should not call `append`. Hint: You should use a helper function, analogous to the (`rev L result`) function that I wrote in class. Feel free to adapt my `rev` code.

This code should be around 9 lines.

4. In Scheme, to compare two numbers, you can use the `=` function, as in:

```
> (= 10 3)
#f
```

To compare two atoms, you can use the `eq?` function, as in:

```
> (eq? 'hello 'goodbye)
#f
> (eq? 'hello 'hello)
#t
> (eq? 3 3)
#t
```

However, `eq?` does not perform an element-by-element comparison on lists. For example,

```
> (eq? '(1 2 3) '(1 2 3))
#f
```

Instead, Scheme provides the function `equal?` that does work on lists (and atoms, too):

```
> (equal? '(1 2 3) '(1 2 3))
#t
> (equal? 3 4)
#f
```

Write your own equality function, (`equalTo? x y`), which works the same as (`equal? x y`). You can call `eq?`, but you cannot use `equal?`.

This function should be around 5 lines of code.

5. Write a function (`equalFns? fn1 fn2 domain`), where the parameters `fn1` and `fn2` are functions and `domain` is a list of values, that returns true iff `fn1` and `fn2` always returns the same value when applied to the same element of `domain`. Don't assume that `fn1` and `fn2` always return atomic values. For example,

```
> (equalFns? (lambda (x) (* x 2)) (lambda (y) (+ y y))
          '(1 2 3 4 5 6 7 8 9 10 11 12))
#t
> (equalFns? (lambda (x) (* x 2)) (lambda (y) (+ y 2)) '(2))
#t
> (equalFns? (lambda (x) (* x 2)) (lambda (y) (+ y 2)) '(2 3 4 5))
#f
> (equalFns? (lambda (L) (car L)) (lambda (L) (cadr L))
          '(((2 3) (2 3)) ((4 5) (4 5))))
#t
```

This function should be around 5 lines of code.

6. Write a function, `(same-vals fn1 fn2 domain)`, that returns the list of all elements x of `domain` such that `(fn1 x)` and `(fn2 x)` return the same value. For example,

```
> (same-vals (lambda (x) x)
              (lambda (y) (abs y)) ;; abs give the absolute value
              '(-3 -2 -1 0 1 2 3))
(0 1 2 3)
```

This function should be around 6 lines of code.

7. Write a function `(split x L)`, where x is a number and L is a list of numbers, that returns a list containing two lists: The first list contains the numbers in L less than or equal to x and the second list contains the numbers in L greater than x . For example,

```
> (split 6 '(1 9 2 8 3 10 4 6 5))
((1 2 3 4 6 5) (9 8 10))
> (split 7 '(1 9 2 8 3 10 4 6 5))
((1 2 3 4 6 5) (9 8 10))
```

Hint: The base case is, when L is an empty list, return `'(()())`. This function should be around 8 lines of code.

8. Write a function `(psort L)` that implements a partition sort (similar to Quicksort). It should use your `split` function, above. Given a list L , if L is non-empty, then `split` should be called using the first element of L to partition the rest of L . Then, `psort` should be called recursively to sort each of the two lists returned by `split`. Finally, the sorted result is constructed from the elements of the two sorted lists, as well as the first element of L . For example,

```
> (psort '(5 3 8 6 1 0 2))
(0 1 2 3 5 6 8)
```

This function should be around 6 lines of code. Be sure to only call `split` once at each level of the recursion.

9. Write a single function `(applyToList f)`, where f is a parameter that is a function, that returns a function that takes a list L as a parameter and applies f to every element of L , returning the resulting list as the result. For example,

```
> ;; define g to be the function resulting from calling applyToList
    (define g (applyToList (lambda (x) (* x 2))))

> ;; call g
    (g '(1 2 3 4 5))
(2 4 6 8 10)

> ;; call the function resulting from calling applyToList
    ((applyToList (lambda (y) (car y))) '((1 2 3) (4 5 6) (7 8 9)))
(1 4 7)
```

You must use the built-in `map` function in your definition of `applyToList`. Thus, you do not need to define a recursive function and therefore no comment showing recursive reasoning is required. This function should be around 2 lines of code.

10. Write a function (`newApplyToList f`) which behaves exactly like `applyToList` above, except that you **cannot** use the built-in `map` or any other built-in function except `cons`, `car`, and `cdr`. Also, you cannot define any helper function outside of `newApplyToList`, but you can define functions within it (Note: do not use (`define ...`) inside a procedure). You do not need to provide a comment showing your recursive reasoning.

This function should be around 6 lines of code.