

# Computational Methods in Physics (PHY 365)

FA23

Dr. Muhammad Kamran

Department of Physics

COMSATS University Islamabad

# Lab 1

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ **Root finding.**



# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ **Root finding.**
  - ◇ **Integration.**

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ **Root finding.**
  - ◇ **Integration.**
  - ◇ **Ordinary differential equations.**

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ Root finding.
  - ◇ Integration.
  - ◇ Ordinary differential equations.
  - ◇ System of linear equations.

# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ **Root finding.**
  - ◇ **Integration.**
  - ◇ **Ordinary differential equations.**
  - ◇ **System of linear equations.**
  - ◇ **Partial differential equations.**

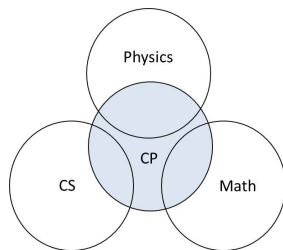
# Introduction to Computational Physics

- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ Root finding.
  - ◇ Integration.
  - ◇ Ordinary differential equations.
  - ◇ System of linear equations.
  - ◇ Partial differential equations.
  - ◇ Matrix eigenvalue problem.

# Introduction to Computational Physics

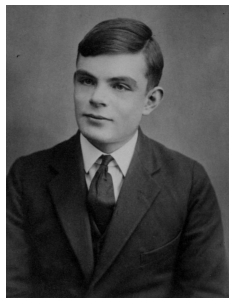
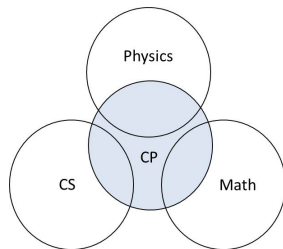
- The field of Computational Physics combines **physics**, **computer science** and **mathematics** to provide scientific solutions to realistic and often complex problems.
- A computational physicist understands
  - the workings of computers and the relevant science and mathematics, and
  - how computer algorithms and simulations connect the two.
- Applications
  - ◇ Root finding.
  - ◇ Integration.
  - ◇ Ordinary differential equations.
  - ◇ System of linear equations.
  - ◇ Partial differential equations.
  - ◇ Matrix eigenvalue problem.
  - ◇ Other applications.

# Introduction to Computational Physics



**Figure:** A representation of the multidisciplinary nature of Computational Physics

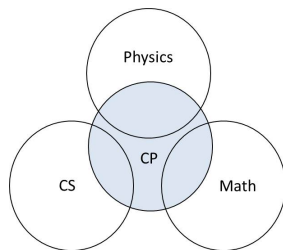
# Introduction to Computational Physics



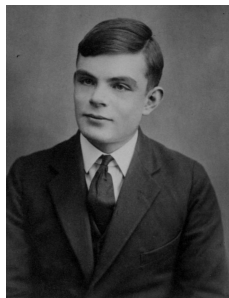
**Figure:** A representation of the multidisciplinary nature of Computational Physics



# Introduction to Computational Physics



**Figure:** A representation of the multidisciplinary nature of Computational Physics



**Figure:** Alan Turing

# Introduction to Computational Physics

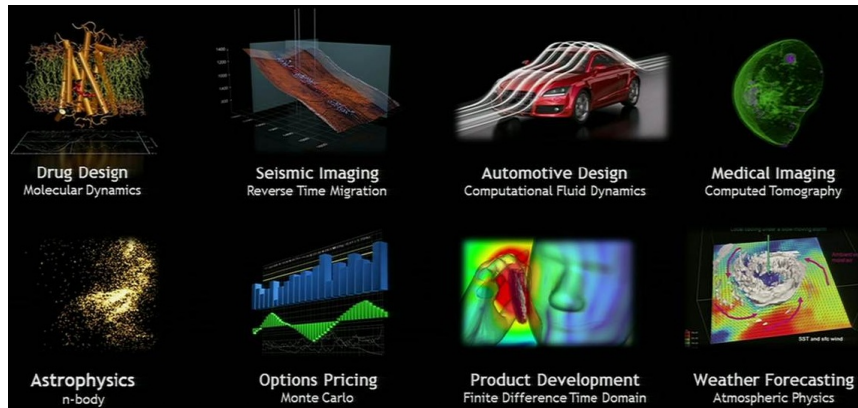


Figure: Some applications of CP

# Introduction to MATLAB

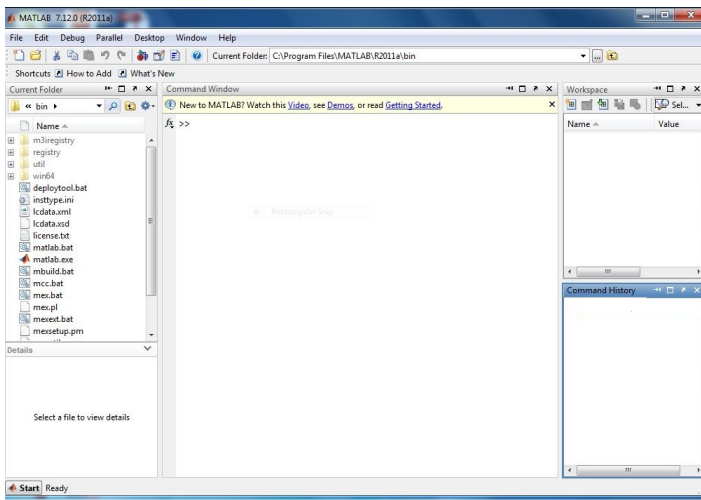


Figure: MATLAB

## Key features

- High-level language for scientific and engineering computing.

## Key features

- High-level language for scientific and engineering computing.
- **Graphics** for visualizing data and tools for creating **custom** plots.

## Key features

- High-level language for scientific and engineering computing.
- **Graphics** for visualizing data and tools for creating **custom** plots.
- Apps for **curve fitting**, **data classification**, **signal analysis**, and many other domain-specific tasks.

## Key features

- High-level language for scientific and engineering computing.
- **Graphics** for visualizing data and tools for creating **custom** plots.
- Apps for **curve fitting**, **data classification**, **signal analysis**, and many other domain-specific tasks.
- Add-on toolboxes for a wide range of engineering and scientific applications.

## Key features

- High-level language for scientific and engineering computing.
- **Graphics** for visualizing data and tools for creating **custom** plots.
- Apps for **curve fitting**, **data classification**, **signal analysis**, and many other domain-specific tasks.
- Add-on toolboxes for a wide range of engineering and scientific applications.
- Tools for building applications with custom user interfaces.



## Some built-in functions

- `zeros(r, c)`.
- `ones(r, c)`.
- `eye(r, c)`.
- `magic(m)`.
- `rand(r, c)`.
- `diag(x)`.
- `linspace(xi, xf, p)`.

## Matrix operations






exponentiation.





## Matrix operations

-  exponentiation.
-  addition.







## Matrix operations

-  exponentiation.
-  addition.
-  subtraction.







## Matrix operations

-  exponentiation.
-  addition.
-  subtraction.
-  (matrix) multiplication.








## Matrix operations

-  exponentiation.
-  addition.
-  subtraction.
-  (matrix) multiplication.
-   (element-wise) multiplication.

## Matrix operations








-  exponentiation.
-  addition.
-  subtraction.
-  (matrix) multiplication.
-  (element-wise) multiplication.
-  (element-wise) division.

## Matrix operations

-  exponentiation.
-  addition.
-  subtraction.
-  (matrix) multiplication.
-  (element-wise) multiplication.
-  (element-wise) division.
-  left division.



## Matrix operations


-  exponentiation.
-  addition.
-  subtraction.
-  (matrix) multiplication.
-  (element-wise) multiplication.
-  (element-wise) division.
-  left division.

→  $A \setminus B = \text{inv}(A) * B$ .




## Relational Operators

-  less than.





## Relational Operators

-  less than.
-  greater than.

## Relational Operators

-  less than.
-  greater than.
-  less than or equal to.

## Relational Operators

-  less than.
-  greater than.
-  less than or equal to.
-  greater than or equal to.

## Relational Operators

- $<$  less than.
- $>$  greater than.
- $<=$  less than or equal to.
- $>=$  greater than or equal to.
- $=$  equal to.

## Relational Operators

- $<$  less than.
- $>$  greater than.
- $<=$  less than or equal to.
- $>=$  greater than or equal to.
- $=$  equal to.
- $\sim$  not equal to.

## Logical Operators

- `&` and.






## Logical Operators

- `&` and.
- `~` not.

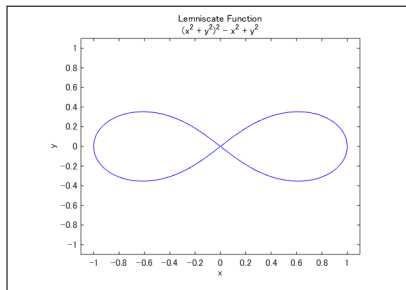
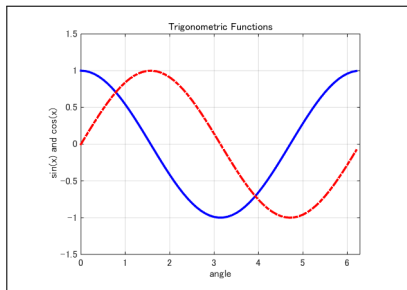
## Logical Operators

-  and.
-  not.
-  or.

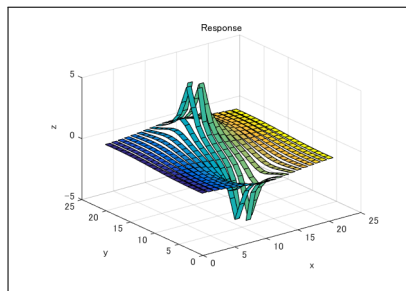
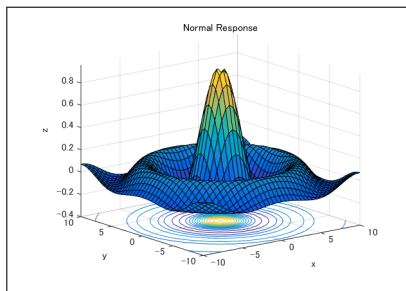
## Logical Operators

-  and.
-  not.
-  or.
- xor exclusive-OR.

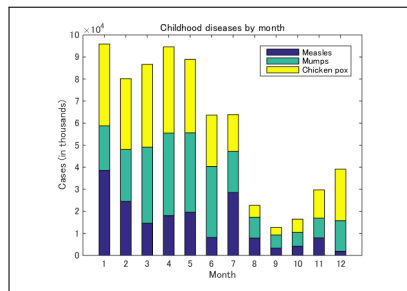
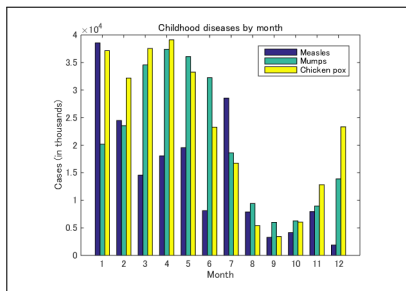
# Plots



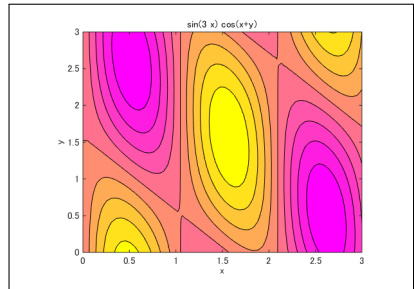
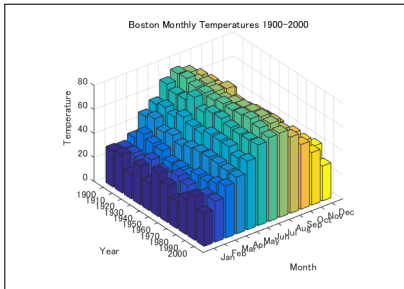
# Plots



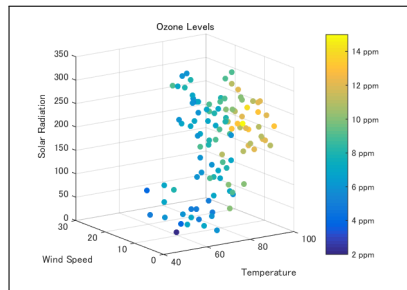
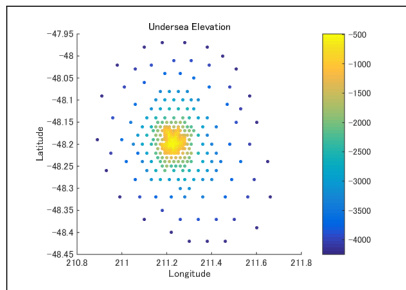
## Plots



# Plots

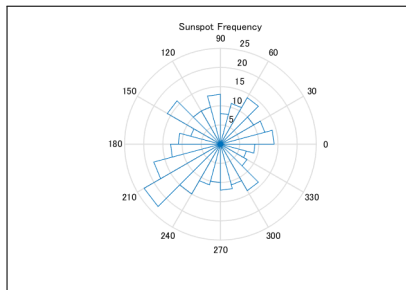
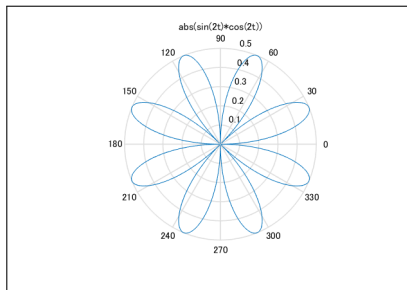


## Plots

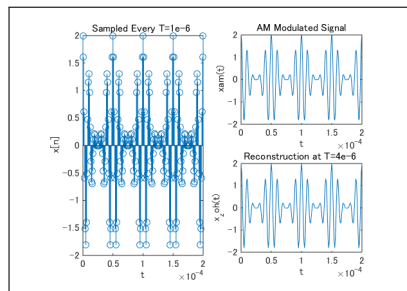
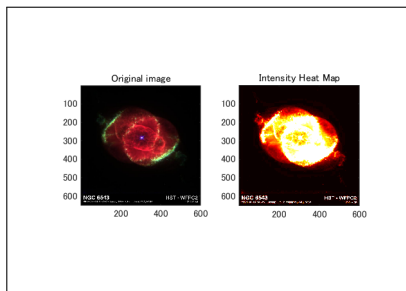




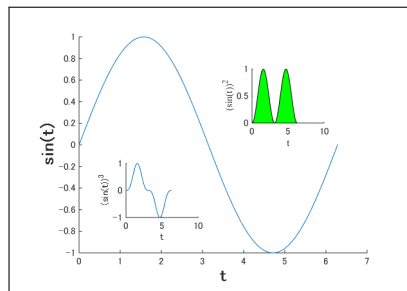
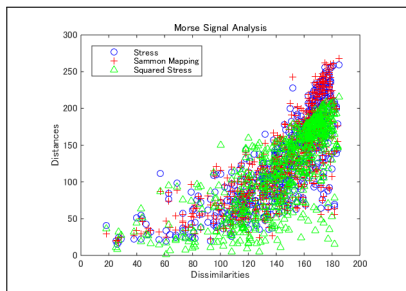
# Plots



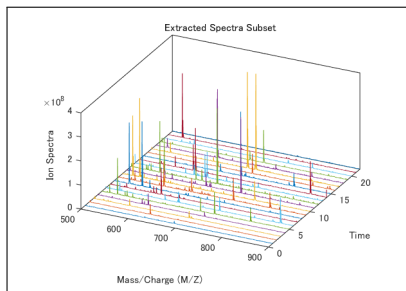
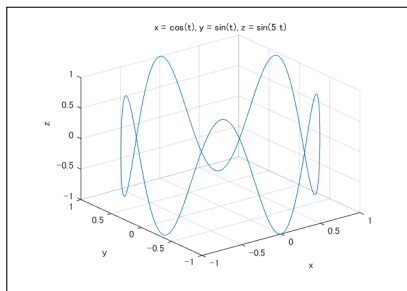
## Plots



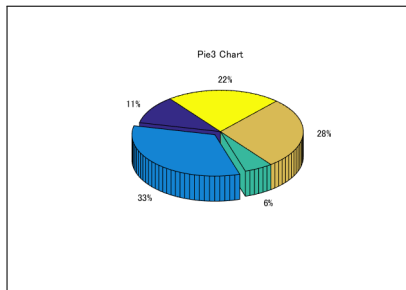
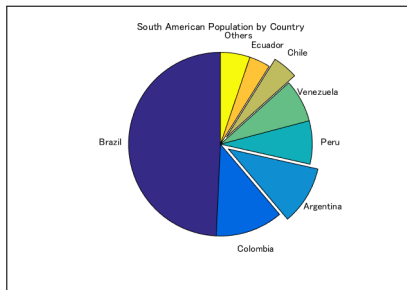
## Plots



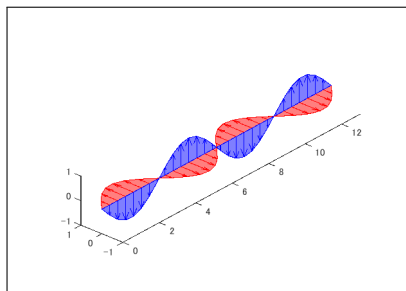
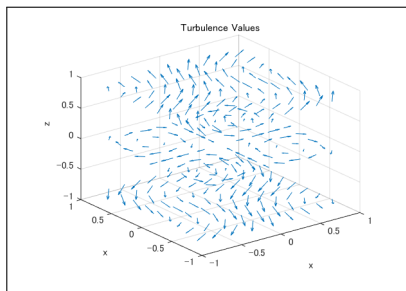
# Plots



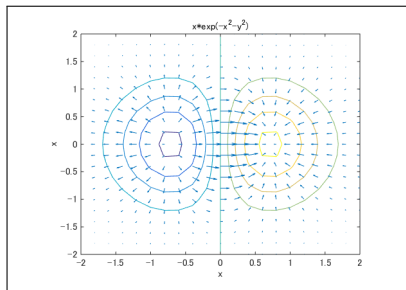
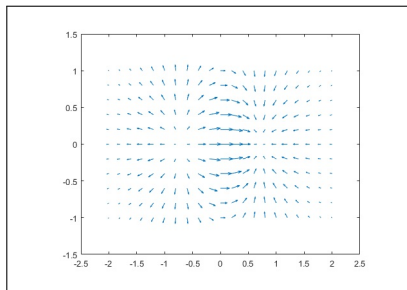
# Plots



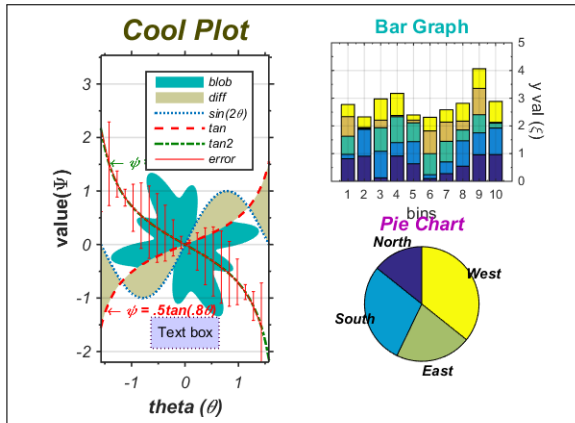
# Plots



## Plots

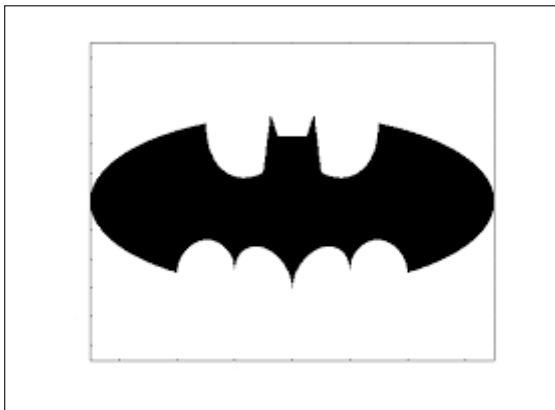


## Plots





# Plots



## Help

- Type “`help` topic” in the command prompt.

## Help

- Type “`help topic`” in the command prompt.
  - ◇ `help sin`

# Help

- Type “[help](#) topic” in the command prompt.
  - ◇ `help sin`

```
>> help sin
SIN      Sine of argument in radians.
        SIN(X) is the sine of the elements of X.

See also asin, sind.

Overloaded methods:
        codistributed/sin

Reference page in Help browser
        doc sin
```

## Help

- Type “[help](#) topic” in the command prompt.
  - ◇ `help sin`

```
>> help sin
SIN      Sine of argument in radians.
        SIN(X) is the sine of the elements of X.

See also asin, sind.

Overloaded methods:
codistributed/sin

Reference page in Help browser
doc sin
```

- Type “[doc](#) topic” in the command prompt.

## M-files

- These are text files containing MATLAB programs.
  - ◇ Have a “.m” extension.

## M-files

- These are text files containing MATLAB programs.
  - ◇ Have a “.m” extension.
- M-files can be called from the **command line** or from **other** M-files.

## M-files

- These are text files containing MATLAB programs.
  - ◇ Have a “.m” extension.
- M-files can be called from the **command line** or from **other** M-files.
- Two kinds
  - ◇ Script file.
  - ◇ Function file.



## M-files

- These are text files containing MATLAB programs.
  - ◇ Have a “.m” extension.
- M-files can be called from the **command line** or from **other** M-files.
- Two kinds
  - ◇ Script file.
  - ◇ Function file.
- A script file contains a sequence of MATLAB statements.
  - ◇ All variables are added to the workspace.

## M-files

- A function file is a program (or routine) that accepts **input** arguments and returns **output** arguments.
  - ◇ Same name as the defined function.
  - ◇ Has its own workspace, which is also called the **local** workspace.
  - ◇ Can accept more than one input arguments and may return more than one output arguments.
  - ◇ The first line starts with the keyword **function**.

## M-files

- A function file is a program (or routine) that accepts **input** arguments and returns **output** arguments.
  - ◇ Same name as the defined function.
  - ◇ Has its own workspace, which is also called the **local** workspace.
  - ◇ Can accept more than one input arguments and may return more than one output arguments.
  - ◇ The first line starts with the keyword **function**.
- Syntax.
  - ◇ `function [y1,...,yN] = myfun (x1,...,xM).`

## Anonymous Functions

- A function that is not stored in a program file, but is associated with a variable whose data type is `function_handle`.

## Anonymous Functions

- A function that is not stored in a program file, but is associated with a variable whose data type is `function_handle`.
- Anonymous functions can accept inputs and return outputs, just as standard functions do.
  - ◇ They can contain only a single executable statement.

## Anonymous Functions

- A function that is not stored in a program file, but is associated with a variable whose data type is `function_handle`.
- Anonymous functions can accept inputs and return outputs, just as standard functions do.
  - ◇ They can contain only a single executable statement.
- Many MATLAB functions accept function handles as inputs.
- Anonymous functions are created by `@` operator.

## Symbolic/Algebraic computation

- Symbolic Math Toolbox provides functions for solving, plotting, and manipulating **symbolic** math equations.

## Symbolic/Algebraic computation

- Symbolic Math Toolbox provides functions for solving, plotting, and manipulating **symbolic** math equations.
- The toolbox provides functions in common mathematical areas such as
  - ◇ Calculus
  - ◇ Linear Algebra
  - ◇ Algebraic and ordinary differential equations
  - ◇ Plotting of analytical functions in 2D and 3D



## Parallel computing

- Parallel Computing Toolbox lets you solve computationally and data-intensive problems using multicore processors, GPUs, and computer clusters.

## Parallel computing

- Parallel Computing Toolbox lets you solve computationally and data-intensive problems using multicore processors, GPUs, and computer clusters.
- The toolbox lets you use the full processing power of multicore machines by executing applications on MATLAB computational engines that run locally.

## Parallel computing

- Parallel Computing Toolbox lets you solve computationally and data-intensive problems using multicore processors, GPUs, and computer clusters.
- The toolbox lets you use the full processing power of multicore machines by executing applications on MATLAB computational engines that run locally.
- Applications can be parallelized without Compute Unified Device Architecture (**CUDA**) or Message Passing Interface (**MPI**) programming.

## Data import/export

- Data import and export functions provide access to data from files, other applications, web services, and external devices.

## Data import/export

- Data import and export functions provide access to data from files, other applications, web services, and external devices.
- You can read popular file formats
  - ◇ Excel spreadsheets
  - ◇ Text
  - ◇ Images
  - ◇ Audio and video
  - ◇ Scientific data formats

## Exercise: Some useful built-in functions and commands

- `A = magic (4)`

## Exercise: Some useful built-in functions and commands

- `A = magic (4)`
- `B = ones (4)`

## Exercise: Some useful built-in functions and commands

- `A = magic (4)`
- `B = ones (4)`
- `C = eye (4)`



## Exercise: Some useful built-in functions and commands

- `A = magic (4)`
- `B = ones (4)`
- `C = eye (4)`
- `D = rand (4)`

## Exercise: Some useful built-in functions and commands

- `A = magic (4)`
- `B = ones (4)`
- `C = eye (4)`
- `D = rand (4)`
- `E = linspace (0, 1, 100)`

## Exercise: Some useful built-in functions and commands

- `A = magic (4)`
- `B = ones (4)`
- `C = eye (4)`
- `D = rand (4)`
- `E = linspace (0, 1, 100)`
- `F = find (D < 0.5)`

## Exercise: Some useful built-in functions and commands

- who

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`
- `clear variables`

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`
- `clear variables`
- `close all`



## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`
- `clear variables`
- `close all`
- `clc`

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`
- `clear variables`
- `close all`
- `clc`
- `A = magic (4)`

## Exercise: Some useful built-in functions and commands

- `who`
- `whos`
- `figure`
- `clear variables`
- `close all`
- `clc`
- `A = magic (4) ;`

## Exercise: Matrix operations

- $B = A;$

## Exercise: Matrix operations

- $B = A;$

- $A \wedge 2$

## Exercise: Matrix operations

- $B = A;$

- $A \wedge 2$

- $A . \wedge 2$

## Exercise: Matrix operations

- $B = A;$

- $A \wedge 2$

- $A \cdot \wedge 2$

- $A / B$

## Exercise: Matrix operations

- $B = A;$

- $A \wedge 2$

- $A \wedge 2$

- $A / B$

- $A ./ B$



## Exercise: Matrix operations

- $B = A;$

- $A ^ 2$

- $A .^ 2$

- $A / B$

- $A ./ B$

- $A \setminus B$

## Exercise: Matrix operations

- $B = A;$
- $A ^ 2$
- $A .^ 2$
- $A / B$
- $A ./ B$
- $A \setminus B$
- $\text{inv}(A) * B$

## Exercise: Matrix operations

- `A1 = magic(4);`

## Exercise: Matrix operations

- `A1 = magic(4);`
- `B1 = magic(6);`

## Exercise: Matrix operations

- `A1 = magic(4);`
- `B1 = magic(6);`
- `C1 = rand(4,6);`

## Exercise: Matrix operations

- `A1 = magic(4);`
- `B1 = magic(6);`
- `C1 = rand(4,6);`
- `D1 = [ A1, B1];`

## Exercise: Matrix operations

- `A1 = magic(4);`
- `B1 = magic(6);`
- `C1 = rand(4,6);`
- `D1 = [ A1, B1];`
- `E1 = [ A1; B1];`

## Exercise: Matrix operations

- $F1 = [A1; C1];$



## Exercise: Matrix operations

- $F1 = [A1; C1];$

- $G1 = [A1, C1];$

## Exercise: Matrix operations

- $F1 = [A1; C1];$

- $G1 = [A1, C1];$

- $A1(2) = 0;$

## Exercise: Matrix operations

- $F1 = [A1; C1];$

- $G1 = [A1, C1];$

- $A1(2) = 0;$

- $H1 = B1(:, 3)$

## Exercise: Matrix operations

- $F1 = [A1; C1];$
- $G1 = [A1, C1];$
- $A1(2) = 0;$
- $H1 = B1(:, 3)$
- $I1 = A1(3:6, 3)$

## Exercise: Matrix operations

- $a = [1 : 3]$

$$b = [5 : 7]$$

## Exercise: Matrix operations

- $a = [1 : 3]$

$$b = [5 : 7]$$

- $a1 = \text{dot}(a, b)$

## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$

## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$
- $a3 = \text{cross}(a, b)$



## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$
- $a3 = \text{cross}(a, b)$
- $a4 = \text{kron}(a, b)$

## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$
- $a3 = \text{cross}(a, b)$
- $a4 = \text{kron}(a, b)$
- $a5 = \text{length}(a)$

## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$
- $a3 = \text{cross}(a, b)$
- $a4 = \text{kron}(a, b)$
- $a5 = \text{length}(a)$
- $a6 = \text{max}(a)$

## Exercise: Matrix operations

- $a = [1 : 3]$   
 $b = [5 : 7]$
- $a1 = \text{dot}(a, b)$
- $a2 = \text{dot}(a, b')$
- $a3 = \text{cross}(a, b)$
- $a4 = \text{kron}(a, b)$
- $a5 = \text{length}(a)$
- $a6 = \text{max}(a)$
- $a7 = \text{min}(b)$

## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

- $B = A(0)$

## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

- $B = A(0)$

- $C = A(1)$



## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

- $B = A(0)$

- $C = A(1)$

- $D = A(4)$

## Exercise: Matrix operations

- $A = [1,2,3,4 ; 5,6,7,8 ; 9,10,11,12]$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

- $B = A(0)$

- $C = A(1)$

- $D = A(4)$

- $E = A(\text{end})$

## Exercise: Matrix operations

- `F = size(A)`

## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$

## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$
- $H = A(2, 3)$

## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$
- $H = A(2, 3)$
- $A(2,2) = 20$

## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$
- $H = A(2, 3)$
- $A(2,2) = 20$
- $I = A(:, 2)$

## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$
- $H = A(2, 3)$
- $A(2,2) = 20$
- $I = A(:, 2)$
- $J = \text{sum}(A)$



## Exercise: Matrix operations

- $F = \text{size}(A)$
- $G = \text{length}(A)$
- $H = A(2, 3)$
- $A(2,2) = 20$
- $I = A(:, 2)$
- $J = \text{sum}(A)$
- $K = \text{max}(A)$

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

```
A2 = sum(A,2)
```

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

```
A2 = sum(A,2)
```

```
A3 = trace(A)
```

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

```
A2 = sum(A,2)
```

```
A3 = trace(A)
```

```
A4 = trace(flip(A))
```

## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

```
A2 = sum(A,2)
```

```
A3 = trace(A)
```

```
A4 = trace(flip(A))
```

- Extract the 3rd row of matrix A.



## Exercise: Matrix operations

- Create a  $5 \times 5$  “magic square”. Verify that the sum of the integers in each row, column and diagonal is equal.

```
A = magic(5);
```

```
A1 = sum(A)
```

```
A2 = sum(A,2)
```

```
A3 = trace(A)
```

```
A4 = trace(flip(A))
```

- Extract the 3rd row of matrix A.

```
A5 = A(3 , :)
```

## Exercise: Matrix operations

- Take transpose of the matrix  $A$ .

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

$$C2 = \max(\max(A))$$

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

$$C2 = \max(\max(A))$$

- Sort the matrix A **column-wise**, in **ascending** order.

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

$$C2 = \max(\max(A))$$

- Sort the matrix A **column-wise**, in **ascending** order.

$$C3 = \text{sort}(A)$$

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

$$C2 = \max(\max(A))$$

- Sort the matrix A **column-wise**, in **ascending** order.

$$C3 = \text{sort}(A)$$

- Sort the matrix A **row-wise**, in **descending** order.



## Exercise: Matrix operations

- Take transpose of the matrix A.

`C1 = A'`

- Determine the highest integer in the matrix A.

`C2 = max( max(A))`

- Sort the matrix A **column-wise**, in **ascending** order.

`C3 = sort(A)`

- Sort the matrix A **row-wise**, in **descending** order.

`C4 = sort(A , 2 , 'descend')`

## Exercise: Matrix operations

- Take transpose of the matrix A.

`C1 = A'`

- Determine the highest integer in the matrix A.

`C2 = max( max(A))`

- Sort the matrix A **column-wise**, in **ascending** order.

`C3 = sort(A)`

- Sort the matrix A **row-wise**, in **descending** order.

`C4 = sort(A , 2 , 'descend')`

- Take determinant of the matrix A.

## Exercise: Matrix operations

- Take transpose of the matrix A.

$$C1 = A'$$

- Determine the highest integer in the matrix A.

$$C2 = \max(\max(A))$$

- Sort the matrix A **column-wise**, in **ascending** order.

$$C3 = \text{sort}(A)$$

- Sort the matrix A **row-wise**, in **descending** order.

$$C4 = \text{sort}(A, 2, 'descend')$$

- Take determinant of the matrix A.

$$C5 = \det(A)$$

## References

- <https://www.mathworks.com/help/matlab/ref/function.html>
- <https://www.mathworks.com/help/matlab/data-import-and-export.html>
- [https://www.mathworks.com/help/matlab/matlab\\_prog/anonymous-functions.html](https://www.mathworks.com/help/matlab/matlab_prog/anonymous-functions.html)
- <https://www.mathworks.com/products/symbolic.html>
- <https://www.mathworks.com/products/parallel-computing.html>
- [https://www.mathworks.com/help/matlab/import\\_export/supported-file-formats.html](https://www.mathworks.com/help/matlab/import_export/supported-file-formats.html)
- <https://www.mathworks.com/help/matlab/math/basic-matrix-operations.html>
- <https://www.mathworks.com/help/matlab/ref/find.html>
- <https://www.mathworks.com/matlabcentral/fileexchange/33124-batman-equation-the-legend>

## References

- [https://www.mathworks.com/help/matlab/matlab\\_prog/loop-control-statements.html](https://www.mathworks.com/help/matlab/matlab_prog/loop-control-statements.html)
- <https://www.mathworks.com/help/matlab/ref/plot.html>
- <https://www.mathworks.com/help/matlab/ref/plot3.html>
- <https://www.mathworks.com/help/matlab/ref/surf.html>
- <https://www.mathworks.com/help/matlab/ref/contour.html>
- [https://www.mathworks.com/help/matlab/creating\\_plots/types-of-matlab-plots.html](https://www.mathworks.com/help/matlab/creating_plots/types-of-matlab-plots.html)