Introduction to TensorFlow

Welcome to this week's programming assignment! Up until now, you've always used Numpy to build neural networks, but this week you'll explore a deep learning framework that allows you to build neural networks more easily. Machine learning frameworks like TensorFlow, PaddlePaddle, Torch, Caffe, Keras, and many others can speed up your machine learning development significantly. TensorFlow 2.3 has made significant improvements over its predecessor, some of which you'll encounter and implement here!

By the end of this assignment, you'll be able to do the following in TensorFlow 2.3:

- Use tf.Variable to modify the state of a variable
- Explain the difference between a variable and a constant
- Apply TensorFlow decorators to speed up code
- Train a Neural Network on a TensorFlow dataset

Programming frameworks like TensorFlow not only cut down on time spent coding, but can also perform optimizations that speed up the code itself.

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1 - Packages

```
In [1]: import h5py
           import numpy as np
import tensorflow as tf
           import tensorflow as or
import matplotlib.pyplot as plt
from tensorflow.python.framework.ops import EagerTensor
            from tensorflow.python.ops.resource_variable_ops import ResourceVariable
```

1.1 - Checking TensorFlow Version

You will be using v2.3 for this assignment, for maximum speed and efficiency.

```
In [2]: tf.__version__
Out[2]: '2.3.0'
```

2 - Basic Optimization with GradientTape

The beauty of TensorFlow 2 is in its simplicity. Basically, all you need to do is implement forward propagation through a computational graph. TensorFlow will compute the derivatives for you, by moving backwards through the graph recorded with GradientTape . All that's left for you to do then is specify the cost function and optimizer you want to use!

When writing a TensorFlow program, the main object to get used and transformed is the tf.Tensor. These tensors are the TensorFlow equivalent of Numpy arrays, i.e. multidimensional arrays of a given data type that also contain information about the computational graph.

Below, you'll use tf. Variable to store the state of your variables. Variables can only be created once as its initial value defines the variable shape and type. Additionally, the dtype arg in tf. Variable can be set to allow data to be converted to that type. But if none is specified, either the datatype will be kept if the initial value is a Tensor, or convert_to_tensor will decide. It's generally best for you to specify directly, so nothing breaks!

Here you'll call the TensorFlow dataset created on a HDF5 file, which you can use in place of a Numpy array to store your datasets. You can think of this as a TensorFlow data generator!

You will use the Hand sign data set, that is composed of images with shape 64x64x3.

```
In [3]: train_dataset = h5py.File('datasets/train_signs.h5', "r")
test_dataset = h5py.File('datasets/test_signs.h5', "r")
In [4]: x train = tf.data.Dataset.from tensor slices(train dataset['train set x'])
           y_train = tf.data.Dataset.from_tensor_slices(train_dataset['train_set_y'])
           x_test = tf.data.Dataset.from_tensor_slices(test_dataset['test_set_x'])
y_test = tf.data.Dataset.from_tensor_slices(test_dataset['test_set_y'])
In [5]: type(x_train)
Out[5]: tensorflow.python.data.ops.dataset_ops.TensorSliceDataset
```

Since TensorFlow Datasets are generators, you can't access directly the contents unless you iterate over them in a for loop, or by explicitly creating a Python iterator using iter and consuming its elements using next . Also, you can inspect the shape and dtype of each element using the element_spec attribute.

```
In [6]: print(y_train.element_spec)
        TensorSpec(shape=(), dtype=tf.int64, name=None)
```

```
In [7]: print(next(iter(x_train)))
                   tf.Tensor(
[[[227 220 214]
[227 221 215]
[227 222 215]
                       [232 230 224]
[231 229 222]
[230 229 221]]
                     [[227 221 214]
[227 221 215]
[228 221 215]
                      [232 230 224]
[231 229 222]
[231 229 221]]
                     [[227 221 214]
[227 221 214]
[227 221 215]
                      [232 230 224]
[231 229 223]
[230 229 221]]
                     [[119 81 51]
[124 85 55]
[127 87 58]
                       ...
[210 211 211]
                       [211 212 210]
[210 211 210]]
                     [[119 79 51]
[124 84 55]
[126 85 56]
                      [210 211 210]
[210 211 210]
[209 210 209]]
                     [[119 81 51]
[123 83 55]
[122 82 54]
                       ...
[209 210 210]
[209 210 209]
[208 209 209]]], shape=(64, 64, 3), dtype=uint8)
In [8]: for element in x_train:
    print(element)
    break
                   tf.Tensor(
[[[227 220 214]
[227 221 215]
[227 222 215]
                      [232 230 224]
[231 229 222]
[230 229 221]]
                     [[227 221 214]
[227 221 215]
[228 221 215]
                      [232 230 224]
[231 229 222]
[231 229 221]]
                     [[227 221 214]
[227 221 214]
[227 221 215]
                       [232 230 224]
[231 229 223]
[230 229 221]]
                     [[119 81 51]
[124 85 55]
[127 87 58]
                      [210 211 211]
[211 212 210]
[210 211 210]]
                     [[119 79 51]
[124 84 55]
[126 85 56]
                       [210 211 210]
[210 211 210]
[209 210 209]]
                     [[119 81 51]
[123 83 55]
[122 82 54]
                       ...
[209 210 210]
                       [209 210 209]
[208 209 209]]], shape=(64, 64, 3), dtype=uint8)
```

There's one more additional difference between TensorFlow datasets and Numpy arrays: If you need to transform one, you would invoke the map method to apply the function passed as an argument to each of the elements.

```
In [9]: def normalize(image):
                 Transform an image into a tensor of shape (64 * 64 * 3, 1) and normalize its components.
                 Arguments
                 image - Tensor.
                 Returns:
                 result -- Transformed tensor
                image = tf.cast(image, tf.float32) / 256.0
image = tf.reshape(image, [-1,1])
return image
In [10]: new_train = x_train.map(normalize)
new_test = x_test.map(normalize)
In [11]: new train.element spec
Out[11]: TensorSpec(shape=(12288, 1), dtype=tf.float32, name=None)
In [12]: print(next(iter(new_train)))
            tf.Tensor(
[[0.88671875]
             [0.859375 ]
[0.8359375 ]
             r0.8125
              10.816406251
              [0.81640625]], shape=(12288, 1), dtype=float32)
```

2.1 - Linear Function

Let's begin this programming exercise by computing the following equation: Y = WX + b, where W and X are random matrices and b is a random vector.

Exercise 1 - linear function

Compute WX + b where W, X, and b are drawn from a random normal distribution. W is of shape (4, 3), X is (3,1) and b is (4,1). As an example, this is how to define a constant X with the shape (3,1):

```
X = tf.constant(np.random.randn(3,1), name = "X")
```

Note that the difference between tf.constant and tf.Variable is that you can modify the state of a tf.Variable but cannot change the state of a tf.constant.

You might find the following functions helpful:

- tf.matmul(..., ...) to do a matrix multiplication
- tf.add(..., ...) to do an addition
- np.random.randn(...) to initialize randomly

```
In [14]: result = linear_function()
print(result)

assert type(result) == EagerTensor, "Use the TensorFlow API"
assert np.allclose(result, [[-2.15657382], [ 2.95891446], [-1.08926781], [-0.84538042]]), "Error"
print("\033[92mAll test passed")

tf.Tensor(
[[-2.15657382]
```

All test passed Expected Output:

[2.95891446] [-1.08926781]

```
result =
[[-2.15657382]
[ 2.95891446]
[-1.08926781]
[-0.84538042]]
```

2.2 - Computing the Sigmoid

Amazing! You just implemented a linear function. TensorFlow offers a variety of commonly used neural network functions like tf.sigmoid and tf.softmax.

For this exercise, compute the sigmoid of \boldsymbol{z} .

[-0.84538042]], shape=(4, 1), dtype=float64)

In this exercise, you will: Cast your tensor to type float 32 using tf.cast , then compute the sigmoid using tf.keras.activations.sigmoid .

Exercise 2 - sigmoid

Implement the sigmoid function below. You should use the following:

- tf.cast("...", tf.float32)tf.keras.activations.sigmoid("...")

```
In [16]: result = sigmoid(-1)
print ("type: " + str(type(result)))
print ("dtype: " + str(result.dtype))
print ("sigmoid(-1) = " + str(result))
print ("sigmoid(0) = " + str(sigmoid(0.0)))
print ("sigmoid(12) = " + str(sigmoid(12)))

def sigmoid_test(target):
    result = target(0)
    assert(type(result) == EagerTensor)
    assert (result.dtype == tf.float32)
    assert sigmoid(0) == 0.5, "Error"
    assert sigmoid(0) == 0.5, "Error"
    assert sigmoid(1) == 0.26894143, "Error"
    assert sigmoid(12) == 0.9999939, "Error"

print("\033[92mAll test passed")

sigmoid_test(sigmoid)
```

type: <class 'tensorflow.python.framework.ops.EagerTensor'>
dtype: <dtype: 'float32'>
sigmoid(-1) = tf.Tensor(0.26894143, shape=(), dtype=float32)
sigmoid(0) = tf.Tensor(0.5, shape=(), dtype=float32)
sigmoid(12) = tf.Tensor(0.9999939, shape=(), dtype=float32)
All test passed

Expected Output:

 type
 class 'tensorflow.python.framework.ops.EagerTensor'

 dtype
 "dtype: 'float32'

 Sigmoid(-1)
 0.2689414

 Sigmoid(0)
 0.5

 Sigmoid(12)
 0.999944

2.3 - Using One Hot Encodings

Many times in deep learning you will have a Y vector with numbers ranging from 0 to C-1, where C is the number of classes. If C is for example 4, then you might have the following y vector which you will need to convert like this:



This is called "one hot" encoding, because in the converted representation, exactly one element of each column is "hot" (meaning set to 1). To do this conversion in numpy, you might have to write a few lines of code. In TensorFlow, you can use one line of code:

• tf.one hot(labels, depth, axis=0) (https://www.tensorflow.org/api_docs/python/tf/one_hot)

axis=0 indicates the new axis is created at dimension 0

Exercise 3 - one_hot_matrix

Implement the function below to take one label and the total number of classes C, and return the one hot encoding in a column whise matrix. Use $f.one_hot()$ to do this, and f.reshape() to reshape your one hot tensor!

• tf.reshape(tensor, shape)

```
In [17]: # GRADED FUNCTION: one_hot_matrix
def one_hot_matrix(label, depth=6):
                    Computes the one hot encoding for a single label
                    Arguments:
                          label -- (int) Categorical labels
depth -- (int) Number of different classes that label can take
                    one_hot -- tf.Tensor A single-column matrix with the one hot encoding.
                    # (approx. 1 line)
# one_hot = ...
# YOUR CODE STARTS HERE
                    one_hot = tf.reshape(tf.one_hot(label, depth, axis = 0), (depth, 1))
                    # YOUR CODE ENDS HERE
                    return one_hot
In [18]: def one_hot_matrix_test(target):
    label = tf.constant(1)
    depth = 4
    result = target(label, depth)
                    print(result)
                    print(result)
assert result.shape[0] == depth, "Use the parameter depth"
assert result.shape[1] == 1, f"Reshape to have only 1 column"
assert np.allclose(result, [[0.], [1.], [0.], [0.]]), "Wrong output. Use tf.one_hot"
... assert np.allclose(result, [[0.], [1.], [0.], [0.]]), "Wrong output."
                    result = target(3, depth)
assert np.allclose(result, [[0.], [0.], [0.], [1.]]), "Wrong output. Use tf.one_hot"
                    print("\033[92mAll test passed")
              one_hot_matrix_test(one_hot_matrix)
              tf.Tensor(
              [[0.]
[1.]
                .01
              [0.]], shape=(4, 1), dtype=float32)
All test passed
              Expected output
                   tf.Tensor(
                   1.011
                     [1.]
                     [0.]
                    [0.]], shape=(4, 1), dtype=float32)
In [19]: new_y_test = y_test.map(one_hot_matrix)
    new_y_train = y_train.map(one_hot_matrix)
In [20]: print(next(iter(new_y_test)))
              tf.Tensor(
              [[1.]
[0.]
[0.]
[0.]
                [0.]], shape=(6, 1), dtype=float32)
```

2.4 - Initialize the Parameters

Now you'll initialize a vector of numbers between zero and one. The function you'll be calling is tf.keras.initializers.GlorotNormal, which draws samples from a truncated normal distribution centered on 0, with stddev = sqrt(2 / (fan_in + fan_out)), where fan_in is the number of input units and fan_out is the number of output units, both in the weight tensor.

To initialize with zeros or ones you could use tf.zeros() or tf.ones() instead.

Exercise 4 - initialize_parameters

Implement the function below to take in a shape and to return an array of numbers between -1 and 1.

- tf.keras.initializers.GlorotNormal(seed=1)
- tf.Variable(initializer(shape=())

In [23]: # GRADED FUNCTION: initialize_parameters

```
def initialize_parameters():
                         Initializes parameters to build a neural network with TensorFlow. The shapes are:
                                                              W1 : [25, 12288]
b1 : [25, 1]
W2 : [12, 25]
b2 : [12, 1]
W3 : [6, 12]
                                                               b3 : [6, 1]
                         parameters -- a dictionary of tensors containing W1, b1, W2, b2, W3, b3
                         initializer = tf.keras.initializers.GlorotNormal(seed=1)
                        initializer = tf.keras.ini:
#/approx. 6 lines of code)
# W1 = ...
# b1 = ...
# b2 = ...
# b3 = ...
# y0ur CODE STARTS HERE
                         W1 = tf.Variable(initializer(shape=(25, 12288)))
                        t1.Variable(initializer(shape=(25, 120))
b1 = tf.Variable(initializer(shape=(12, 25)))
w2 = tf.Variable(initializer(shape=(12, 25)))
b2 = tf.Variable(initializer(shape=(12, 1)))
w3 = tf.Variable(initializer(shape=(6, 12)))
b3 = tf.Variable(initializer(shape=(6, 1)))
                         # YOUR CODE ENDS HERE
                         parameters = {"W1": W1,
                                                    "b1": b1,
"W2": W2,
"b2": b2,
                                                     "W3": W3.
                                                    "b3": b3}
                         return parameters
In [24]: def initialize_parameters_test(target):
    parameters = target()
                         values = {"W1": (25, 12288),
                                            "b1": (25, 1),
"W2": (12, 25),
"b2": (12, 1),
"W3": (6, 12),
                                             "b3": (6, 1)}
                         for key in parameters:
                                 key in parameters:

print(f"(key) shape: {tuple(parameters[key].shape)}")

assert type(parameters[key]) == ResourceVariable, "All parameter must be created using tf.Variable"

assert tuple(parameters[key].shape) == values[key], f"(key): wrong shape"

assert np.abs(np.mean(parameters[key].numpy())) < 0.5, f"(key): Use the GlorotNormal initializer"

assert np.std(parameters[key].numpy()) > 0 and np.std(parameters[key].numpy()) < 1, f"(key): Use the GlorotNormal initializer"
                         print("\033[92mAll test passed")
                  initialize_parameters_test(initialize_parameters)
                  W1 shape: (25, 12288)
b1 shape: (25, 1)
W2 shape: (12, 25)
b2 shape: (12, 1)
                  W3 shape: (6, 12)
b3 shape: (6, 1)
                  All test passed
                  Expected output
                        W1 shape: (25, 12288)
                        b1 shape: (25, 1)
                        W2 shape: (12, 25)
                        b2 shape: (12, 1)
                        W3 shape: (6, 12)
                        b3 shape: (6, 1)
```

3 - Building Your First Neural Network in TensorFlow

In this part of the assignment you will build a neural network using TensorFlow. Remember that there are two parts to implementing a TensorFlow model:

Implement forward propagation

In [25]: parameters = initialize_parameters()

Retrieve the gradients and train the model

Let's get into it!

3.1 - Implement Forward Propagation

One of TensorFlow's great strengths lies in the fact that you only need to implement the forward propagation function.

Here, you'll use a TensorFlow decorator, <code>@tf.function</code>, which builds a computational graph to execute the function. <code>@tf.function</code> is polymorphic, which comes in very handy, as it can support arguments with different data types or shapes, and be used with other languages, such as Python. This means that you can use data dependent control flow statements.

When you use <code>@tf.function</code> to implement forward propagation, the computational graph is activated, which keeps track of the operations. This is so you can calculate your gradients with backpropagation.

Exercise 5 - forward_propagation

 $Implement \ the \ \ forward_propagation \ \ function.$

Note Use only the TF API.

- tf.math.add
- tf.linalg.matmul
- tf.keras.activations.relu

```
In [26]: # GRADED FUNCTION: forward_propagation
              @tf.function
              def forward_propagation(X, parameters):
                   Implements the forward propagation for the model: LINEAR -> RELU -> LINEAR -> RELU -> LINEAR
                   Arguments:

X -- input dataset placeholder, of shape (input size, number of examples)

parameters -- python dictionary containing your parameters "Wl", "b1", "W2", "b2", "W3", "b3"

the shapes are given in initialize_parameters
                   Returns:
                   Z3 -- the output of the last LINEAR unit
                    # Retrieve the parameters from the dictionary "parameters"
                  # Ketrieve the parameters ['M1']
b1 = parameters ['M1']
b2 = parameters ['M2']
b3 = parameters ['M2']
b3 = parameters ['M3']
                   #(approx. 5 lines)
                                                                         # Numpy Equivalents:
                                                                         # Numpy Equivalents:

# Z1 = np.dot(W1, X) + b1

# A1 = relu(Z1)

# Z2 = np.dot(W2, A1) + b2

# A2 = relu(Z2)

# Z3 = np.dot(W3, A2) + b3
                   # Z1 = ...
# A1 = ...
# Z2 = ...
# A2 = ...
# Z3 = ...
                   # Z3 = ... # Z3 = np.c
# YOUR CODE STARTS HERE
Z1 = tf.math.add(tf.linalg.matmul(W1, X) , b1)
                                                                                                              \# Z1 = np.dot(W1, X) + b1
                  # YOUR CODE ENDS HERE
                   return 73
In [27]: def forward propagation test(target, examples):
```

```
tf.Tensor(
[-0.13082162]
  [ 0.21228778]
  [ 0.7050022 ]
  [-1.1224034 ]
  [-0.20386729]
  [ 0.9526217 ]], shape=(6, 1), dtype=float32)
All test passed
```

Expected output

```
tf.Tensor(
[[-0.13082162]
  [ 0.21228778]
  [ 0.7050022 ]
  [-1.1224034 ]
  [-0.20386732]
  [ 0.9526217 ]], shape=(6, 1), dtype=float32)
```

3.2 Compute the Cost

Here again, the delightful @tf.function decorator steps in and saves you time. All you need to do is specify how to compute the cost, and you can do so in one simple step by using:

 $\texttt{tf.reduce_mean(tf.keras.losses.binary_crossentropy(y_true = ..., y_pred = ..., from_logits=True))}$

Exercise 6 - compute_cost

Implement the cost function below.

• It's important to note that the "y_pred" and "y_true" inputs of ff.keras.losses.binary_crossentropy_(https://www.tensorflow.org/api_docs/python/tf/keras/losses/binary_crossentropy) are expected to be of shape (number of examples, num_classes). Since both the transpose and the original tensors have the same values, just in different order, the result of calculating the binary_crossentropy should be the same if you transpose or not the logits and labels. Just for reference here is how the Binary Cross entropy is calculated in TensorFlow:

```
mean_reduce(max(logits, 0) - logits * labels + log(1 + exp(-abs(logits))), axis=-1)
```

• tf.reduce_mean basically does the summation over the examples

```
In [29]:
    def compute_cost_test(target):
        labels = np.array([[0., 1.], [0., 0.], [1., 0.]])
        logits = np.array([[0.6, 0.4], [0.4, 0.6], [0.4, 0.6]])
        result = compute_cost(logits, labels)
        print(result)
        assert(type(result) == EagerTensor), "Use the TensorFlow API"
        assert (np.abs(result - (0.7752516 + 0.9752516 + 0.7752516) / 3.0) < le-7), "Test does not match. Did you get the mean of your cost functions?"
        print("\033[92mAll test passed")
        compute_cost_test(compute_cost)

tf.Tensor(0.8419182681095858, shape=(), dtype=float64)</pre>
```

Expected output

tf.Tensor(0.87525165, shape=(), dtype=float32)

3.3 - Train the Model

Let's talk optimizers. You'll specify the type of optimizer in one line, in this case tf.keras.optimizers.Adam (though you can use others such as SGD), and then call it within the training loop.

Notice the tape.gradient function: this allows you to retrieve the operations recorded for automatic differentiation inside the GradientTape block. Then, calling the optimizer method apply_gradients, will apply the optimizer's update rules to each trainable parameter. At the end of this assignment, you'll find some documentation that explains this more in detail, but for now, a simple explanation will do.;)

Here you should take note of an important extra step that's been added to the batch training process:

• tf.Data.dataset = dataset.prefetch(8)

What this does is prevent a memory bottleneck that can occur when reading from disk. prefetch() sets aside some data and keeps it ready for when it's needed. It does this by creating a source dataset from your input data, applying a transformation to preprocess the data, then iterating over the dataset the specified number of elements at a time. This works because the iteration is streaming, so the data doesn't need to fit into the memory.

```
In [30]: def model(X_train, Y_train, X_test, Y_test, learning_rate = 0.0001,
    num_epochs = 1500, minibatch_size = 32, print_cost = True):
                            Implements a three-layer tensorflow neural network: LINEAR->RELU->LINEAR->RELU->LINEAR->SOFTMAX.
                            Arguments:
                           Arguments:
X_train -- training set, of shape (input size = 12288, number of training examples = 1080)
Y_train -- test set, of shape (output size = 6, number of training examples = 1080)
X_test -- training set, of shape (input size = 12288, number of training examples = 120)
Y_test -- test set, of shape (output size = 6, number of training examples = 120)
learning_rate -- learning rate of the optimization
num_epochs -- number of epochs of the optimization loop
minibatch_size -- size of a minibatch
print_cost -- True to print the cost every 100 epochs
                            parameters -- parameters learnt by the model. They can then be used to predict.
                                                                                                                                      # To keep track of the cost
                            # Initialize your parameters
                            #(1 line)
parameters = initialize_parameters()
                           W1 = parameters['W1']
b1 = parameters['b1']
W2 = parameters['W2']
b2 = parameters['b2']
W3 = parameters['w3']
b3 = parameters['b3']
                            optimizer = tf.keras.optimizers.SGD(learning_rate)
                            X_train = X_train.batch(minibatch_size, drop_remainder=True).prefetch(8)# <<< extra step
Y_train = Y_train.batch(minibatch_size, drop_remainder=True).prefetch(8) # loads memory faster</pre>
                            # Do the training loop
for epoch in range(num epochs):
                                     epoch_cost = 0.
                                    for (minibatch_X, minibatch_Y) in zip(X_train, Y_train):
    # Select a minibatch
                                             with tf.GradientTape() as tape:
                                                     # 1. predict
23 = forward_propagation(minibatch_X, parameters)
                                                      minibatch_cost = compute_cost(Z3, minibatch_Y)
                                             trainable_variables = [W1, b1, W2, b2, W3, b3]
grads = tape.gradient(minibatch_cost, trainable_variables)
optimizer.apply_gradients(zip(grads, trainable_variables))
epoch_cost += minibatch_cost / minibatch_size
                                    # Print the cost every epoch
if print_cost == True and epoch % 10 == 0:
    print ("Cost after epoch %1: %f" % (epoch, epoch_cost))
if print_cost == True and epoch % 5 == 0:
    costs.append(epoch_cost)
                             # Plot the cost
                           # Plot the cost
plt.plot(np.squeeze(costs))
plt.ylabel('cost')
plt.xlabel('iterations (per fives)')
plt.title("Learning rate =" + str(learning_rate))
                            # Save the parameters in a variable
print ("Parameters have been trained!")
                            return parameters
```

```
In [31]: model(new_train, new_y_train, new_test, new_y_test, num_epochs=200)
                     Cost after epoch 0: 0.742591
Cost after epoch 10: 0.614557
                     Cost after epoch 20: 0.598900
Cost after epoch 30: 0.588907
Cost after epoch 40: 0.579898
Cost after epoch 50: 0.570628
                     Cost after epoch 60: 0.560898

Cost after epoch 70: 0.550808

Cost after epoch 80: 0.540497

Cost after epoch 90: 0.488142
                     Cost after epoch 100: 0.478271
Cost after epoch 110: 0.472863
Cost after epoch 120: 0.468990
                     Cost after epoch 130: 0.4666014
Cost after epoch 140: 0.463661
Cost after epoch 150: 0.461677
Cost after epoch 160: 0.459951
                     Cost after epoch 170: 0.458391
Cost after epoch 180: 0.456969
Cost after epoch 190: 0.455648
                                                             Learning rate =0.0001
                           0.75
                           0.65
                       ₩ 0.60
                           0.55
                           0.50
                                                          10
                                                                     15
                                                                               20
                      Parameters have been trained!
Out[31]: {'W1': <tf.Variable 'Variable:0' shape=(25, 12288) dtype=float32, numpy=array([[ 0.00159527, -0.00737913, 0.00893296, ..., -0.01227794, 0.01642206, 0.00506491],
                                       0.02264025, 0.0067227, 0.00795862, ..., 0.00284724, 0.01910819, 0.00122853], [-0.00173585, -0.00872453, -0.01410444, ..., -0.00733837, 0.0205085, -0.02683027],
                                        [-0.00126929, 0.01729332, 0.02082342, ..., 0.01709594,
                                            0.00429358, -0.007332631,
                                                                                                     0.00936713, ..., 0.01222287,
                                        [ 0.00268262, 0.004105
                        [ 0.00268262, 0.004105 , 0.00936713, ..., 0.01222287, -0.02717604, 0.01498359], [-0.00145541, 0.02459595, 0.00339064, ..., -0.02478788, 0.02716016, -0.00306428]], dtype=float32)>, 'b1': <tf.Variable 'Variable:0' shape=(25, 1) dtype=float32, numpy=array([[ 0.03964256], [ -0.15545043], [ 0.19888883].
                                         r 0.198858831
                                          [-0.24874453]
                                        [-0.24674433],
[-0.2867676],
[-0.12604603],
                                         r=0.012130981
                                           0.14784063],
-0.00413172],
                                          -0.4408977 1
                                           0.540541771
                                           -0.4345032 ],
0.11763882],
                                           0.215238871
                                           _0 067725871
                                         [-0.05259617]
                                         [-0.18479495]
                                         [-0.00280256],
[-0.06777475],
                                           0.092268091
                                            0.020676521
                                            -0.05682073],
                                            0.37065902],
                        -0.10598166, -0.01016674, 0.12317107, 0.45312327, -0.36423257, 0.09766971, -0.13796303, -0.04518652, -0.15597364, 0.07734591, 0.01733258, -0.04763132, [0.275006, 0.0652916, 0.19277105, -0.04379591, 0.00529772, 0.14074473, -0.10437229, -0.27877635, -0.22737731, 0.42841426, 0.04013019, 0.14082581, -0.08289494, 0.19833343, -0.18854785, (0.02337856, 0.0233785)
                                                                                                                                  0.18042907, -0.05753209,
-0.00236228, -0.05681378,
0.31054643, 0.18095495]
                                        r 0.275006
                                                                                                                                   0.00808901, -0.35061046,
                                                                                                                                  -0.22700697, -0.08254652,
-0.15467171, -0.30434608,
0.40803406, 0.19127996,
                                                                       0.1983343, -0.18854785,

0.19833434, -0.18854785,

0.12879197, -0.38048682,

0.08047906, -0.1422226,

0.1428981, 0.4108547,

0.2571582, -0.1236593,

-0.11918075, -0.5031594,

0.19529893, -0.13205278,
                                                                                                                                    0.11045384, -0.102935141.
                                        [ 0.07370555,
-0.12560502,
                                                                                                                                  -0.1428371 ,
-0.3291437 ,
                                                                                                                                                                -0.16866712,
0.11487076,
                                            0.21897362,
                                                                                                                                  -0.02966296,
                                                                                                                                                                 -0.11487766,
                                        0.2835236, 0.2571582,
-0.11544652, -0.11918075,
[-0.11886349, 0.19529893,
-0.36992028, -0.06379852,
                                                                                                                                  0.1469501 , -0.39992067,
-0.16647008, -0.0463655 ]
-0.46206364, 0.07806116,
                                                                                                       0.37158278,
                                                                                                                                    0.0755597 ,
0.17954443,
                                                                                                                                                                  0.5198782
                                           -0.01714175, 0.35476214, 0.09361284, 0.04280831, 0.1051797, 0.03766964, -0.07444265, -0.30713868, -0.11694647,
                                          -0.01714175,
0.04280831,
                                                                                                                                                                  0.00514452
                                                                                                                                    -0.23309673,
                                                                                                                                    0.3292588 ,
                                                                                                                                                                 -0.09511968],
                                       -0.07444265, -0.30713868, -0.11694647, [0.1594041, 0.0393942, 0.47869283, -0.51921755, -0.01731534, -0.31578013, 0.04947535, -0.29094276, -0.03152779, 0.0473902, 0.07770423, 0.3139462, -0.05332499, -0.34107792, -0.13928485, [-0.14994699, 0.03965309, -0.47870195, -0.00232862, -0.26367775, -0.23967475, -0.3073658, 0.1017215, 0.03063034
                                                                                                                                   0.2265753 .
                                                                                                                                                                  0.03725046.
                                                                                                                                  -0.21672064,
0.47902155,
                                                                                                                                                                  0.04122872
                                                                                                                                  -0.02500637,
                                                                                                                                                                  0.10048122
                                                                                                                                   0.12402116,
-0.07975383,
0.24946521,
                                                                                                                                                                 -0.413008181
                                                                                                                                                                  0.09755022,
                                        -0.30773658, 0.1017215,
-0.08669744, 0.03128893,
-0.09631125, 0.2553377,
[-0.20329641, -0.2922766,
                                                                                                      0.03053034,
0.28504866,
0.0313108,
-0.03024991,
                                                                                                                                    0.26468748.
                                                                                                                                                                 -0.51858497.
                                                                                                                                    0.20724739,
0.28684464,
0.00603078,
                                                                                                                                                               -0.14461054
                                                                                                                                                                  0.34428513,
                                                                                                      0.07875892,
0.2890019,
0.02522451,
                                            0.14932795, -0.42723438,
                                                                                                                                    0.06157893.
                                                                                                                                                                 -0.19437575
                                            0.03054013, -0.20949648,
-0.17629069, -0.2162296,
                                                                                                                                    0.03168807,
-0.17976451,
                                                                                                                                                                  0.18291238
                                            0.13074148,
                                                                         0.12900151, -0.29620144,
                                                                                                                                    0.39828372,
                                                                                                                                                                  0.355817561,
                                            0.130/4148, 0.12900151, -0.29620144, -0.08132942, 0.0508789, 0.03970909, 0.21220328, 0.16169944, -0.05766107, 0.2551639, -0.2933403, -0.16104451, 0.50502181, 0.18621859, -0.07766819, 0.41251048, -0.01803587, 0.04746069,
                                        r-0.08132942.
                                                                                                      0.03970909, -0.06884057, -0.07758211,
                                                                                                                                  -0.04837854, -0.23052695,
-0.11232601, -0.1305835,
                                                                                                                                  0.10281896, -0.06372993,
0.27628538, -0.21901166]
```

Expected output

```
Cost after epoch 0: 0.742591
Cost after epoch 10: 0.614557
Cost after epoch 20: 0.598900
Cost after epoch 30: 0.588907
Cost after epoch 40: 0.579898
```

Congratulations! You've made it to the end of this assignment, and to the end of this week's material. Amazing work building a neural network in TensorFlow 2.3!

Here's a quick recap of all you just achieved:

- Used tf.Variable to modify your variables
- Applied TensorFlow decorators and observed how they sped up your code
- Trained a Neural Network on a TensorFlow dataset
- Applied batch normalization for a more robust network

You are now able to harness the power of TensorFlow's computational graph to create cool things, faster. Nice!

4 - Bibliography

In this assignment, you were introducted to tf.GradientTape, which records operations for differentation. Here are a couple of resources for diving deeper into what it does and why:

Introduction to Gradients and Automatic Differentiation: https://www.tensorflow.org/guide/autodiff (<a href="

GradientTape documentation: https://www.tensorflow.org/api_docs/python/tf/GradientTape (https://www.tensorflow.org/api_docs/python/tf/GradientTape)

In []: