Functional Programming in R A Pragmatic Introduction

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- 4 Closure

Overview

- We'll start by reviewing basics
- We'll see the ideas at action first (by solving problems) and abstractions later
- We'll digress a lot

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Writing a function in R

```
functionname <- function(arg1, arg2, ...) {
     <<expressions>>
     [return(<<expression>>)]
}
```

- return() is optional
- last statement of the function body is returned by default

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Example of a Function

```
square.of <- function(x) {
    x*x
}</pre>
```

Call the function

```
square.of(4)

y <- square.of(x=4)

square.of(z=4)
```

More on Functions

- Arguments of R functions can be either required or optional, indicated by syntax
- Required arguments have no default value
- Optional arguments are defined to have a default value

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More on Functions - Example

```
add <- function(x, y = 2) {
    x+y
}</pre>
```

```
add(3)
add(3,2)
add(x=3)
add(x=3, y=2)
add(y=2)
add(, 3)
```

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Example - Computing Power I

Write a function that computes the kth power of an argument x, using one default argument, and one optional argument, i.e. an argument that has a default value.

We'll be coming back to this function later on.



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Example - Computing Power II

power
$$<-$$
 function(x, k=2) x^k

The apply family of functions

 lapply(X, FUN, ...)
 returns a list of the same length as X, each element of which is the result of applying FUN to the corresponding element of X

sapply(X, FUN, ...)
 a user-friendly version of lapply by default returning a vector or matrix if appropriate

Read the Documentation



Vectorized Functions

... functions that operate on vectors or matrices or dataframes.

- Often much faster than looping over a vector, often use
 .Internal or .Primitive
- Higher abstraction less code to write, less to debug

.Internal and .Primitive - |

```
log
## function (x, base = exp(1)) .Primitive("log")
```

```
## function (..., sep = " ", collapse = NULL)
## .Internal(paste(list(...), sep, collapse))
## <bytecode: 0x1f8a2c8>
## <environment: namespace:base>
```

Vectorization

.Internal and .Primitive - |

```
colMeans
## function (x, na.rm = FALSE, dims = 1L)
## {
       if (is.data.frame(x))
##
##
            x <- as.matrix(x)
        if (!is.array(x) || length(dn \leftarrow dim(x)) < 2L)
##
            stop("'x' must be an array of at least two dimen
##
        if (dims < 1L || dims > length(dn) - 1L)
##
            stop("invalid 'dims'")
##
##
       n <- prod(dn[1L:dims])</pre>
       dn \leftarrow dn[-(1L:dims)]
##
       z \leftarrow if (is.complex(x))
##
              Internal (colMeans (Re(x) n prod (dn) na rm)).
##
              Soumendra Prasad Dhanee
```

Examples of Vectorized Functions

- ifelse()
- is.na()
- log()
- sqrt()
- rnorm()
- colMeans()
- rowSums()
- x > y
- x == y
- !x

Primality Testing I

Given a number, decide if it is a prime or not.

Hint 1: min(x) gives the lowest element of vector x

```
min(c(2, 1, 3))
## [1] 1
```

Primality Testing II

```
min( x%%( 2:(x-1) ) )>0
```

The Deconstruction

```
2:(x-1)
x\%\%(2:(x-1))
min(x\%\%(2:(x-1)))>0
```

Lists of functions

```
x < -1:10
funs <- list(</pre>
  sum = sum,
  mean = mean,
  median = median
sapply(funs, function(f) f(x))
            mean median
##
      sum
##
     55.0 5.5 5.5
```

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First-class Functions

Let's get started

Problem 1

- InputA numeric vector (1:200000)
- Output
 A vector containing the even numbers in the input vector, listed in the order they appeared in the input vector

Solution - for loop I



Solution using for loop

```
x <- 1:200000
ans <- logical(200000)
for(i in x)
{
  if(i%%2==0) { ans[i] = TRUE } else {
    ans[i] = FALSE }
}
x[ans]</pre>
```

```
## user system elapsed
## 0.542 0.005 0.546
```

Solution - for loop II



Solution using for loop

```
x <- 1:200000
ans <- c()
for(i in x)
{
  if(i%2==0) { ans[i] = TRUE } else {
    ans[i] = FALSE }
}
x[ans]</pre>
```

```
## user system elapsed
## 56.511 2.631 59.333
```

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Solution - vectorized functions

```
Solution using vectorized functions
x <- 1:200000
ans <- x\%/2 == 0
x[ans]
##
      user system elapsed
     0.013 0.000 0.013
##
```

Solution - higher-order functions

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What are higher-order functions?



A higher-order function (also functional form, functional or functor) is a function that does at least one of the following:

- takes one or more functions as an input
- outputs a function
- -source Wikipedia



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An example

sapply
sapply(X, FUN, ...)

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What are first-class functions?

Pirst-class Functions

First-class functions are functions that can be treated like any other piece of data ...

- can be stored in a variable
- can be stored in a list
- can be stored in an object
- can be passed to other functions
- can be returned from other functions
- ... just like any other piece of data.



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Rounding off

Problem 2a

- Input A numeric vector (rnorm(100, 0, 1))
- Output
 A vector containing all the numbers in the input vector rounded to the nearest integer

Solution 2a - Rounding off



Rounding off

Problem 2b

- Input A numeric vector (rnorm(100, 0, 1))
- Output
 A vector containing all the numbers in the input vector rounded to two decimal places

Solution 2b - Rounding off



sapply(rnorm(100, 0, 1), function(x) round(x, 2))

Anonymous Functions

Anonymous Functions

Anonymous function is a function that is not bound to an identifier.

source - Wikipedia

Acting on Matrices

Problem 3

- InputA 3-by-3 matrix (matrix(1:9, ncol=3))
- OutputAdd 1 to row 1, 4 to row 2, 7 to row 3

Solution 3 - Matrix Addition

- Solution using sweep

```
m <- matrix (1:9, ncol=3)
sweep (m, 1, c(1, 4, 7), "+")
```

```
## [,1] [,2] [,3]
## [1,] 2 5 8
## [2,] 6 9 12
## [3,] 10 13 16
```

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Applicative Programming

Calling by function B of function A, where function A was originally supplied to function B as an argument.



- map
- reduce (fold)
- filter

Мар

```
Map(f, x, ...)
```

mapply

mapply is a multivariate version of sapply.

```
mapply(rep, 1:4, 4:1)

mapply(rep, times = 1:4, x = 4:1)

mapply(rep, x = 1:4, times = 4:1)
```

Filter I

Choose all the even numbers.

```
Filter(function(x) x2/42, 1:200000)
```

```
## user system elapsed
## 0.419 0.004 0.424
```

Filter II

The previous solution was wrong.

Now what is the output of the following -

$$\mathsf{Filter}\left({\color{red} \mathbf{c}} (\mathsf{T}, \;\; \mathsf{F}) \;, \;\; 1{:}200000 \right)$$

1

Filter III

```
function (f, x)
{
   ind <- as.logical(unlist(lapply(x, f)))
   x[!is.na(ind) & ind]
}
<bytecode: 0x4f87f00>
<environment: namespace:base>
```

Negate 1

What is the outcome?

1

Negate II

What is the outcome?

```
Filter (Negate (function (x) \times \%2), 1:10)
```

Negate III

```
function (f)
{
    f <- match.fun(f)
    function(...) !f(...)
}
<bytecode: 0x4e9c250>
<environment: namespace:base>
```

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Computing Power Revisited

Write a function that computes the kth power of an argument x, using one default argument, and one optional argument, i.e. an argument that has a default value.

```
power <- function(x, k=2) {
    x^k
}</pre>
```

Function Factory with Closures

A function returning a function:

```
power <- function(exponent) {</pre>
  function(x) {
    x ^ exponent
square <- power(2)</pre>
square(2)
square (4)
cube <- power(3)
                                                                    11
cube(2)
cube (4)
                                                                    13
```

What are Closures?

An object is data with functions. A closure is a function with data.

- John D. Cook

... an abstraction binding a function to its scope.

- Wikipedia

Closures get their name because they enclose the environment of the parent function and can access all its variables.

- Hadley Wickham



Closer look at closures I

```
square
## function(x) {
##
       x ^ exponent
## }
## <environment: 0x217dcf8>
cube
## function(x) {
##
       x ^ exponent
##
## <environment: 0x26cb1d0>
```

Closer look at closures II

```
as.list(environment(square))

## $exponent

## [1] 2

as.list(environment(cube))

## $exponent

## [1] 3
```

Closer look at closures III

```
library (pryr)
unenclose (square)

function (x)

{

x x^2

}

unenclose (cube)

function (x)

{

x x^3

}
```