Model I. Locations of N drones' platform and warehouse

Introduction:

- Target: Define the most appropriate locations of drones' platform and warehouses
- Input: The number(N) of warehouse, order sample with address(sample size 200)
- Output: N suitable locations of drones' platform and warehouses

Model special function:

- · Automaticly convert address into earth distance by using google map geocoding api
- Automaticly calculate distance between order and warehouses by calling geopy function, getcircle
- Apply optimization by using IBM Cplex to figure out N most appropriate locations

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```
- Basic library - sys, docplex
```

- Setup docplex engine

In this case, we use cplex cloud to solve optimization problem. Please be noted that this case could also be solved by Cplex community with preinstalled IBM Cplex software.

```
In [2]: url = "https://api-oaas.docloud.ibmcloud.com/job_manager/rest/v1/"
    key = "api_3d568d67-19d8-4b62-894b-d31981859867"
```

- Step 1 Import dataset and manipulate the dataset
 - We will collect the list of address of each order. And then, we will convert those addresses into ponit (longitude,latitute), which could be used to calculate the distance.
 - Define NamedPoint to collect information with same factors.

```
In [3]:
    class XPoint(object):
        def __init__(self, x, y):
            self.x = x
            self.y = y
        def __str__(self):
            return "P(%g_%g)" % (self.x, self.y)

class NamedPoint(XPoint):
    def __init__(self, name, x, y):
        XPoint.__init__(self, x, y)
        self.name = name
    def __str__(self):
        return self.name
```

- Import library geopy.distance
- Define Function 1: computing the earth distance between 2 points on map

- Import library googlemaps, json
 Define Function 2: Exchange the address into latitude and longitude, collect lat and lng
- In [5]: import json
 import googlemaps

 def getlat(address):
 gmap = googlemaps.Client(key='AIzaSyD2fUATZAJtzmVCTQi5Fe6xpboAgR5-7J4')
 origin_earth_location = gmap.geocode(address)
 lat=origin_earth_location[0]['geometry']['location']['lat']
 return lat

 def getlng(address):
 gmap = googlemaps.Client(key='AIzaSyD2fUATZAJtzmVCTQi5Fe6xpboAgR5-7J4')
 origin_earth_location = gmap.geocode(address)
 lng = origin_earth_location[0]['geometry']['location']['lng']
 return lng
 - Import library xlrd
 - Load required dataset
 - "order" list represent a collection of all destination addresses of historical orders

```
In [6]: import xlrd
    mydataset=xlrd.open_workbook('Order_target_address.xlsx')
    mytable = mydataset.sheets()[0]

order = []

pos = 1
    order.extend(mytable.col_values(pos)[1:])
    #a = len(order)
    #print(order, a)
```

- Create empty list of lat, lng and warehouse lat lng list.
- Apply function 2 to each address of warehouse list

- And then use warehouse_lat_lng to collect information of address_with_point(address, longitude, latitude)

```
In [7]: #empty list to collect latitude, longitude and address with point info.
    lat = []
    lng = []
    order_lat_lng = []

for i in range(len(order)):
        latitude = getlat(order[i])
        longitude = getlng(order[i])
        name = order[i]
        cp = NamedPoint(name, longitude, latitude)
        order_lat_lng.append(cp)

print("There are %d orders in NYC" % (len(order_lat_lng)))
```

There are 200 orders in NYC

- Step 2 Visualizaiton of data
 - import library folium
 - design folium visualization
 - print map

```
In [8]: try:
    import folium
except:
    if hasattr(sys, 'real_prefix'):
        #we are in a virtual env.
        !pip install folium
else:
        !pip install --user folium

import folium
map_osm = folium.Map(location=[40.712765, -73.950882], zoom_start=11)
for order in order_lat_lng:
    lt = order.y
    lg = order.x
    folium.Marker([lt, lg]).add_to(map_osm)
map_osm
```





*Please be noted that this map just represent the result of order list with 200 sample size. Since we only generated the historical order list, it may not represent the real case.

*More data and real data should be input to get a more accurative result.

- Step 3: Optimization of location of warehouse
 Set up DOcplex to write and solve an optimization model that will help us determine where to locate the warehouse in an optimal way.
 - Define number of warehouse required to be built

 The number, 7, of warehouses is come from our estimated analysis of NYC(excluding Stanley Is land)

```
In [9]: nb_warehouse = 7
print("We would like to open %d warehouses." % nb_warehouse)
```

We would like to open 7 warehouses.

- Set up the prescriptive model
- create docplex model

```
In [10]: from docplex.mp.environment import Environment
    env = Environment()
    env.print_information()
    from docplex.mp.model import Model
    mdl = Model("Warehouse location")
```

- * system is: Darwin 64bit
- * Python is present, version is 3.5.4
- * docplex is present, version is (2, 3, 44)
- * CPLEX wrapper is present, version is 12.7.0.0, located at: /Applications/anaconda3/envs/cplexenv/lib/python3.5/site-packages

- Define the Decision Variables

```
In [11]: # Ensure unique points
BIGNUM = 999999999

order_lat_lng = set(order_lat_lng)
warehouse_locations = order_lat_lng

# Decision vars
# Binary vars indicating which warehouse locations will be actually selected
warehouse_vars = mdl.binary_var_dict(warehouse_locations, name="is_warehouse")

# Binary vars representing the "assigned" order for each warehouse
link_vars = mdl.binary_var_matrix(warehouse_locations, order_lat_lng, "link")
```

- Define the constraints #constraint 1: if the distance is suspect, it needs to be excluded from the problem.

```
In [12]: for c_loc in warehouse_locations:
    for b in order_lat_lng:
        if get_distance(c_loc, b) >= BIGNUM:
             mdl.add_constraint(link_vars[c_loc, b] == 0, "ct_forbid_{0!s}_{1!s}".format(c_loc, b))
```

#constraint 2: each order must be linked to a warehouse that is open.

```
In [13]: mdl.add_constraints(link_vars[c_loc, b] <= warehouse_vars[c_loc]</pre>
                             for b in order lat lng
                             for c loc in warehouse locations)
         mdl.print_information()
         Model: Warehouse location
          - number of variables: 40200
            - binary=40200, integer=0, continuous=0
          - number of constraints: 40000
             - linear=40000
          - parameters: defaults
                 #constraint 3: each order is linked to exactly one warehouse.
In [14]: mdl.add_constraints(mdl.sum(link_vars[c_loc, b] for c_loc in warehouse_locations) == 1
                             for b in order_lat_lng)
         mdl.print_information()
         Model: Warehouse location
          - number of variables: 40200
            - binary=40200, integer=0, continuous=0
          - number of constraints: 40200
             - linear=40200
```

#constraint 4: there is a fixed number of warehouse to open.

- parameters: defaults

```
In [15]: # Total nb of open warehouse
          mdl.add constraint(mdl.sum(warehouse vars[c loc] for c loc in warehouse locations) == nb warehouse)
          # Print model information
          mdl.print information()
          Model: Warehouse location
           - number of variables: 40200
             - binary=40200, integer=0, continuous=0
           - number of constraints: 40201
             - linear=40201
           - parameters: defaults
           • Step 4 - Express the objective
             The objective is to minimize the total distance from order to warehouse so that customer always receive packages with less waiting
             time
In [16]: # Minimize total distance from points to hubs
          total_distance = mdl.sum(link_vars[c_loc, b] * get_distance(c_loc, b) for c_loc in warehouse_locations f
          mdl.minimize(total distance)
                 - Solve with the Decision Optimization solve service
In [17]: print("# Order = %d" % len(warehouse locations))
          print("# warehouse = %d" % nb warehouse)
          assert mdl.solve(url=url, key=key), "!!! Solve of the model fails"
          # Order = 200
          # warehouse = 7
```

- create list of open warehouse, not warehouse, edges for visualization of data

```
In [18]: total_distance = mdl.objective_value
    open_warehouse = [c_loc for c_loc in warehouse_locations if warehouse_vars[c_loc].solution_value == 1]
    not_warehouse = [c_loc for c_loc in warehouse_locations if c_loc not in open_warehouse]
    edges = [(c_loc, b) for b in order_lat_lng for c_loc in warehouse_locations if int(link_vars[c_loc, b])

print("Total distance = %g" % total_distance)
    print("# warehouse = {0}".format(len(open_warehouse)))
    for c in open_warehouse:
        print("new warehouse: {0!s}".format(c))
```

```
Total distance = 288.635

# warehouse = 7

new warehouse: 546 W 146th St, New York, NY 10031

new warehouse: 1370 E 18th St Brooklyn, NY 11230

new warehouse: 1035 Park Ave New York, NY 10028

new warehouse: 2552 Holland Ave Bronx, NY 10467

new warehouse: 88-35 212th Pl Queens Village, NY 11427

new warehouse: 207 E 15th St, New York, NY 10003

new warehouse: 32-23 100th St Flushing, NY 11369
```

- visualization of final results

```
import folium
In [19]:
           map osm = folium.Map(location=[40.712765, -73.950882], zoom start=11)
           for warehouse in open warehouse:
               lt = warehouse.y
               lg = warehouse.x
               folium.Marker([lt, lg], icon=folium.Icon(color='red',icon='info-sign')).add to(map osm)
           for b in order_lat_lng:
               if b not in open_warehouse:
                    lt = b.y
                    lg = b.x
                    folium.Marker([lt, lg]).add_to(map_osm)
           for (c, b) in edges:
               coordinates = [[c.y, c.x], [b.y, b.x]]
               map osm.add child(folium.PolyLine(coordinates, color='#FF0000', weight=5))
           map osm
                                            New Rochelle
Out[19]:
                                                                   Bayville
                 Hackensack
                                                                              Huntington
                                                                     Oyster Bay
              Hasbrouck
                                                           Glen Cove
                                                                                                      Smithtown Lake Grove
               Heights
            Rutherford
                                                                                                             Long Island
                                                                                            I 495
                                                                           NY 135
           h Arlington
                                                                                                                Long Island
                                                                                                                 MacArthur
                                                                                                                        Patchoque
                                                                                                                 Airport
                                                           Mineola
                                                                                                       Islip
                                                           Garden City
                                                                                      West Babylon
                                                            Hempstead
                                                                                    Lindenhurst
```

Freeport

Valley-Stream

John F. Kennedy / International

Airport

East Rockaway

Long Beach

Bayonne

I 278

In []: #End