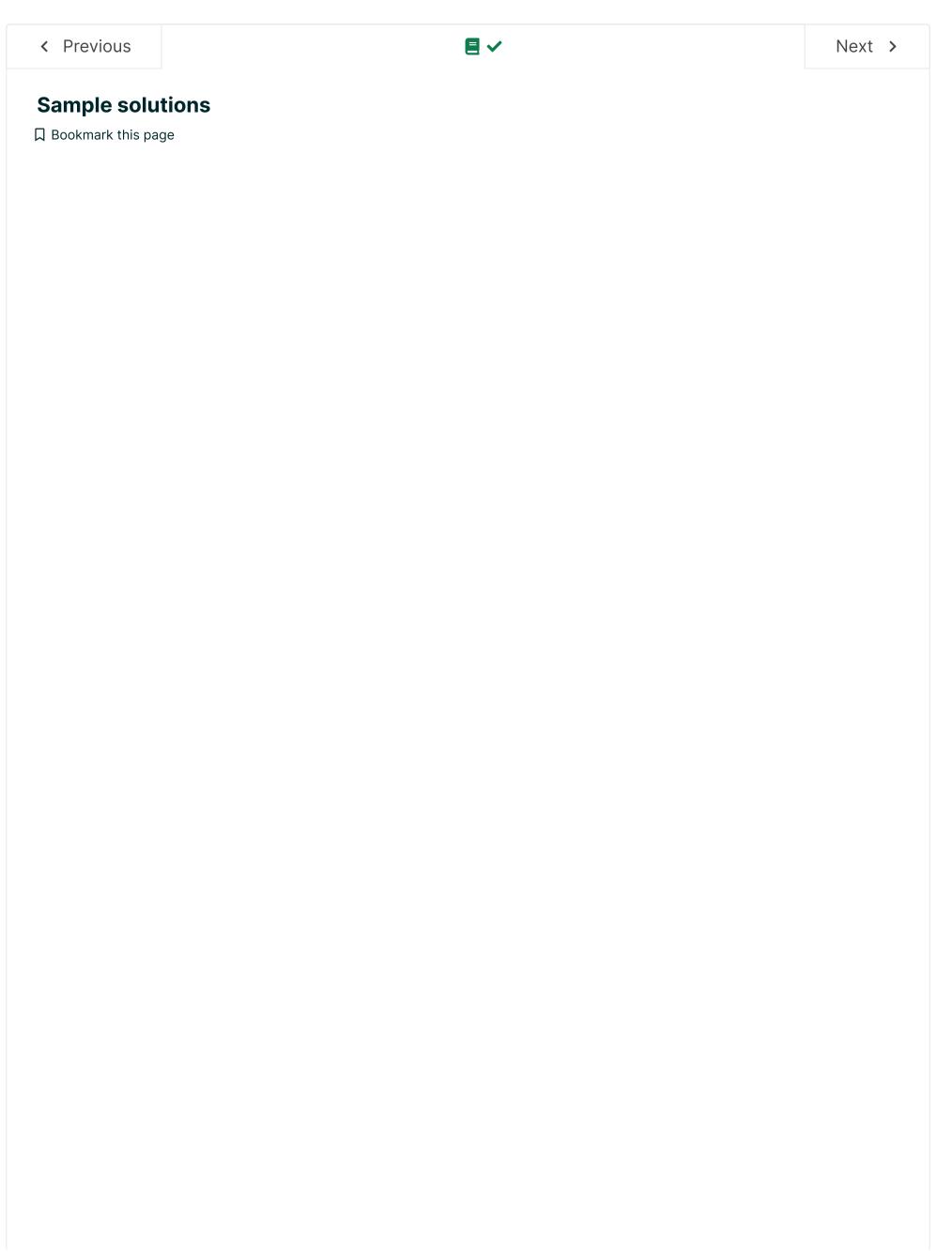
<u>Help</u>

mrajagopal6 v

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★ Course / Module 2: The Analysis of Data / Solution: Notebook 14





Clustering via k-means

We previously studied the classification problem using the logistic regression algorithm. Since we had labels for each data point, we may regard as one of supervised learning. However, in many applications, the data have no labels but we wish to discover possible labels (or other hidden structures). This problem is one of unsupervised learning. How can we approach such problems?

Clustering is one class of unsupervised learning methods. In this lab, we'll consider the following form of the clustering task. Suppose you are

- a set of observations, $X \equiv \{\hat{x}_i \mid 0 \le i < n\}$, and
- a target number of *clusters*, *k*.

Your goal is to partition the points into k subsets, $C_0, \ldots, C_{k-1} \subseteq X$, which are

- disjoint, i.e., $i \neq j \implies C_i \cap C_j = \emptyset$;
- but also complete, i.e., $C_0 \cup C_1 \cup \cdots \cup C_{k-1} = X$.

Intuitively, each cluster should reflect some "sensible" grouping. Thus, we need to specify what constitutes such a grouping.

Setup: Dataset

The following cell will download the data you'll need for this lab. Run it now.

```
In [1]: import requests
        import os
        import hashlib
        import io
        def on vocareum():
            return os.path.exists('.voc')
        def download(file, local_dir="", url_base=None, checksum=None):
            local file = "{}{}".format(local dir, file)
            if not os.path.exists(local_file):
                if url base is None:
                    url_base = "https://cse6040.gatech.edu/datasets/"
                url = "{}{}".format(url_base, file)
                print("Downloading: {} ...".format(url))
                r = requests.get(url)
                with open(local file, 'wb') as f:
                    f.write(r.content)
            if checksum is not None:
                with io.open(local_file, 'rb') as f:
                    body = f.read()
                    body checksum = hashlib.md5(body).hexdigest()
                    assert body_checksum == checksum, \
                         "Downloaded file '{}' has incorrect checksum: '{}' instead of '{}'".format(local
                                                                                                     checl
            print("'{}' is ready!".format(file))
        if on vocareum():
            URL_BASE = "https://cse6040.gatech.edu/datasets/kmeans/"
            DATA_PATH = "../resource/asnlib/publicdata/"
            URL BASE = "https://github.com/cse6040/labs-fa17/raw/master/datasets/kmeans/"
            DATA PATH = ""
        datasets = {'logreg_points_train.csv': '9d1e42f49a719da43113678732491c6d',
                     centers_initial_testing.npy': '8884b4af540c1d5119e6e8980da43f04',
                     'compute_d2_soln.npy': '980fe348b6cba23cb81ddf703494fb4c',
                     'y_test3.npy': 'df322037ea9c523564a5018ea0a70fbf',
                     'centers_test3_soln.npy': '0c594b28e512a532a2ef4201535868b5',
                     'assign cluster labels S.npy': '37e464f2b79dc1d59f5ec31eaefe4161',
                     'assign_cluster_labels_soln.npy': 'fc0e084ac000f30948946d097ed85ebc'}
        for filename, checksum in datasets.items():
            download(filename, local dir=DATA PATH, url base=URL BASE, checksum=checksum)
        print("\n(All data appears to be ready.)")
        'logreg points train.csv' is ready!
         'y_test3.npy' is ready!
        'compute d2 soln.npy' is ready!
```

```
'assign_cluster_labels_soln.npy' is ready!
'centers_test3_soln.npy' is ready!
'assign_cluster_labels_S.npy' is ready!
'centers_initial_testing.npy' is ready!
(All data appears to be ready.)
```

The k-means clustering criterion

Here is one way to measure the quality of a set of clusters. For each cluster C, consider its center μ and measure the distance $||x - \mu||$ of each $x \in C$ to the center. Add these up for all points in the cluster; call this sum is the within-cluster sum-of-squares (WCSS). Then, set as our goal t clusters that minimize the total WCSS over all clusters.

More formally, given a clustering $C = \{C_0, C_1, \dots, C_{k-1}\}$, let

WCSS(C)
$$\equiv \sum_{i=0}^{k-1} \sum_{x \in C_i} ||x - \mu_i||^2,$$

where μ_i is the center of C_i . This center may be computed simply as the mean of all points in C_i , i.e.,

$$\mu_i \equiv \frac{1}{|C_i|} \sum_{x \in C_i} x.$$

Then, our objective is to find the "best" clustering, C_* , which is the one that has a minimum WCSS.

$$C_* = \arg\min_{C} \text{WCSS}(C).$$

The standard k-means algorithm (Lloyd's algorithm)

Finding the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is NP-hard (https://en.wikipedia.org/wiki/NP-hardness), which is computer science mumbo jumbo for "we don't known that the global optimum is not the global opt there is an algorithm to calculate the exact answer in fewer steps than exponential in the size of the input." Nevertheless, there is an iterative m algorithm, that can quickly converge to a local (as opposed to global) minimum. The procedure alternates between two operations: assignment

Step 1: Assignment. Given a fixed set of k centers, assign each point to the nearest center:

$$C_i = {\hat{x} : ||\hat{x} - \mu_i|| \le ||\hat{x} - \mu_i||, 1 \le j \le k}.$$

Step 2: Update. Recompute the *k* centers ("centroids") by averaging all the data points belonging to each cluster, i.e., taking their mean:

$$\mu_i = \frac{1}{|C_i|} \sum_{\hat{x} \in C_i} \hat{x}$$

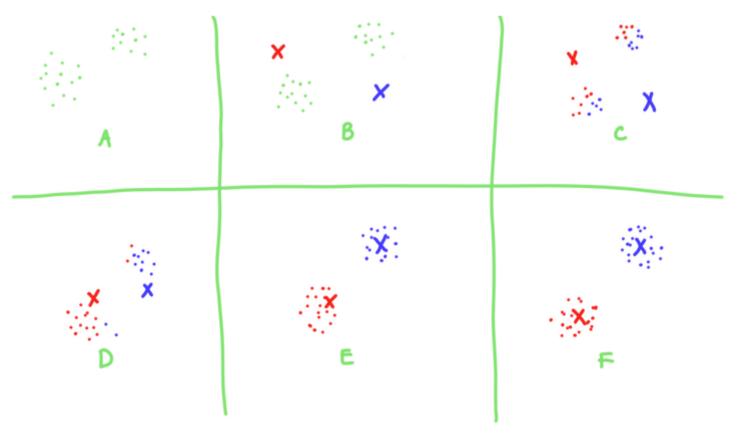


Figure adapted from: http://stanford.edu/~cpiech/cs221/img/kmeansViz.png) (http://stanford.edu/~cpiech/cs221/img/kmeansViz.png)

In the code that follows, it will be convenient to use our usual "data matrix" convention, that is, each row of a data matrix X is one of m observed each column (coordinate) is one of d predictors. However, we will not need a dummy column of ones since we are not fitting a function.

$$X \equiv \begin{pmatrix} \hat{x}_0^T \\ \vdots \\ \hat{x}_m^T \end{pmatrix} = \begin{pmatrix} x_0 & \cdots & x_{d-1} \end{pmatrix}.$$

In [2]: import numpy as np import pandas as pd

```
import seaborn as sns
import matplotlib.pyplot as plt
%matplotlib inline
import matplotlib as mpl
mpl.rc("savefig", dpi=100) # Adjust for higher-resolution figures
```

We will use the following data set which some of you may have seen previously.

```
In [3]: | df = pd.read_csv('{}logreg_points_train.csv'.format(DATA_PATH))
```

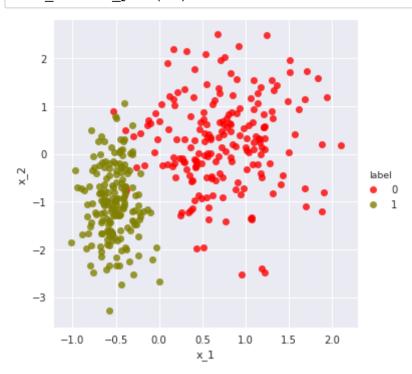
Out[3]:

	x_1	x_2	label
0	-0.234443	-1.075960	1
1	0.730359	-0.918093	0
2	1.432270	-0.439449	0
3	0.026733	1.050300	0
4	1.879650	0.207743	0

```
In [4]: # Helper functions from Logistic Regression Lesson
        def make_scatter_plot(df, x="x_1", y="x_2", hue="label",
                               palette={0: "red", 1: "olive"},
                               size=5,
                               centers=None):
            sns.lmplot(x=x, y=y, hue=hue, data=df, palette=palette,
                       fit_reg=False)
            if centers is not None:
                plt.scatter(centers[:,0], centers[:,1],
                            marker=u'*', s=500,
                            c=[palette[0], palette[1]])
        def mark_matches(a, b, exact=False):
            Given two Numpy arrays of {0, 1} labels, returns a new boolean
            array indicating at which locations the input arrays have the
            same label (i.e., the corresponding entry is True).
            This function can consider "inexact" matches. That is, if `exact`
            is False, then the function will assume the {0, 1} labels may be
            regarded as the same up to a swapping of the labels. This feature
            allows
              a == [0, 0, 1, 1, 0, 1, 1]
              b == [1, 1, 0, 0, 1, 0, 0]
            to be regarded as equal. (That is, use `exact=False` when you
            only care about "relative" labeling.)
            assert a.shape == b.shape
            a_int = a.astype(dtype=int)
            b int = b.astype(dtype=int)
            all_axes = tuple(range(len(a.shape)))
            assert ((a_int == 0) | (a_int == 1)).all()
            assert ((b_int == 0) | (b_int == 1)).all()
            exact matches = (a int == b int)
            if exact:
                return exact_matches
            assert exact == False
            num_exact_matches = np.sum(exact_matches)
            if (2*num_exact_matches) >= np.prod (a.shape):
                return exact_matches
            return exact_matches == False # Invert
        def count_matches(a, b, exact=False):
            Given two sets of \{0, 1\} labels, returns the number of mismatches.
            This function can consider "inexact" matches. That is, if `exact`
            is False, then the function will assume the {0, 1} labels may be
            regarded as similar up to a swapping of the labels. This feature
              a == [0, 0, 1, 1, 0, 1, 1]
              b == [1, 1, 0, 0, 1, 0, 0]
            to be regarded as equal. (That is, use `exact=False` when you
            only care about "relative" labeling.)
            matches = mark matches(a. b. exact=exact)
```

```
return np.sum(matches)
```

```
In [5]: make_scatter_plot(df)
```



Let's extract the data points as a data matrix, points, and the labels as a vector, labels. Note that the k-means algorithm you will implement reference labels -- that's the solution we will try to predict given only the point coordinates (points) and target number of clusters (k).

```
In [6]: | points = df.as_matrix(['x_1', 'x_2'])
        labels = df['label'].as_matrix()
        n, d = points.shape
        k = 2
```

Note that the labels should *not* be used in the k-means algorithm. We use them here only as ground truth for later verification.

How to start? Initializing the k centers

To start the algorithm, you need an initial guess. Let's randomly choose k observations from the data.

Exercise 1 (2 points). Complete the following function, init_centers(X, k), so that it randomly selects k of the given observations to serve should return a Numpy array of size k-by-d, where d is the number of columns of x.

```
In [7]: def init_centers(X, k):
            Randomly samples k observations from X as centers.
            Returns these centers as a (k \times d) numpy array.
             ### BEGIN SOLUTION
             from numpy.random import choice
             samples = choice(len(X), size=k, replace=False)
             return X[samples, :]
             ### END SOLUTION
```

```
In [8]: # Test cell: `init_centers_test`
        centers initial = init centers(points, k)
        print("Initial centers:\n", centers_initial)
        assert type(centers initial) is np.ndarray, "Your function should return a Numpy array instead (
        rmat(type(centers_initial))
        assert centers_initial.shape == (k, d), "Returned centers do not have the right shape (\{\} \times \{\})
        assert (sum(centers_initial[0, :] == points) == [1, 1]).all(), "The centers must come from the :
        assert (sum(centers_initial[1, :] == points) == [1, 1]).all(), "The centers must come from the :
        print("\n(Passed!)")
        Initial centers:
         [[ 0.428191 -1.9734 ]
         [ 0.75525 2.03587 ]]
        (Passed!)
```

Computing the distances

Exercise 2 (3 points). Implement a function that computes a distance matrix, $S=(s_{ij})$ such that $s_{ij}=d_{ij}^2$ is the squared distance from point \hat{x}_i It should return a Numpy matrix S[:m, :k].

```
In [9]: | def compute_d2(X, centers):
            m = len(X)
            k = len(centers)
            S = np.empty((m, k))
            ### BEGIN SOLUTION
            for i in range(m):
                 d_i = np.linalg.norm(X[i, :] - centers, ord=2, axis=1)
                 S[i, :] = d_i**2
             ### END SOLUTION
            return S
```

```
In [10]: # Test cell: `compute_d2_test`
         centers_initial_testing = np.load("{}centers_initial_testing.npy".format(DATA_PATH))
         compute d2 soln = np.load("{}compute d2 soln.npy".format(DATA PATH))
         S = compute_d2 (points, centers_initial_testing)
         assert (np.linalg.norm (S - compute_d2_soln, axis=1) <= (20.0 * np.finfo(float).eps)).all ()</pre>
         print("\n(Passed!)")
         (Passed!)
```

Exercise 3 (2 points). Write a function that uses the (squared) distance matrix to assign a "cluster label" to each point.

That is, consider the $m \times k$ squared distance matrix S. For each point i, if $s_{i,j}$ is the minimum squared distance for point i, then the index j is i's In other words, your function should return a (column) vector y of length m such that

```
y_i = \operatorname{argmin} \ s_{ii}.
         j \in \{0,...,k-1\}
```

Hint: Judicious use of Numpy's argmin() (https://docs.scipy.org/doc/numpy/reference/generated/numpy.argmin.html) makes for a nice line solution.

```
In [11]: def assign cluster labels(S):
             ### BEGIN SOLUTION
             return np.argmin(S, axis=1)
             ### END SOLUTION
         # Cluster labels:
                               0
                                    1
         S_test1 = np.array([[0.3, 0.2], # --> cluster 1
                              [0.1, 0.5], # --> cluster 0
                              [0.4, 0.2]]) # --> cluster 1
         y test1 = assign cluster labels(S test1)
         print("You found:", y_test1)
         assert (y_test1 == np.array([1, 0, 1])).all()
         You found: [1 0 1]
In [12]: # Test cell: `assign_cluster_labels_test`
         S_test2 = np.load("{}assign_cluster_labels_S.npy".format(DATA_PATH))
         y_test2_soln = np.load("{}assign_cluster_labels_soln.npy".format(DATA_PATH))
         y_test2 = assign_cluster_labels(S_test2)
         assert (y_test2 == y_test2_soln).all()
         print("\n(Passed!)")
         (Passed!)
```

Exercise 4 (2 points). Given a clustering (i.e., a set of points and assignment of labels), compute the center of each cluster.

```
In [13]: def update centers(X, y):
              # X[:m, :d] == m points, each of dimension d
              # y[:m] == cluster labels
             m, d = X.shape
             k = max(y) + 1
             assert m == len(y)
             assert (min(y) >= 0)
             centers = np.empty((k, d))
             for j in range(k):
                  # Compute the new center of cluster j,
                  # i.e., centers[j, :d].
                  ### BEGIN SOLUTION
                  centers[j, :d] = np.mean(X[y == j, :], axis=0)
                  ### END SOLUTION
             return centers
```

```
IN [II]. | # IEDE CEIT. NAMME CENCEID CEDE
         y_test3 = np.load("{}y_test3.npy".format(DATA_PATH))
         centers test3 soln = np.load("{}centers test3 soln.npy".format(DATA PATH))
         centers_test3 = update_centers(points, y_test3)
         delta_test3 = np.abs(centers_test3 - centers_test3_soln)
         assert (delta_test3 <= 2.0*len(centers_test3_soln)*np.finfo(float).eps).all()</pre>
         print("\n(Passed!)")
         (Passed!)
```

Exercise 5 (2 points). Given the squared distances, return the within-cluster sum of squares.

In particular, your function should have the signature,

```
def WCSS(S):
```

where S is an array of distances as might be computed from Exercise 2.

For example, suppose S is defined as follows:

```
S = np.array([[0.3, 0.2],
                     [0.1, 0.5],
                     [0.4, 0.2]]
Then WCSS(S) == 0.2 + 0.1 + 0.2 == 0.5.
```

Hint: See https://docs.scipy.org/doc/numpy/reference/generated/numpy.amin.html#numpy.amin).

```
In [15]: def WCSS(S):
             ### BEGIN SOLUTION
             return np.sum(np.amin(S, axis=1))
              ### END SOLUTION
          # Quick test:
         print("S == \n", S_test1)
         WCSS_test1 = WCSS(S_test1)
         print("\nWCSS(S) ==", WCSS(S_test1))
         S ==
          [[0.3 0.2]
          [0.1 \ 0.5]
          [0.4 \ 0.2]]
         WCSS(S) == 0.5
In [16]: # Test cell: `WCSS_test`
         assert np.abs(WCSS_test1 - 0.5) <= 3.0*np.finfo(float).eps, "WCSS(S_test1) should be close to 0.5
          .format(WCSS_test1)
         print("\n(Passed!)")
          (Passed!)
```

Lastly, here is a function to check whether the centers have "moved," given two instances of the center values. It accounts for the fact that the centers may have changed.

```
In [17]: | def has_converged(old_centers, centers):
             return set([tuple(x) for x in old centers]) == set([tuple(x) for x in centers])
```

Exercise 6 (3 points). Put all of the preceding building blocks together to implement Lloyd's k-means algorithm.

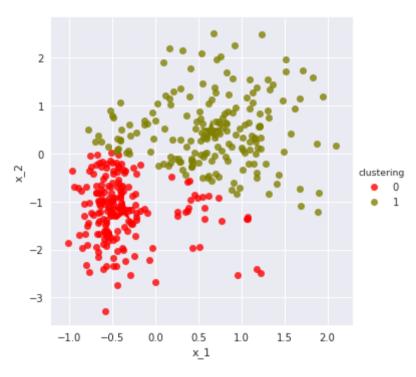
```
In [18]: def kmeans(X, k,
                     starting centers=None,
                     max_steps=np.inf):
              if starting_centers is None:
                  centers = init_centers(X, k)
              else:
                  centers = starting centers
             converged = False
             labels = np.zeros(len(X))
             i = 1
             while (not converged) and (i <= max steps):</pre>
                  old centers = centers
                  ### BEGIN SOLUTION
                  S = compute_d2(X, centers)
                  labels = assign_cluster_labels(S)
                  centers = update centers(X. labels)
```

```
converged = has_converged(old_centers, centers)
        ### END SOLUTION
        print ("iteration", i, "WCSS = ", WCSS (S))
        i += 1
    return labels
clustering = kmeans(points, k, starting_centers=points[[0, 187], :])
iteration 1 WCSS = 549.9175535488309
iteration 2 WCSS = 339.80066330255096
iteration 3 WCSS = 300.330112922328
iteration 4 WCSS = 289.80700777322045
iteration 5 WCSS = 286.0745591062787
iteration 6 WCSS = 284.1907705579879
iteration 7 WCSS = 283.22732249939105
iteration 8 WCSS = 282.456491302569
iteration 9 WCSS = 281.84838225337074
iteration 10 WCSS = 281.57242082723724
iteration 11 WCSS = 281.5315627987326
```

Let's visualize the results.

```
In [19]: # Test cell: `kmeans_test`
         df['clustering'] = clustering
         centers = update_centers(points, clustering)
         make_scatter_plot(df, hue='clustering', centers=centers)
         n_matches = count_matches(df['label'], df['clustering'])
         print(n matches,
                "matches out of",
               len(df), "possible",
                "(~ {:.1f}%)".format(100.0 * n_matches / len(df)))
         assert n matches >= 320
```

329 matches out of 375 possible (~ 87.7%)



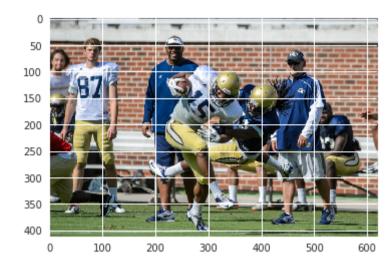
Applying k-means to an image. In this section of the notebook, you will apply k-means to an image, for the purpose of doing a "stylized recol (You can view this example as a primitive form of artistic style transfer (http://genekogan.com/works/style-transfer/), which state-of-the-art met accomplish using neural networks (https://medium.com/artists-and-machine-intelligence/neural-artistic-style-transfer-a-comprehensive-look-ff

In particlar, let's take an input image and cluster pixels based on the similarity of their colors. Maybe it can become the basis of your own Instal (https://blog.hubspot.com/marketing/instagram-filters)!

```
In [20]: from PIL import Image
         from matplotlib.pyplot import imshow
         %matplotlib inline
         def read img(path):
             Read image and store it as an array, given the image path.
             Returns the 3 dimensional image array.
             img = Image.open(path)
             img_arr = np.array(img, dtype='int32')
             img.close()
             return img arr
         def display_image(arr):
             display the image
             input : 3 dimensional array
```

```
arr = arr.astype(dtype='uint8')
    img = Image.fromarray(arr, 'RGB')
    imshow(np.asarray(img))
img_arr = read_img("../resource/asnlib/publicdata/football.bmp")
display image(img arr)
print("Shape of the matrix obtained by reading the image")
print(img_arr.shape)
```

Shape of the matrix obtained by reading the image (412, 620, 3)



Note that the image is stored as a "3-D" matrix. It is important to understand how matrices help to store a image. Each pixel corresponds to a i for Red, Green and Blue. If you note the properties of the image, its resolution is 620 x 412. The image width is 620 pixels and height is 412 pix pixel has three values - **R**, **G**, **B**. This makes it a 412 x 620 x 3 matrix.

Exercise 7 (1 point). Write some code to reshape the matrix into "img_reshaped" by transforming "img_arr" from a "3-D" matrix to a flattened " which has 3 columns corresponding to the RGB values for each pixel. In this form, the flattened matrix must contain all pixels and their corresp intensity values. Remember in the previous modules we had discussed a C type indexing style and a Fortran type indexing style. In this probler C type indexing style. The numpy reshape function may be of help here.

```
In [21]: ### BEGIN SOLUTION
         r, c, l = img arr.shape
         img_reshaped = np.reshape(img_arr, (r*c, 1), order="C")
         ### END SOLUTION
In [22]: # Test cell - 'reshape_test'
         r, c, l = img_arr.shape
         # The reshaped image is a flattened '2-dimensional' matrix
         assert len(img reshaped.shape) == 2
         r reshaped, c reshaped = img reshaped.shape
         assert r * c * l == r_reshaped * c_reshaped
         assert c reshaped == 3
         print("Passed")
         Passed
```

Exercise 8 (1 point). Now use the k-means function that you wrote above to divide the image in 3 clusters. The result would be a vector which label to each pixel.

```
In [23]: ### BEGIN SOLUTION
         labels = kmeans(img_reshaped, 3)
         ### END SOLUTION
         iteration 1 WCSS = 3191006513.0
         iteration 2 WCSS = 887886047.4271191
         iteration 3 \text{ WCSS} = 669086576.3837116
         iteration 4 WCSS = 640418622.8330001
         iteration 5 WCSS = 636366884.6415913
         iteration 6 WCSS = 635141015.9468135
         iteration 7 WCSS = 634601099.9963626
         iteration 8 WCSS = 634372413.2726401
         iteration 9 WCSS = 634266793.5137541
         iteration 10 WCSS = 634214992.2303745
         iteration 11 WCSS = 634190480.2853614
         iteration 12 WCSS = 634179610.7516326
         iteration 13 WCSS = 634176205.8989807
         iteration 14 WCSS = 634174590.2671936
         iteration 15 WCSS = 634173984.4367541
         iteration 16 WCSS = 634173813.1828784
         iteration 17 WCSS = 634173778.4150583
         iteration 18 WCSS = 634173759.7959646
         iteration 19 WCSS = 634173756.0509284
         iteration 20 WCSS = 634173755.1569637
In [24]: # Test cell - 'labels'
```

```
assert len(labels) == r reshaped
assert set(labels) == \{0, 1, 2\}
print("\nPassed!")
```

Passed!

Exercise 9 (2 points). Write code to calculate the mean of each cluster and store it in a dictionary as label:array(cluster_center). For 3 clusters, should have three keys as the labels and their corresponding cluster centers as values, i.e. {0:array(center0), 1: array(center1), 2:array(center2)}

```
In [25]: ### BEGIN SOLUTION
         ind = np.column_stack((img_reshaped, labels))
         centers = {}
         for i in set(labels):
             c = ind[ind[:,3] == i].mean(axis=0)
             centers[i] = c[:3]
          ### END SOLUTION
```

In [26]: print("Free points here! But you need to implement the above section correctly for you to see where the points here! But you need to implement the above section correctly for you to see where the points here! you to see later.") print("\nPassed!")

Free points here! But you need to implement the above section correctly for you to see what we v o see later.

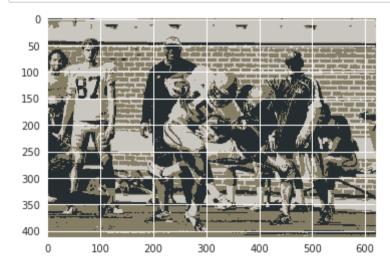
Passed!

Below, we have written code to generate a matrix "img_clustered" of the same dimensions as img_reshaped, where each pixel is replaced by tl center to which it belongs.

```
In [27]: img_clustered = np.array([centers[i] for i in labels])
```

Let us display the clustered image and see how kmeans works on the image.

```
In [28]: r, c, l = img arr.shape
         img_disp = np.reshape(img_clustered, (r, c, 1), order="C")
         display_image(img_disp)
```



You can visually inspect the original image and the clustered image to get a sense of what kmeans is doing here. You can also try to vary the nu clusters to see how the output image changes

Built-in k-means

The preceding exercises walked you through how to implement k-means, but as you might have imagined, there are existing implementations a following shows you how to use Scipy's implementation, which should yield similar results. If you are asked to use k-means in a future lab (or e can use this one.

```
In [29]: from scipy.cluster import vq
In [30]: # `distortion` below is the similar to WCSS.
         # It is called distortion in the Scipy documentation
         # since clustering can be used in compression.
         centers vq, distortion vq = vq.kmeans(points, k)
         # vq return the clustering (assignment of group for each point)
         # based on the centers obtained by the kmeans function.
         # _ here means ignore the second return value
         clustering_vq, _ = vq.vq(points, centers_vq)
         print("Centers:\n", centers_vq)
         print("\nCompare with your method:\n", centers, "\n")
         print("Distortion (WCSS):", distortion vq)
```

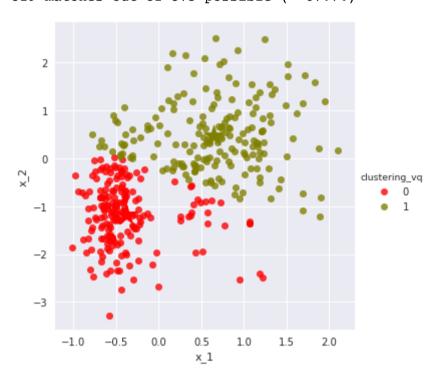
```
df['clustering_vq'] = clustering_vq
make_scatter_plot(df, hue='clustering_vq', centers=centers_vq)
n_matches_vq = count_matches(df['label'], df['clustering_vq'])
print(n_matches_vq,
      "matches out of",
      len(df), "possible",
      "(~ {:.1f}%)".format(100.0 * n_matches_vq / len(df)))
Centers:
```

```
[[-0.37382602 -1.18565619]
[ 0.64980076  0.4667703 ]]
```

Compare with your method:

{0: array([202.52108949, 198.84707504, 192.62337998]), 1: array([134.23584777, 125.34568766, 10 8]), 2: array([38.7890798 , 45.35163548, 48.17869416])}

Distortion (WCSS): 0.7500461744207869 329 matches out of 375 possible (~ 87.7%)



Fin! That marks the end of this notebook. Don't forget to submit it!

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