

PRACTICAL NO: 1.

Topic: Random Variable.

Q1. Find the mean and Variance for the following:

(a)	x	-1	0	1	2	
	P(x)	0.1	0.2	0.3	0.4	

x	P(x)	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	0.1	-0.1	0.1	0.01
0	0.2	0	0	0
1	0.3	0.3	0.3	0.09
2	0.4	0.8	1.6	0.64
TOTAL	$\sum = 1$	$\sum = 1$	$\sum E(x)^2 = 0.2$	$\sum [E(x)]^2 = 0.74$

$$\therefore \text{Mean} = E(x) = \sum x_i \cdot P(x) = 1$$

$$\begin{aligned} \therefore \text{Variance} &= V(x) = \sum E(x)^2 - [E(x)]^2 \\ &= 0.2 - 0.74 \\ &= 1.24 \end{aligned}$$

$$\therefore \text{Mean } E(x) = 1 \text{ & Variance } V(x) = 1.24$$

(b)	x	-1	0	1	2
	P(x)	1/8	1/8	1/4	1/2

Soln
=

Soln

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	1/8	-1/8	1/8	1/64
0	1/8	0	0	0
1	1/8	1/8	1/8	1/16
2	1/8	1	2	1
3	1/8	3	9	9
Total	$\sum = 1$	$\sum = 9/8$	$\sum = 19/8$	$\sum = 69/64$

$$\therefore \text{Mean} = E(x) = \sum x \cdot P(x) = 9/8.$$

$$\therefore \text{Variance} = V(x) = \sum E(x)^2 - \sum [E(x)]^2$$

$$= \frac{19}{8} - \frac{69}{64}$$

$$= \frac{152 - 69}{64}$$

$$= \frac{83}{64}$$

$$\therefore \text{Mean } E(x) = 9/8 \text{ and Variance } V(x) = 83/64.$$

(C)	x	-3	10	15
	$P(x)$	0.4	0.35	0.25

	x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
	-3	0.4	-1.2	3.6	1.44
	10	0.35	3.5	35	12.25
	15	0.25	3.75	56.25	14.0625
Total	$\sum = 1$	$\sum = 6.05$	$\sum = 94.85$	$\sum = 27.7525$	

$$\therefore \text{Mean} = E(x) = \sum x \cdot p(x) = 6.05$$

$$\begin{aligned}\text{Variance } V(x) &= \sum E(x)^2 - \sum [E(x)]^2 \\ &= 44.85 - 27.7525 \\ &= 67.0975\end{aligned}$$

$$\therefore \text{Mean } E(x) = 6.05 \text{ & Variance } V(x) = 67.097.$$

Q2. If $p(x)$ is pmf of a random variable x . If $p(x)$ represents pmf for random variable x . Find value of k . Then evaluate mean and variance.

Soln: As $P(x_i)$ is a pmf it should satisfy the properties of pmf which are:

a] $P(x_i) > 0$ for all i in sample space

b] $\sum P(x_i) = 1$

x	-1	0	1	2
$P(x)$	$k+1/13$	$k/13$	$1/13$	$k-4/13$

$$\therefore \sum P(x_i) = 1 = \frac{k+1}{13} + \frac{k}{13} + \frac{1}{13} + \frac{k-4}{13}$$

$$1 = \frac{k+1+k+1+k-4}{13}$$

$$13 = 3k - 2$$

$$15 = 3k$$

$$k = 5$$

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	6/13	-6/13	6/13	36/169
0	5/13	0	0	0
1	1/13	1/13	1/13	1/169
2	1/13	2/13	4/13	4/169
TOTAL	$\sum = 11/13$	$\sum = -3/13$	$\sum = 11/13$	$\sum = 41/169$

$\therefore \text{Mean} = E(x) = \sum x \cdot p(x) = \frac{-3}{13}$

$$\begin{aligned}\therefore \text{Variance} &= V(x) = \sum [E(x)]^2 - [\sum E(x)]^2 \\ &= \frac{11}{13} - \frac{41}{169} \\ &= \frac{143 - 41}{169} \\ &= \frac{102}{169}\end{aligned}$$

$\therefore \text{Mean} = -3/13 \text{ & Variance} = 102/169$

Q3. The pmf of random variable x is given by

x	-3	-1	0	1	2	3	5	8
$P(x)$	0.1	0.2	0.15	0.2	0.1	0.15	0.05	0.05

Obtain cdf find (i) $P(-1 \leq x \leq 2)$ (ii) $P(1 \leq x \leq 5)$

(iii) $P(x \leq 2)$ (iv) $P(x \geq 0)$

Soln

x	-3	-1	0	1	2	3	5	8
$p(x)$	0.1	0.2	0.15	0.2	0.1	0.15	0.05	0.05
$F(x)$	0.1	0.3	0.45	0.65	0.75	0.90	0.95	1.0

$$\begin{aligned}
 ① P(-1 \leq x \leq 2) &= p(x \leq 2) - p(x \leq -1) + p(x = -1) \\
 &= F(x_b) - F(x_a) + p(a) \\
 &= F(2) - F(-1) + p(-1) \\
 &= 0.75 - 0.3 + 0.2 \\
 &= 0.25
 \end{aligned}$$

$$\begin{aligned}
 ② P(1 \leq x \leq 5) &= p(x_b) - p(x_a) + p(a) \\
 &= F(5) - F(1) + p(1) \\
 &= 0.95 - 0.65 + 0.2 \\
 &= 0.15
 \end{aligned}$$

$$\begin{aligned}
 ③ P(x \leq 2) &= p(x = -3) + p(x = -1) + p(x = 0) + p(x = 1) + \\
 &\quad p(x = 2) \\
 &= 0.1 + 0.2 + 0.15 + 0.2 + 0.1 \\
 &= 0.75
 \end{aligned}$$

$$\begin{aligned}
 ④ p(x \geq 0) &= 1 - f(0) + p(0) \\
 &= 1 - 0.45 + 0.15 \\
 &= 0.40
 \end{aligned}$$

Q4. Let f be continuous random variable with pdf
 $\therefore Pf(x) = \frac{x+1}{2}, -1 < x < 1$
 $= 0, \text{ otherwise}$

Obtain cdf of x . Find mean and variance.

Soln: By definition of cdf we have

$$\begin{aligned} F(x) &= \int_{-1}^x t dt \\ &= \int_{-1}^x \frac{x+1}{2} dx \\ &= \frac{1}{2} \left(\frac{1}{2} x^2 + x \right) \text{ for } -1 \leq x \leq 1 \end{aligned}$$

Hence the cdf is

$$\begin{aligned} F(x) &= 0 \text{ for } x \leq -1 \\ &= \frac{1}{2} x^2 + \frac{1}{2} x \text{ for } -1 \leq x \leq 1 \\ &= 1 \text{ for } x \geq 1 \end{aligned}$$

Q5. Let f be continuous random variable with
pdf $f(x) = \frac{x+2}{18}$ for $-2 < x < 4$

calculate cdf

Soln: By definition of cdf we have

$$\begin{aligned} F(x) &= \int_{-2}^x t dt \\ &= \int_2^x \frac{x+2}{18} dx \\ &= \frac{1}{18} \left(\frac{1}{2} x^2 + 2x \right) \end{aligned}$$

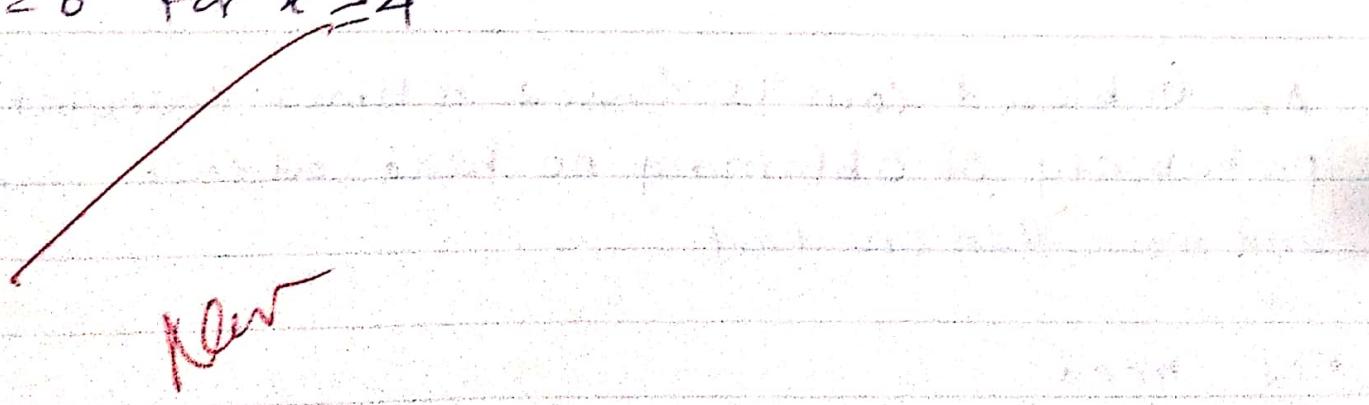
for $-2 < x < 4$

Hence cdf is

$$\begin{aligned} F(x) &= 0 \text{ for } x < -2 \\ &= \frac{1}{18} \left(\frac{1}{2} x^2 + 2x \right) \end{aligned}$$

for $-2 < x < 4$

$= 0$ for $x \geq 4$



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PRACTICAL No: 2

Topic: Binomial Distribution.

Q1. An Unbiased coin is tossed 4 times. calculate the probability of obtaining no head, atleast one head and more than one fail.

• No head:

$$> \text{dbinom}(0, 4, 0.5)$$

[1] 0.0625

• Atleast one head :

$$> 1 - \text{dbinom}(0, 4, 0.5)$$

[1] 0.9375

• More than one Tail:

$$> \text{pbinom}(1, 4, 0.5, \text{lower.tail} = F)$$

[1] 0.4375

Q2. The probability that student is accepted to a prestigious college is 0.3. If 5 students apply, what's the probability of atmost 2 are accepted.

$$> \text{pbinom}(2, 5, 0.3)$$

[1] 0.83692

Q3 An unbiased coin is tossed 6 times. The probability of head at any toss = 0.3. Let x be no. of heads that comes up. Calculate $P(x=2)$, $P(x=2)$, $P(1 < x < 5)$

> `dbinom(2, 6, 0.3)`

[1] 0.324135

> `dbinom(3, 6, 0.3)`

[1] 0.18522

> `dbinom(2, 6, 0.3) + dbinom(3, 6, 0.3) + dbinom(4,`

[1] 0.74373

Q4 For $n=10$, $p=0.6$, evaluate binomial probabilities and plot the graphs of pmf and cdf.

> `x = seq(0, 10)`

> `y = dbinom(x, 10, 0.6)`

> `y`

[1] 0.0001048576 0.0015728640 0.0106168320

0.0424673280 0.114767360 0.2006581248

0.2508226560 0.2149108480 0.1209323520

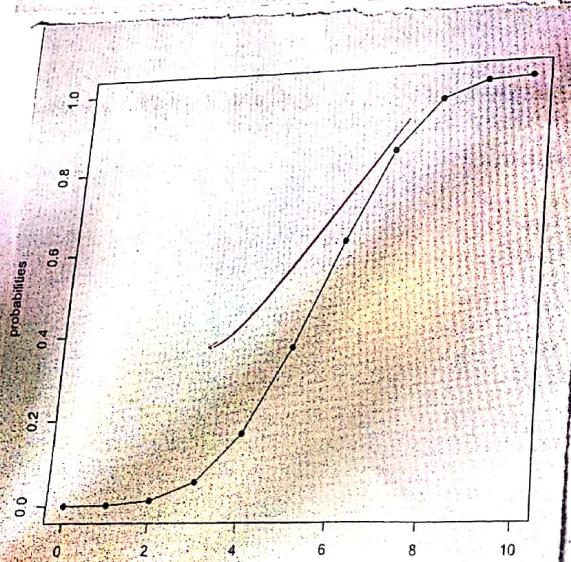
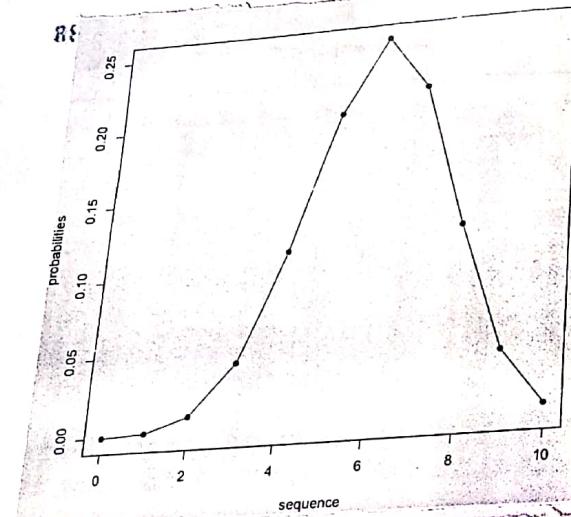
0.0403107840 0.0060466146

> `plot(x, y, xlab = "sequence", ylab = "probabilities", lty = 1, pch = 1)`

> `x = seq(0, 10)`

> `y = pbinom(x, 10, 0.6)`

> `plot(x, y, xlab = "sequence", ylab = "probabilities", lty = 1, pch = 1)`



PE

Q5 Generate a random sample of size 10 for a $B \rightarrow B(8, 0.3)$. Find the mean and the variance of the sample.

> $x = rbinom(8, 10, 0.3)$

[1] 2 2 3 4 3 4 2 3

> $rbinom(8, 10)$ summary(x)

[1] 2.375

> var(x)

[1] 3.125

Q6. The probability of men hitting the target is $1/4$ if he shoots 10 times what is the probability that he hits the target exactly 3 times, probability that he hits target atleast one time.

> $dbinom(3, 10, 0.25)$

[1] 0.2502823

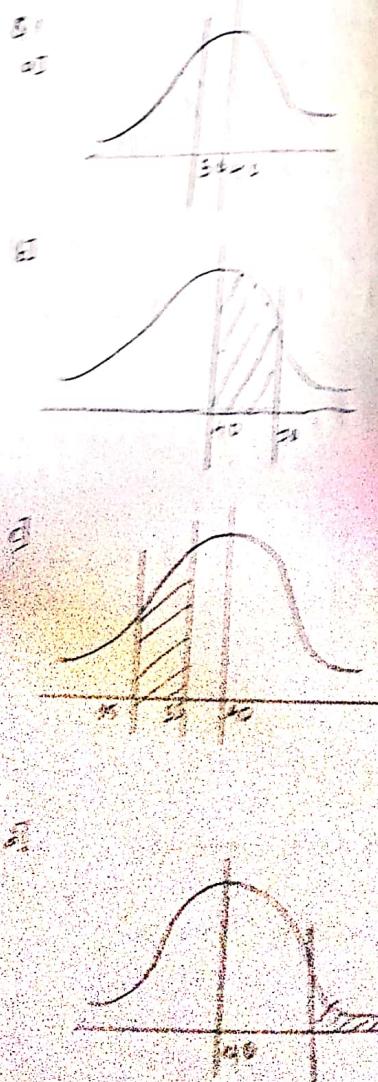
> $1 - dbinom(1, 10, 0.25)$

[1] 0.8122883

Q7 Bits are sent for communication channel in packet of 12. If the probability of bit being corrupted is 0.1. what is the probability of no more than 2 bits are corrupted in a packet?

> $pbinom(2, 12, 0.1, \text{lower.tail} = F) + dbinom(2, 12, 0.1)$

[1] 0.3409977



Topic 2: Normal distribution

A normal distribution of 100 students with mean = 40, $\sigma = 15$

Find no of student whose marks are
 ① $P(X < 30)$ ② $P(40 < X < 70)$ ③ $P(25 < X < 25)$ ④ $P(X > 60)$

> pnorm(30, 40, 15)

[1] 0.2524925

> pnorm(70, 40, 15) - pnorm(40, 40, 15)

[1] 0.4772499

> pnorm(35, 40, 15) - pnorm(25, 40, 15)

[1] 0.2107361

> 1 - pnorm(60, 40, 15)

[1] 0.09121122

- Q2: If the random variable x follows the normal distribution with mean = 50, $\sigma = 10$.
 Find ① $P(X < 30)$ ② $P(X > 65)$ ③ $P(X \leq 30)$
 ④ $P(35 < X < 60)$ ⑤ $P(20 < X < 30)$

> pnorm(70, 50, 10)

[1] 0.4772499

> $1 - \text{pnorm}(65, 50, 10)$
[1] 0.0668072.

> $\text{pnorm}(32, 50, 10)$
[1] 0.03593032

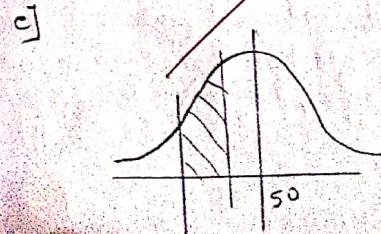
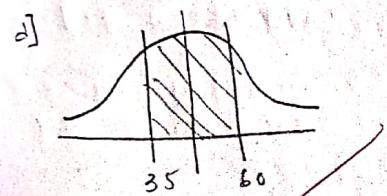
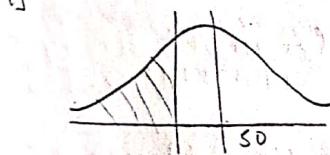
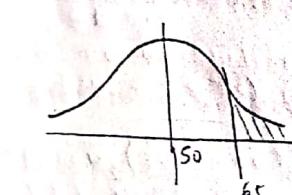
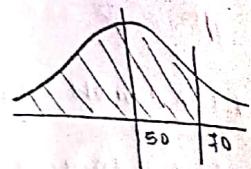
> $\text{pnorm}(60, 50, 10) - \text{pnorm}(35, 50, 10)$
[1] 0.7746375

> $\text{pnorm}(30, 50, 10) - \text{pnorm}(20, 50, 10)$
[1] 0.02140023

Q3. Let $x \sim N(160, 400)$ find k_1 & k_2
such that $P(x < k_1) = 0.6$ & $P(x > k_2) = 0.8$

> $qnorm(0.6, 160, 20)$
[1] 165.0669

> $qnorm(0.2, 160, 20)$
[1] 176.8324



A random variable x follow normal distribution with $\mu = 10$, $\sigma^2 = 2$. Generate 100 observations and evaluate its mean, median, and variance

```
> x = rnorm(100, 10, 2)
```

```
> summary(x)
```

	Min	1st Q	Median	Mean	3rd Q	Max
[1]	5.713	8.444	9.723	9.914	11.325	14.238

```
> var(x)
```

```
[1] 3.648924
```

Q5 write a command to generate 10 random numbers for normally distribution with $\mu = 50$, $\sigma = 4$. Find the sample mean and median

```
> x = rnorm(10, 50, 4)
```

```
> summary(x)
```

	Min	1st Q	Median	Mean	3rd Q	Max
[1]	44.73	50.46	52.01	52.35	54.34	58.85

Ans

PRACTICAL NO: 4

Topic: Testing of hypothesis

CASE 1: Sample mean and Standard deviation given
single population

- Q1. Suppose the food label on cookies bag states that it has almost 2g of saturated fat in a single cookie. In sample of 35 cookies it was found that mean amount of saturated fat per cookie is 2.1g assume that the sample S.D is 0.3 at 0.5 level of significance (5%). Can we reject the claim on food label?

$$H_0 = \mu < 2$$

$$H_1 = \mu > 2$$

$$> z = (2.1 - 2) / (0.3 / \sqrt{35})$$

$$[1] 1.972027$$

$$> 1 - \text{pnorm}(z)$$

$$[1] 0.0243$$

- Reject the null hypothesis
- Accept H_1

- (2) A sample of 1000 customers was randomly selected and it was found that average spending was 275/- . The $S.D = 30$. Using 0.05 level of significance would you conclude that amount spent by customer is more than 250/-

$$H_0 = \mu < 250$$

$$H_1 = \mu > 250$$

$$>z = (275 - 250) / (30 / \sqrt{100})$$

>z

$$[1] 8.333$$

$$> 1 - pnorm(z, 99)$$

$$[1] 2.3057$$

∴ Reject the null hypothesis

∴ Accept H_1

- (3) A quality control of engineers finds that sample of 100 light have average life of 470 hours. Assuming population $\sigma = 25$ test whether the population mean is 480 hours
 $\alpha \rightarrow 0.05$

$$H_0 = \mu < 480$$

$$H_1 = \mu > 480$$

$$>z = (470 - 480) / (25 / \sqrt{100})$$

>z

$$[1] -4$$

$$>pz(z, 99, \text{lowertail} = T)$$

$$[1] 6.11257$$

∴ Reject the null hypothesis

∴ Accept H_1

Q4. A principle at school claims that the IQ is 100 of the students. A random sample of 30 students whose IQ was found to 118. The S.D of population = 15 - test the claim of principle

$$H_0 = \mu = 100$$

$$H_1 = \mu > 100$$

$$>z = (118 - 100) / (15 / \sqrt{30})$$

$$>z$$

$$[1] 4.38178$$

$$>p_t(z, 99, \text{lower-tail} = F)$$

$$[1] 5.8856e-06$$

\therefore Reject null hypothesis.

* SINGLE POPULATION PROPORTION.

Q1. It is believed that coin is fair. The coin is tossed 40 times; 28 times - head occurs. Indicate whether the coin is fair or not at 95%. Now $P_0 = 0.5$ $q_0 = 1 - P_0 = 0.5$ $p = 28/40 = 0.7$ $n = 40$ $H_0 = \mu = 0.5$ $H_1 = \mu \neq 0.5$

~~$$>z = (0.7 - 0.5) / \sqrt{(0.5 * 0.5) / 40}$$~~

~~$$>z = 2 * (1 - pnorm(\text{abs}(z)))$$~~

~~$$[1] 0.0141204$$~~

~~Reject null hypothesis
Accept the H₀~~

v) In a hospital 400 females and 520 males are born in a week. Do this confirm male and female are born equal in number?

$$H_0 = \mu = 0.5$$

$$H_1 = \mu \neq 0.5$$

$$\gt z = (0.52 - 0.5) / (\text{sqrt}((0.5 * 0.5) / 1000))$$

$$\gt z$$

$$[1] 1.2645$$

$$\gt 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[1] 0.2060506$$

Reject H_0

Accept H_1

v) In a big city, 325 men out of 600 men were found to be self employed. Conclusion is that maximum men in city are self employed.

$$H_0 = \mu = 0.5$$

$$H_1 = \mu \neq 0.5$$

$$\gt z = (0.5 - 0.325) / \text{sqrt}((0.5 * 0.5) / 600)$$

$$\gt 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[1] 0.04155234$$

~~Reject H_0~~

Accept H_1

Q4 Experience Shows that 20% of manuf acture products are of top quality. In 1 day production of 400 articles only 50 are top quality. Test hypothesis that experience of 20% of manuf acture is wrong.

$$H_0 = \mu = 0.2$$

$$H_1 = \mu \neq 0.2$$

$$> z = (0.125 - 0.2) / \text{sqrt}(0.2 * 0.8) / 400$$

$$> z * 1 - pnorm(abs(z))$$

$$[1] 0.0001768346$$

Reject H_0 , Accept H_1 .

Q. Equality of 2 population proportion

- i) In an early election campaign a telephone poll of 800 registered voters shows favor 460. In second poll opinion 520 of 1000 registered voters favoured the candidate at 5% level of confidence is there sufficient evidence that popularity has decreased.

$$H_0 = p_1 = p_2$$

$$H_1 = p_1 \neq p_2$$

$$> p = (460 * 800 + 520 * 1000) / (520 + 1000)$$

$$> p$$

$$> [1] 0.544$$

$$> 1 - 0.544$$

$$> 0.455$$

$$> z = qnt(0.544 + 0.455 * (1 / (520 + 1) / 1000))$$

49.

> $2 * (1 - pnorm(\text{abs}(z)))$

[1] 0.5444

Accept H_0 .

- (e) from a consignment 200 articles are drawn and 44 was found defective from consignment B, 200 sample are drawn out of which 30 was found defective test whether the proportion of defective items in 2 consignment are significantly different

$$H_0 = P_1 = P_2$$

$$H_1 = P_1 \neq P_2$$

$$> (0.22 * 200 + 0.15 * 200) / (1/200 + 1/200)$$

$$> 0.185$$

$$> 1 - 0.185$$

$$> 0.815 \text{ sort}$$

$$> z = (0.185 * 0.815 * (1/200 + 1/200))$$

$$> 2 * (1 - pnorm(\text{abs}(z)))$$

[1] 0.9969018

Accept H_0 .

new

PA

PRACTICAL NO. 5

Aim: Chi-Square Test

- Q. Use the following data to test whether the attribute Conditions of home and Child are independent.

		Condition of Home	
		Clean	Dirth
Condition of child	Clean	70	50
	Unclean	80	20
	dirty	35	45

H_0 = Both are independent, H_1 = Both are dependent

> $x = c(70, 80, 35)$

> $y = c(50, 20, 45)$

> $z = \text{data.frame}(x, y)$

> z

[1]	x	y
1	70	50
2	80	20
3	35	45

> $\text{chisq.test}(z)$

Pearson's Chi-squared test
data: z

$\chi^2 = 8.646$, df = 2, p-value = $2.695e^{-02}$

- Reject the null hypothesis
• Both are dependent

A dice is tossed 120 times and following results are obtained:

No. of teams	frequency
1	30
2	25
3	18
4	10
5	22
6	15

Test the hypothesis that dice is unbiased.

H_0 = dice is unbiased

H_1 = dice is biased

> obs = c(30, 25, 18, 10, 22, 15)

> exp = sum(obs) / length(obs)

> exp

[1] 20

> z = sum((obs - exp)^2 / exp)

> pchisq(z, df = length(obs) - 1)

[1] 0.956659

∴ Accept the null hypothesis.

∴ dice is unbiased.

Q3

An IQ test was conducted and the students were observed before and after training the result are following

before	after
110	120
120	118
123	125
132	136
125	121

Test whether there is change in the IQ after the training

$\therefore H_1 = \text{no change in IQ}$

$\therefore H_0 = \text{IQ increased after training}$

$> a = (120, 118, 125, 136, 121)$

$> b = (110, 120, 123, 132, 125)$

$> z = \text{sum}((b-a)^2 / 10)$

$> \text{pcchiq}(z, df = \text{length}(b) - 1)$

[1] 0.1135959

Accept the null hypothesis.

\therefore There is change in IQ "after training"

Q4

Graduate

Under graduate

online

20

25

face to

40

5

face

Is there any association between student's preference for type of education and method?

$\therefore H_0$: independent

H_1 : Dependent

$> x = c(20, 40, 25, 5)$

$> z = \text{matrix}(x, \text{nrow} = 2)$

$> \text{chisq.test}(z)$

pearson's chi squared test with Yates' continuity correction

data : z

χ^2 squared = 18.05, df = 1, p-value = 2.157 e -05

\therefore Reject null hypothesis

\therefore Both are dependent.

Q5 A dice is tossed 180 times

No. of items	frequency
1	20
2	30
3	35
4	40
5	12
6	43

Test the hypothesis that dice is unbiased

H_0 = dice is biased

H_1 = dice is unbiased

$> x = c(20, 30, 35, 40, 12, 43)$

$> \text{chisq.test}(x)$

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Chi squared test for given
probabilities

data: Z

$\chi^2_{\text{observed}} = 23.933$, df = 5, p-value = 0.0002236

Reject null hypothesis.

∴ dice is unbiased

Topic: t test

Let $x = 3366, 3337, 3361, 3410, 3316, 3357, 3348, 3356, 3376, 3382, 3377, 3355, 3408, 3401, 3398, 3424, 3383, 3374, 3384, 3374$

Write the R command for following to test hypothesis

$$(1) H_0: \mu = 3400, H_1: \mu \neq 3400$$

$$(2) H_0: \mu = 3400, H_1: \mu > 3400$$

$$(3) H_0: \mu = 3400, H_1: \mu < 3400$$

at 95% level of confidence. Also check at 97% level of confidence

$$\rightarrow (1) H_0: \mu = 3400$$

$$H_1: \mu \neq 3400$$

$\rightarrow x = c(3366, 3337, 3361, 3410, 3316, 3357, 3348, 3356, 3376, 3382, 3377, 3355, 3408, 3401, 3398, 3424, 3383, 3374, 3384, 3374)$

$\rightarrow t\text{-test}(x, \text{mu} = 3400, \text{alt} = \text{"two.sided"},$
 $\text{conf.level} = 0.95)$

one sample t-test

data: x

~~t = -4.4865, df = 19, p value = 0.0002528.~~

~~alternative hypothesis: True mean is not equal to 3400~~

95 percent confidence level:

~~3361.797 3386.103~~

Sample estimates:

mean of x:

~~3373.95~~

Q8

- ∴ Reject H_0
- ∴ Accept H_1

$\gtreqless t\text{-test}(\mathbf{x}, \mu = 3400, \text{alt} = \text{"two-sided"}, \text{conf.level} = 0.95)$

One Sample t-test

data: \mathbf{x}

$t = -4.4865, df = 19, P\text{-Value} = 0.00002528$

alternative hypothesis: true mean is not equal to 3400

3360.83 3384.87

Sample estimates:

mean of \mathbf{x} :

3343.95

- ∴ Reject H_0

- ∴ Accept H_1

→ ② $H_0: \mu = \bar{x} = 3400$

$H_1: \mu > 3400$

$\gtreqless t\text{-test}(\mathbf{x}_1, \mu = 3400, \text{alt} = \text{"greater"}, \text{conf.level} = 0.95)$

One Sample t-test

data: \mathbf{x}_1

$t = -4.4865, df = 19, P\text{-Value} = 0.9999$

alternative hypothesis: true mean is greater than 3400
3363.91 Inf

Sample estimates:

mean of \mathbf{x}_1 :

3343.95

- ∴ Accept H_0

$\gt t\text{-test}(x, \mu = 3400, \text{alter} = \text{"greater"}, \text{conf.level} = 0.97)$
One sided t-test

data: x

$t = -4.4865, df = 19, p\text{value} = 0.9979$ alternative hypothesis: true mean is greater than 3400.

3367.37 Inf

Sample estimates:

mean of x:

3373.95

\therefore Accept H_0 .

$\text{③ } H_0: \mu = 3400$

$H_1: \mu < 3400$

$\gt t\text{-test}(x, \mu = 3400, \text{alter} = \text{"less"}, \text{conf.level} = 0.95)$

one sided t-test

data: x

$t = -4.4865, df = 19, p\text{value} = 0.0001264$

alternative hypothesis: true mean is less than 3400

95 percent level of confidence

-Inf 3353.99

Sample estimates:

mean of x:

3373.95

\therefore Reject H_0

\therefore Accept H_1

$\gt t\text{-test}(x, \mu = 3400, \text{alter} = \text{"less"}, \text{conf.level} = 0.99)$

One sample t-test

data: x

$t = -4.4865, df = 19, p\text{value} = 0.0001264$

alternative hypothesis: true mean is less than 3400

Q3

95 percent level of confidence

- Int 3385.563

Sample estimates:

mean of \bar{x} :

3373.95

∴ Reject H_0

∴ Accept H_1

Q2. Below are the data of gain in weights on 2 different diets A and B

Diet A: 25, 32, 30, 43, 24, 14, 32, 24, 31, 31, 35, 25

Diet B: 44, 34, 22, 10, 47, 31, 40, 30, 32, 35, 18, 21

→ $H_0 = a - b = 0$

∴ $H_1 = a - b \neq 0$

$\gt a = c(25, 32, 30, 43, 24, 14, 32, 24, 31, 31, 35, 25)$

$\gt b = c(44, 34, 22, 10, 47, 31, 40, 30, 32, 35, 18, 21)$

$\gt t\text{test}(a, b, \text{Paired} = T, \text{alter} = \text{"two-sided",}$
 $\text{Conf. level} = 0.95)$

Paired t test

data: a and b

$t = -0.62787$, df = 11, p-value = 0.5429

alternative hypothesis: true difference in means is not equal to 0

95% confidence interval:

-14.267330 7.933997

Sample estimates:

mean of the differences

$$= 3.16667$$

\therefore Accept H_0 .

\therefore There is no difference in weights.

Eleven students gave the test after 1 month they again gave the test after the tuitions, do the marks given evidence that students have benifitted by coaching.

$$E_1: 23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19$$

$$E_2: 24, 19, 22, 18, 20, 22, 20, 20, 23, 20, 17$$

t-test at 99 level of confidence

$$E_1: 23, 20, 19, 21, 18, 20, 18, 17, 23, 16, 19$$

$$E_2: 24, 19, 22, 18, 20, 22, 20, 20, 23, 20, 17$$

$\therefore H_0: e_1 = e_2$

$\therefore H_1: e_1 < e_2$

$\Rightarrow t\text{-test}(e_1, e_2, \text{Paired} = T, \text{alter} = \text{"less"}, \text{Conf. level} = 0.99)$

paired t test

data: e_1 and e_2

$$t = -1.4832, df = 10, p\text{-value} = 0.08441$$

alternative hypothesis: true difference in means is less than 0

99 percent confidence interval:

$$[-\infty, 0.86333]$$

Sample estimates:

mean of the differences

$$-1$$

\therefore Accept H_0

Q.6

- Q4. Two drugs for BP was given and data was collected
- $d_1: 0.7, -1.6, -0.2, -1.2, -0.1, 3.4, 3.7, 0.8, 0.2$
 $d_2: 1.9, 0.8, 1.1, 0.1, 0.1, 4.4, 5.5, 1.6, 4.6, 3.4$.

The two drugs have same effect, check whether two drugs have same effect on patient or not.

$$\rightarrow H_0: d_1 = d_2$$

$$H_1: d_1 \neq d_2$$

$$> d_1 = c(0.7, -1.6, -0.2, -1.2, -0.1, 3.4, 3.7, 0.8, 0.2)$$

$$> d_2 = c(1.9, 0.8, 1.1, 0.1, -0.1, 4.4, 5.5, 1.6, 4.6, 3.4)$$

$$> t\text{-test}(d_1, d_2, \text{alter} = \text{"two-sided"}, \text{paired} = \text{T}, \text{Conf.level} = 0.95)$$

Paired t test

data: d_1 and d_2

$$t = -4.0621, df = 9, P\text{-value} = 0.002833$$

alternative hypothesis: true difference in means is not equal to 0.

95 percent confidence interval:
mean of the differences:

$$-1.58$$

∴ Reject H_0

∴ Accept H_1

- Q5. If there is difference in salaries for the same job in 2 different countries

CA: 53000, 49958, 41974, 44316, 40470, 36963

CB: 62440, 58850, 49495, 52263, 47674, 43552

→ $H_0: S_1 = S_2$

$\therefore H_1: S_1 \neq S_2$

> $CA = c(53000, 49958, 49974, 44368, 46476, 36963)$

> $CB = c(62490, 58850, 49495, 52263, 47674, 43552)$

> $t\text{-test}(ca - cb, \text{paired} = \text{t}, \text{alt} = \text{"two.sided"},$
 $\text{conf.level} = 0.95)$

Paired t-test
 data: ca and cb

$t = -4.4564, df = 5, p\text{-value} = 0.00666$

alternative hypothesis: true difference in means is not equal to 0.

95 percent confidence interval:

-10404.821 - 2792.846

Sample estimates:

mean of the differences:

- 6598.833

~~- Reject H_0~~

~~- Reject H_0~~

~~- Accept H_1~~

New

¹⁸
PRACTICAL NO: 7.

Q1. hi TITLE: F Test.

Q1. Life expectancy in 10 region of India in 1990 and 2000 are given below test whether the Variance at the 2 times are same.

1990 37, 39, 36, 42, 45, 44, 46, 49, 50, 51
 2000 44, 45, 47, 43, 42, 49, 50, 41, 48, 52, 42, 59

$$\rightarrow x = c(37, 39, 36, 42, 45, 44, 46, 49, 50, 51)$$

$$y = c(44, 45, 47, 43, 42, 49, 50, 41, 48, 52, 42, 59)$$

Var.test(x, y)

F test to compare two Variances.

data: x and y

F = 1.0548, num df = 9, denom df = 11, p-value = 0.9173

alternative hypothesis: true ratio of Variance is not equal to 95 percent confidence interval:

0.2939977 - 4.1265887

Sample estimates

ratio of Variance

1.054834

∴ Accept H₀

∴ Variance at 2 times are Same.

Q2: I 25 28 26 22 22 29 31 31 26 31

II 30 25 31 32 23 25 36 26 51 32 27 31 38, 24

at 95% of confidence-level check the ratio of two population variance

$$\text{H}_0: \sigma_1^2 = \sigma_2^2 \quad \text{H}_1: \sigma_1^2 \neq \sigma_2^2$$

$\gtimes x = (25, 28, 26, 22, 27, 31, 31, 26, 31)$

$\gtimes y = (30, 25, 31, 32, 23, 25, 26, 25, 31, 32, 32, 23, 31, 32, 21)$

$\gtimes \text{var} \cdot \text{t-test}(x, y)$

t Test to compare two variance

p-value = 0.4535

∴ Accept H_0 . i.e. $H_0: \sigma_1^2 = \sigma_2^2$

i. Variance of I and II are same.

Q3

For the following data test the hypothesis for
 (1) Equality of 2 population mean $\rightarrow t$ test
 (2) Equality of proportion Nastane $\rightarrow \chi^2$ test

Sample 1: 175, 168, 145, 190, 181, 185, 175, 200

Sample 2: 180, 170, 153, 180, 179, 183, 187, 205

$\rightarrow (1) H_0: \mu_1 = \mu_2$

$H_1: \mu_1 \neq \mu_2$

$\gtimes x = (175, 168, 145, 190, 181, 185, 175, 200)$

$\gtimes y = (180, 170, 153, 180, 179, 183, 187, 205)$

$\gtimes \text{t-test}(x, y, \text{cldf} = "two.sided", \text{conf.level} = 0.95)$

which two sample t-test

p-value = 0.7771

∴ Accept H_0

Equality of 2 population mean are same

8.8

→ ② Equality of proportion Variance
>> val-test (x, y)

F test to compare two variances

$$P\text{-value} = 0.7759$$

∴ Accept H_0

∴ equality of proportion variance are same.

Q4. The following are the price of commodity in the sample of shops selected at random from different city.

City A: 74.10, 77.70, 75.35, 74, 73.80, 79.30,
75.80, 76.80, 77.10, 76.40,

City B: 70.80, 74.90, 76.20, 72.80, 78.10, 74.70,
69.80, 81.20.

$$\therefore H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

> $x = C(74.80, 77.10, 75.35, 74, 73.80, 79.30, 75.80,$
 $79.30, 76.80, 77.10, 76.40)$

> $y = C(70.80, 74.90, 76.20, 72.80, 78.10, 74.70, 69.80,$
 $81.20)$

> val-test (x, y)

f test to compare two variance

$$P\text{-value} = 0.02756$$

∴ Reject H_0

equality of 2 population mean are not same

$> t\text{-test}(x, y, \text{val.equal} = F, \text{paired} = F)$

welch Two Sample t-test

p-value = 0.3244

\therefore Accept H_0 .

\therefore mean of two population is same

Q5 Prepare a CSV file in excel import the file in R and apply the test to check the equality of variance of 2 data.

Observed 1: 10 15 17 11 16 20

observed 2: 15 14 16 11 12 19

$\therefore H_0: \sigma_1^2 = \sigma_2^2$

$H_1: \sigma_1^2 \neq \sigma_2^2$

Save the above observation in excel file in CSV (ms-DOS) format.

$> \text{data} = \text{read.csv}(\text{file.choose()}, \text{header} = T)$

$> \text{data}$.

	OB.1	OB.2
1	10	15
2	15	14
3	17	16
4	11	11
5	16	12
6	20	19

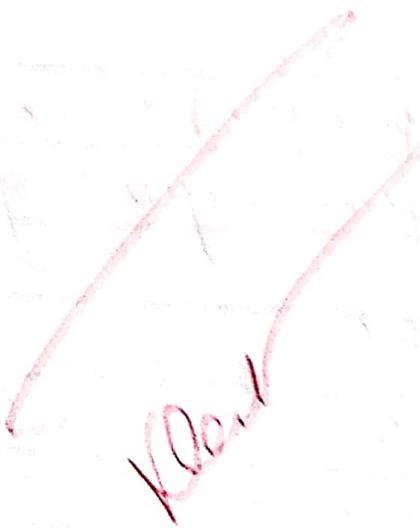
$> \text{attach(data)}$

$> \text{var.test(OB.1, OB.2)}$

H_0 : Test to compare two variances
 F -value = 5.717 > critical value = 3.888

i. Accept H_0

ii. the variance of σ^2 after σ^2 same



TITLE: Non-parametric Task

The times of battery in hours of 10 randomly selected 9 volt battery of a certain company are as follows:

28.1, 15.2, 28.7, 32.8, 48.6, 52.4, 37.6, 49.5,
62.1, 54.5

Test the hypothesis that the population median is 63 against the alternative that it is less than 63 at 5% level of significance.

$$H_0: \text{median} = 63$$

$$H_1: \text{median} \neq 63$$

$x = [28.1, 15.2, 28.7, 32.8, 48.6, 52.4, 37.6,$
 $49.5, 62.1, 54.5]$

$lsp = \text{which}(x < 63)$

$l0 = \text{length}(lsp)$

$> d$

$> [1] 1$

$s_n = \text{length}(\text{which}(x < 63))$

$> s_n$

$> [1] 9$

$> n = 10 + s_n$

$\# \text{binom}(0.05, n, 0.5)$

$> D_2$

$\# \text{binom}(s_n$

$\# \text{accept the null hypothesis}$

Q2. The following data gives the weight of 40 student in random sample.

46, 49, 52, 64, 46, 67, 54, 48, 69, 61, 57, 59, 51, 65, 61, 66, 54, 50, 48, 49, 62, 47, 40, 55, 58, 63, 53, 56, 67, 49, 60, 64, 53, 50, 51, 52, 54,

Use the sign test to test whether the median weight of population is 50 kgs against the alternative that is greater than 50.

$$\rightarrow H_0: \text{median} = 50$$

$$H_1: \text{median} \neq 50$$

$$> x = C(46, 49, 52, 64, 46, 67, 54, 48, 69, 61, 57, 59, 51, 65, 61, 66, 54, 50, 48, 49, 62, 47, 40, 42, 55, 58, 63, 53, 56, 67, 49, 60, 64, 53, 50, 51, 52, 54)$$

$$> sp = \text{length}(\text{which}(x < 50))$$

$$> sp$$

$$[1] 15$$

$$> sn = \text{length}(\text{which}(x > 50))$$

$$> sn$$

$$[1] 12$$

$$> n = sn + sp$$

$$> q = \text{qbinom}(0.05, n, 0.5)$$

$$14:$$

$$\therefore q < sp < sn$$

\therefore Reject H_0

The median age of tourist visiting to certain place is claim to be 41 yrs. A random sample of 15 tourist have the ages 25, 29, 52, 48, 57, 39, 45, 36, 30, 49, 28, 37, 44, 63, 32, 65, 42. Use the sign test to check the claim.

$$H_0: \text{median} = 41$$

$$H_1: \text{median} \neq 41$$

$$x = \{25, 29, 52, 48, 57, 39, 45, 36, 30, 49, 28, 37, 44, 63, 32, 65, 42\}$$

$$> Sp = \text{length}(\text{which}(x > 41))$$

$$> Sp$$

$$[1] 9$$

$$> Sn = \text{length}(\text{which}(x < 41))$$

$$> Sn$$

$$[1] 8$$

$$n = Sp + Sn$$

$$\text{qbinom}(0.05, n, 0.5)$$

$$[1] 5$$

$$\text{qbinom} < Sn$$

Accept the H_0

Q.4

The times in minutes that the patient has to wait for consultation.

15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26.

use the wilcoxon sign test to check whether the median waiting time is more than 20 at 5% level of significance.

H_0 : median ≥ 20 H_1 : median < 20 .



$x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26)$

$> \text{wilcox.test}(x, \text{alternative} = \text{"greater"})$

p-value = 0.001253

∴ Reject H_0 .

∴ median < 20 .

Q5

The weight in kgs of the person before and after thus stop smoking are as follows

weight before

65

75

75

62

72

weight after

72

82

72

66

73

use wilcoxon test to check whether the weight of person increase after stop smoking at 5% level of significance.

* H_0 : weight increase after stopping
 H_1 : weight not increases.

$x = c(65, 75, 75, 62, 72)$

> y = c(72, 82, 72, 66, 73)

> z = x - 4

> wilcox.test(z, mu=0)

p-value = 0.1756.

∴ Accept H_0

Ans

PRACTICAL NO: 9

TITLE: ANOVA.

Q1. The following data gives the effect of three treatments.

$$T_1: 2, 3, 7, \cancel{7}, 2, 6$$

$$T_2: 10, 8, 7, 5, 10$$

$$T_3: 10, 13, 14, 13, 15$$

Test the hypothesis that all treatments are equally effective

$$\rightarrow H_0: t_1 = t_2 = t_3$$

$$H_1: t_1 \neq t_2 \neq t_3$$

$$> t_1 = c(2, 3, 7, 2, 6)$$

$$> t_2 = c(10, 8, 7, 5, 10)$$

$$> t_3 = c(10, 13, 14, 13, 15)$$

$$> \text{data} = \text{data.frame}(t_1, t_2, t_3)$$

$$> e = \text{stack}(\text{data})$$

$$> \text{One-way.test}(\text{values} \sim \text{ind}, \text{data} = e)$$

$$[1] \text{ p-value} = 0.0086232$$

∴ Reject H_0

All treatments are not equally effective

Q2. The following gives the life of tyres of 4 brands

$$A: 20, 23, 18, 17, 22, 24$$

$$B: 19, 15, 17, 20, 16, 17$$

$$C: 21, 19, 22, 17, 20$$

$$D: 15, 14, 16, 18, 14, 16$$

Test the hypothesis that the average life of all the tyres are same

$H_1: A = B = C = D$

$H_0: A \neq B \neq C \neq D$

$> A = C(20, 23, 18, 17, 22, 24)$

$> B = C(19, 15, 17, 20, 16, 19)$

$> C = C(21, 19, 22, 17, 20)$

$> D = C(15, 14, 16, 18, 14, 16)$

$> e = list(a_1 = a, b_1 = b, c_1 = c, d_1 = d)$

$> f = stack(e)$

$> oneway.test(values ~ ind, data = f)$

[1] p-value = 0.006291

\therefore Reject H_0

\therefore All the average life of all brands are not same.

Q3 The types of waxes is applied for, the proportion of calls and number of days of protection were noted. Test whether these are equally effective.

$\rightarrow A: 44, 45, 46, 47, 48, 49,$

$B: 40, 42, 51, 52, 55$

$C: 50, 53, 58, 59$

$H_0: A = B = C = D$

$H_1: A \neq B \neq C$

$> A = C(44, 45, 46, 47, 48, 49)$

$> B = C(40, 42, 51, 52, 55)$

$> C = C(50, 53, 58, 59)$

$> d = list(a_1 = a, b_1 = b, c_1 = c)$

$> e = stack(d)$

$> one way . test(values ~ ind, data = e)$

Q.15

[1] p-value = 0.03822

∴ Reject H₀.

∴ These are not equally effective.

Q.16 An experiment was conducted on 8 persons and the observations were noted. Test the hypothesis that all groups have equal result on three health.

→

No exercise: 23, 26, 51, 48, 58, 37, 29, 44

20 min exercise: 22, 27, 29, 39, 46, 48, 49, 65

60 min exercise: 59, 66, 38, 49, 56, 60, 56, 62

> a = c(23, 26, 51, 48, 58, 37, 29, 44)

> b = c(22, 27, 29, 39, 46, 48, 49, 65)

> c = c(59, 66, 38, 49, 56, 60, 56, 62)

> d = data.frame(a, b, c)

> e = stack(d)

> oneway.test(values ~ ind, data = e)

[1] p-value = 0.01935

∴ Reject H₀.

∴ All the groups not have equal result on three health.

Next